The cosmic merger rate of neutron stars and black holes

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ABSTRACT

Six gravitational wave detections have been reported so far, providing crucial insights on the merger rate of double compact objects. We investigate the cosmic merger rate of double neutron stars (DNSs), neutron star-black hole binaries (NSBHs) and black hole binaries (BHBs) by means of population-synthesis simulations coupled with the Illustris cosmological simulation. We have performed six different simulations, considering different assumptions for the efficiency of common envelope (CE) ejection and exploring two distributions for the supernova (SN) kicks. The current BHB merger rate derived from our simulations spans from ~ 150 to ~ 240 Gpc^{-3} yr^{-1} and is only mildly dependent on CE efficiency. In contrast, the current merger rates of DNSs (ranging from ~ 20 to ~ 600 Gpc^{-3} yr^{-1}) and NSBHs (ranging from ~ 10 to ~ 100 Gpc^{-3} yr^{-1}) strongly depend on the assumptions on CE and natal kicks. The merger rate of DNSs is consistent with the one inferred from the detection of GW170817 only if a high efficiency of CE ejection and low SN kicks (drawn from a Maxwellian distribution with one dimensional root mean square $\sigma = 15$ km s^{-1}) are assumed.

Key words: stars: black holes – stars: neutron – gravitational waves – methods: numerical – stars: mass-loss – black hole physics

1 INTRODUCTION

The LIGO-Virgo collaboration (Aasi et al. et al. 2015; Acernese et al. 2015) has reported six gravitational wave (GW) events so far, five of them involving the merger of two black holes (BHs, Abbott et al. 2016b; Abbott et al. 2016d,c,a, 2017a,b,e) and one (GW170817) interpreted as the merger of two neutron stars (NSs, Abbott et al. 2017c,d). The merger rate of NSs and BHs can be inferred from these six detections, providing some crucial insights on the formation channels of compact-object binaries.

Recent estimates of the BH binary (BHB) merger rate from GW detections span from ~ 9 to ~ 240 events Gpc^{-3} yr^{-1} (Abbott et al. 2016a), while for NS–BH binaries (NSBHs) an upper limit of ~ 3600 events Gpc^{-3} yr^{-1} (Abbott et al. 2016e) was derived from the first observing (O1) run. Finally, a rate of 1540^{+3200}_{-1220} Gpc^{-3} yr^{-1} was inferred for double NS (DNS) mergers, based on GW170817 (Abbott et al. 2017c).

Alternative observational estimates of the DNS merger rate are based either on the rate of short gamma-ray bursts (Coward et al. 2012; Petrillo et al. 2013; Siellez et al. 2014; Fong et al. 2015), or on kilonova observations (Jin et al. 2015), or on the properties of Galactic DNSs (Kim et al. 2015). Overall, the DNS merger rate derived from gamma-ray bursts and from kilonovae (ranging from few tens to several thousands of mergers Gpc^{-3} yr^{-1}) is consistent with the one inferred from GW events.

From a theoretical perspective, predicting the cosmic merger rate of compact objects is quite an ordeal, because of the involved dynamical range: we need to put the mergers of compact-object binaries (with an initial orbital separation of tens of solar radii) in a large cosmological framework. The early work of Dominik et al. (2013) achieves this result by combining the results of their population-synthesis simulations with a description of the cosmic star-formation rate (SFR) density and of the average metallicity evolution, predicting a local merger rate of ~ 30, ~ 60 and ~ 2 Gpc^{-3} yr^{-1} for BHB, DNS and NSBH mergers, respectively, according to their fiducial model. Since then, many studies (Belczynski et al. 2016; Dvorkin et al. 2016; Elbert et al. 2018; Lamberts et al. 2016; O'Shaughnessy et al. 2017; Lamberts et al. 2018; Cao et al. 2018) have focused on the cosmic merger rate of BHBs adopting a number of approaches. In particular, Schneider et al. (2017) and Mapelli et al. (2017) have combined catalogues of merging BHBs from population-synthesis simulations with the outputs of cosmological simulations. Following this approach, Mapelli et al. (2017) find a local BHB merger rate of $\sim 120 - 180$ Gpc^{-3}

yr^{-1} for their fiducial model, consistent with the results of the LIGO-Virgo collaboration.

As to DNS mergers, population-synthesis simulations have been used to predict merging rates spanning from few tens to several hundreds mergers Gpc^{-3} yr^{-1} (e.g. Abadie et al. 2010; Dominik et al. 2013, 2015; Ziosi et al. 2014; de Mink & Belczynski 2015). Recently, Chruslinska et al. (2018) have claimed that their population-synthesis models can obtain a local DNS merger rate consistent with GW detections only if they use a very optimistic description for the common-envelope (CE) phase, assuming that Hertzsprung gap (HG) donor stars can avoid merger during CE. This description of CE, if applied to merging BHBs, overestimates the merger rate of BHBs by a large factor. Their main conclusion is that either CE works differently for DNSs and BHBs, or high natal kicks for BHs are needed to match the results of GW detections. Similarly, Kruckow et al. (2018) obtain a local DNS merger rate density of only ~ 10 Gpc^{-3} yr^{-1} for their fiducial model and a strong upper limit to the local DNS merger rate of ~ 400 Gpc^{-3} yr^{-1}.

In this paper, we use the same approach as Mapelli et al. (2017) to estimate the cosmic merger rate of BHBs, DNSs and NSBH binaries: we use a Monte Carlo code to combine the results of advanced population-synthesis simulations (Giacobbo et al. 2018; Giacobbo & Mapelli 2018a) with the outputs of the Illustris-1 cosmological simulation (Vogelsberger et al. 2014b). This method enables us to account for the cosmic SFR density and for the metallicity evolution in the host galaxies, within the limitations posed by state-of-the-art cosmological simulations.

