# Standard Code Library

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## 一切的开始

### 宏定义

● 需要 C++11

```
#include <bits/stdc++.h>
   using namespace std;
   using LL = long long;
   #define FOR(i, x, y) for (decay<decltype(y)>::type i = (x), _##i = (y); i < _##i; ++i)</pre>
    \textit{\#define FORD(i, x, y) for (decay < decltype(x) > :: type i = (x), \_\textit{\#ii} = (y); i > \_\textit{\#ii}; --i) } 
   #ifdef DEBUG
   #ifndef ONLINE_JUDGE
   #define zerol
   #endif
   #endif
   #ifdef zerol
11
   #define dbg(x...) do { cout << "\033[32;1m" << \#x << " -> "; err(x); } while (0)
   void err() { cout << "\033[39;0m" << endl; }</pre>
13
   template<template<typename...> class T, typename t, typename... A>
   void err(T<t> a, A... x) { for (auto v: a) cout << v << ' '; err(x...); }</pre>
   template<typename T, typename... A>
16
   void err(T a, A... x) { cout << a << ' '; err(x...); }</pre>
   #else
18
   #define dbg(...)
   #define err(...)
20
21
       • 调试时添加编译选项 -DDEBUG, 提交时注释
       ● 注意检查判题系统编译选项, 修改 #ifndef ONLINE_JUDGE
       ● FOR ++ 循环 FOR (循环变量名称,循环变量起始值,循环变量结束值(不含))
       ● FORD -循环
       ● err() 调试时输出(支持单层迭代)
```

- dbg() 变色输出变量名和变量值(支持单层迭代)
- 黄色 33,蓝色 34,橙色 31

#### 对拍

• Linux

```
#!/usr/bin/env bash
   g++ -o r main.cpp -02 -std=c++11
   g++ -o std std.cpp -02 -std=c++11
    while true; do
       python gen.py > in
        ./std < in > stdout
        ./r < in > out
        if test $? -ne 0; then
            exit 0
10
        if diff stdout out; then
           printf "AC\n"
12
13
            printf "GG\n"
14
            exit 0
15
        fi
   done
17

    Windows

    @echo off
   setlocal enabledelayedexpansion
    g^{++} -o r main.cpp -02 -std=c++11
   g^{++} -o std std.cpp -02 -std=c^{++}11
   :loop
```

python gen.py > in

if !errorlevel! neq 0 exit /b

```
11
   std.exe < in > stdout
   if !errorlevel! neq 0 exit /b
12
13
   r.exe < in > out
   if !errorlevel! neq 0 exit /b
15
   fc /b stdout out > nul
17
   if !errorlevel! equ 0 (
18
19
       echo AC
   ) else (
20
21
       echo GG
22
       exit /b
23
24
   goto loop
25
   快速编译运行(配合无插件 VSC)
       • Linux
   #!/bin/bash
   g++ $1.cpp -o $1 -02 -std=c++14 -Wall -Dzerol -g
   if $? -eq 0; then
       ./$1

    Windows

   @echo off
    :: 参数为文件名(不含.cpp后缀)
    g++ %1.cpp -o %1 -02 -std=c++14 -Wall -Dzerol -g
   if %errorlevel% equ 0 (
        %1.exe
    数据结构
   ST 表
       一维
   #define M 10
    struct RMQ {
       int f[22][M];
       inline int highbit(int x) { return 31 - __builtin_clz(x); }
       void init(int* v, int n) {
           FOR (i, 0, n) f[0][i] = v[i];
           FOR (x, 1, highbit(n) + 1)
           FOR (i, 0, n - (1 << x) + 1)
           f[x][i] = min(f[x - 1][i], f[x - 1][i + (1 << (x - 1))]);
11
       int get_min(int l, int r) {
           assert(l <= r);</pre>
13
           int t = highbit(r - l + 1);
14
15
           return min(f[t][l], f[t][r - (1 << t) + 1]);</pre>
       }
16
   };
       二维
   #define maxn 10
   LL n, m, a[maxn][maxn];
2
   struct RMQ2D{
       int f[maxn][maxn][10][10];
       inline int highbit(int x) { return 31 - __builtin_clz(x); }
```

```
inline int calc(int x, int y, int xx, int yy, int p, int q) {
8
            return max(
                \max(f[x][y][p][q], f[xx - (1 << p) + 1][yy - (1 << q) + 1][p][q]),
                \max(f[xx - (1 << p) + 1][y][p][q], f[x][yy - (1 << q) + 1][p][q])
10
12
        void init() {
13
            FOR (x, 0, highbit(n) + 1)
14
            FOR (y, 0, highbit(m) + 1)
15
            FOR (i, 0, n - (1 << x) + 1)
            FOR (j, 0, m - (1 << y) + 1) {
17
18
                if (!x && !y) { f[i][j][x][y] = a[i][j]; continue; }
19
                f[i][j][x][y] = calc(
                    i, j,
20
                    i + (1 << x) - 1, j + (1 << y) - 1,
21
                    max(x - 1, 0), max(y - 1, 0)
22
23
                    );
            }
24
25
        inline int get_max(int x, int y, int xx, int yy) {
26
27
            return calc(x, y, xx, yy, highbit(xx - x + 1), highbit(yy - y + 1));
28
   };
29
```

## 线段树

#### 朴素线段树

- 默认为最大值, 可自行修改 struct Q struct PP operator &
- 注意建树时的下标问题 (1-based)

```
const LL INF = LONG_LONG_MAX;
    #define maxn 10
   LL n;
    namespace SGT {
5
        struct Q {
            LL setv:
            explicit Q(LL setv = -1): setv(setv) {}
            void operator += (const Q& q) { if (q.setv != -1) setv = q.setv; }
        }:
10
11
        struct P {
            LL max:
12
            explicit P(LL max = -INF): max(max) {}
13
14
            void up(Q\& q) { if (q.setv != -1) max = q.setv; }
        };
15
16
        template<typename T>
        P operator & (T&& a, T&& b) {
17
            return P(max(a.max, b.max));
19
        }
        P p[maxn << 2];
20
        Q q[maxn << 2];
21
    #define lson o * 2, l, (l + r) / 2
22
    #define rson o * 2 + 1, (l + r) / 2 + 1, r
        void up(int o, int l, int r) {
24
25
            if (l == r) p[o] = P();
            else p[o] = p[o * 2] & p[o * 2 + 1];
26
            p[o].up(q[o]);
27
28
        void down(int o, int l, int r) {
29
            q[o * 2] += q[o]; q[o * 2 + 1] += q[o];
            q[o] = Q();
31
32
            up(lson); up(rson);
33
        template<typename T>
34
        void build(T&& f, int o = 1, int l = 1, int r = n) {
35
            if (l == r) q[o] = f(l);
36
            else { build(f, lson); build(f, rson); q[o] = Q(); }
37
38
            up(o, l, r);
39
        P query(int ql, int qr, int 0 = 1, int l = 1, int r = n) {
```

```
if (ql > r || l > qr) return P();
41
42
            if (ql <= l && r <= qr) return p[o];</pre>
43
            down(o, l, r);
44
            return query(ql, qr, lson) & query(ql, qr, rson);
45
        void update(int ql, int qr, const Q& v, int o = 1, int l = 1, int r = n) {
46
            if (ql > r || l > qr) return;
47
            if (ql <= l && r <= qr) q[o] += v;</pre>
48
            else {
49
50
                 down(o, l, r);
                 update(ql, qr, v, lson); update(ql, qr, v, rson);
51
52
53
            up(o, l, r);
54
   }
55
56
57
    void solve(){
58
        vector<LL> arr = {1, 5, 7, 4, 2, 8, 3, 6, 10, 9};
59
60
        n = arr.size();
        SGT::build([&](int idx){
61
62
            return SGT::Q(arr[idx-1]);
63
        for(LL i=1; i<=n; i++){</pre>
            dbg(SGT::query(1, i).max);
65
66
        SGT::update(2, 4, SGT::Q(-3));
67
        cout << "MODIFIED\n";</pre>
68
        for(LL i=1; i<=n; i++){</pre>
            dbg(SGT::query(1, i).max);
70
71
   }
72
        • 区间修改,区间累加,查询区间和、最大值、最小值。
    #define maxn 100005
1
    #define INF LONG_LONG_MAX
   LL a[maxn], n;
    struct IntervalTree {
    #define ls \ o \ * \ 2, l, m
    #define rs \ o \ * \ 2 \ + \ 1, \ m \ + \ 1, \ r
        static const LL M = maxn * 4, RS = 1E18 - 1;
        LL addv[M], setv[M], minv[M], maxv[M], sumv[M];
        void init() {
10
            memset(addv, 0, sizeof addv);
11
12
            fill(setv, setv + M, RS);
            memset(minv, 0, sizeof minv);
13
            memset(maxv, 0, sizeof maxv);
14
            memset(sumv, \Theta, sizeof sumv);
15
16
17
        void maintain(LL o, LL l, LL r) {
            if (l < r) {
18
19
                 LL lc = o * 2, rc = o * 2 + 1;
                 sumv[o] = sumv[lc] + sumv[rc];
20
                 minv[o] = min(minv[lc], minv[rc]);
21
                 maxv[o] = max(maxv[lc], maxv[rc]);
22
            } else sumv[o] = minv[o] = maxv[o] = 0;
23
            if (setv[o] != RS) { minv[o] = maxv[o] = setv[o]; sumv[o] = setv[o] * (r - l + 1); }
24
            if (addv[o]) { minv[o] += addv[o]; maxv[o] += addv[o]; sumv[o] += addv[o] * (r - l + 1); }
25
        void build(LL o, LL l, LL r) {
27
            if (l == r) addv[o] = a[l];
28
29
            else {
                 LL m = (l + r) / 2;
30
31
                 build(ls); build(rs);
32
            }
            maintain(o, l, r);
33
34
35
        void pushdown(LL o) {
            LL lc = 0 * 2, rc = 0 * 2 + 1;
36
            if (setv[o] != RS) {
37
```

```
setv[lc] = setv[rc] = setv[o];
38
39
                 addv[lc] = addv[rc] = 0;
                 setv[o] = RS;
40
41
             if (addv[o]) {
42
                 addv[lc] += addv[o]; addv[rc] += addv[o];
43
                 addv[o] = 0;
44
             }
45
46
         void update(LL p, LL q, LL o, LL l, LL r, LL v, LL op) {
47
             if (p <= r && l <= q){
48
49
                 if (p <= l && r <= q) {
                     if (op == 2) { setv[o] = v; addv[o] = 0; }
50
                      else addv[o] += v;
51
52
                 } else {
                      pushdown(o);
53
                      LL m = (l + r) / 2;
54
                      update(p, q, ls, v, op); update(p, q, rs, v, op);
55
                 }
             }
57
58
             maintain(o, l, r);
59
         void query(LL p, LL q, LL o, LL l, LL r, LL add, LL& ssum, LL& smin, LL& smax) {
60
             if (p > r || l > q) return;
             if (setv[o] != RS) {
62
                 LL v = setv[o] + add + addv[o];
63
                 ssum += v * (min(r, q) - max(l, p) + 1);
64
                 smin = min(smin, v);
65
                 smax = max(smax, v);
             } else if (p <= l && r <= q) {
67
                 ssum += sumv[o] + add \star (r - l + 1);
68
                 smin = min(smin, minv[o] + add);
69
                 smax = max(smax, maxv[o] + add);
70
71
             } else {
                 LL m = (l + r) / 2;
72
                 query(p, q, ls, add + addv[o], ssum, smin, smax);
73
                 query(p, q, rs, add + addv[o], ssum, smin, smax);
74
75
             }
76
         }
         // 简化接口
77
78
         void build(int n) {
             build(1, 1, n);
79
80
81
         void range_add(int l, int r, int val) {
82
83
             update(l, r, 1, 1, n, val, 1);
84
85
         void range_set(int l, int r, int val) {
86
87
             update(l, r, 1, 1, n, val, 2);
88
89
         void range_query(int l, int r, LL& sum, LL& min_val, LL& max_val) {
             sum = 0;
91
92
             min_val = INF;
             max_val = -INF;
93
             query(l, r, 1, 1, n, \theta, sum, min_val, max_val);
94
95
         }
96
    } IT;
97
98
    void solve(){
99
        IT.init();
100
         n = 5;
101
102
         vector<int> data = {1, 3, 5, 7, 9};
         for (int i = 0; i < n; i++) {</pre>
103
104
             a[i + 1] = data[i]; // 注意: 线段树从 1 开始索引
105
         }
106
107
         IT.build(n);
108
```

```
LL sum, min_val, max_val;
109
          IT.range_query(1, 5, sum, min_val, max_val);
110
          cout << " " << sum << " " << min_val << " " << max_val << endl;
111
112
113
          IT.range_add(2, 4, 2);
         IT.range_query(1, 5, sum, min_val, max_val);
cout << " " << sum << " " << min_val << " " << max_val << endl;</pre>
114
115
116
          IT.range_set(3, 5, 10);
117
118
          IT.range_query(1, 5, sum, min_val, max_val);
          cout << " " << sum << " " << min_val << " " << max_val << endl;</pre>
119
120
121
          IT.range_query(2, 4, sum, min_val, max_val);
          cout << " " << sum << " " << min_val << " " << max_val << endl;
122
123
    }
```

