

# Introduction to NLP

242.

Introduction to Parsing

# Parsing programming languages

```
#include <stdio.h>

int main()
{
    int n, reverse = 0;

    printf("Enter a number to reverse\n");
    scanf("%d", &n);

    while (n != 0)
    {
        reverse = reverse * 10;
        reverse = reverse + n%10;
        n = n/10;
    }
    printf("Reverse of entered number is = %d\n", reverse);

    return 0;
}
```

# Parsing human languages

- Rather different than computer languages
  - Can you think in which ways?

# Parsing human languages

- Rather different than computer languages
  - No types for words
  - No brackets around phrases
  - Ambiguity
    - Words
    - Parses
  - Implied information

# The parsing problem

- Parsing means associating tree structures to a sentence, given a grammar (e.g., CFG)
  - There may be exactly one such tree structure
  - There may be many such structures
  - There may be none
- Grammars (e.g., CFG) are declarative
  - They don't specify how the parse tree will be constructed

# Syntactic Issues

- PP attachment
  - I saw the man with the telescope
- Gaps
  - Mary likes Physics but hates Chemistry
- Coordination scope
  - Small boys and girls are playing
- Particles vs. prepositions
  - She ran up a large bill
- Gerund vs. adjective
  - Frightening kids can cause trouble

# Applications of parsing

- Grammar checking
  - I want to return this shoes.
- Question answering
  - How many people in sales make \$40K or more per year?
- Machine translation
  - E.g., word order – SVO vs. SOV
- Information extraction
  - *Breaking Bad* takes place in New Mexico.
- Speech generation
- Speech understanding

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Parsing Evaluation



# Parsing Evaluation

- Parseval: precision and recall
  - get the proper constituents
- Labeled precision and recall
  - also get the correct non-terminal labels
- F1
  - harmonic mean of precision and recall
- Crossing brackets
  - (A (B C)) vs ((A B) C)
- PTB corpus
  - training 02-21, development 22, test 23

# Evaluation Example

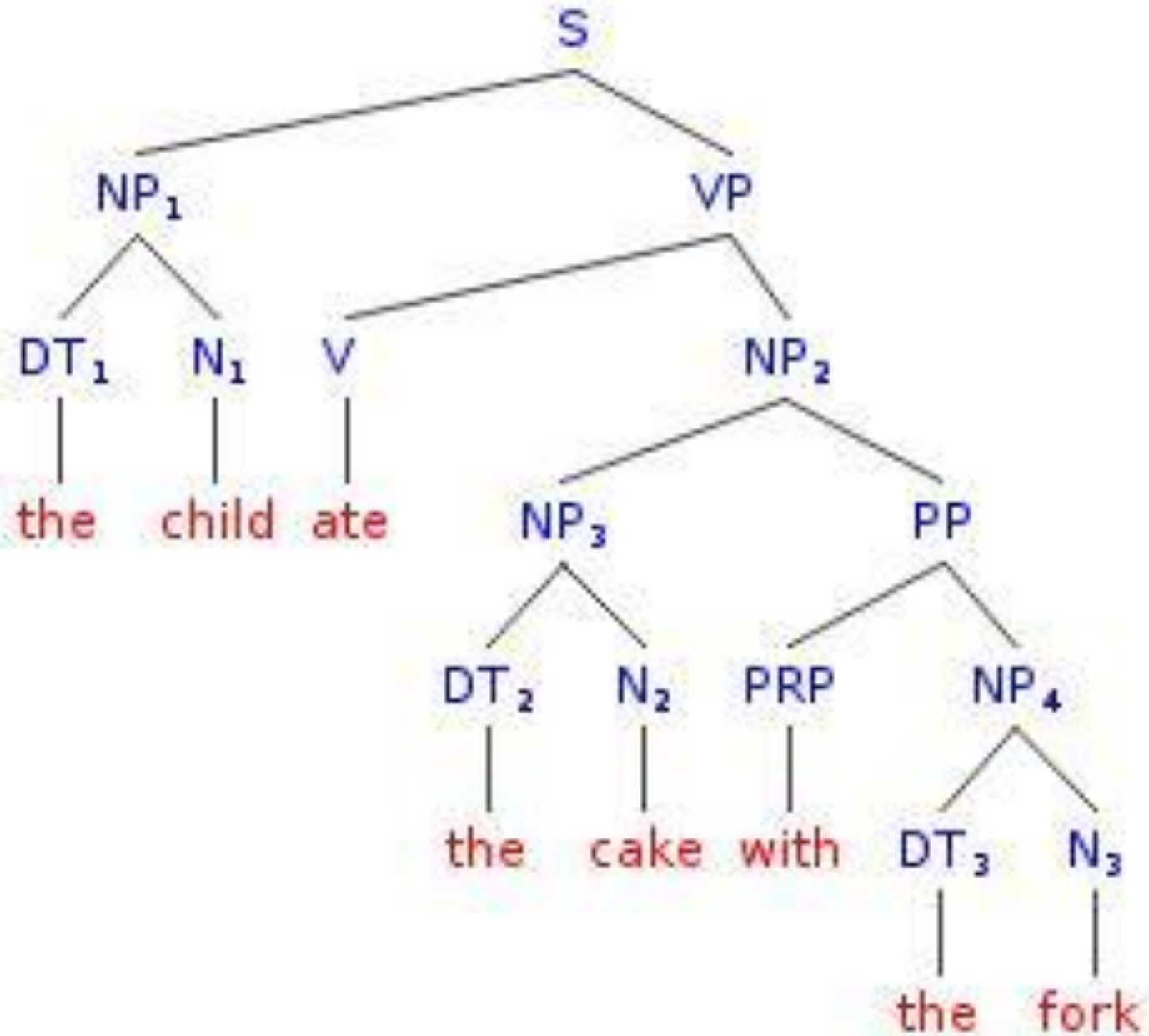
GOLD = (S (NP (DT The) (JJ Japanese) (JJ industrial) (NNS companies))  
(VP (MD should) (VP (VB know) (ADVP (JJR better))))) (. .)