2 METHODS

2.1 Population-synthesis simulations with MOBSE

We have run a large grid of binary population-synthesis simulations with the code MOBSE (Giacobbo et al. 2018), to derive catalogues of merging DNSs, NSBHs and BHBs. MOBSE is an upgraded version of BSE (Hurley et al. 2000, 2002). The main updates of MOBSE with respect to BSE are the following (see Giacobbo et al. 2018 and Giacobbo & Mapelli 2018a for details).

- Stellar winds of hot massive stars (O- and B- type, Wolf-Rayet and luminous blue variable stars) have been updated including a dependence of mass loss on metallicity as $\dot{M} \propto Z^{\beta}$, with $\beta = 0.85$ if $\Gamma_e < 2/3$, $\beta = 2.45 - 2.4\,\Gamma_e$ if $2/3 \leq \Gamma_e \leq 1$, and $\beta = 0.05$ if $\Gamma_e \geq 1$ (where Γ_e is the electron-scattering Eddington ratio, i.e. the ratio between current stellar luminosity and Eddington luminosity, Vink et al. 2001; Vink & de Koter 2005; Gräfener & Hamann 2008; Chen et al. 2015).

- The core radii of massive evolved stars have been updated as in Hall & Tout (2014).

- Core-collapse supernovae (SNe) are described through the rapid and the delayed SN mechanism described in Fryer et al. (2012). In the simulations performed for this paper we adopt the *rapid* core-collapse SN model (changing the core-collapse SN model from rapid to delayed would have a minor effect on the merger rate, as already shown in Figure 1 of Mapelli et al. 2017).

- Pulsational pair-instability and pair-instability SNe are

included, according to Spera & Mapelli (2017) (see also Woosley 2017 and Giacobbo et al. 2018).

- Electron-capture SNe (ECSNe) are described as in Hurley et al. (2000), the only update being the minimum Oxygen-Neon core mass for an ECSN to occur (which is set to be 1.38 $M_{\odot}$ instead of 1.44 $M_{\odot}$, see Giacobbo & Mapelli 2018b).

- The natal kick of NSs is obtained by randomly picking a number according to a Maxwellian distribution. For ECSNe, the Maxwellian distribution is assumed to have a one dimensional root mean square (1D rms) $\sigma_{\mathrm{ECSN}} = 15$ $\mathrm{km\ s}^{-1}$, which was found to maximize the number of merging DNSs in Giacobbo & Mapelli (2018b). For core-collapse SNe, the Maxwellian distribution has a 1D rms $\sigma_{\mathrm{CCSN}} = 265$ $\mathrm{km\ s}^{-1}$ (consistent with the proper motions of 233 single pulsars reported in Hobbs et al. 2005) in the fiducial case, and a 1D rms $\sigma_{\mathrm{CCSN}} = 15$ $\mathrm{km\ s}^{-1}$ in the runs labeled as "low σ" (see Table 1).

For BHs, the amount of kick is scaled by the fallback as $v_{\mathrm{BH}} = v_{\mathrm{NS}} (1 - f_{\mathrm{fb}})$, where v_{BH} is the natal kick for the BH, v_{NS} is the natal kick for a NS (drawn from a Maxwellian distribution as described above), and f_{fb} (ranging from 0 to 1) is the amount of fallback on the proto-NS (Fryer et al. 2012; Spera et al. 2015).

- We describe common envelope (CE) with the same formalism as in Hurley et al. (2002). This formalism depends on two free parameters, α (describing the efficiency of energy transfer) and λ (describing the geometry of the envelope and the importance of recombinations). In the current paper, λ is defined as in Claeys et al. (2014), to account for the contribution of recombinations, while α is a constant.

The main change in the description of CE with respect to BSE consists in the treatment of Hertzsprung gap (HG) stars. In the standard version of BSE, HG donors entering a CE phase are allowed to survive the CE phase. In MOBSE, HG donors are forced to merge with their companion if they enter a CE. Models in which HG donors are allowed to survive a CE phase produce a local BHB merger rate $R_{\mathrm{BHB}} \sim 600 - 800$ Gpc^{-3} yr^{-1}, which is not consistent with LIGO-Virgo results (Mapelli et al. 2017).

We have run six different sets of population-synthesis simulations with this version of MOBSE, adopting $\alpha = 1, 3$, and 5 and by changing the value of $\sigma_{\mathrm{CCSN}} = 15, 265$ $\mathrm{km\ s}^{-1}$. The details of the six runs can be found in Table 1.

For each of the six simulation sets described in Table 1, we have simulated 12 sub-sets with metallicity $Z = 0.0002$, 0.0004, 0.0008, 0.0012, 0.0016, 0.002, 0.004, 0.006, 0.008, 0.012, 0.016, and 0.02. Throughout the paper, we define solar metallicity as $Z_{\odot} = 0.02$. Thus, the 12 sub-sets correspond to metallicity $Z = 0.01, 0.02, 0.04, 0.06, 0.08, 0.1, 0.2, 0.3$, 0.4, 0.6, 0.8, and 1.0 $Z_{\odot}$. In each sub-set we have simulated 10^7 stellar binaries. Thus, each of the six sets of simulations is composed of 1.2×10^8 massive binaries.

For each binary, the mass of the primary (m_{p}) is randomly drawn from a Kroupa initial mass function (Kroupa 2001) ranging[1] from 5 to 150 $M_{\odot}$, and the mass of the secondary (m_{s}) is sampled according to the distribution

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[1] The fitting formulas by Hurley et al. (2000) might be inaccurate for very massive stars. To improve the treatment of massive stars, we impose that the values of the radius of single stars are consis-

Table 1. Properties of the population-synthesis simulations.

Name	α	σ_{CCSN} [km s^{-1}]
$\alpha = 1$	1.0	265
$\alpha = 1$, low σ	1.0	15
$\alpha = 3$	3.0	265
$\alpha = 3$, low σ	3.0	15
$\alpha = 5$	5.0	265
$\alpha = 5$, low σ	5.0	15

Column 1: model name; column 2: value of α in the CE formalism; column 3: 1D rms of the Maxwellian distribution for the core-collapse SN kick. See the text for details.