#### 树状数组

- 单点修改,区间查询
- 频次统计下的 k 小值
- 维护差分数组时的区间修改, 单点查询

```
#define M 100005
2
   namespace BIT {
3
        LL c[M]; // 注意初始化开销
        inline int lowbit(int x) { return x & -x; }
        void add(int x, LL v) { // 单点加
            for (int i = x; i < M; i += lowbit(i))</pre>
                c[i] += v;
8
        LL sum(int x) { // 前缀和
10
            LL ret = 0;
            for (int i = x; i > 0; i -= lowbit(i))
12
                ret += c[i];
13
14
            return ret;
15
        int kth(LL k) { // 频次统计下从小到大第 k 个, 详见应用
            int p = 0;
17
            for (int lim = 1 << 20; lim; lim /= 2)</pre>
18
                if (p + lim < M && c[p + lim] < k) {</pre>
19
                    p += lim;
20
21
                    k = c[p];
                }
22
23
            return p + 1;
24
        LL sum(int l, int r) { return sum(r) - sum(l - 1); } // 区间和
25
        // 区间加(此时树状数组为差分数组, sum(x) 为第 x 个数的值)
26
        void add(int l, int r, LL v) { add(l, v); add(r + 1, -v); }
27
28
   // ---
29
    void solve(){
30
31
        vector<LL> a={9, 9, 9, 9, 5, 3, 3, 1, 1};
        LL n = a.size(), i;
32
33
        for(i=1; i<=n; i++) BIT::add(a[i-1], 1);</pre>
        // 1 1 3 3 3 5 9 9 9 9
34
        for(i=1; i<=n; i++) cout << BIT::kth(i) << ' ';</pre>
35
36
   }
       ● 区间修改、区间查询
   #define maxn 100005
   namespace BIT {
        int n;
        int c[maxn], cc[maxn];
       inline int lowbit(int x) { return x & -x; }
        void init(int siz){ // 初始化
            n = siz;
            for(LL i=0; i<=n; i++){</pre>
                c[i] = cc[i] = 0;
```

```
}
11
12
        void add(int x, int v) { // 不要用这个
13
            for (int i = x; i <= n; i += lowbit(i)) {</pre>
14
                 c[i] += v; cc[i] += x * v;
15
            }
16
17
        void add(int l, int r, int v) { add(l, v); add(r + 1, -v); } // 区间修改
18
        int sum(int x) { // 前缀和
19
20
             int ret = 0;
             for (int i = x; i > 0; i -= lowbit(i))
21
22
                 ret += (x + 1) * c[i] - cc[i];
23
            return ret;
24
        int sum(int l, int r) { return sum(r) - sum(l - 1); } // 区间和
25
    }
26
27
    // --
    void solve(){
28
29
        LL i, n=8;
        BIT::init(n);
30
        BIT::add(2, 4, 2);
31
        for(i=1; i<=n; i++) cout << BIT::sum(i, i) << ' ';</pre>
32
        cout << '\n';
33
        cout << BIT::sum(5) << '\n';</pre>
        cout << BIT::sum(2, 3) << '\n';</pre>
35
   }
36
        三维
    #define maxn 105
2
    namespace BIT{
3
        int n;
        LL c[maxn][maxn][maxn];
5
        inline int lowbit(int x) { return x & -x; }
        void init(int siz){
7
            n = siz;
            for(int i=0; i<=n; i++){</pre>
                 for(int j=0; j<=n; j++){</pre>
10
                     for(int k=0; k<=n; k++){
11
12
                          c[i][j][k] = 0;
13
                     }
                 }
14
            }
15
16
        void update(int x, int y, int z, int d) {
17
            for (int i = x; i <= n; i += lowbit(i))</pre>
18
                 for (int j = y; j <= n; j += lowbit(j))</pre>
19
                     for (int k = z; k <= n; k += lowbit(k))</pre>
20
                         c[i][j][k] += d;
21
22
23
        LL query(int x, int y, int z) {
            LL ret = 0;
24
25
            for (int i = x; i > 0; i -= lowbit(i))
                 for (int j = y; j > 0; j -= lowbit(j))
26
                     for (int k = z; k > 0; k -= lowbit(k))
27
                         ret += c[i][j][k];
28
29
            return ret;
        LL solve(int x, int y, int z, int xx, int yy, int zz) {
31
            return query(xx, yy, zz)
32
            - query(xx, yy, z - 1)
33
34
            - query(xx, y - 1, zz)
35
            - query(x - 1, yy, zz)
            + query(xx, y - 1, z - 1)
36
37
            + query(x - 1, yy, z - 1)
            + query(x - 1, y - 1, zz)
38
            - query(x - 1, y - 1, z - 1);
39
40
        }
   }
41
```

## 数学

## 快速乘

```
LL mul(LL a, LL b, LL m) {
       LL ret = 0;
        while (b) {
            if (b & 1) {
4
                ret += a;
                if (ret >= m) ret -= m;
            a += a;
            if (a >= m) a -= m;
            b >>= 1;
        }
11
        return ret;
12
13
   }
       • O(1)
   LL mul(LL u, LL v, LL p) {
        return (u * v - LL((long double) u * v / p) * p + p) % p;
   }
3
   LL mul(LL u, LL v, LL p) { // 卡常
        LL t = u * v - LL((long double) u * v / p) * p;
        return t < 0 ? t + p : t;
   }
```

## 高斯消元

- n 是方程个数, m 是未知量个数, a[n][m+1] 是增广矩阵
- x[m] 是每个未知量的解(如果有), free\_x[m] 是每个未知量是否为自由变量。

```
typedef double LD;
    const LD eps = 1E-10;
2
    const int maxn = 2000 + 10;
    int n, m;
    LD a[maxn][maxn], x[maxn];
    bool free_x[maxn];
    inline int sgn(LD x) { return (x > eps) - (x < -eps); }</pre>
    int gauss(LD a[maxn][maxn], int n, int m) {
11
    //int gauss() {
12
        memset(free_x, 1, sizeof free_x); memset(x, 0, sizeof x);
13
        int r = 0, c = 0;
14
        while (r < n \&\& c < m)  {
            int m_r = r;
16
            FOR (i, r + 1, n)
17
18
            if (fabs(a[i][c]) > fabs(a[m_r][c])) m_r = i;
            if (m r != r)
19
                 FOR (j, c, m + 1)
                 swap(a[r][j], a[m_r][j]);
21
22
            if (!sgn(a[r][c])) {
                 a[r][c] = 0;
23
                 ++c;
24
                 continue;
26
27
            FOR (i, r + 1, n)
            if (a[i][c]) {
28
                 LD t = a[i][c] / a[r][c];
29
                 FOR (j, c, m + 1) a[i][j] -= a[r][j] * t;
30
            }
31
32
            ++r; ++c;
33
        FOR (i, r, n)
34
        if (sgn(a[i][m])) return -1;
35
        if (r < m) {
36
37
            FORD (i, r - 1, -1) {
                 int f_{cnt} = 0, k = -1;
38
```

```
FOR (j, \theta, m)
39
40
                  if (sgn(a[i][j]) && free_x[j]) {
                      ++f_cnt;
41
                      k = j;
42
                  if(f_cnt > 0) continue;
44
                  LD s = a[i][m];
45
                  FOR (j, \theta, m)
46
                  if (j != k) s -= a[i][j] * x[j];
47
48
                  x[k] = s / a[i][k];
                  free_x[k] = 0;
49
             }
50
51
             return m - r;
52
        FORD (i, m - 1, -1) \{
53
             LD s = a[i][m];
54
55
             FOR (j, i + 1, m)
             s -= a[i][j] * x[j];
56
             x[i] = s / a[i][i];
        }
58
59
        return 0;
60
    }
```