CHAR = (S (NP (DT The) (JJ Japanese) (JJ industrial) (NNS companies))  
(VP (MD should) (VP (VB know)) ((ADVP (**RBR** better))))) (. .))

# Introduction to NLP

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Classic parsing methods



S -> NP VP

NP -> DT N | NP PP

PP -> PRP NP

VP -> V NP | VP PP

DT -> 'a' | 'the'

N -> 'child' | 'cake' | 'fork'

PRP -> 'with' | 'to'

V -> 'saw' | 'ate'

# Parsing as search

- There are two types of constraints on the parses
  - From the input sentence
  - From the grammar
- Therefore, two general approaches to parsing
  - Top-down
  - Bottom-up

# Top down parsing

S

S → NP VP

NP → DT N | NP PP

PP → PRP NP

VP → V NP | VP PP

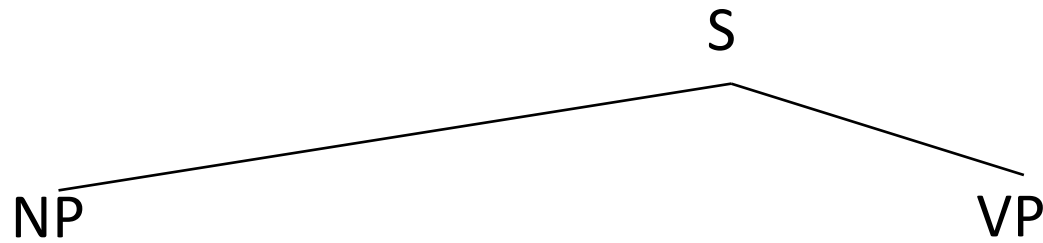
DT → 'a' | 'the'

N → 'child' | 'cake' | 'fork'

PRP → 'with' | 'to'

V → 'saw' | 'ate'

# Top down parsing



S -> NP VP

NP -> DT N | NP PP

PP -> PRP NP

VP -> V NP | VP PP

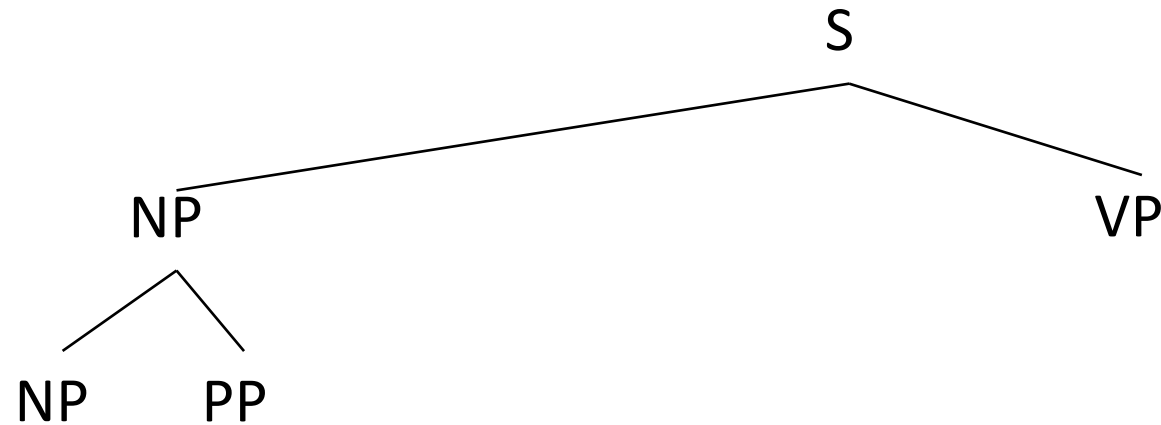
DT -> 'a' | 'the'

N -> 'child' | 'cake' | 'fork'

PRP -> 'with' | 'to'

V -> 'saw' | 'ate'

# Top down parsing



S → NP VP

NP → DT N | NP PP

PP → PRP NP

VP → V NP | VP PP

DT → 'a' | 'the'