$\mathcal{F}(q) \propto q^{-0.1}$ (where $q = m_{\mathrm{s}}/m_{\mathrm{p}}$) in a range $[0.1 - 1]\, m_{\mathrm{p}}$. The orbital period P and the eccentricity e are randomly extracted from the distribution $\mathcal{F}(P) \propto (\log_{10} P)^{-0.55}$, with $0.15 \leq \log_{10}(P/\mathrm{day}) \leq 5.5$, and $\mathcal{F}(e) \propto e^{-0.42}$, with $0 \leq e < 1$, as suggested by Sana et al. (2012).

2.2 The Illustris cosmological simulation

The Illustris-1 is the highest resolution hydrodynamical simulation run in the frame of the Illustris project (Vogelsberger et al. 2014b,a; Nelson et al. 2015). In the following, we refer to it simply as the Illustris. It covers a comoving volume of $(106.5\,\mathrm{Mpc})^3$, and has an initial dark matter and baryonic matter mass resolution of 6.26×10^6 and 1.26×10^6 M$_\odot$, respectively (Vogelsberger et al. 2014b,a). At redshift zero the softening length is ~ 710 pc, while the smallest hydrodynamical cells have a length of 48 pc.

The size of the Illustris' box ensures that we include the most massive haloes. On the other hand, the population of dwarf galaxies is under-resolved. In Mapelli et al. (2017) we estimate in less than ~ 40 per cent the effect of resolution limitations on the merger rate. In a forthcoming paper, we will describe the contribution of dwarf galaxies to the merger rate by adopting a smaller box, higher resolution cosmological simulation. At redshift $z < 0.3$ the Illustris simulation predicts a higher SFR density by a factor of ~ 1.5 with respect to the observed one (Madau & Dickinson 2014). This suggests that the local merger rate density might be slightly overestimated in our calculations.

The Illustris includes a treatment for sub-grid physics (cooling, star formation, SNe, super-massive BH formation, accretion and merger, AGN feedback, etc), as described in Vogelsberger et al. (2013). The model of sub-grid physics adopted in the Illustris is known to produce a mass-metallicity relation (Genel et al. 2014; Genel 2016) which is sensibly steeper than the observed one (see the discussion in Vogelsberger et al. 2013 and Torrey et al. 2014). Moreover, the simulated mass-metallicity relation does not show the observed turnover at high stellar mass ($\gtrsim 10^{10}$ M$_\odot$). In Mapelli et al. (2017), we estimate that the impact on the BHB merger rate of the difference between the Illustris mass-metallicity relation and the observational relation

tent with PARSEC stellar evolution tracks (Chen et al. 2015) for stars with mass > 100 M$_\odot$, as discussed in Mapelli (2016).

(Maiolino et al. 2008; Mannucci et al. 2009) is of the order of 20 per cent. As shown in Giacobbo & Mapelli (2018a), the merger rate of DNSs does not significantly depend on the metallicity of their progenitors. Thus, the DNS merger rate is essentially unaffected by the deviation between the mass-metallicity relation of the Illustris and the observed one.

As for the cosmology, the Illustris adopts WMAP-9 results for the cosmological parameters (Hinshaw et al. 2013), that is $\Omega_{\mathrm{M}} = 0.2726$, $\Omega_{\Lambda} = 0.7274$, $\Omega_b = 0.0456$, and $H_0 = 100\,h$ km s^{-1} Mpc^{-1}, with $h = 0.704$.

2.3 Planting BHBs into a cosmological simulation

We combine the catalogues of merging DNSs, NSBHs and BHBs with the Illustris simulations as described in Mapelli et al. (2017). In particular, we store the initial mass M_{Ill}, formation redshift z_{Ill} and metallicity Z_{Ill} of each stellar particle of the Illustris. From the MOBSE simulations, we extract the compact-object masses and the delay time t_{delay} (i.e. the time elapsed between the formation of the progenitor stars and the merger of the compact-object binary) for all compact-object binaries merging in less than a Hubble time. We also extract the total initial mass M_{BSE} of the stellar population simulated with MOBSE for a given run and metallicity.

Through a Monte Carlo scheme, we associate to each newly born Illustris stellar particle (see equation 1 of Mapelli et al. 2017) a number $n_{\mathrm{CO,i}}$ of compact-object binaries (where the index $i = $ BHB, NSBH or DNS) as given by

$$n_{\mathrm{CO,i}} = N_{\mathrm{BSE,i}} \frac{M_{\mathrm{Ill}}}{M_{\mathrm{BSE}}} f_{\mathrm{corr}} f_{\mathrm{bin}}, \qquad (1)$$

where $N_{\mathrm{BSE,i}}$ is the number of merging compact objects within the simulated sub-set of initial stellar mass M_{BSE} (with $i = $ BHB, NSBH or DNS), and $f_{\mathrm{corr}} = 0.285$ is a correction factor, accounting for the fact that we actually simulate only primaries with $m_{\mathrm{p}} \geq 5$ M$_\odot$, neglecting lower mass stars. Finally, f_{bin} accounts for the fact that we simulate only binary systems, whereas a fraction of stars are single. Here we assume that 50 per cent of stars are in binaries, thus $f_{\mathrm{bin}} = 0.5$. We note that f_{bin} is only a scale factor and our results can be re-scaled to a different f_{bin} a posteriori.

We associate an Illustris stellar particle to a population-synthesis simulation set by looking for the population-synthesis simulation set with the closest metallicity to Z_{Ill} among the 12 metallicities simulated with MOBSE[2].

