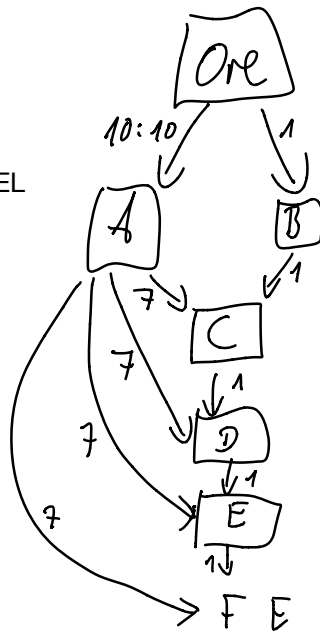


Each reaction gives specific quantities for its inputs and output; reactions cannot be partially run, so only whole integer multiples of these quantities can be used. (It's okay to have leftover chemicals when you're done, though.) For example, the reaction $1\text{ A}, 2\text{ B}, 3\text{ C} \Rightarrow 2\text{ D}$ means that exactly 2 units of chemical D can be produced by consuming exactly 1 A, 2 B and 3 C. You can run the full reaction as many times as necessary; for example, you could produce 10 D by consuming 5 A, 10 B, and 15 C.

Suppose your nanofactory produces the following list of reactions:

$10\text{ ORE} \Rightarrow 10\text{ A}$
 $1\text{ ORE} \Rightarrow 1\text{ B}$
 $7\text{ A}, 1\text{ B} \Rightarrow 1\text{ C}$
 $7\text{ A}, 1\text{ C} \Rightarrow 1\text{ D}$
 $7\text{ A}, 1\text{ D} \Rightarrow 1\text{ E}$
 $7\text{ A}, 1\text{ E} \Rightarrow 1\text{ FUEL}$

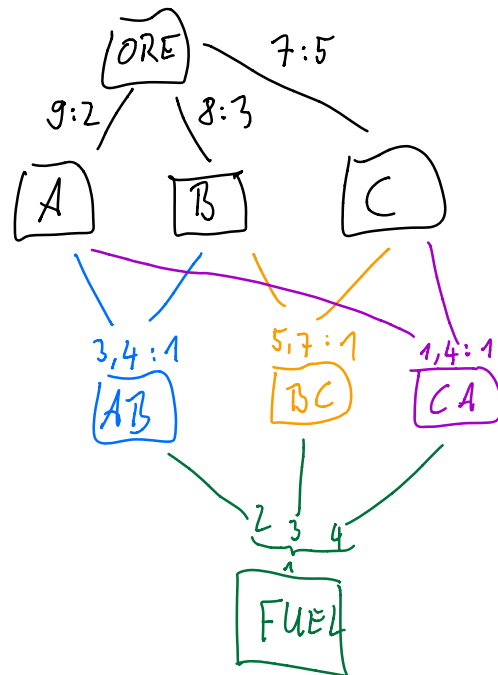


The first two reactions use only ORE as inputs; they indicate that you can produce as much of chemical A as you want (in increments of 10 units, each 10 costing 10 ORE) and as much of chemical B as you want (each costing 1 ORE). To produce 1 FUEL, a total of 31 ORE is required: 1 ORE to produce 1 B, then 30 more ORE to produce the $7 + 7 + 7 + 7 = 28$ A (with 2 extra A wasted) required in the reactions to convert the B into C, C into D, D into E, and finally E into FUEL. (30 A is produced because its reaction requires that it is created in increments of 10.)

9 ORE \Rightarrow 2 A
 8 ORE \Rightarrow 3 B
 7 ORE \Rightarrow 5 C
 3 A, 4 B \Rightarrow 1 AB
 5 B, 7 C \Rightarrow 1 BC
 4 C, 1 A \Rightarrow 1 CA
 2 AB, 3 BC, 4 CA \Rightarrow 1 FUEL

The above list of reactions requires 165 ORE to produce 1 FUEL:

Consume 45 ORE to produce 10 A.
 Consume 64 ORE to produce 24 B.
 Consume 56 ORE to produce 40 C.
 Consume 6 A, 8 B to produce 2 AB.
 Consume 15 B, 21 C to produce 3 BC.
 Consume 16 C, 4 A to produce 4 CA.
 Consume 2 AB, 3 BC, 4 CA to produce 1 FUEL.



$$\begin{aligned}
 2 AB &= 2(3A + 4B) = 6A + 8B \\
 3 BC &= 3(5B + 7C) = 15B + 21C \\
 4 CA &= 4(4C + 1A) = 16C + 4A
 \end{aligned}$$

$$\begin{aligned}
 10A &= 10 \left(\frac{9 \text{ ORE}}{2A} \right) = 5 \cdot 9 \text{ ORE} = 45 \text{ ORE for } 10A \\
 24B &= 24 \left(\frac{8 \text{ ORE}}{3B} \right) = \frac{24}{3} \cdot 8 \text{ ORE} = 64 \text{ ORE for } 24B \\
 40C &= 40 \left(\frac{7 \text{ ORE}}{5C} \right) = \frac{40}{5} \cdot 7 \text{ ORE} = 56 \text{ ORE for } 40C
 \end{aligned}$$

$$\begin{array}{r}
 45 \\
 64 \\
 56 \\
 \hline
 165 \text{ ORE} \\
 \hline
 1 \text{ FUEL}
 \end{array}$$