### 快速幂

● 如果模数是素数,则可在函数体内加上 n %= MOD - 1; (费马小定理)。

```
LL bin(LL x, LL n, LL MOD) {
       LL ret = MOD != 1;
3
       for (x %= MOD; n; n >>= 1, x = x * x % MOD)
           if (n & 1) ret = ret * x % MOD;
       return ret;
5
   }
      ● 防爆 LL
       ● 前置模板: 快速乘
   LL bin(LL x, LL n, LL MOD) {
       LL ret = MOD != 1;
2
       for (x \% = MOD; n; n >>= 1, x = mul(x, x, MOD))
3
           if (n & 1) ret = mul(ret, x, MOD);
       return ret;
   }
6
```

## 高精度

- https://github.com/Baobaobear/MiniBigInteger/blob/main/bigint\_tiny.h, 带有压位优化
- 按需实现

```
#include <algorithm>
1
   #include <cstdio>
   #include <string>
   #include <vector>
    struct BigIntTiny {
        int sign;
        std::vector<int> v;
        BigIntTiny() : sign(1) {}
10
        BigIntTiny(const std::string &s) { *this = s; }
11
        BigIntTiny(int v) {
12
            char buf[21];
13
            sprintf(buf, "%d", v);
14
            *this = buf;
15
16
        void zip(int unzip) {
17
            if (unzip == 0) {
18
                for (int i = 0; i < (int)v.size(); i++)</pre>
19
                    v[i] = get_pos(i * 4) + get_pos(i * 4 + 1) * 10 + get_pos(i * 4 + 2) * 100 + get_pos(i * 4 + 3) * 1000;
20
21
            } else
```

```
for (int i = (v.resize(v.size() * 4), (int)v.size() - 1), a; i >= 0; i--)
22
23
                     a = (i % 4 >= 2) ? v[i / 4] / 100 : v[i / 4] % 100, v[i] = (i & 1) ? a / 10 : a % 10;
24
            setsign(1, 1);
        }
25
        int get_pos(unsigned pos) const { return pos >= v.size() ? 0 : v[pos]; }
        BigIntTiny &setsign(int newsign, int rev) {
27
             for (int i = (int)v.size() - 1; i > 0 && v[i] == 0; i--)
28
                 v.erase(v.begin() + i);
29
            sign = (v.size() == 0 \mid | (v.size() == 1 && v[0] == 0)) ? 1 : (rev ? newsign * sign : newsign);
30
31
            return *this;
32
33
        std::string to_str() const {
34
            BigIntTiny b = *this;
            std::string s;
35
            for (int i = (b.zip(1), 0); i < (int)b.v.size(); ++i)</pre>
36
                 s += char(*(b.v.rbegin() + i) + '0');
37
            return (sign < 0 ? "-" : "") + (s.empty() ? std::string("0") : s);</pre>
38
39
40
        bool absless(const BigIntTiny &b) const {
            if (v.size() != b.v.size()) return v.size() < b.v.size();</pre>
41
             for (int i = (int)v.size() - 1; i >= 0; i--)
42
                 if (v[i] != b.v[i]) return v[i] < b.v[i];</pre>
43
            return false;
44
45
        BigIntTiny operator-() const {
46
47
            BigIntTiny c = *this;
            c.sign = (v.size() > 1 || v[0]) ? -c.sign : 1;
48
            return c;
49
50
        BigIntTiny &operator=(const std::string &s) {
51
            if (s[0] == '-')
52
                 *this = s.substr(1);
53
            else {
54
55
                 for (int i = (v.clear(), 0); i < (int)s.size(); ++i)</pre>
                     v.push_back(*(s.rbegin() + i) - '0');
56
57
                 zip(0);
            }
58
            return setsign(s[0] == '-'? -1 : 1, sign = 1);
59
60
        bool operator<(const BigIntTiny &b) const {</pre>
61
62
            return sign != b.sign ? sign < b.sign : (sign == 1 ? absless(b) : b.absless(*this));</pre>
63
        bool operator==(const BigIntTiny &b) const { return v == b.v && sign == b.sign; }
64
65
        BigIntTiny &operator+=(const BigIntTiny &b) {
            if (sign != b.sign) return *this = (*this) - -b;
66
67
            v.resize(std::max(v.size(), b.v.size()) + 1);
            for (int i = 0, carry = 0; i < (int)b.v.size() || carry; i++) {</pre>
68
                 carry += v[i] + b.get_pos(i);
                 v[i] = carry % 10000, carry /= 10000;
70
71
            return setsign(sign, 0);
72
73
        BigIntTiny operator+(const BigIntTiny &b) const {
            BigIntTiny c = *this;
75
            return c += b;
76
77
        void add_mul(const BigIntTiny &b, int mul) {
78
            v.resize(std::max(v.size(), b.v.size()) + 2);
79
80
            for (int i = 0, carry = 0; i < (int)b.v.size() || carry; i++) {</pre>
                 carry += v[i] + b.get_pos(i) * mul;
81
                 v[i] = carry % 10000, carry /= 10000;
82
            }
83
84
        BigIntTiny operator-(const BigIntTiny &b) const {
85
86
            if (b.v.empty() || b.v.size() == 1 && b.v[0] == 0) return *this;
            if (sign != b.sign) return (*this) + -b;
87
88
            if (absless(b)) return -(b - *this);
            BigIntTiny c;
            for (int i = 0, borrow = 0; i < (int)v.size(); i++) {</pre>
90
                 borrow += v[i] - b.get_pos(i);
91
                 c.v.push_back(borrow);
92
```

```
c.v.back() -= 10000 * (borrow >>= 31);
93
94
             }
95
             return c.setsign(sign, 0);
96
         }
97
         BigIntTiny operator*(const BigIntTiny &b) const {
             if (b < *this) return b * *this;</pre>
98
             BigIntTiny c, d = b;
99
             for (int i = 0; i < (int)v.size(); i++, d.v.insert(d.v.begin(), 0))</pre>
100
                 c.add_mul(d, v[i]);
101
102
             return c.setsign(sign * b.sign, 0);
103
104
         BigIntTiny operator/(const BigIntTiny &b) const {
             BigIntTiny c, d;
105
             BigIntTiny e=b;
106
107
             e.sign=1;
108
             d.v.resize(v.size());
             double db = 1.0 / (b.v.back() + (b.get_pos((unsigned)b.v.size() - 2) / 1e4) +
110
111
                                  (b.get_pos((unsigned)b.v.size() - 3) + 1) / 1e8);
             for (int i = (int)v.size() - 1; i >= 0; i--) {
112
                 c.v.insert(c.v.begin(), v[i]);
113
                 int m = (int)((c.get_pos((int)e.v.size()) * 10000 + c.get_pos((int)e.v.size() - 1)) * db);
114
                 c = c - e * m, c.setsign(c.sign, \theta), d.v[i] += m;
115
                 while (!(c < e))
116
                      c = c - e, d.v[i] += 1;
117
             }
118
119
             return d.setsign(sign * b.sign, 0);
120
         BigIntTiny operator%(const BigIntTiny &b) const { return *this - *this / b * b; }
121
         bool operator>(const BigIntTiny &b) const { return b < *this; }</pre>
122
         bool operator<=(const BigIntTiny &b) const { return !(b < *this); }</pre>
123
         bool operator>=(const BigIntTiny &b) const { return !(*this < b); }</pre>
124
         bool operator!=(const BigIntTiny &b) const { return !(*this == b); }
125
    };
    矩阵运算
    #define MOD 998244353
2
    #define M 10
3
4
    struct Mat {
        LL m;
         LL v[M][M];
         Mat(int siz=2) {
             m = siz;
8
             for(int i=0; i<=m; i++){</pre>
                 for(int j=0; j<=m; j++){</pre>
10
                      v[i][j] = 0;
11
                 }
12
             }
13
14
15
         void eye() { FOR (i, 0, m) v[i][i] = 1; }
         LL* operator [] (LL x) { return v[x]; }
16
17
         const LL* operator [] (LL x) const { return v[x]; }
         Mat operator * (const Mat& B) {
18
19
             const Mat& A = *this;
20
             Mat ret;
21
             FOR (k, 0, m)
22
             FOR (i, 0, m) if (A[i][k])
                 FOR (j, 0, m)
23
24
                  ret[i][j] = (ret[i][j] + A[i][k] * B[k][j]) % MOD;
             return ret;
25
27
         Mat pow(LL n) const {
             Mat A = *this, ret; ret.eye();
28
29
             for (; n; n >>= 1, A = A \star A)
                 if (n & 1) ret = ret * A;
30
31
             return ret;
32
         Mat operator + (const Mat& B) {
33
             const Mat& A = *this:
34
```

```
Mat ret;
35
36
            FOR (i, \Theta, m)
            FOR (j, \Theta, m)
37
            ret[i][j] = (A[i][j] + B[i][j]) % MOD;
38
            return ret;
40
41
        void pprint() const {
            FOR (i, 0, m)
42
            FOR (j, 0, m)
43
            printf("%lld%c", (*this)[i][j], j == m - 1 ? '\n' : ' ');
44
45
46
   };
47
    //
    void solve(){
48
        Mat mat1, mat2;
49
50
        mat1.eye();
51
        mat1[1][0] = 2; // 0-based
        mat2.eye();
52
53
        mat2[1][1] = 4;
        Mat mat3 = mat1 * mat2;
54
55
        mat3.pprint();
   }
56
    数论分块
    f(i) = \left| \frac{n}{i} \right| = v 时 i 的取值范围是 [l, r]。
    void sqrt_decomposition(LL n){
        for (LL l = 1, v, r; l <= n; l = r + 1) {
            v = n / l; r = n / v;
            printf("%lld / [%lld, %lld] = %lld\n", n, l, r, v);
        }
   }
    质数筛
       \bullet \mathcal{O}(n)
   const LL p_max = 1E6 + 100;
   LL pr[p_max], p_sz;
    void get_prime() {
        static bool vis[p_max];
        FOR (i, 2, p_max) {
5
            if (!vis[i]) pr[p_sz++] = i;
            FOR (j, 0, p_sz) {
                 if (pr[j] * i >= p_max) break;
8
                 vis[pr[j] * i] = 1;
                 if (i % pr[j] == 0) break;
            }
        }
12
   }
13
    欧拉函数
    朴素
    int phi(int x)
1
2
        int res = x;
        for (int i = 2; i <= x / i; i ++ )</pre>
             if (x % i == 0)
             {
                 res = res / i * (i - 1);
                 while (x % i == 0) x /= i;
        if (x > 1) res = res / x * (x - 1);
11
        return res;
12
   }
13
```