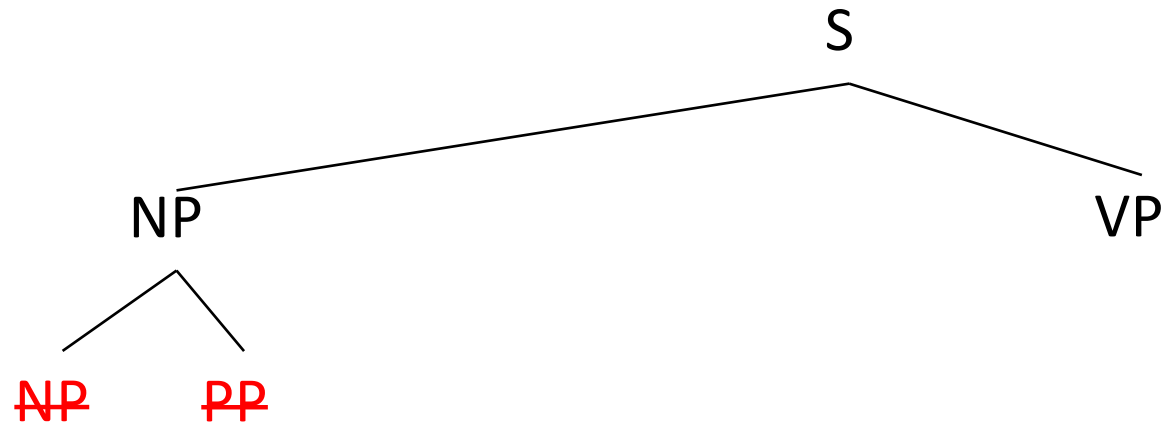
N → 'child' | 'cake' | 'fork'

PRP → 'with' | 'to'

V → 'saw' | 'ate'



# Top down parsing



S → NP VP

NP -> DT N | NP PP

PP → PRP NP

VP  $\rightarrow$  V NP | VP PP

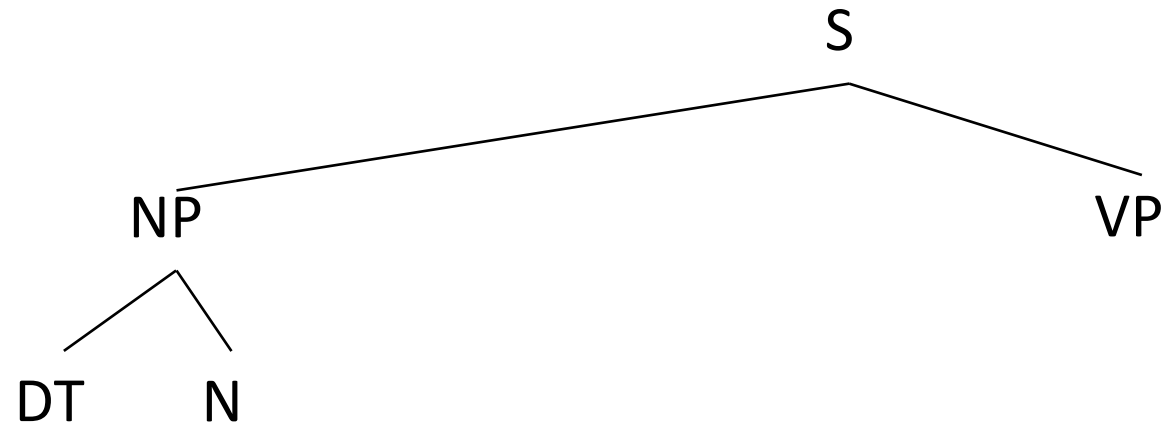
DT -&gt; 'a' | 'the'

N -> 'child' | 'cake' | 'fork'

```
PRP -> 'with' | 'to'
```

V → 'saw' | 'ate'