We then estimate the look-back time of the merger (t_{merg}) of each compact-object binary in the randomly selected sample as $t_{\mathrm{merg}} = t_{\mathrm{form}} - t_{\mathrm{delay}}$, where t_{delay} is the time between the formation of the progenitor stellar binary and the merger of the compact-object binary, and t_{form} is the look back time at which the Illustris' particle has formed,

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[2] If $Z_{\mathrm{Ill}} > 0.02$ ($Z_{\mathrm{Ill}} < 0.0002$), we associate to the Illustris's particle a MOBSE set with $Z_{\mathrm{Ill}} = 0.02$ ($Z_{\mathrm{Ill}} = 0.0002$), since the maximum (minimum) metallicity we simulated with BSE is 0.02 (0.0002).
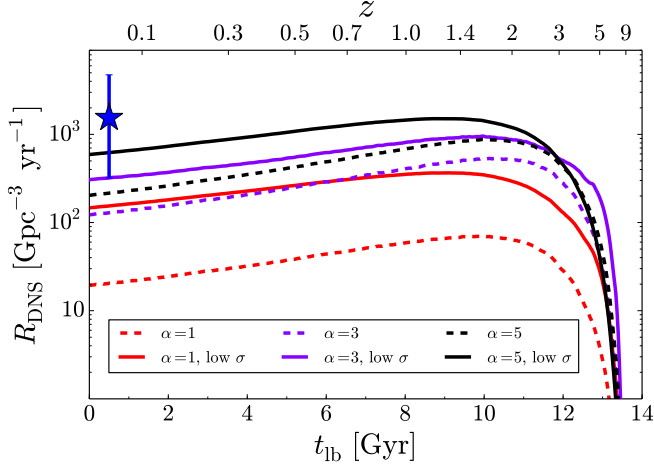
Figure 1. Cosmic merger rate density of DNSs ($R_{\rm DNS}$) in the comoving frame, as a function of the look-back time $t_{\rm lb}$ (bottom x axis) and of the redshift z (top x axis) in our models (see Table 1). Blue error bar with star: DNS merger rate inferred from GW170817 (Abbott et al. 2017c). The position of the data point along the x axis (corresponding to $t_{\rm lb} = 0.5$ Gyr) is just for visualization purposes.

Figure 2. Cosmic merger rate density of NSBHs ($R_{\rm NSBH}$) in the comoving frame, as a function of the look-back time $t_{\rm lb}$ (bottom x axis) and of the redshift z (top x axis) in our models (see Table 1). Blue arrow: upper limit to the NSBH merger rate inferred from the LIGO O1 run (Abbott et al. 2016e). The position of the upper limit along the x axis (corresponding to $t_{\rm lb} = 0.5$ Gyr) is just for visualization purposes.

calculated as

$$t_{\rm form} = \frac{1}{H_0} \int_0^{z_{\rm Ill}} \frac{1}{(1+z)\,[\Omega_{\rm M}\,(1+z)^3 + \Omega_\Lambda]^{1/2}}\,{\rm d}z, \quad (2)$$

where the cosmological parameters are set to WMAP-9 values (for consistency with the Illustris) and $z_{\rm Ill}$ is the formation redshift of the Illustris' particle.

According to this definition, $t_{\rm merg}$ is also a look back time: it tells us how far away from us the compact objects have merged. For our analysis, we consider only compact objects with $t_{\rm merg} \geq 0$, i.e. we do not consider compact objects that will merge in the future. We repeat the same procedure for each of the six simulation sets in Table 1 and we obtain six different models of the cosmic merger evolution for BHBs, NSBHs and DNSs.

3   RESULTS

3.1   Merger rate

The compact-object binary merger rate density in the comoving frame $R_{\rm CO,i}$ (with $i =$ BHB, NSBH or DNS) can be derived from our simulations as:

$$R_{\rm CO,i} = N_{\rm CO,i}\,{\rm Gpc}^{-3}\,{\rm yr}^{-1} \left(\frac{l_{\rm box}}{\rm Gpc}\right)^{-3} \left(\frac{\Delta t}{\rm yr}\right)^{-1}, \quad (3)$$

where $N_{\rm CO,i}$ is the number of compact-object mergers (with $i =$ BHB, NSBH or DNS) per time bin Δt in the entire Illustris box, $l_{\rm box} = 106.5$ Mpc is the size of the Illustris box (in the comoving frame) and Δt is the size of the time bin (we adopt $\Delta t = 10$ Myr).

The resulting merger rate $R_{CO,i}$ is affected by stochastic fluctuations due to the Monte Carlo sampling. By running several random realisations of the population synthesis
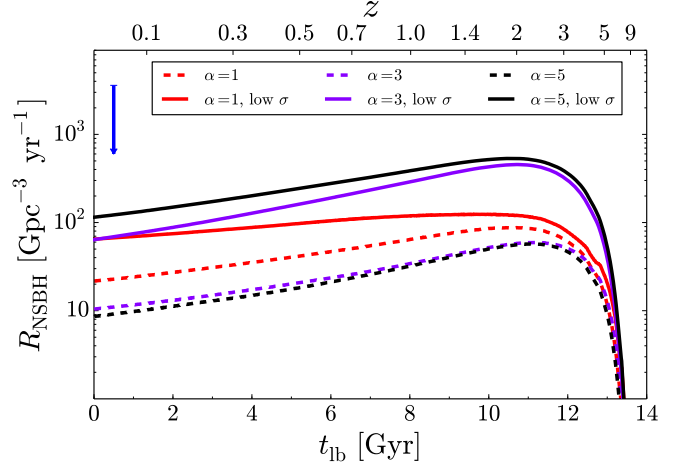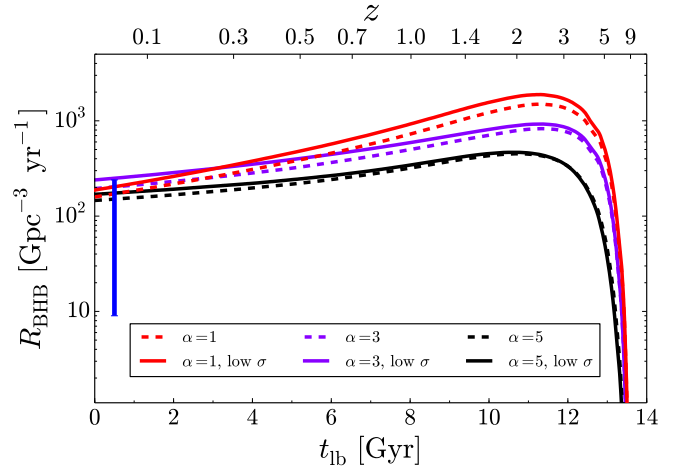

