Table 1. Initial values and default settings of the population synthesis simulation with COMPAS for our fiducial model. Cyan star symbols in front of a row indicate prescriptions and assumptions that we vary in this study.

Description and name	Value/range	Note / setting
Initial conditions		
Initial mass $m_{1,i}$ Initial mass ratio $q_i = m_{2,i}/m_{1,i}$ Initial semi-major axis $a_i$ Initial metallicity $Z_i$ Initial orbital eccentricity $e_i$	$ \begin{bmatrix} 5,150 \end{bmatrix}  \mathrm{M}_{\odot} \\ [0,1] \\ [0.01,1000]  \mathrm{AU} \\ [0.0001,0.03] \\ 0 \\ \\ \end{bmatrix} $	Kroupa (2001) IMF $\propto m_{1,i}^{-\alpha}$ with $\alpha_{\rm IMF} = 2.3$ for stars above $5  {\rm M}_{\odot}$ We assume a flat mass ratio distribution $p(q_{\rm i}) \propto 1$ with $m_{2,i} \geq 0.1  {\rm M}_{\odot}$ Distributed flat-in-log $p(a_{\rm i}) \propto 1/a_{\rm i}$ Distributed using a close to uniform grid in $\log_{10}(Z_{\rm i})$ with 53 metallicities All binaries are assumed to be circular at birth
Fiducial parameter settings:		
Stellar winds for hydrogen rich stars Stellar winds for hydrogen-poor helium stars Max transfer stability criteria  * Mass transfer accretion rate  Non-conservative mass loss	Belczynski et al. (2010a) Belczynski et al. (2010b) $\zeta$ -prescription thermal timescale Eddington-limited isotropic re-emission	Based on Vink et al. (2000, 2001), including LBV wind mass loss with f <sub>LBV</sub> = 1.5.  Based on Hamann & Koesterke (1998) and Vink & de Koter 2005.  Based on Vigna-Gómez et al. (2018) and references therein  Limited by thermal timescale for stars Vigna-Gómez et al. (2018); Vinciguerra et al. (2020)  Accretion rate is Eddington-limit for compact objects  Massevitch & Yungelson (1975); Bhattacharya & van den Heuvel (1991); Soberman et al. (1997)  Tauris & van den Heuvel (2006)
<ul> <li>★ Case BB mass transfer stability</li> <li>CE prescription</li> <li>★ CE efficiency α-parameter</li> </ul>	always stable $\alpha - \lambda$ 1.0	Based on Tauris et al. (2015, 2017); Vigna-Gómez et al. (2018) based on Webbink (1984); de Kool (1990)
CE $\lambda$ -parameter  * Hertzsprung gap (HG) donor in CE  SN natal kick magnitude $v_k$ SN natal kick polar angle $\theta_k$ SN natal kick azimuthal angle $\phi_k$ SN mean anomaly of the orbit  * Core-collapse SN remnant mass prescription  * USSN remnant mass prescription  ECSN remnant mass prescription  * Core-collapse SN velocity dispersion $\sigma_{rms}^{1D}$ USSN and ECSN velocity dispersion $\sigma_{rms}^{1D}$	$N_{\text{Nanjing}}$ pessimistic $[0, \infty) \text{ km s}^{-1}$ $[0, \pi]$ $[0, 2\pi]$ $[0, 2\pi]$ delayed delayed $m_f = 1.26 \text{ M}_{\odot}$ $265 \text{ km s}^{-1}$ $30 \text{ km s}^{-1}$	Based on Xu & Li (2010a,b) and Dominik et al. (2012) Defined in Dominik et al. (2012): HG donors don't survive a CE phase Drawn from Maxwellian distribution with standard deviation $\sigma_{rms}^{1D}$ $p(\theta_k) = \sin(\theta_k)/2$ Uniform $p(\phi) = 1/(2\pi)$ Uniformly distributed From (Fryer et al. 2012), which has no lower BH mass gap From (Fryer et al. 2012) Based on Equation 8 in Timmes et al. (1996) 1D rms value based on Hobbs et al. (2005) 1D rms value based on e.g., Pfahl et al. (2002); Podsiadlowski et al. (2004)
★ PISN / PPISN remnant mass prescription     ★ Maximum NS mass     Tides and rotation	Marchant et al. (2019) $max_{NS} = 2.5 M_{\odot}$	As implemented in Stevenson et al. (2019)  We do not include prescriptions for tides and/or rotation
Simulation settings		
Total number of binaries sampled per metallicity Sampling method Binary fraction Solar metallicity $Z_{\odot}$ Binary population synthesis code	$\approx 10^6$ STROOPWAFEL $f_{bin} = 1$ $Z_{\odot} = 0.0142$ COMPAS	We simulate about a million binaries per Z <sub>i</sub> grid point Adaptive importance sampling from Broekgaarden et al. (2019). Corrected factor to be consistent with e.g., Sana (2017) based on Asplund et al. (2009) Stevenson et al. (2017); Barrett et al. (2018); Vigna-Gómez et al. (2018); Neijssel et al. (2019) Broekgaarden et al. (2019).

