



$$\begin{cases}
 \text{input } x \in \mathbb{R}^D \\
 \text{encoder network } h = \text{ReLU}(Wx + b) \\
 \text{decoder network } \hat{x} = \text{ReLU}(\tilde{W}h + \tilde{b}) \\
 \text{output } \hat{x} \in \mathbb{R}^D
 \end{cases}$$

$W \in \mathbb{R}^{H \times D}$   $b \in \mathbb{R}^H$   
 $\tilde{W} \in \mathbb{R}^{D \times H}$   $\tilde{b} \in \mathbb{R}^D$   
 $\text{ReLU} = \max(0, x)$   
 applied element-wise

Training Objective :

$$L = \frac{1}{n} \sum_{i=1}^n \|x_i - \text{ReLU}(\tilde{W} \text{ReLU}(Wx_i + b) + \tilde{b})\|_2^2$$

Using back-propagation to find optimal solution of weights  $W, \tilde{W}$  and bias  $b, \tilde{b}$

- ① Randomly initiate  $W, b, \tilde{W}, \tilde{b}$
- ② Compute gradient of Loss function with respect to  $W, b, \tilde{W}, \tilde{b}$
- ③ Use stochastic gradient descent to update  $W, b, \tilde{W}, \tilde{b}$  until convergence.

## Quiz4: Algorithm of an one layer Autoencoder