Figure 3. Cosmic merger rate density of BHBs ($R_{\rm BHB}$) in the comoving frame, as a function of the look-back time $t_{\rm lb}$ (bottom x axis) and of the redshift z (top x axis) in our models (see Table 1). Blue error bar: BHB merger rate inferred from the LIGO O1 run (Abbott et al. 2016a). The position of the data point along the x axis (corresponding to $t_{\rm lb} = 0.5$ Gyr) is just for visualization purposes.

simulations, we have estimated the fluctuations of $R_{\rm CO,i}$ to be less than few per cent between two different realisations.

Figure 1 shows the cosmic merger rate density of DNSs ($R_{\rm DNS}$) in the comoving frame, derived from our simulations using equation 3. The corresponding values of the merger rate at redshift $z = 0$ are shown in Table 2.

From Fig. 1 it is apparent that our estimate of the

DNS merger rate is consistent with the rate inferred from GW170817 (Abbott et al. 2017c) only if we assume a large value of the CE parameter α ($\alpha \geq 3$) and low kicks for both ECSNe and core-collapse SNe. Lower values of α and larger kicks produce lower values of the DNS merger rate.

The magnitude of the natal kick is particularly important for DNSs, because a large kick can easily unbind the binary. A large value of α means that CE ejection is particularly efficient, preventing a binary to merge after CE.

The DNS merger rate increases with redshift, reaching a maximum at $z \sim 1.5 - 2.5$, depending on the model. This result is consistent with the trend found by Mapelli et al. (2017) for BHBs and is the effect of a convolution between the cosmic SFR density and the distribution of delay times.

Figure 2 shows our prediction for the NSBH merger rate in the comoving frame (R_{NSBH}), obtained from equation 3 when considering the number of NSBH mergers per time bin (N_{NSBH}). The estimated merger rate of NSBHs is consistent with the upper limit from O1 in all considered models. The merger rate of NSBHs increases with redshift, reaching a maximum at $z \sim 1.5 - 3$, similar to the behaviour of DNSs.

Models with low kicks produce higher local NSBH merger rates by a factor of $3 - 10$ with respect to models with large SN kicks. If low kicks are assumed for the core-collapse SNe, the NSBH merger rate increases by increasing α. In contrast, if larger kicks are assumed for core-collapse SNe, a larger value of α reduces the number of NSBH mergers.

This happens because a large core-collapse SN kick increases the semi-major axis of the NSBH or even breaks the system. Binary systems that went through a CE phase with a small value of α are more likely to avoid being broken and to remain sufficiently bound after the second core-collapse SN, because a small value of α implies that the system's semi-major axis shrinks considerably during CE, before the CE is ejected. In contrast, a large value of α means that the CE is expelled without much shrinking of the orbital separation and makes easier for the second SN to unbind the system.

Finally, Fig. 3 shows the merger rate of BHBs, calculated adopting the number of BHB mergers per time bin (N_{BHB}) in equation 3. The estimated BHB merger rate is consistent with the range inferred from the O1 run, although close to the upper limit (90% credible level). In contrast with DNSs, different values of α and of the SN kick do not seem to affect the BHB merger rate significantly.

This happens because the natal kicks of BHs are quite low in our models, even if $\sigma_{\mathrm{CCSN}} = 265$ km s^{-1} is assumed, because the kick is modulated by fallback. The effect would have been much more important if we would not have assumed a dependence of the kick on the amount of fallback, as shown by model DK of Mapelli et al. (2017) (see their Figure 1).

The BHB merger rate increases with redshift, reaching a maximum at $z \sim 2 - 4$. The increase of the merger rate with redshift is much steeper for BHBs than for DNSs and NSBHs, because of the dependence of BHB mergers on metallicity. As shown in Figure 12 of Giacobbo et al. (2018), the number of BHB mergers per unit mass is ~ 2 orders of magnitude larger at low metallicity ($Z \leq 0.002$) than at high metallicity. This means that we expect a much higher BHB merger rate in the early Universe (which is predominantly

Table 2. Comoving merger-rate density of DNSs NSBHs and BHBs at redshift $z = 0$ ($t_{\mathrm{lb}} = 0$).

Name	R_{DNS} [Gpc^{-3} yr^{-1}]	R_{NSBH} [Gpc^{-3} yr^{-1}]	R_{BHB} [Gpc^{-3} yr^{-1}]
$\alpha = 1$	19	22	159
$\alpha = 1$, low σ	147	65	188
$\alpha = 3$	122	10	195
$\alpha = 3$, low σ	306	64	240
$\alpha = 5$	204	9	146
$\alpha = 5$, low σ	591	115	169

Column 1: model name; column 2: DNS merger rate density at $z = 0$; column 3: NSBH merger rate density at $z = 0$; column 4: BHB merger rate density at $z = 0$. Uncertainties in the tabulated rates are of the order of few per cent, because of stochastic fluctuations.
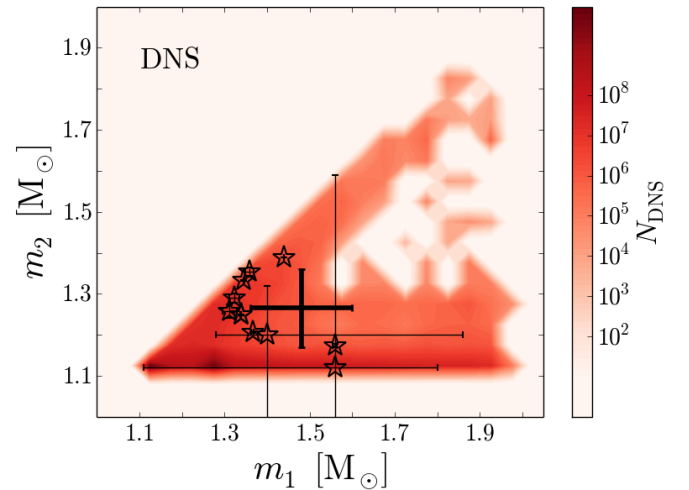