# Top down parsing



**S** -> **NP VP**

**NP** -> **DT N | NP PP**

**PP** -> **PRP NP**

**VP** -> **V NP | VP PP**

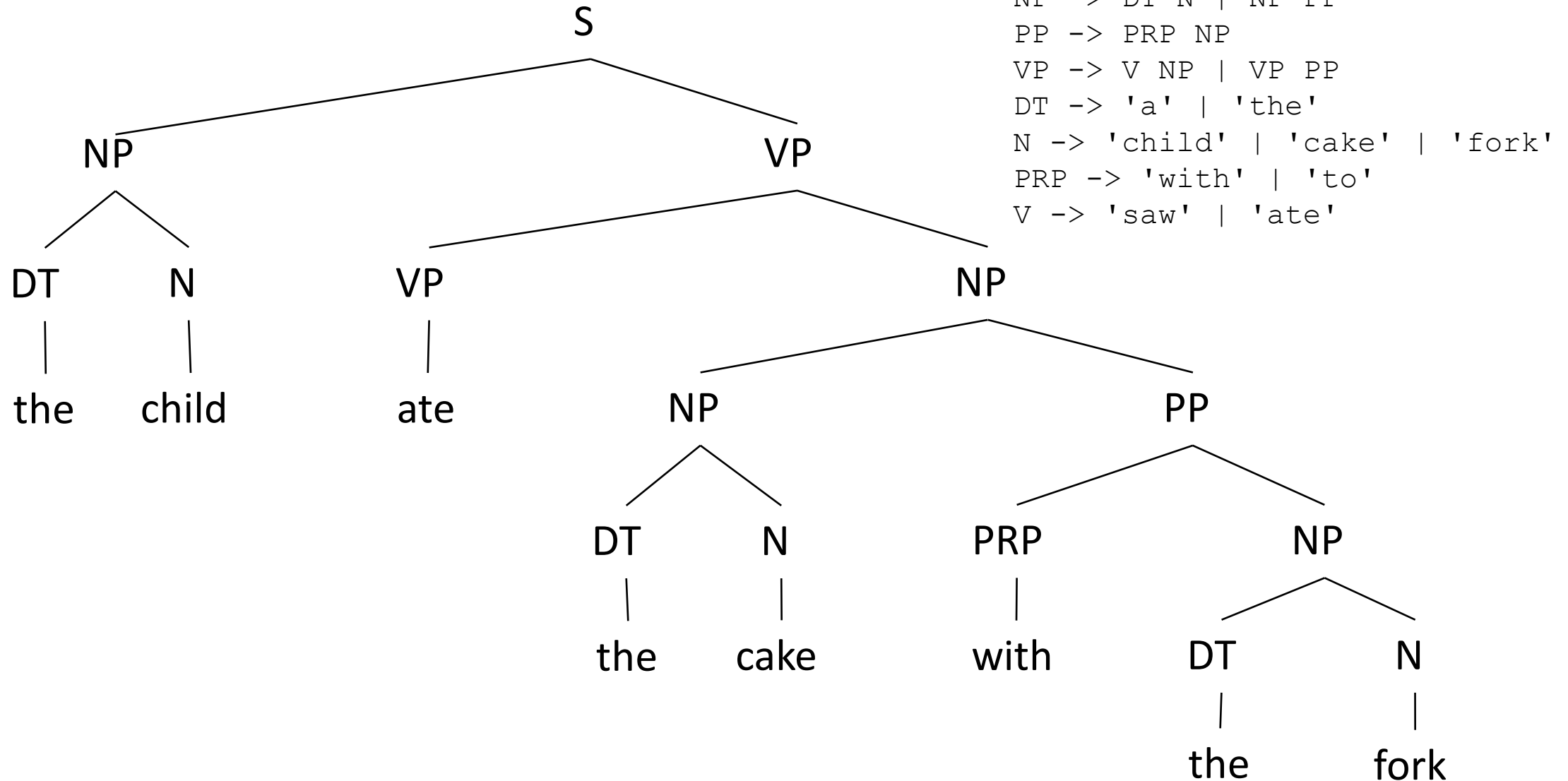
**DT** -> **'a' | 'the'**

**N** -> **'child' | 'cake' | 'fork'**

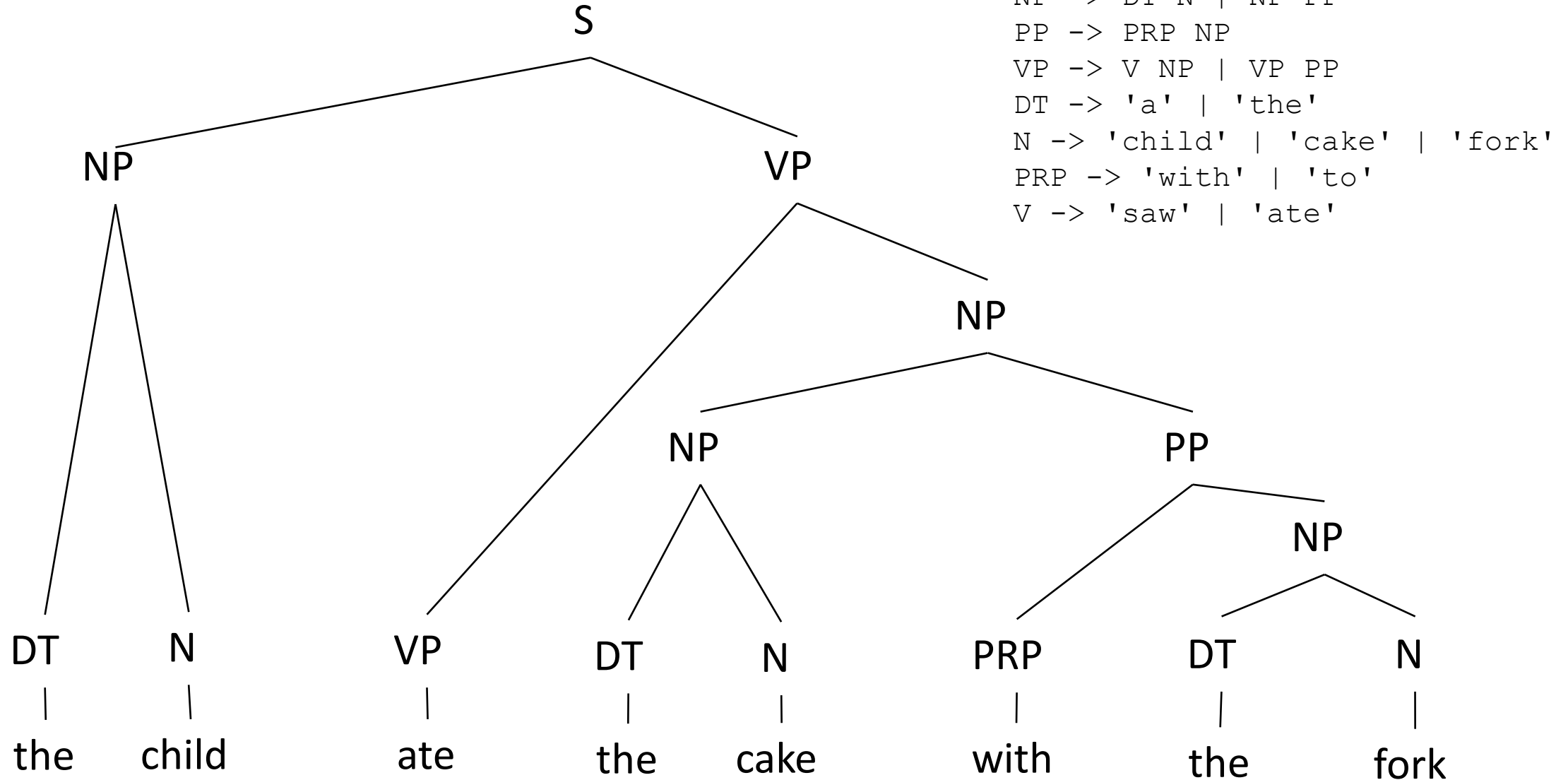
**PRP** -> **'with' | 'to'**

**V** -> **'saw' | 'ate'**

# Top down parsing



# Bottom up parsing



# Bottom up vs. top down methods

- Bottom up
  - explores options that won't lead to a full parse
  - Example: shift-reduce (srparser in nltk)
  - Example: CKY (Cocke-Kasami-Younger)
- Top down
  - explores options that don't match the full sentence
  - Example: recursive descent (rdparser in nltk)
  - Example: Earley parser
- Dynamic programming
  - caches of intermediate results (memoization)