#### 筛法求欧拉函数

● 前置模板: 质数筛

```
const LL p_max = 1E5 + 100;
   LL phi[p_max];
   void get_phi() {
        phi[1] = 1;
        static bool vis[p_max];
        static LL prime[p_max], p_sz, d;
        FOR (i, 2, p_max) {
            if (!vis[i]) {
                prime[p_sz++] = i;
                phi[i] = i - 1;
10
11
            for (LL j = 0; j < p_sz && (d = i * prime[j]) < p_max; ++j) {
12
13
                vis[d] = 1;
14
                if (i % prime[j] == 0) {
                    phi[d] = phi[i] * prime[j];
15
16
                    break;
17
                else phi[d] = phi[i] * (prime[j] - 1);
18
19
            }
        }
20
   }
```

## 素性测试

#### 试除法

2

3

•  $\mathcal{O}(\sqrt{n})$ 

```
bool is_prime(int x)
{
    if (x < 2) return false;
    for (int i = 2; i <= x / i; i ++ )
        if (x % i == 0)
            return false;
    return true;
}</pre>
```

#### Miller-Rabin

- 前置: 快速幂
- $\mathcal{O}(k \times \log^3 n)$

```
bool miller_rabin(LL n) {
        static vector<LL> tester = {2, 3, 5, 7, 11, 13, 17, 19, 23, 29, 31, 37};
2
        if (n < 3 || n % 2 == 0) return n == 2;</pre>
        if (n % 3 == 0) return n == 3;
        LL u = n - 1, t = 0;
        while (u % 2 == 0) u /= 2, ++t;
        for (auto nt: tester) {
            if(nt >= n) continue;
            LL v = bin(nt, u, n);
            if (v == 1) continue;
            LL s;
11
            for (s = 0; s < t; ++s) {
12
                if (v == n - 1) break;
13
                v = v * v % n;
14
15
16
            if (s == t) return false;
        return true;
18
   }
19
```

```
质因数分解
    朴素质因数分解
       • 前置模板:素数筛
       • 带指数
       • \mathcal{O}(\frac{\sqrt{N}}{\ln N})
    LL factor[30], f_sz, factor_exp[30];
    void get_factor(LL x) {
        f_sz = 0;
        LL t = sqrt(x + 0.5);
        for (LL i = 0; pr[i] <= t; ++i)</pre>
5
            if (x % pr[i] == 0) {
                factor_exp[f_sz] = 0;
                while (x % pr[i] == 0) {
                    x /= pr[i];
                     ++factor_exp[f_sz];
10
                }
11
                factor[f_sz++] = pr[i];
12
            }
        if (x > 1) {
14
            factor_exp[f_sz] = 1;
15
16
            factor[f_sz^{++}] = x;
17
   }
       • 不带指数
    LL factor[30], f_sz;
    void get_factor(LL x) {
        f_sz = 0;
        LL t = sqrt(x + 0.5);
4
        for (LL i = 0; pr[i] <= t; ++i)</pre>
            if (x % pr[i] == 0) {
                factor[f_sz++] = pr[i];
                while (x % pr[i] == 0) x /= pr[i];
10
        if (x > 1) factor[f_sz++] = x;
   }
11
```

#### Pollard-Rho

• 前置:素数测试

```
mt19937 mt(time(0));
    LL pollard_rho(LL n, LL c) {
        LL x = uniform_int_distribution < LL > (1, n - 1)(mt), y = x;
        auto f = [\&](LL \ v) \{ LL \ t = mul(v, v, n) + c; return \ t < n ? \ t : t - n; \};
        while (1) {
            x = f(x); y = f(f(y));
            if (x == y) return n;
            LL d = gcd(abs(x - y), n);
            if (d != 1) return d;
        }
10
11
   }
12
    LL fac[100], fcnt;
13
    void get_fac(LL n, LL cc = 19260817) {
14
        if (n == 4) { fac[fcnt++] = 2; fac[fcnt++] = 2; return; }
15
16
        if (miller_rabin(n)) { fac[fcnt++] = n; return; }
        LL p = n;
17
        while (p == n) p = pollard_rho(n, --cc);
        get_fac(p); get_fac(n / p);
19
20
21
   void go_fac(LL n) { fcnt = 0; if (n > 1) get_fac(n); }
```

## 原根

- 前置模板: 质因数分解、快速幂
- 要求 p 为质数
- 别忘了调用质因数分解的函数

```
LL find_smallest_primitive_root(LL p) {
2
        get_factor(p - 1);
        FOR (i, 2, p) {
3
            bool flag = true;
            FOR (j, 0, f_sz)
            if (bin(i, (p - 1) / factor[j], p) == 1) {
                flag = false;
                break;
            if (flag) return i;
10
11
        }
12
       assert(0);
        return -1;
13
```

#### 欧几里得

朴素

```
int gcd(int a, int b)
1
2
   {
        return b ? gcd(b, a % b) : a;
3
   }
       ● 卡常
    inline int ctz(LL x) { return __builtin_ctzll(x); }
   LL gcd(LL a, LL b) {
2
        if (!a) return b; if (!b) return a;
        int t = ctz(a | b);
4
        a >>= ctz(a);
5
        do {
            b >>= ctz(b);
            if (a > b) swap(a, b);
            b -= a;
        } while (b);
11
        return a << t;</pre>
   }
12
```

#### 扩展欧几里得

- 求 ax + by = gcd(a, b) 的一组解
- 如果 a 和 b 互素, 那么 x 是 a 在模 b 下的逆元
- 注意 *x* 和 *y* 可能是负数

```
LL ex_gcd(LL a, LL b, LL &x, LL &y) {
    if (b == 0) { x = 1; y = 0; return a; }

LL ret = ex_gcd(b, a % b, y, x);

y -= a / b * x;

return ret;

}
```

## 二次剩余

- 求解二次同余方程
- 给定 a, p,求一组 x 满足  $x^2 \equiv a \pmod{p}$
- 前置模板: 快速幂

```
1  LL q1, q2, w;
2  struct P { // x + y * sqrt(w)}
3   LL x, y;
4  };
```

```
P pmul(const P& a, const P& b, LL p) {
6
7
       res.x = (a.x * b.x + a.y * b.y % p * w) % p;
8
       res.y = (a.x * b.y + a.y * b.x) % p;
10
       return res;
   }
11
12
   P bin(P x, LL n, LL MOD) {
13
       P ret = \{1, 0\};
14
       for (; n; n >>= 1, x = pmul(x, x, MOD))
15
          if (n & 1) ret = pmul(ret, x, MOD);
16
17
       return ret;
   }
18
   LL Legendre(LL a, LL p) { return bin(a, (p - 1) >> 1, p); }
19
20
   LL equation_solve(LL b, LL p) {
21
       if (p == 2) return 1;
22
       if ((Legendre(b, p) + 1) % p == 0)
23
24
           return -1;
       LL a;
25
       while (true) {
26
27
          a = rand() % p;
28
           w = ((a * a - b) \% p + p) \% p;
           if ((Legendre(w, p) + 1) % p == 0)
30
              break;
31
       }
       return bin({a, 1}, (p + 1) >> 1, p).x;
32
   }
33
   34
   void solve(){
35
       LL a, p; cin >> a >> p;
36
       a = a % p;
37
38
       LL x = equation_solve(a, p);
       if (x == -1) {
39
           puts("No root");
40
41
       } else {
           LL y = p - x;
42
           if (x == y){
43
              cout << x << endl;</pre>
44
           }else{
45
46
              LL tx = min(x, y), ty = max(x, y);
              cout << tx << " " << ty << endl;
47
48
49
       }
50
   51
```

## 中国剩余定理

• 求解线性同余方程组

•

$$\begin{cases} x & \equiv r_1 \pmod{m_1} \\ x & \equiv r_2 \pmod{m_2} \\ & \vdots \\ x & \equiv r_k \pmod{m_k} \end{cases}$$