Figure 4. Mass of the primary NS versus the mass of the secondary NS for all simulated merging DNSs for the run with $\alpha = 5$ and $\sigma_{\mathrm{CCSN}} = 15$ km s^{-1}. The colour-coded map (in a logarithmic scale) indicates the number of merging DNSs per cell. The open stars with thin error bars are the masses of the DNSs observed in the Milky Way with $1 - \sigma$ errors (Martinez et al. 2015; Antoniadis et al. 2016; Tauris et al. 2017). The thick error bars show the mass of the NSs in GW170817 within 90% credible level assuming the system has low-spin (Abbott et al. 2017d).

metal poor) with respect to the nearby Universe (where high metallicity is more common). In contrast, the merger rate of DNSs does not seem to depend on metallicity.

3.2 Mass distribution

From our simulations we can derive the mass distribution of merging DNSs (Fig. 4), NSBHs (Fig. 5) and BHBs (Fig. 6) across cosmic time.

Figure 4 shows the distribution of the mass of the secondary NS (defined as the least massive member of the binary system) with respect to the primary NS (defined as the most massive member of the binary system) for the run with
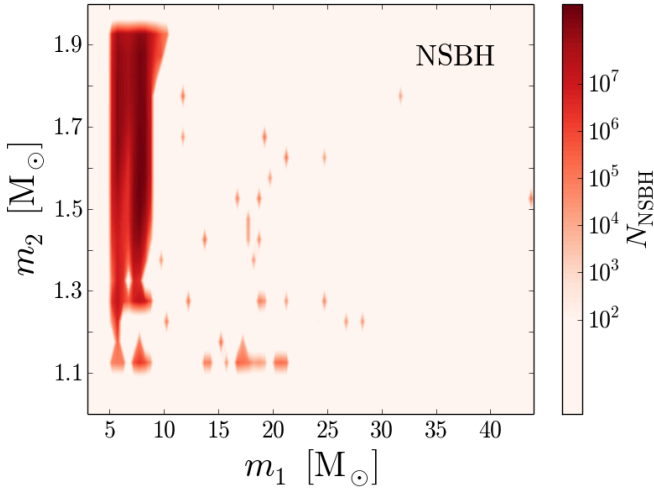
Figure 5. Mass of the NS versus the mass of the BH for all simulated merging NSBHs for the run with $\alpha = 5$ and $\sigma_{CCSN} = 15$ km s^{-1}. The colour-coded map (in a logarithmic scale) indicates the number of merging NSBHs per cell.

Figure 6. Mass of the secondary BH versus the mass of the primary BH for all simulated merging BHBs for the run with $\alpha = 5$ and $\sigma_{CCSN} = 15$ km s^{-1}. The colour-coded map (in a logarithmic scale) indicates the number of merging BHBs per cell. The open stars are the five reported GW events associated with BHBs (the error bars show the 90% credible levels).

$\alpha = 5$ and $\sigma_{CCSN} = 15$ km s^{-1}. Primary masses range from 1.1 to ~ 2 M$_\odot$, the most frequent masses being ~ 1.3 and ~ 1.1 M$_\odot$. Secondary masses also range from 1.1 to ~ 1.9 M$_\odot$, but the vast majority of the secondary NSs has either a low mass (~ 1.1 M$_\odot$) or a mass very similar to that of the primary.

In Fig. 4 we also show the masses of the observed Galactic DNSs and of the components of GW170817. The observed NS masses lie in a region of the $m_1 - m_2$ plane populated by a large number of simulated systems ($> 10^5$ per grid cell), although the simulated secondary NSs tend to cluster at smaller masses than the observed ones. This might suggest that either the prescriptions of Fryer et al. (2012) tend to underestimate NS masses or our population-synthesis simulations underestimate the efficiency of mass accretion onto NSs. We deem the latter hypothesis quite unlikely, because theoretical arguments and observations indicate that the mass accreted by a NS during its life should be $\lesssim 0.02$ M$_\odot$, unless dynamical interactions allow the NS to exchange stellar companion (see Tauris et al. 2017 and references therein).

Figure 5 shows the mass of the NS versus the mass of the BH for all merging NSBHs for the run with $\alpha = 5$ and $\sigma_{CCSN} = 15$ km s^{-1}. The mass of the NS in these systems spans from ~ 1.1 to ~ 2 M$_\odot$. NS masses > 1.3 M$_\odot$ are favoured in NSBHs. Most BH masses in merging NSBH systems are < 10 M$_\odot$ and preferentially ~ 5 and ~ 8 M$_\odot$. Few NSBH systems host more massive BHs, up to ~ 45 M$_\odot$. The predominance of small BHs in NSBHs comes from the fact that mass transfer in isolated binaries tends to lead to systems with $m_2/m_1 \sim 1$.