# Introduction to NLP

Shift-Reduce Parsing

# Shift-Reduce Parsing

- A bottom-up parser
  - Tries to match the RHS of a production until it can build an S
- *Shift* operation
  - Each word in the input sentence is pushed onto a stack
- *Reduce-n* operation
  - If the top  $n$  words on the top of the stack match the RHS of a production, then they are popped and replaced by the LHS of the production
- Breadth-first search
- Stopping condition
  - The process stops when the input sentence has been processed and S has been popped from the stack

# Shift-Reduce Parsing Example

```
[ * the child ate the cake]
S [ 'the' * child ate the cake]
R [ DT * child ate the cake]
S [ DT 'child' * ate the cake]
R [ DT N * ate the cake]
R [ NP * ate the cake]
S [ NP 'ate' * the cake]
R [ NP V * the cake]
S [ NP V 'the' * cake]
R [ NP V DT * cake]
S [ NP V DT 'cake' * ]
R [ NP V DT N * ]
R [ NP V NP * ]
R [ NP VP * ]
R [ S * ]
```

**(S (NP (DT the) (N child)) (VP (V ate) (NP (DT the) (N cake))))**



# Shift-Reduce Parsing

- In nltk

```
>>> from nltk.app import srparser;  
>>> srparser()
```

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Cocke-Kasami-Younger (CKY) Parsing

# Notes on Left Recursion

- Problematic for many parsing methods
  - Infinite loops when expanding
- But appropriate linguistically
  - NP → DT N
  - NP → PN
  - DT → NP 's
  - Mary's mother's sister's friend

# Chart Parsing

- Top-down parsers have problems with expanding the same non-terminal
  - In particular, pre-terminals such as POS
  - Bad idea to use top-down (recursive descent) parsing as is
- Bottom-up parsers have problems with generating locally feasible subtrees that are not viable globally
- Chart parsing will address these issues

# Dynamic Programming

- **Motivation**

- A lot of the work is repeated
- Caching intermediate results improves the complexity

- **Dynamic programming**

- Building a parse for a substring  $[i,j]$  based on all parses  $[i,k]$  and  $[k, j]$  that are included in it.

- **Complexity**

- $O(n^3)$  for recognizing an input string of length  $n$

# Dynamic Programming

- CKY (Cocke-Kasami-Younger)
  - bottom-up
  - requires a normalized (binarized) grammar
- Earley parser
  - top-down
  - more complicated
  - (separate lecture)

# CKY Algorithm

```
function cky (sentence W, grammar G) returns table
  for i in 1..length(W) do
    table[i-1,i] = {A|A->Wi in G}
  for j in 2..length(W) do
    for i in j-2 down to 0 do
      for k in (i+1) to (j-1) do
        table[i,j] = table[i,j] union {A|A->BC in G, B in
table [I,k], C in table [k,j]}
```

If the start symbol  $S$  is in table  $[0,n]$  then  $W$  is in  $L(G)$

# Example

`["the", "child", "ate", "the", "cake", "with", "the", "fork"]`

`S -> NP VP`

`NP -> DT N | NP PP`

`PP -> PRP NP`

`VP -> V NP | VP PP`

`DT -> 'a' | 'the'`

`N -> 'child' | 'cake' | 'fork'`

`PRP -> 'with' | 'to'`

`V -> 'saw' | 'ate'`



the

child

ate

the

cake

with

the

fork

the

DT							
child							
ate							
the							
cake							
with							
the							
fork							

the

DT							
child	N						
ate							
the							
cake							
with							
the							
fork							

the

DT	NP						
child	N						
	ate						
		the					
			cake				
				with			
					the		
						fork	

the	DT	NP					
		/					
child	N						
	ate						
		the					
			cake				
				with			
					the		
						fork	

the	DT	NP						
child	N							
ate	V							
the								
cake								
with								
the								
fork								

the

DT	NP						
child	N						
	ate	V					
		the	DT				
			cake				
				with			
					the		
						fork	

the	DT	NP					
child	N						
ate	V						
the	DT						
cake	N						
with							
the							
fork							



the	DT	NP						
child	N							
ate	V							
the	DT	NP						
cake	N							
with								
the								
fork								

the	DT	NP						
child	N							
ate	V							
the	DT	NP						
cake	N							
with								
the								
fork								

the

DT	NP						
child	N						
ate	V			VP			
the	DT			NP			
cake	N						
with							
the							
fork							

the

DT	NP						
child	N						
ate	V			VP			
		the	DT	NP			
			cake	N			
				with			
					the		
						fork	

the

DT	NP			S			
child	N						
ate	V			VP			
the	DT			NP			
cake	N						
with							
the							
fork							

the

DT	NP			S			
child	N						
ate	V			VP			
the	DT			NP			
cake	N						
with							
the							
fork							

the

DT	NP			S			
child	N						
ate	V			VP			
the	DT			NP			
cake	N						
with	PRP						
the							
fork							

the

DT	NP			S			
child	N						
ate	V			VP			
the	DT	NP				NP	
cake	N						
with	PRP					PP	
the	DT					NP	
fork	N						



the

DT	NP			S			
child	N						
ate	V			VP			VP
the		DT	NP				NP
cake			N				
with				PRP			PP
the					DT	NP	
fork						N	

the

DT	NP			S			
child	N						
ate	V			VP			VP
							/
		the	DT	NP			NP
				N			
			cake				
				with	PRP		PP
					the	DT	NP
						fork	N