- 无解返回 -1
- 前置模板: 扩展欧几里得

```
1 LL CRT(LL *m, LL *r, LL n) {
2    if (!n) return 0;
3    LL M = m[0], R = r[0], x, y, d;
4    FOR (i, 1, n) {
5         d = ex_gcd(M, m[i], x, y);
6         if ((r[i] - R) % d) return -1;
7         x = (r[i] - R) / d * x % (m[i] / d);
```

```
// 防爆 LL
8
           // x = mul((r[i] - R) / d, x, m[i] / d);
           R += x * M;
10
           M = M / d * m[i];
11
          R %= M;
       }
13
14
       return R >= 0 ? R : R + M;
   }
15
   逆元
      ● 如果 p 是素数, 使用快速幂 (费马小定理)
      ● 前置模板: 快速幂
   inline LL get_inv(LL x, LL p) { return bin(x, p - 2, p); }
       如果 p 不是素数,使用拓展欧几里得
       ● 前置模板: 扩展欧几里得
   LL get_inv(LL a, LL M) {
       static LL x, y;
2
       assert(exgcd(a, M, x, y) == 1);
       return (x % M + M) % M;
      ● 预处理 1~n 的逆元
   LL inv[N];
   void inv_init(LL n, LL p) {
       inv[1] = 1;
       FOR (i, 2, n)
5
          inv[i] = (p - p / i) * inv[p % i] % p;
   }
       • 预处理阶乘及其逆元
   LL invf[M], fac[M] = {1};
1
   void fac_inv_init(LL n, LL p) {
       FOR (i, 1, n)
3
           fac[i] = i * fac[i - 1] % p;
       invf[n - 1] = bin(fac[n - 1], p - 2, p);
       FORD (i, n - 2, -1)
          invf[i] = invf[i + 1] * (i + 1) % p;
   }
   组合数
   组合数预处理 (递推法)
   LL C[M][M];
   void init_C(int n) {
2
       FOR (i, 0, n) {
          C[i][0] = C[i][i] = 1;
           FOR (j, 1, i)
              C[i][j] = (C[i - 1][j] + C[i - 1][j - 1]) % MOD;
   }
   预处理逆元法
      • 如果数较小,模较大时使用逆元
       • 前置模板: 逆元-预处理阶乘及其逆元
   inline LL C(LL n, LL m) \{ // n >= m >= 0 \}
2
       return n < m \mid \mid m < 0 ? 0 : fac[n] * invf[m] % MOD * invf[n - m] % MOD;
   }
3
```

#### Lucas 定理

```
● 如果模数较小,数字较大,使用 Lucas 定理
● 前置模板可选 1: 求组合数(如果使用阶乘逆元,需 fac_inv_init(MOD, MOD);)
```

#### 求具体值

• 分解质因数法

```
int primes[N], cnt;
                         // 存储所有质数
                 // 存储每个质数的次数
   int sum[N];
                   // 存储每个数是否已被筛掉
   bool st[N];
   void get_primes(int n)
                               // 线性筛法求素数
        for (int i = 2; i <= n; i ++ )</pre>
8
        {
            if (!st[i]) primes[cnt ++ ] = i;
            for (int j = 0; primes[j] <= n / i; j ++ )</pre>
10
11
            {
                st[primes[j] * i] = true;
12
                if (i % primes[j] == 0) break;
13
14
        }
15
16
   }
17
18
    int get(int n, int p)
                              // 求 n! 中的次数
19
    {
20
21
        int res = 0;
        while (n)
22
23
            res += n / p;
24
            n /= p;
25
27
        return res;
   }
28
29
30
   vector<int> mul(vector<int> a, int b) // 高精度乘低精度模板
32
33
        vector<int> c;
        int t = 0;
34
        for (int i = 0; i < a.size(); i ++ )</pre>
35
37
            t += a[i] * b;
            c.push_back(t % 10);
38
            t /= 10;
39
        }
40
41
        while (t)
42
43
            c.push_back(t % 10);
44
45
            t /= 10;
        }
46
47
48
        return c;
```

```
}
49
50
    get_primes(a); // 预处理范围内的所有质数
51
52
                                      // 求每个质因数的次数
   for (int i = 0; i < cnt; i ++ )</pre>
54
   {
55
        int p = primes[i];
        sum[i] = get(a, p) - get(b, p) - get(a - b, p);
56
   }
57
58
    vector<int> res;
59
    res.push_back(1);
61
    for (int i = 0; i < cnt; i ++ ) // 用高精度乘法将所有质因子相乘
62
        for (int j = 0; j < sum[i]; j ++ )</pre>
63
            res = mul(res, primes[i]);
64
    FFT & NTT & FWT
    FFT
       • 计算多项式乘法, 可用于高精度乘法
       • \mathcal{O}(n \log n)
    typedef double LD;
    const LD PI = acos(-1.0);
    struct Complex {
        LD r, i;
        Complex(LD r = 0, LD i = 0) : r(r), i(i) {}
        Complex operator + (const Complex& other) const {
            return Complex(r + other.r, i + other.i);
        Complex operator - (const Complex& other) const {
10
11
            return Complex(r - other.r, i - other.i);
12
13
        Complex operator * (const Complex& other) const {
            return Complex(r * other.r - i * other.i, r * other.i + i * other.r);
14
15
   };
16
17
    // 快速傅里叶变换, p=1 为正向, p=-1 为反向
18
    void FFT(vector<Complex>& x, int p) {
19
        int n = x.size();
21
        for (int i = 0, t = 0; i < n; ++i) {
            if (i > t) swap(x[i], x[t]);
22
            for (int j = n >> 1; (t ^{-}= j) < j; j >>= 1);
23
24
        for (int h = 2; h <= n; h <<= 1) {
            Complex wn(cos(p * 2 * PI / h), sin(p * 2 * PI / h));
26
            for (int i = 0; i < n; i += h) {</pre>
27
28
                Complex w(1, 0);
                for (int j = 0; j < h / 2; ++j) {
29
                    Complex u = x[i + j];
                    Complex v = x[i + j + h/2] * w;
31
32
                    x[i + j] = u + v;
                    x[i + j + h/2] = u - v;
33
                    w = w * wn;
34
35
                }
            }
36
37
        if (p == −1) {
38
            for (int i = 0; i < n; ++i) {</pre>
39
40
                x[i].r /= n;
            }
41
42
   }
43
44
    // 计算两个多项式的卷积, 返回结果多项式的系数向量
45
    vector<LD> convolution(const vector<LD>& a, const vector<LD>& b) {
46
47
        int len = 1;
```

```
int n = a.size(), m = b.size();
48
49
        while (len < n + m - 1) len <<= 1;</pre>
        vector<Complex> fa(len), fb(len);
50
        for (int i = 0; i < n; ++i) fa[i] = Complex(a[i], 0);</pre>
51
52
        for (int i = 0; i < m; ++i) fb[i] = Complex(b[i], 0);</pre>
        FFT(fa, 1);
53
        FFT(fb, 1);
54
        for (int i = 0; i < len; ++i) {</pre>
55
            fa[i] = fa[i] * fb[i];
56
57
        FFT(fa, -1);
58
59
        vector<LD> res(n + m - 1);
        for (int i = 0; i < n + m - 1; ++i) {</pre>
60
            res[i] = fa[i].r;
61
        }
62
        return res;
63
    }
    NTT
        • 用于大整数乘法时,位数不宜过高(在 MOD=998244353 的情况下,总位数不超过 12324004(3510^2)))
        ● 前置模板: 快速幂、逆元
    const int N = 1e5+10;
    const int MOD = 998244353; // 模数
    const int G = 3; // 原根
    LL wn[N << 2], rev[N << 2];
    int NTT_init(int n_) {
        int step = 0; int n = 1;
        for ( ; n < n_; n <<= 1) ++step;</pre>
        FOR (i, 1, n)
        rev[i] = (rev[i >> 1] >> 1) | ((i & 1) << (step - 1));
10
11
        int g = bin(G, (MOD - 1) / n, MOD);
        wn[0] = 1;
12
        for (int i = 1; i <= n; ++i)</pre>
13
           wn[i] = wn[i - 1] * g % MOD;
14
        return n;
15
16
    }
17
18
    void NTT(vector<LL> &a, int n, int f) {
        FOR (i, 0, n) if (i < rev[i])
19
            std::swap(a[i], a[rev[i]]);
20
21
        for (int k = 1; k < n; k <<= 1) {
            for (int i = 0; i < n; i += (k << 1)) {
   int t = n / (k << 1);</pre>
22
23
                 FOR (j, 0, k) {
24
                     LL w = f == 1 ? wn[t * j] : wn[n - t * j];
25
                     LL x = a[i + j];
26
                     LL y = a[i + j + k] * w % MOD;
27
28
                     a[i + j] = (x + y) % MOD;
                     a[i + j + k] = (x - y + MOD) \% MOD;
29
                 }
30
            }
31
32
        if (f == -1) {
33
            LL ninv = get_inv(n, MOD);
34
            FOR (i, 0, n)
            a[i] = a[i] * ninv % MOD;
36
37
    }
38
39
    vector<LL> conv(vector<LL> a, vector<LL> b){
        int len_a = a.size(), len_b = b.size();
41
        int len = len_a + len_b - 1;
42
        int n = NTT_init(len);
43
        a.resize(n);
44
45
        b.resize(n);
        NTT(a, n, 1);
46
        NTT(b, n, 1);
47
        vector<LL> c(n);
48
```

```
for (int i = 0; i < n; ++i) {
49
50
            c[i] = a[i] * b[i] % MOD;
51
        NTT(c, n, -1);
52
53
        vector<LL> res(len);
        for (int i = 0; i < len; ++i) {</pre>
54
55
            res[i] = c[i];
56
        return res;
57
58
    }
    FWT
    const LL MOD = 998244353;
2
    template<typename T>
    void fwt(vector<LL> &a, int n, T f) {
        for (int d = 1; d < n; d *= 2)</pre>
            for (int i = 0, t = d * 2; i < n; i += t)
                 FOR (j, 0, d)
                 f(a[i + j], a[i + j + d]);
    }
    void AND(LL& a, LL& b) { a += b; }
11
12
    void OR(LL& a, LL& b) { b += a; }
    \boldsymbol{\text{void}} XOR (LL& a, LL& b) {
13
        LL x = a, y = b;
14
        a = (x + y) \% MOD;
15
        b = (x - y + MOD) \% MOD;
16
17
    void rAND(LL& a, LL& b) { a -= b; }
18
    void rOR(LL& a, LL& b) { b -= a; }
19
    void rXOR(LL& a, LL& b) {
        static LL INV2 = (MOD + 1) / 2;
21
22
        LL x = a, y = b;
        a = (x + y) * INV2 % MOD;
23
        b = (x - y + MOD) * INV2 % MOD;
24
25
26
27
    int next_power_of_two(int n) {
        if (n <= 0) return 1;
28
        // __lg(n-1) 返回 n-1 的最高位所在位置 (0-based)
29
        return 1 << (__lg(n - 1) + 1);
30
    }
31
32
    template<typename T, typename F>
33
    vector<LL> conv(vector<LL> a, vector<LL> b, T f, F inv_f){
        LL len_a = a.size(), len_b = b.size(), len = max(len_a, len_b), n = next_power_of_two(len);
35
        a.resize(n), b.resize(n);
36
        fwt(a, n, f), fwt(b, n, f);
37
        vector<LL> c(n);
38
        for (int i = 0; i < n; i++) {</pre>
39
            c[i] = a[i] * b[i] % MOD;
40
41
        fwt(c, n, inv_f);
42
        // 提取结果 (可选)
43
44
        c.resize(len);
45
        return c;
    }
    线性基
    贪心法
    可查询最大异或和
    struct BasisGreedy{
        ULL p[64];
        BasisGreedy(){memset(p, 0, sizeof p);}
        void insert(ULL x) {
```

```
for (int i = 63; ~i; --i) {
                 if (!(x >> i)) // x 的第 i 位是 0
                     continue;
                 if (!p[i]) {
                     p[i] = x;
                     break;
10
11
                 x ^= p[i];
12
            }
13
14
        ULL query_max(){
15
16
             ULL ans = 0;
             for (int i = 63; ~i; --i) {
17
                 ans = std::max(ans, ans ^ p[i]);
18
            }
19
20
            return ans;
21
    };
22
    高斯消元法
    可查询任意大异或和
    struct BasisGauss{
1
        vector<ULL> a;
2
        LL n, tmp, cnt;
3
5
        BasisGauss()\{a = \{0\};\}
        void insert(ULL x){
             a.push_back(x);
        }
10
        void init(){
11
            n = (LL)a.size() - 1;
12
             LL k=1;
13
             for(int i=63;i>=0;i--){
14
                 int t=0;
15
16
                 for(LL j=k;j<=n;j++){</pre>
                     if((a[j]>>i)&1){
17
18
                          t=j;
                          break;
19
                     }
20
21
                 if(t){
22
                     swap(a[k],a[t]);
                     for(LL j=1;j<=n;j++){</pre>
24
                          if(j!=k&&(a[j]>>i)&1) a[j]^=a[k];
25
26
                     k++;
27
                 }
            }
29
30
             cnt = k-1;
             tmp = 1LL << cnt;</pre>
31
            if(cnt==n) tmp--;
32
33
34
35
        LL query_xth(LL x){ // 从小到大, 若 x 为负数,则查询倒数第几个
             if(x<0) x = tmp + x + 1;
36
37
             if(x>tmp) return -1;
             else{
38
                 if(n>cnt) x--;
39
40
                 LL ans=0;
                 for(LL i=0; i<cnt; i++){</pre>
41
                     if((x>>i)&1) ans^=a[cnt-i];
42
43
                 return ans;
44
45
            }
        }
46
    };
```