Finally, Figure 6 shows the mass of the secondary BH (the lighter one) versus the mass of the primary BH (the heavier one) of merging BHBs for the run with $\alpha = 5$ and $\sigma_{CCSN} = 15$ km s^{-1}. The mass range spans from 5 to $\sim 41 - 43$ M$_\odot$ for both members of the BHB. Light BHBs (with both BH masses $\sim 5 - 15$ M$_\odot$) are more com-
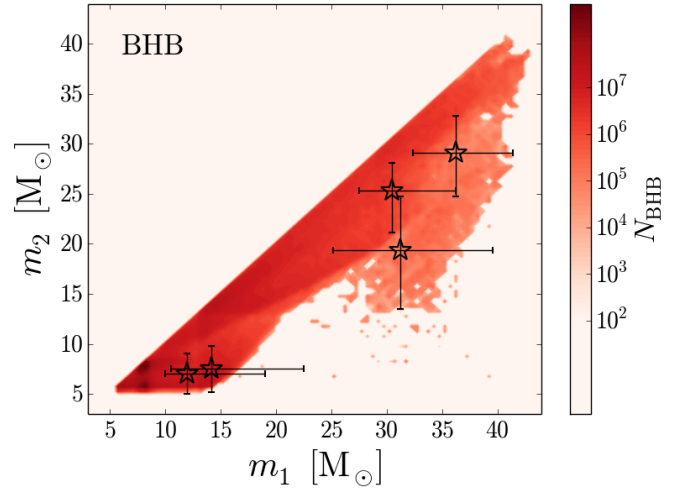
mon than heavy BHBs (with both BH masses > 15 M$_\odot$). Figure 6 also shows the mass of the five GW events interpreted as BHB mergers (Abbott et al. 2016b; Abbott et al. 2016c,a, 2017a,b,e). All observed merging BHBs lie in regions of the $m_1 - m_2$ plane which are densely populated by simulated BHs indicating that our models match the GW observations. Three of the observed GW events (GW150914, GW170104 and GW170814) lie in the region of massive BHBs (> 15 M$_\odot$), while only two GW events (GW151226 and GW170608) lie in the most densely populated region of low-mass BHBs ($5 - 15$ M$_\odot$). This is not in tension with our models, because GW interferometers have a higher chance of detecting GWs from massive BHBs than from light BHBs. In a forthcoming study, we will produce mock GW observations of our models, to quantify the agreement between them and GW detections.

4   DISCUSSION

We have shown that it is quite difficult to obtain a DNS merger rate consistent with the one inferred from GW170817: a high value of the CE α parameter and low SN kicks are both needed.

Our models demonstrate that it is possible to predict a merger rate of DNSs, NSBHs and BHBs consistent with those inferred from GW detections with the same assumptions for the CE phase, unlike the conclusions of Chruslinska et al. (2018). The CE is certainly a process which can make the difference, as already highlighted by Chruslinska et al. (2018). However, we do not need to make any extreme assumptions about the CE phase: by increasing the value of α and by assuming low SN kicks, we recover the merger rate of both DNSs and BHBs. Unlike Chruslinska et al. (2018), we do not need to assume that HG donors survive the CE phase only in the case of NS progenitors, while they merge

in the case of BH progenitors. The fact that we consider large values of α is also one of the most likely reasons why our DNS merger rates are significantly larger than the ones obtained by Kruckow et al. (2018), who assume $\alpha < 1$ (but our treatment of both binary evolution processes and the cosmological framework are also significantly different from the approach adopted in Kruckow et al. 2018).

CE appears once more to be a crucial evolutionary phase for merging compact objects. We stress that our understanding of CE is still far from satisfactory and there is still a large uncertainty on CE (see Ivanova et al. 2013; Tauris et al. 2017 for a review). In this paper, we neglect alternative models for the formation of merging compact objects, which do not require a CE phase. For example, Marchant et al. (2016) proposed that two very massive metal-poor stars in a close binary can remain fully mixed because of their tidally induced high spin and thus evolve as a massive over-contact binary: a binary whose components both overfill their Roche lobe but avoid merger, evolving into two nearly equal-mass, very close, Helium stars. These two stars can evolve into a merging BHB or DNS even without CE. According to Mandel & de Mink (2016) and de Mink & Mandel (2016), the two fully-mixed stars can even avoid filling their Roche lobe (because they become Helium stars fast enough), and then evolve into a merging BHB or DNS. These models are not considered in this paper and should be investigated in the future.

Our work suggests that low kicks for DNSs (of the order of $\sim 0 - 50$ km s^{-1}) are needed to explain the high merger rate of DNSs inferred from the LIGO-Virgo scientific collaboration. Other indirect observational estimates of SN kicks give contrasting results (see Tauris et al. 2017 for a recent discussion). Hobbs et al. (2005) found that a single Maxwellian with root mean square $\sigma_{\mathrm{CCSN}} = 265$ km s^{-1} can match the proper motions of 233 single pulsars. Other works suggest a bimodal velocity distribution, with a first peak at low velocities (e.g. ~ 0 km s^{-1} according to Fryer et al. 1998 or ~ 90 km s^{-1} according to Arzoumanian et al. 2002) and a second peak at high velocities (> 600 km s^{-1} according to Fryer et al. 1998 or ~ 500 km s^{-1} for Arzoumanian et al. 2002). Similarly, the recent work of Verbunt et al. (2017) indicates that a double Maxwellian distribution provides a significantly better fit to the observed velocity distribution than a single Maxwellian. Finally, the analysis of Beniamini & Piran (2016) shows that low kick velocities ($\lesssim 30$ km s^{-1}) are required to match the majority of Galactic DNSs, especially those with low eccentricity.

Our results are even more extreme, suggesting that the vast majority of DNSs should be born with a relatively low kick velocity. A possible physical interpretation for the small natal kicks of DNSs is that these systems undergo ultra-stripped SNe (see Tauris et al. 2017 and references therein for more details). A star can undergo an ultra-stripped SN explosion only if it was heavily stripped by mass transfer to a companion (Tauris et al. 2013, 2015). The flavour of an ultra-stripped SN can be either an ECSN or an iron core-collapse SN. Tauris et al. (2015) suggest that the natal kick of an ultra-stripped SN should be low because of the small mass of the ejecta (~ 0.1 M$_\odot$). Low kicks ($\lesssim 50$ km s^{-1}) for ultra-stripped iron core-collapse SNe are also confirmed by recent hydrodynamical simulations simulations (Suwa et al. 2015; Janka 2017). Consistently with our results, also Kruckow

et al. (2018) find significantly larger DNS merger rates when assuming lower kicks for the ultra-stripped SNe (see their table 6).