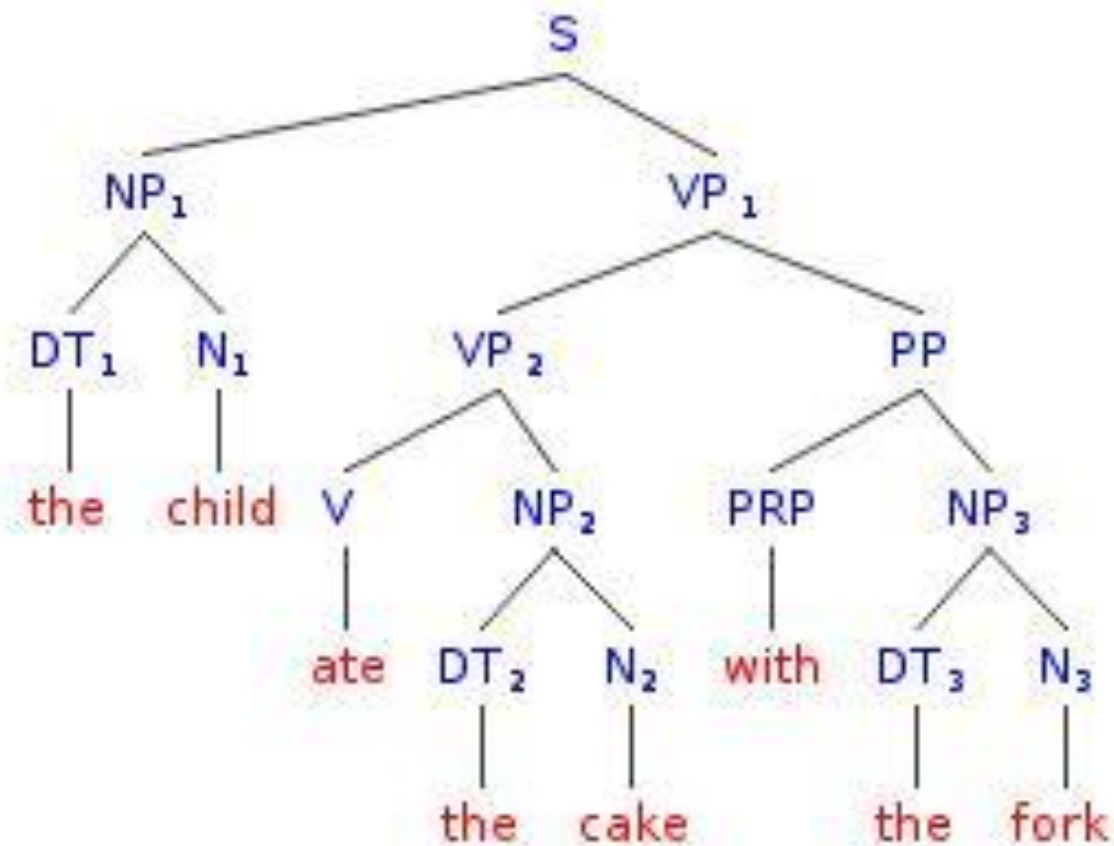
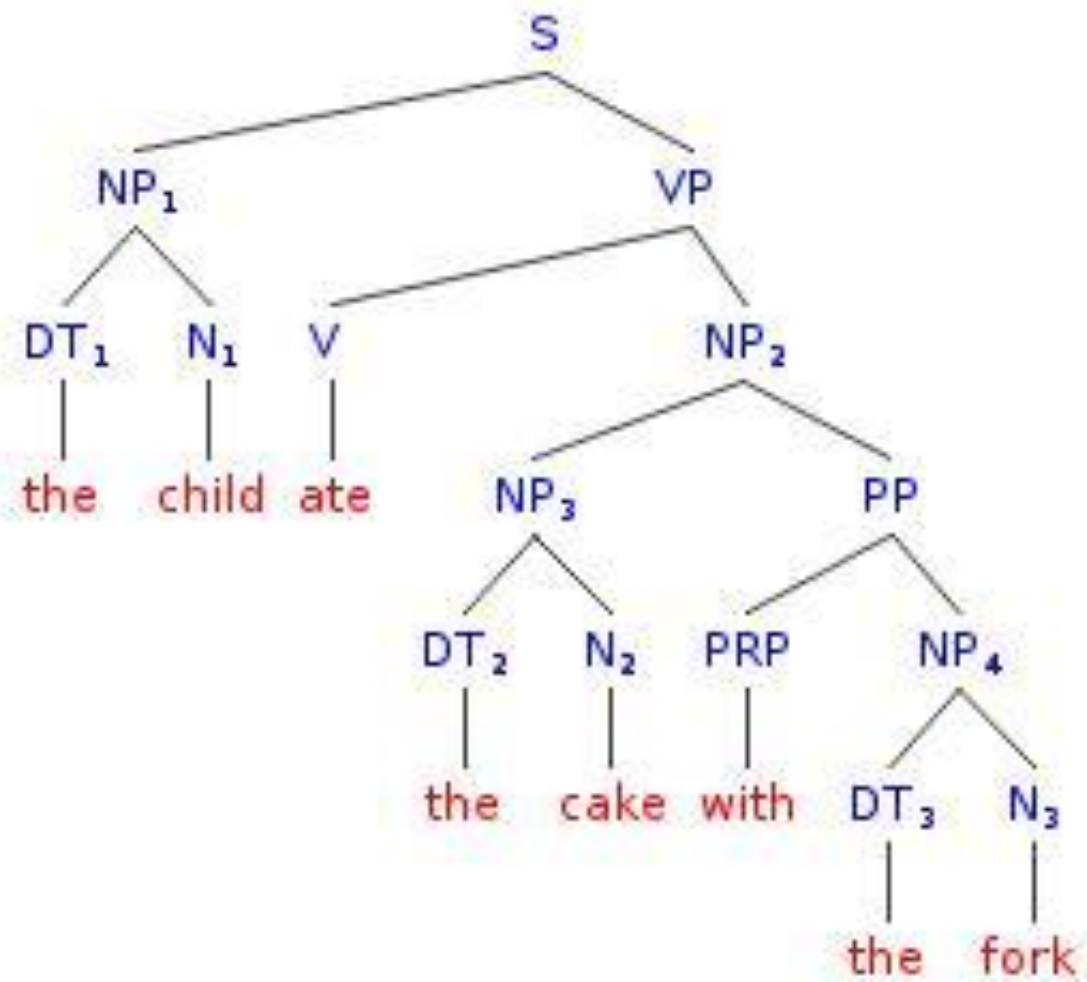
the