## 性质与公式

#### 低阶等幂求和

 $\begin{array}{l} \bullet \ \, \sum_{i=1}^n i^1 = \frac{n(n+1)}{2} = \frac{1}{2}n^2 + \frac{1}{2}n \\ \bullet \ \, \sum_{i=1}^n i^2 = \frac{n(n+1)(2n+1)}{6} = \frac{1}{3}n^3 + \frac{1}{2}n^2 + \frac{1}{6}n \\ \bullet \ \, \sum_{i=1}^n i^3 = \left[\frac{n(n+1)}{2}\right]^2 = \frac{1}{4}n^4 + \frac{1}{2}n^3 + \frac{1}{4}n^2 \\ \bullet \ \, \sum_{i=1}^n i^4 = \frac{n(n+1)(2n+1)(3n^2+3n-1)}{30} = \frac{1}{5}n^5 + \frac{1}{2}n^4 + \frac{1}{3}n^3 - \frac{1}{30}n \\ \bullet \ \, \sum_{i=1}^n i^5 = \frac{n^2(n+1)^2(2n^2+2n-1)}{12} = \frac{1}{6}n^6 + \frac{1}{2}n^5 + \frac{5}{12}n^4 - \frac{1}{12}n^2 \end{array}$ 

#### 一些组合公式

- 错排公式 (对于  $1 \sim n$  的排列 P,满足  $P_i \neq i$ ):  $D_1 = 0, D_2 = 1, D_n = (n-1)(D_{n-1} + D_{n-2}) = n!(\frac{1}{2!} \frac{1}{3!} + \dots + (-1)^n \frac{1}{n!}) = \lfloor \frac{n!}{e} + 0.5 \rfloor$
- 卡塔兰数 (n) 对括号合法方案数,n 个结点二叉树个数, $n\times n$  方格中对角线下方的单调路径数,凸 n+2 边形的三角形划分数,n 个元素的合法出栈序列数):  $C_n=\frac{1}{n+1}\binom{2n}{n}=\frac{(2n)!}{(n+1)!n!}$

#### 互质

若整数 a 与 m 互质(即 gcd(a, m) = 1)

- 对于整数 k = 0, 1, 2, ..., m 1,  $ak \mod m$  的结果恰好是 0, 1, 2, ..., m 1 的一个**排列**(每个数出现且仅出现一次)。
- 存在唯一的整数 b  $(1 \le b < m)$ ,使得  $ab \equiv 1 \mod m$ ,此时 b 称为 a 在模 m 下的**乘法逆元**(记为  $a^{-1} \mod m$ )。

## 图论

### 最近公共祖先

```
const LL N = 5e5+10, SP = log2(N)+1;
    vector<int> G[N];
    int pa[N][SP], dep[N];
    void dfs(int u, int fa) {
        pa[u][0] = fa; dep[u] = dep[fa] + 1;
        FOR (i, 1, SP) pa[u][i] = pa[pa[u][i - 1]][i - 1];
        for (int& v: G[u]) {
            if (v == fa) continue;
            dfs(v, u);
10
11
        }
   }
12
    int lca(int u, int v) {
14
        if (dep[u] < dep[v]) swap(u, v);</pre>
15
        int t = dep[u] - dep[v];
16
        FOR (i, 0, SP) if (t & (1 << i)) u = pa[u][i];
17
        FORD (i, SP - 1, -1) {
            int uu = pa[u][i], vv = pa[v][i];
19
            if (uu != vv) { u = uu; v = vv; }
21
        return u == v ? u : pa[u][0];
22
```

#### 网络流

● 最大流

```
const LL INF = LONG_LONG_MAX;

struct E {
    LL to, cp;
    E(LL to, LL cp): to(to), cp(cp) {}
};

struct Dinic {
```

```
static const LL M = 1E5 * 5;
10
        LL m, s, t;
        vector<E> edges;
11
        vector<LL> G[M];
12
13
        LL d[M];
        LL cur[M];
14
15
        void init(LL n, LL s, LL t) {
16
             this->s = s; this->t = t;
17
             for (LL i = 0; i <= n; i++) G[i].clear();</pre>
18
             edges.clear(); m = 0;
19
20
21
        void addedge(LL u, LL v, LL cap) {
22
             edges.emplace_back(v, cap);
23
             edges.emplace_back(u, 0);
24
25
             G[u].push_back(m++);
             G[v].push_back(m++);
26
27
        }
28
        bool BFS() {
29
30
            memset(d, 0, sizeof d);
             queue<LL> Q;
31
             Q.push(s); d[s] = 1;
32
             while (!Q.empty()) {
33
                 LL x = Q.front(); Q.pop();
34
                 for (LL& i: G[x]) {
35
                     E &e = edges[i];
36
37
                     if (!d[e.to] && e.cp > 0) {
                          d[e.to] = d[x] + 1;
38
                          Q.push(e.to);
39
                     }
40
41
                 }
42
             }
             return d[t];
43
44
45
        LL DFS(LL u, LL cp) {
46
47
            if (u == t || !cp) return cp;
            LL tmp = cp, f;
48
49
             for (LL& i = cur[u]; i < G[u].size(); i++) {</pre>
                 E& e = edges[G[u][i]];
50
                 if (d[u] + 1 == d[e.to]) {
51
52
                     f = DFS(e.to, min(cp, e.cp));
                     e.cp -= f;
53
54
                     edges[G[u][i] ^{\land} 1].cp += f;
                     cp -= f;
55
                     if (!cp) break;
                 }
57
58
59
            return tmp - cp;
        }
60
        LL go() {
62
63
             LL flow = 0;
             while (BFS()) {
64
                 memset(cur, 0, sizeof cur);
65
                 flow += DFS(s, INF);
67
            return flow;
68
69
    } DC;
        ● 最小费用最大流
    const LL M = 5e4+10;
    const int INF = INT_MAX;
2
    struct E {
        int from, to, cp, v;
5
        E() {}
        E(int f, int t, int cp, int v) : from(f), to(t), cp(cp), v(v) {}
```

```
16
        void init(int _n, int _s, int _t) {
17
            n = _n; s = _s; t = _t;
18
19
            FOR (i, 0, n + 1) G[i].clear();
            edges.clear(); m = 0;
20
21
22
        void addedge(int from, int to, int cap, int cost) {
23
24
            edges.emplace_back(from, to, cap, cost);
            edges.emplace_back(to, from, \theta, -cost);
25
            G[from].push_back(m++);
            G[to].push_back(m++);
27
        }
28
29
        bool BellmanFord(int &flow, int &cost) {
30
            FOR (i, 0, n + 1) d[i] = INF;
            \texttt{memset(inq, 0, sizeof inq);}
32
33
            d[s] = 0, a[s] = INF, inq[s] = true;
            queue<int> Q; Q.push(s);
34
            while (!Q.empty()) {
35
                int u = Q.front(); Q.pop();
                inq[u] = false;
37
                 for (int& idx: G[u]) {
38
                     E &e = edges[idx];
39
                     if (e.cp && d[e.to] > d[u] + e.v) {
40
41
                         d[e.to] = d[u] + e.v;
                         p[e.to] = idx;
42
43
                         a[e.to] = min(a[u], e.cp);
                         if (!inq[e.to]) {
44
45
                             Q.push(e.to);
46
                             inq[e.to] = true;
                         }
47
48
                     }
                }
49
50
51
            if (d[t] == INF) return false;
            flow += a[t];
52
            cost += a[t] * d[t];
53
            int u = t;
54
            while (u != s) {
                edges[p[u]].cp -= a[t];
56
57
                edges[p[u] ^ 1].cp += a[t];
58
                u = edges[p[u]].from;
            }
59
            return true;
61
62
        pair<int, int> go() {
63
            int flow = 0, cost = 0;
64
            while (BellmanFord(flow, cost));
65
            return {flow, cost};
66
67
   } MM;
68
    树上路径交
        • 前置模板: 最近公共祖先
    int intersection(int x1, int y1, int x2, int y2) {
2
        int t[4] = {lca(x1, x2), lca(x1, y2), lca(y1, x2), lca(y1, y2)};
        int p1 = 0,p2 = 0;
3
        FOR(j,0,4)
        if(dep[t[j]] > dep[p1]) p2 = p1, p1 = t[j];
                                                                27
```