We have considered only isolated binaries: no dynamical effects are accounted for. Dynamics was demonstrated to have a possibly large impact on the merger rate of compact objects (see e.g. Portegies Zwart & McMillan 2000; Mapelli et al. 2013; Mapelli & Zampieri 2014; Ziosi et al. 2014; Rodriguez et al. 2015, 2016; Mapelli 2016; Askar et al. 2017; Kimpson et al. 2016; Banerjee 2017; Zevin et al. 2017; Fujii et al. 2017). In particular, single NSs might be efficient in entering DNSs by dynamical exchanges in old globular clusters (Belczynski et al. 2017). Alternatively, it is possible that dynamics breaks some BHBs, especially the light ones (Zevin et al. 2017), reducing R_{BHB}. The contribution of stellar dynamics might increase the DNS merger rate, relaxing the constraints on CE efficiency and natal kicks we discussed in this paper. We will account for the contribution of dynamics in future works.

Finally, our models suffer from several uncertainties connected with the cosmological framework. In particular, the Illustris simulation predicts a factor of ~ 40 per cent higher SFR at low redshift and a steeper mass-metallicity relation than the observed one. Moreover, dwarf galaxies are unresolved in the Illustris. In Mapelli et al. (2017) we have estimated that these issues affect the merger rate by a factor of ~ 2. We can compare our results for the DNS merger rate with the complementary approach followed by Giacobbo & Mapelli (2018a). Giacobbo & Mapelli (2018a) use the same population-synthesis simulations as we do and derive the local DNS merger rate from the fit to the observed cosmic SFR density (Madau & Dickinson 2014), by making the reasonable assumption that the merger rate of DNSs does not depend on the metallicity of the progenitor stars. For the model with $\alpha = 5$ and low SN kicks, Giacobbo & Mapelli (2018a) find values of the local merger rate $R_{\mathrm{DNS}} \sim 200 - 1400$ Gpc^{-3} yr^{-1}, which are perfectly consistent with the results presented in this paper ($R_{\mathrm{DNS}} \sim 600$ Gpc^{-3} yr^{-1}). Future studies, adopting other cosmological simulations with different box size and resolution, will help us better quantifying the uncertainty of our predicted rates.

5 SUMMARY

We have investigated the merger rate of DNSs, NSBHs and BHBs as a function of redshift, by coupling our population-synthesis simulations with the Illustris cosmological simulation. We have considered three different values of the α parameter describing the efficiency of CE ejection ($\alpha = 1, 3,$ and 5) and we have explored two different cases for the distribution of core-collapse SN kicks (a Maxwellian distribution with 1D rms $\sigma_{\mathrm{CCSN}} = 265$ km s^{-1} and $\sigma_{\mathrm{CCSN}} = 15$ km s^{-1}, respectively).

As already discussed in Mapelli et al. (2017), the merger rate of BHBs steadily increases with redshift reaching a maximum at $z \sim 2 - 3$ and then it drops at higher redshift. The merger rate of DNSs and NSBHs follows a similar trend, with a maximum at $z \sim 1 - 2$ and at $z \sim 2 - 3$ for DNSs and NSBHs, respectively. This trends depends on the cosmic SFR density, on the metallicity evolution and on the distribution of the delay times between the formation of the

progenitor binary system and the merger of the two compact objects.

The BHB merger rate depends only slightly on the value of α and on the 1D rms of the natal kick distribution. In our population-synthesis simulations, we have assumed that the natal kicks of BHs are reduced depending on the amount of fallback; thus natal kicks are low for heavy BHs even when we assume a Maxwellian distribution with high 1D rms ($\sigma_{\rm CCSN} = 265$ km s^{-1}). This explains why the BHB merger rate does not depend significantly on the assumed dispersion of the kick distribution. As already shown in Mapelli et al. (2017), the BHB merger rate strongly depends on the natal kick of BHs if this is not reduced by the fallback.

The merger rate of both DNSs and NSBHs strongly depends on the choice of α and on the assumed kick distribution. In particular, the merger rate of DNSs increases for a larger value of α and for a lower value of $\sigma_{\rm CCSN}$. The merger rate of NSBHs also increases for a lower value of $\sigma_{\rm CCSN}$, while the effect of α strongly depends on the choice of $\sigma_{\rm CCSN}$.

The current merger rate of BHBs ranges from ~ 150 to ~ 240 Gpc^{-3} yr^{-1}, consistent with the merger rate inferred from O1 GW detections although close to the upper limit of the allowed range. The current merger rate of NSBHs spans from ~ 10 (for low natal kicks) to ~ 100 Gpc^{-3} yr^{-1} (for large natal kicks), consistent with the upper limit from the O1 run. Finally, the current merger rate of DNSs ranges from ~ 20 Gpc^{-3} yr^{-1} (for $\alpha = 1$ and $\sigma_{\rm CCSN} = 265$ km s^{-1}) to ~ 600 Gpc^{-3} yr^{-1} (for $\alpha = 5$ and $\sigma_{\rm CCSN} = 15$ km s^{-1}).

The current merger rate of DNSs is consistent with the one inferred from the detection of GW170817 only if $\alpha \geq 3$ and only if the natal kick distribution is assumed to be low ($\sigma_{\rm ECSN} = \sigma_{\rm CCSN} = 15$ km s^{-1}). A possible physical interpretation is that the vast majority of DNSs form from ultra-stripped SNe, which are expected to produce very small natal kicks (< 50 km s^{-1}, Suwa et al. 2015; Tauris et al. 2015, 2017).

Finally, we have studied the mass distribution of merging BHBs, NSBHs and DNSs in our simulations. Merging DNS masses range from ~ 1.1 to ~ 2 M$_\odot$ with a prevalence of small masses. Most BHs in merging NSBHs have mass < 10 M$_\odot$, while the masses of BHs in merging BHBs span from 5 to ~ 40 M$_\odot$. In our simulations we find merging systems with mass consistent with all GW events reported by the LIGO-Virgo collaboration so far.

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