DT	NP			S			S
child	N						
ate	V		VP				VP
the	DT	NP					NP
cake	N						
with	PRP						PP
the	DT	NP					
fork	N						

the

DT	NP			S			S
child	N						
ate	V		VP			VP	
the	DT	NP				NP	
cake	N						
with	PRP					PP	
the	DT	NP					
fork		N					

[0] DT [1] N [2] ==> [0] NP [2]  
[3] DT [4] N [5] ==> [3] NP [5]  
[6] DT [7] N [8] ==> [6] NP [8]  
[2] V [3] NP [5] ==> [2] VP [5]  
[5] PRP [6] NP [8] ==> [5] PP [8]  
[0] NP [2] VP [5] ==> [0] S [5]  
[3] NP [5] PP [8] ==> [3] NP [8]  
**[2] V [3] NP [8] ==> [2] VP [8]**  
**[2] VP [5] PP [8] ==> [2] VP [8]**  
[0] NP [2] VP [8] ==> [0] S [8]



What is the *meaning* of each of these sentences?

```
(S
  (NP (DT the) (N child))
  (VP
    (VP (V ate) (NP (DT the) (N cake)))
    (PP (PRP with) (NP (DT the) (N fork))))))
```

```
(S
  (NP (DT the) (N child))
  (VP
    (VP (V ate) (NP (DT the) (N cake)))
    (PP (PRP with) (NP (DT the) (N fork))))))
```

```
(S
  (NP (DT the) (N child))
  (VP
    (V ate)
    (NP
      (NP (DT the) (N cake))
      (PP (PRP with) (NP (DT the) (N fork))))))
```

# Complexity of CKY

- Space complexity
  - There are  $O(n^2)$  cells in the table
- Single parse
  - Each cell requires a linear lookup.
  - Total time complexity is  $O(n^3)$
- All parses
  - Total time complexity is exponential



# A longer example

["take", "this", "book"]

S -> NP VP | Aux NP VP | VP

NP -> PRON | Det Nom

Nom -> N | Nom N | Nom PP

PP -> PRP NP

VP -> V | V NP | VP PP

Det -> 'the' | 'a' | 'this'

PRON -> 'he' | 'she'

N -> 'book' | 'boys' | 'girl'

PRP -> 'with' | 'in'

V -> 'takes' | 'take'

# Non-binary productions

["take", "this", "book"]

S -> NP VP | **Aux NP VP** | **VP**

NP -> **PRON** | Det Nom

Nom -> **N** | Nom N | Nom PP

PP -> PRP NP

VP -> **V** | V NP | VP PP

Det -> 'the' | 'a' | 'this'

PRON -> 'he' | 'she'

N -> 'book' | 'boys' | 'girl'

PRP -> 'with' | 'in'

V -> 'takes' | 'take'

# Chomsky Normal Form (CNF)

- All rules have to be in binary form:
  - $X \rightarrow YZ$  or  $X \rightarrow w$
- This introduces new non-terminals for
  - hybrid rules
  - n-ary rules
  - unary rules
  - epsilon rules (e.g.,  $NP \rightarrow \varepsilon$ )
- Any CFG can be converted to CNF
  - See Aho & Ullman p. 152