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REFERENCES
Asplund M., Grevesse N., Sauval A. J., Scott P., 2009, ARA&A, 47, 481
Barrett J. W., Gaebel S. M., Neijssel C. J., Vigna-Gómez A., Stevenson S., Berry C. P. L., Farr W. M., Mandel I., 2018, MNRAS, 477, 4685
Belczynski K., Bulik T., Fryer C. L., Ruiter A., Valsecchi F., Vink J. S., Hurley J. R., 2010a, ApJ, 714, 1217
Belczynski K., Dominik M., Bulik T., O'Shaughnessy R., Fryer C., Holz D. E., 2010b, ApJ, 715, L138
Bhattacharya D., van den Heuvel E. P. J., 1991, Phys. Rep., 203, 1
Broekgaarden F. S., et al., 2019, MNRAS, 490, 5228
de Kool M., 1990, ApJ, 358, 189
Dominik M., Belczynski K., Fryer C., Holz D. E., Berti E., Bulik T., Mand el I., O'Shaughnessy R., 2012, ApJ, 759, 52
Fryer C. L., Belczynski K., Wiktorowicz G., Dominik M., Kalogera V., Holz D. E., 2012, ApJ, 749, 91
Hamann W. R., Koesterke L., 1998, A&A, 335, 1003
Hobbs G., Lorimer D. R., Lyne A. G., Kramer M., 2005, MNRAS, 360, 974
Kroupa P., 2001, MNRAS, 322, 231
Kruckow M. U., Tauris T. M., Langer N., Kramer M., Izzard R. G., 2018, MNRAS, 481, 1908
Marchant P., Renzo M., Farmer R., Pappas K. M. W., Taam R. E., de Mink S. E., Kalogera V., 2019, ApJ, 882, 36
Massevitch A., Yungelson L., 1975, Mem. Soc. Astron. Italiana, 46, 217
Neijssel C. J., et al., 2019, MNRAS, 490, 3740
Pfahl E., Rappaport S., Podsiadlowski P., 2002, ApJ, 571, L37
```

Sana H., 2017, in Eldridge J. J., Bray J. C., McClelland L. A. S., Xiao L., eds, IAU Symposium Vol. 329, The Lives and Death-Throes of Massive Stars. pp 110–117 (arXiv:1703.01608), doi:10.1017/S1743921317003209
Soberman G. E., Phinney E. S., van den Heuvel E. P. J., 1997, A&A, 327, 620
Stevenson S., Vigna-Gómez A., Mandel I., Barrett J. W., Neijssel C. J., Perkins D., de Mink S. E., 2017, Nature Communications, 8, 14906
Stevenson S., Sampson M., Powell J., Vigna-Gómez A., Neijssel C. J., Szécsi D., Mandel I., 2019, ApJ, 882, 121

Tauris T. M., van den Heuvel E. P. J., 2006, Formation and evolution of compact stellar X-ray sources. pp 623-665

Podsiadlowski P., Langer N., Poelarends A. J. T., Rappaport S., Heger A., Pfahl E., 2004, ApJ, 612, 1044

```
Tauris T. M., Langer N., Podsiadlowski P., 2015, MNRAS, 451, 2123 Tauris T. M., et al., 2017, ApJ, 846, 170
Timmes F. X., Woosley S. E., Weaver T. A., 1996, ApJ, 457, 834 Vigna-Gómez A., et al., 2018, MNRAS, 481, 4009
Vinciguerra S., et al., 2020, MNRAS, 498, 4705
Vink J. S., de Koter A., 2005, A&A, 442, 587
Vink J. S., de Koter A., Lamers H. J. G. L. M., 2000, A&A, 362, 295 Vink J. S., de Koter A., Lamers H. J. G. L. M., 2001, A&A, 369, 574 Webbink R. F., 1984, ApJ, 277, 355
Xu X.-J., Li X.-D., 2010a, ApJ, 716, 114
Xu X.-J., Li X.-D., 2010b, ApJ, 722, 1985
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