8 };

10 11

12

13

14

15

struct MCMF {

int n, m, s, t;
vector<E> edges;

vector<int> G[M];

int d[M], p[M], a[M];

bool inq[M];

```
else if(dep[t[j]] > dep[p2]) p2 = t[j];
7
        int h1 = lca(x1,y1), h2 = lca(x2,y2);
        if(p1 == p2){
8
            if(dep[p1] < dep[h1] || dep[p1] < dep[h2]) return 0;</pre>
            else return 1;
        }
11
12
            int ans = dep[p1]+dep[p2]-2*dep[lca(p1,p2)]+1;
13
            return ans;
14
15
   }
16
    树上点分治(树的重心)
    const LL N = 2e4+10, N2 = N * 2;
    int h[N], e[N2], ne[N2], idx;
3
   void add(int a, int b){
        e[idx] = b, ne[idx] = h[a], h[a] = idx++;
   vector<bool> vis;
   // 获取子树的重心(自动处理父子关系)(如果有两个重心,输出编号小的那个)
   // 若重心为 u, 则 mx[u] 为以 u 为重心子树大小的最大值
12
    int q[N], fa[N], sz[N], mx[N];
13
    int get_rt(int u) {
14
        int p = 0, cur = -1;
15
16
        q[p++] = u; fa[u] = -1;
        while (++cur < p) {
17
            u = q[cur]; mx[u] = 0; sz[u] = 1;
18
            for (int i = h[u]; i!=-1; i=ne[i]){
19
                int j = e[i];
                if(vis[j] or j == fa[u]) continue;
21
                fa[q[p++] = j] = u;
22
            }
23
24
25
        FORD (i, p - 1, -1) \{
26
            u = q[i];
            mx[u] = max(mx[u], p - sz[u]);
27
            if (mx[u] * 2 <= p) return u;
28
            sz[fa[u]] += sz[u];
29
            mx[fa[u]] = max(mx[fa[u]], sz[u]);
31
       assert(0);
32
33
   }
34
   // 分治 dfs (起点任意)
35
    void dfs(int u) {
36
        cout << "u: " << u;
37
38
        u = get_rt(u);
        vis[u] = true;
39
        // 处理子树逻辑
40
        cout << " centroid: " << u << '\n';</pre>
41
42
        // 如果在此处 DFS, 会遍历整棵子树 (if(vis[u]) return)
        // ...
43
44
45
        for(int i=h[u]; i!=-1; i=ne[i]){
            int j = e[i];
46
47
            if(vis[j]) continue;
            dfs(j);
48
        }
   }
```

## 二分图

#### 最大匹配

● 最小覆盖数 = 最大匹配数

- 最大独立集 = 顶点数 二分图匹配数
- DAG 最小路径覆盖数 = 结点数 拆点后二分图最大匹配数

```
const int N = 500+10;
2
    struct MaxMatch {
3
        int n;
        vector<int> G[N];
        int vis[N], left[N], clk;
        void init(int n) {
           this->n = n;
            FOR (i, 0, n + 1) G[i].clear();
10
           memset(left, -1, sizeof left);
11
            memset(vis, -1, sizeof vis);
12
13
14
15
        bool dfs(int u) {
            for (int v: G[u])
16
                if (vis[v] != clk) {
17
18
                    vis[v] = clk;
                    if (left[v] == -1 || dfs(left[v])) {
19
                        left[v] = u;
                       return true;
21
22
                    }
               }
23
           return false;
24
       }
25
26
        int match() {
27
28
           int ret = 0;
            for (clk = 0; clk <= n; ++clk)</pre>
29
               if (dfs(clk)) ++ret;
            return ret;
31
32
       }
   } MM;
33
   34
    void solve(){
       LL n1, n2, m, n, i, t1, t2;
36
37
        cin >> n1 >> n2 >> m;
       n = n1 + n2;
38
       MM.init(n);
39
        for(i=0; i<m; i++){</pre>
40
           cin >> t1 >> t2;
41
42
           MM.G[t1].push_back(n1+t2);
43
44
        cout << MM.match() << '\n';</pre>
45
   }
    最大权匹配
       py[j] = i表示右侧顶点j与左侧顶点i匹配
    namespace R {
        const int M = 400 + 5;
        const int INF = 2E9;
3
        int w[M][M], kx[M], ky[M], py[M], vy[M], slk[M], pre[M];
        LL KM() {
           FOR (i, 1, n + 1)
8
            FOR (j, 1, n + 1)
            kx[i] = max(kx[i], w[i][j]);
10
11
            FOR (i, 1, n + 1) {
                fill(vy, vy + n + 1, \theta);
12
                fill(slk, slk + n + 1, INF);
13
14
                fill(pre, pre + n + 1, \theta);
                int k = 0, p = -1;
15
                for (py[k = 0] = i; py[k]; k = p) {
16
                    int d = INF;
17
                    vy[k] = 1;
18
```

```
int x = py[k];
19
20
                    FOR (j, 1, n + 1)
                    if (!vy[j]) {
21
                         int t = kx[x] + ky[j] - w[x][j];
22
                         if (t < slk[j]) { slk[j] = t; pre[j] = k; }</pre>
                         if (slk[j] < d) { d = slk[j]; p = j; }</pre>
24
25
                    FOR (j, 0, n + 1)
26
                    if (vy[j]) { kx[py[j]] -= d; ky[j] += d; }
27
28
                    else slk[j] -= d;
29
30
                for (; k; k = pre[k]) py[k] = py[pre[k]];
            }
31
            LL ans = 0;
32
            FOR (i, 1, n + 1) ans += kx[i] + ky[i];
33
            return ans;
34
35
   }
36
   void solve(){
38
        LL n1, n2, i, t1, t2, t3, m, n, j;
39
        cin >> n1 >> n2 >> m;
40
41
        // 初始化
42
        n = max(n1, n2);
        R::n = n;
43
44
        for(i=0; i<=n; i++){</pre>
            for(j=0; j<=n; j++){</pre>
45
                R::w[i][j] = 0;
46
47
        }
48
        // 读数据
49
        for(i=0; i<m; i++){</pre>
50
51
            cin >> t1 >> t2 >> t3;
52
            R::w[t1][t2] = t3;
        }
53
        // 计算
54
        LL maxx = R::KM();
55
        cout << maxx << '\n';</pre>
56
        // 结果转换
57
        vector<pair<LL, LL>> anss;
for(i=1; i<=n; i++){ // 注意遍历最大范围
58
59
            if(R::w[R::py[i]][i]){
60
                anss.push_back({R::py[i], i});
61
62
            }else{
63
64
                anss.push_back({R::py[i], 0});
            }
65
        sort(anss.begin(), anss.end());
67
68
        for(i=0; i<n1; i++){</pre>
            cout << anss[i].second << ' ';</pre>
69
70
   }
    Tarjan
    割点
       ● 判断割点(无向图)
       • 注意原图可能不连通
    int dfn[N], low[N], clk;
    void init() { clk = 0; memset(dfn, 0, sizeof dfn); }
    void tarjan(int u, int fa) {
        low[u] = dfn[u] = ++clk;
        int cc = fa != -1;
        for (int& v: G[u]) {
            if (v == fa) continue;
            if (!dfn[v]) {
                tarjan(v, u);
                low[u] = min(low[u], low[v]);
```

```
cc += low[v] >= dfn[u];
11
12
           } else low[u] = min(low[u], dfn[v]);
13
       if (cc > 1) // u 是割点
14
15
   }
   桥
      无向图
       ● 注意原图不连通和重边
   int dfn[N], low[N], clk;
   void init() { memset(dfn, 0, sizeof dfn); clk = 0; }
   void tarjan(int u, int fa) {
       low[u] = dfn[u] = ++clk;
5
       int _fst = 0;
       for (E& e: G[u]) {
           int v = e.to; if (v == fa && ++_fst == 1) continue;
           if (!dfn[v]) {
               tarjan(v, u);
               if (low[v] > dfn[u]) // (u, v) 是桥
10
               low[u] = min(low[u], low[v]);
11
12
           } else low[u] = min(low[u], dfn[v]);
       }
13
   }
   强连通分量缩点
      • 有向图
      ● B: 强连通分量的数量计数器
      • bl[N]: 记录每个顶点所属的强连通分量编号
```

● bcc[N]:存储每个强连通分量包含的顶点列表

```
int low[N], dfn[N], clk, B, bl[N];
   vector<int> bcc[N];
    void init() { B = clk = 0; memset(dfn, 0, sizeof dfn); }
3
    void tarjan(int u) {
        static int st[N], p;
        static bool in[N];
        dfn[u] = low[u] = ++clk;
        st[p++] = u; in[u] = true;
8
        for (int& v: G[u]) {
            if (!dfn[v]) {
10
                tarjan(v);
                low[u] = min(low[u], low[v]);
12
            } else if (in[v]) low[u] = min(low[u], dfn[v]);
13
14
        if (dfn[u] == low[u]) {
15
            while (1) {
                int x = st[--p]; in[x] = false;
17
                bl[x] = B; bcc[B].push_back(x);
18
                if (x == u) break;
19
            }
20
            ++B;
22
        }
   }
```