# ATIS grammar

## Original version

$S \rightarrow NP VP$

$S \rightarrow Aux NP VP$

$S \rightarrow VP$

$NP \rightarrow Pronoun$

$NP \rightarrow Proper-Noun$

$NP \rightarrow Det Nominal$

$Nominal \rightarrow Noun$

$Nominal \rightarrow Nominal Noun$

$Nominal \rightarrow Nominal PP$

$VP \rightarrow Verb$

$VP \rightarrow Verb NP$

$VP \rightarrow VP PP$

$PP \rightarrow Prep NP$

# ATIS grammar in CNF

## Original version

$S \rightarrow NP VP$

$S \rightarrow \mathbf{Aux NP VP}$

$S \rightarrow VP$

$NP \rightarrow \text{Pronoun}$

$NP \rightarrow \text{Proper-Noun}$

$NP \rightarrow \text{Det Nominal}$

$\text{Nominal} \rightarrow \text{Noun}$

$\text{Nominal} \rightarrow \text{Nominal Noun}$

$\text{Nominal} \rightarrow \text{Nominal PP}$

$VP \rightarrow \text{Verb}$

$VP \rightarrow \text{Verb NP}$

$VP \rightarrow VP PP$

$PP \rightarrow \text{Prep NP}$

## CNF version

$S \rightarrow NP VP$

$S \rightarrow \mathbf{X1 VP}$

$\mathbf{X1} \rightarrow \mathbf{Aux NP}$

$S \rightarrow \text{book} \mid \text{include} \mid \text{prefer}$

$S \rightarrow \text{Verb NP}$

$S \rightarrow VP PP$

$NP \rightarrow \text{I} \mid \text{he} \mid \text{she} \mid \text{me}$

$NP \rightarrow \text{Houston} \mid \text{NWA}$

$NP \rightarrow \text{Det Nominal}$

$\text{Nominal} \rightarrow \text{book} \mid \text{flight} \mid \text{meal} \mid \text{money}$

$\text{Nominal} \rightarrow \text{Nominal Noun}$

$\text{Nominal} \rightarrow \text{Nominal PP}$

$VP \rightarrow \text{book} \mid \text{include} \mid \text{prefer}$

$VP \rightarrow \text{Verb NP}$

$VP \rightarrow VP PP$

$PP \rightarrow \text{Prep NP}$

# ATIS grammar in CNF

## Original version

$S \rightarrow NP VP$   
 $S \rightarrow Aux NP VP$

$S \rightarrow VP$

$NP \rightarrow \text{Pronoun}$   
 $NP \rightarrow \text{Proper-Noun}$   
 $NP \rightarrow \text{Det Nominal}$   
 $\text{Nominal} \rightarrow \text{Noun}$   
 $\text{Nominal} \rightarrow \text{Nominal Noun}$   
 $\text{Nominal} \rightarrow \text{Nominal PP}$   
 $VP \rightarrow \text{Verb}$   
 $VP \rightarrow \text{Verb NP}$   
 $VP \rightarrow VP PP$   
 $PP \rightarrow \text{Prep NP}$

## CNF version

$S \rightarrow NP VP$   
 $S \rightarrow X1 VP$   
 $X1 \rightarrow Aux NP$   
 $S \rightarrow \text{book} \mid \text{include} \mid \text{prefer}$   
 $S \rightarrow \text{Verb NP}$   
 $S \rightarrow VP PP$   
 $NP \rightarrow \text{I} \mid \text{he} \mid \text{she} \mid \text{me}$   
 $NP \rightarrow \text{Houston} \mid \text{NWA}$   
 $NP \rightarrow \text{Det Nominal}$   
 $\text{Nominal} \rightarrow \text{book} \mid \text{flight} \mid \text{meal} \mid \text{money}$   
 $\text{Nominal} \rightarrow \text{Nominal Noun}$   
 $\text{Nominal} \rightarrow \text{Nominal PP}$   
 $VP \rightarrow \text{book} \mid \text{include} \mid \text{prefer}$   
 $VP \rightarrow \text{Verb NP}$   
 $VP \rightarrow VP PP$   
 $PP \rightarrow \text{Prep NP}$

# Chomsky Normal Form

- All rules have to be in binary form:
  - $X \rightarrow YZ$  or  $X \rightarrow w$
- New non-terminals for hybrid rules, n-ary and unary rules:
  - $\text{INF-VP} \rightarrow \text{to VP}$  *becomes*
    - $\text{INF-VP} \rightarrow \text{TO VP}$
    - $\text{TO} \rightarrow \text{to}$
  - $S \rightarrow \text{Aux NP VP}$  *becomes*
    - $S \rightarrow \text{R1 VP}$
    - $\text{R1} \rightarrow \text{Aux NP}$
  - $S \rightarrow \text{VP}$     $\text{VP} \rightarrow \text{Verb}$     $\text{VP} \rightarrow \text{Verb NP}$     $\text{VP} \rightarrow \text{Verb PP}$  *becomes*
    - $S \rightarrow \text{book}$
    - $S \rightarrow \text{buy}$
    - $S \rightarrow \text{R2 PP}$
    - $S \rightarrow \text{Verb PP}$
  - etc.

# Issues with CKY

- Weak equivalence only
  - Same language, different structure
  - If the grammar had to be converted to CNF, then the final parse tree doesn't match the original grammar
  - However, it can be converted back using a specific procedure
- Syntactic ambiguity
  - (Deterministic) CKY has no way to perform syntactic disambiguation



# Notes

- Demo:
  - <http://lxmls.it.pt/2015/cky.html>
- Recognizing vs. parsing
  - Recognizing just means determining if the string is part of the language defined by the CFG
  - Parsing is more complicated – it involves producing a parse tree