## 点双连通分量 / 广义圆方树

- 数组开两倍
- 一条边也被计入点双了(适合拿来建圆方树),可以用点数 <= 边数过滤
- B: 双连通分量的数量(编号从0开始)。
- bc[B]:存储第 B 个双连通分量包含的节点。
- be[B]:存储第 B 个双连通分量包含的边(索引)。
- bno[x]: 标记节点 x 属于哪个双连通分量(用于去重)。

```
struct E { int to, nxt; } e[N];
1
2
    int hd[N], ecnt;
    void addedge(int u, int v) {
        e[ecnt] = {v, hd[u]};
        hd[u] = ecnt++;
   }
6
    int low[N], dfn[N], clk, B, bno[N];
   vector<int> bc[N], be[N];
    bool vise[N];
    void init() {
        memset(vise, 0, sizeof vise);
11
12
        memset(hd, -1, sizeof hd);
        memset(dfn, 0, sizeof dfn);
13
        memset(bno, -1, sizeof bno);
14
        B = clk = ecnt = 0;
15
   }
16
17
    void tarjan(int u, int feid) {
18
        static int st[N], p;
19
        static auto add = [&](int x) {
20
            if (bno[x] != B) { bno[x] = B; bc[B].push_back(x); }
21
22
        low[u] = dfn[u] = ++clk;
23
        for (int i = hd[u]; ~i; i = e[i].nxt) {
            if ((feid ^ i) == 1) continue;
25
26
            if (!vise[i]) { st[p++] = i; vise[i] = vise[i ^ 1] = true; }
27
            int v = e[i].to;
            if (!dfn[v]) {
28
                tarjan(v, i);
                low[u] = min(low[u], low[v]);
30
                 if (low[v] >= dfn[u]) {
31
                     bc[B].clear(); be[B].clear();
32
                     while (1) {
33
34
                         int eid = st[--p];
                         add(e[eid].to); add(e[eid ^ 1].to);
35
                         be[B].push_back(eid);
36
                         if ((eid ^ i) <= 1) break;</pre>
37
                     }
38
                     ++B;
39
                }
40
41
            } else low[u] = min(low[u], dfn[v]);
        }
42
   }
43
```

## 计算几何

## 字符串

## 最小表示法

• 寻找一个字符串的循环同构串中最小的那一个, 输出偏移量

```
int min_string(string s){
        int k = 0, i = 0, j = 1, n = s.length();
2
        while (k < n && i < n && j < n) {
3
            if (s[(i + k) \% n] == s[(j + k) \% n]) {
4
                k++;
5
            } else {
                s[(i + k) \% n] > s[(j + k) \% n] ? i = i + k + 1 : j = j + k + 1;
                if (i == j) i++;
                k = 0;
            }
10
11
12
        return min(i, j);
   }
```

## 字符串哈希

```
// 双值哈希开关
    #define ENABLE_DOUBLE_HASH
2
    typedef long long LL;
    typedef unsigned long long ULL;
    const int x = 135;
    const int N = 4e5 + 10;
    const int p1 = 1e9 + 7, p2 = 1e9 + 9;
   ULL xp1[N], xp2[N], xp[N];
11
    void init_xp() {
12
        xp1[0] = xp2[0] = xp[0] = 1;
13
        for (int i = 1; i < N; ++i) {</pre>
14
15
            xp1[i] = xp1[i - 1] * x % p1;
            xp2[i] = xp2[i - 1] * x % p2;
16
            xp[i] = xp[i - 1] * x;
17
        }
18
   }
19
20
    struct String {
21
22
        string s;
        int length, subsize;
23
        bool sorted;
24
        ULL h[N], hl[N];
25
26
        // 预处理并返回全串哈希 O(n)
27
        ULL hash() {
28
            length = s.length();
30
            ULL res1 = 0, res2 = 0;
            h[length] = 0; // ATTENTION!
31
32
            for (int j = length - 1; j >= 0; --j) {
    #ifdef ENABLE_DOUBLE_HASH
33
34
                res1 = (res1 * x + s[j]) % p1;
                res2 = (res2 * x + s[j]) % p2;
35
36
                h[j] = (res1 << 32) | res2;
37
    #else
                res1 = res1 * x + s[j];
38
39
                h[j] = res1;
    #endif
40
41
                // printf("%llu\n", h[j]);
            }
42
            return h[0];
43
44
        }
45
        // 获取子串哈希, 左闭右开区间 O(1)
46
        ULL get_substring_hash(int left, int right) const {
47
            int len = right - left;
49
    #ifdef ENABLE_DOUBLE_HASH
            // get hash of s[left...right-1]
50
51
            unsigned int mask32 = \sim(0u);
            ULL left1 = h[left] >> 32, right1 = h[right] >> 32;
52
            ULL left2 = h[left] & mask32, right2 = h[right] & mask32;
            return (((left1 - right1 * xp1[len] % p1 + p1) % p1) << 32) |</pre>
54
55
            (((left2 - right2 * xp2[len] % p2 + p2) % p2));
   #else
56
            return h[left] - h[right] * xp[len];
57
    #endif
59
60
        void get_all_subs_hash(int sublen) {
61
            subsize = length - sublen + 1;
62
            for (int i = 0; i < subsize; ++i)</pre>
63
                hl[i] = get_substring_hash(i, i + sublen);
64
65
            sorted = 0;
66
        }
67
        void sort_substring_hash() {
68
            sort(hl, hl + subsize);
69
```

```
sorted = 1;
70
71
72
        bool match(ULL key) const {
73
74
             if (!sorted) assert (0);
             if (!subsize) return false;
75
             return binary_search(hl, hl + subsize, key);
76
77
78
        void init(string t) {
79
            length = t.length();
80
81
             s = t;
82
    };
83
84
    String S, T; // 栈溢出
85
    // 验证 S 中长度为 ans 的子串是否都存在于 T 中(是 0 否 1)
87
    int check(String &S, String &T, int ans) {
        if (T.length < ans) return 1;</pre>
89
        T.get_all_subs_hash(ans); T.sort_substring_hash();
90
91
        for (int i = 0; i < S.length - ans + 1; ++i)</pre>
             if (!T.match(S.get_substring_hash(i, i + ans)))
92
                 return 1;
93
        return 0;
94
95
    }
96
    // 返回是否匹配
97
    bool match_once(String &S, String &T){
        S.get_all_subs_hash(T.length);
99
        S.sort_substring_hash();
100
        \textbf{return} \ \texttt{S.match}(\texttt{T.get\_substring\_hash}(\texttt{0}, \ \texttt{T.length}));
101
    }
102
103
    // 返回匹配下标
104
    vector<int> match_any(const String &text, const String &pattern) {
105
        vector<int> positions:
106
        int n = text.length;
107
108
        int m = pattern.length;
109
110
        if (m == 0 || m > n) return positions;
111
        ULL pattern_hash = pattern.get_substring_hash(0, m);
112
113
        for (int i = 0; i <= n - m; ++i) {</pre>
114
115
             ULL text_sub_hash = text.get_substring_hash(i, i + m);
             if (text_sub_hash == pattern_hash) {
116
117
                 positions.push_back(i);
             }
118
119
120
        return positions;
    }
121
122
    // 最长公共前缀 a[ai...] == b[bi...]
123
    int LCP(const String &a, const String &b, int ai, int bi) {
124
125
        int l = 0, r = min(a.length - ai, b.length - bi);
        while (l < r) {</pre>
126
127
             int mid = (l + r + 1) / 2;
             if (a.get_substring_hash(ai, ai + mid) == b.get_substring_hash(bi, bi + mid))
128
129
             else r = mid - 1;
130
        }
131
        return l;
132
    }
133
134
    // ----- Template End -----
135
    136
137
    void solve(){
138
139
    // cout << "AA\n";
        init_xp(); // DON'T FORGET TO DO THIS!
140
```

```
// cout << "BB\n";
141
         string s, t;
142
         cin >> s >> t;
143
         S.init(s), T.init(t);
144
145
         S.hash(), T.hash();
         cout << match_once(S, T) << '\n';</pre>
146
147
         vector<int> v = match_any(S, T);
148
         for(int ii: v) cout << ii << ' ';</pre>
149
150
         cout << '\n';</pre>
151
         cout << "LCP:" << LCP(S, T, 0, 0) << '\n';
152
153
         // S 中所有长度为 l 的子串均在 T 中出现, 且 l 最大
154
         LL l=0, r=S.length;
155
         while (l < r){
156
157
              int mid = l + r + 1 >> 1;
              if (!check(S, T, mid)) l = mid;
158
              else r = mid - 1;
159
160
         cout << "check: " << l << '\n';</pre>
161
162
163
```

## 杂项

## 日期

```
string day_of_week[] = {"Mo", "Tu", "We", "Th", "Fr", "Sa", "Su"};
    // 格里高利历 (yyyy-mm-dd) 转儒略历 (整型/天)
3
4
    int date_to_int(int y, int m, int d){
        return
        1461 * (y + 4800 + (m - 14) / 12) / 4 +
        367 * (m - 2 - (m - 14) / 12 * 12) / 12 -
        3 * ((y + 4900 + (m - 14) / 12) / 100) / 4 +
        d - 32075;
   }
10
11
    // 儒略历转格里高利历
12
13
    void int_to_date(int jd, int &y, int &m, int &d){
        int x, n, i, j;
14
        x = jd + 68569;
15
16
        n = 4 * x / 146097;
        x = (146097 * n + 3) / 4;
17
        i = (4000 * (x + 1)) / 1461001;
18
        x = 1461 * i / 4 - 31;
19
        j = 80 * x / 2447;
21
        d = x - 2447 * j / 80;
        x = j / 11;
22
        m = j + 2 - 12 * x;
23
        y = 100 * (n - 49) + i + x;
24
25
   }
```