# Can we predict house prices using known features of each house and a supervised learning approach?

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# 1 Background:

House prices are an important part of the economy and usually reflect trends in it. They can be influenced by the physical condition of the house and by other attributes such as location (Bin 2004). Prices are important for homeowners, prospective buyers and estate agents. Prediction methods could help lead to more informed decisions to each of these stakeholders. Gao et al. (2019) suggest that prediction models may be useful for narrowing down the range of available houses for prospective buyers and allowing sellers to predict optimal times to list their houses on the market. Prediction accuracy would be important in all of these situations as inaccurate models would not be trusted by their users.

Something else to take into account is that it may be difficult for prospective buyers to visualise how square footage measurements of a house are calculated or how this measurement translates into physical size if they have not visited the house themselves. Buyers therefore rely on factors such as the number of bedrooms, bathrooms or house age to get an idea of the value of the house. This analysis will focus on which features of a house have the **largest influence** on the prediction of house prices. This report does not look at the effect of time on house prices. It is already well known that house prices tend to increase year on year (Alfiyatin et al. 2017).

In most countries there is some form of house price index that measures changes in prices (Lu et al. 2017). This contains a summary of all transactions that take place but not the individual features of each house sold, therefore it cannot be used to make predictions of house price.

Many house price prediction models have been created using machine learning methods. The hedonic price model is the most extensively researched and uses regression methods (Gao et al. 2019). Hedonic models assume that the value of a house is reflected by a set of attributes (Bin 2004). The goal of a regression approach is to build an equation which defines y, the dependent variable as a function of the x variable(s). This equation can then be used for prediction of y when given unseen values of x. Machine learning methods use data in a 'training set' to build a model, this model is then used to make predictions on an unseen 'test set' of data. The accuracy of models can be calculated by taking the predicted values from the actual values and squaring it, this value is known as mean squared error (MSE) and the square root of this (RMSE) will be used in this analysis for model comparison. The reason for using the RMSE for comparison is because it is in the same units as the response variable, in this case, thousands of pounds.

## 1.1 Objectives:

- Understand which attributes of houses can be used to construct a prediction model for house price.
- Minimize the differences between predicted and actual house prices by using model selection to choose the most accurate model.

## 2 Data:

### 2.1 Data Description

The dataset chosen for this analysis contains the house sale price, in US dollars, along with attributes of each house such as number of bedrooms, number of bathrooms, etc. The houses were all sold in Washington in 2014, a state in the Northwest of the USA. There were 4600 observations with 17 variables in the original data set downloaded from [Kaggle] (https://www.kaggle.com/shree1992/housedata). Although the dataset was from 2014, it was particularly interesting because it contained a large amount of information and an interesting selection of variables. A more recent data set, or one from the UK could not be found, and so the analysis went ahead with this data set.

# 2.2 Data Preparation and Exploration

The first task was preparing and cleaning the dataset. This served two purposes, firstly to get to know the different variables in the data and existing patterns or correlations between them and secondly to carry out feature selection. Variables that contained a majority missing data, those with constant variables (e.g. Country contained the value USA for all observations) and the date column were removed. Any observations in which price was equal to zero were removed. The cleaned dataset was exported ready for use in the main analysis. This cleaned data set contained 4492 observations and 11 variables (Table 1). Some alterations were made to existing variables, these are listed in the descriptions of table 1 alongside the variable.

**Table 1**: Description of all variables present in the cleaned dataset and explanations of how they were calculated if they have been altered from the original dataset

Variable	Description of Variable
price	House sale price in thousands of US dollars, the original data was divided by
	1000 to give this value, numeric
bedrooms	Number of bedrooms, numeric
bathrooms	Number of bathrooms, numeric
sqft_living	Area of house in square feet, numeric
sqft_lot	Area of whole housing lot in square feet, numeric
floors	Number of floors in the house, numeric
condition	Condition of house from 1 to 5, numeric
if_basement	1 = if house has a basement, 0 = if house has no basement, this was
	originally showing the size of the basement, but not all houses had
	basements so it was changed to binary
house_age	House Age in years, calculated by 2014 minus the year the house was built
if_renovated	1 = if house has been renovated, 0 = if no renovation, again this was
	originally showing the year of renovation however not all houses had been
	renovated and so it was changed to binary
city	Factor variable (32 levels) giving location of house to the nearest city in
	Washington, USA, any city that had less than 10 houses was removed

#### 2.3 Data Visualisation

The cleaned data set was explored to look for any correlations between variables (Figure 1). Spearmans correlation was used to produce a correlation coefficient giving the strength of the linear relationship between two variables. This method of correlation was chosen as not all of the relationships looked entirely linear when they were plotted. The dependent variable (price) had a positive correlation with house size, number of bathrooms and number of bedrooms. The strongest relationship seen was between sqft\_living and number of bathrooms. It is interesting to note that the only non significant correlation involving price is between price and house age. Multicollinearity occurs when two variables are heavily intercorrelated in a regression

model and it can lead to less accurate predictions, the presence or absence of this in the data will be explored further on in the methods.

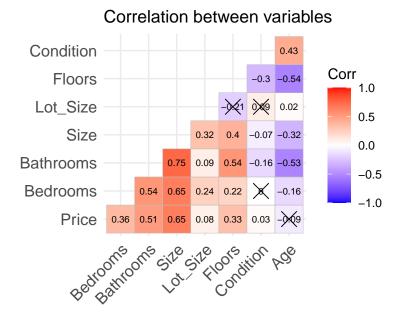


Figure 1: A correlation map showing the correlations between variables according to spearmans correlation (excluding city, if\_basement and if\_renovated), the colours represent strength of correlation, the crosses show where the correlation is not significant.

# 3 Methods

A supervised learning approach was chosen throughout this analysis. In a supervised learning approach there is a continuous response variable of which predictions are to be made, and a number of predictor variables. In all the approaches tried house price was a quantitative variable.

The dataset was split randomly into two parts, a training set containing 80% of the observations and a test set containing the remaining 20%. The training set was used to train all of the models and the test set to assess accuracy of the models. This split was completed using the *sample* function, which took a random sample of 80% of the data without replacement to act as the train data, everything remaining was the test set.

#### 3.1 Linear Regression

Firstly, a simple linear regression model was created using price as the dependent variable (y) and square foot living area (sqft\_living) as the independent variable (x). Sqft\_living was chosen because it was shown to be the most correlated variable to house price in the exploratory data analysis. A simple linear regression model uses the *lm()* function. This linear regression takes a model with equation

and estimates coefficients which produce a line of best fit, minimising the difference between predicted and actual values. This type of simple linear regression is known as ordinary least squares. In the equation above, B0 is the intercept, B1 is the coefficient produced by the model and E is the error term.

This simple model was then expanded to allow all the other variables in the dataset to act as predictor variables, this is known as multiple linear regression. The model output showed that 17 of these variables

had a significant impact (P<0.05) on the price. The coefficients and P values of each of these variables are shown below.

**Table 2**: Names and Coefficient estimates of only the variables that showed significant P-values in the multiple linear regression model involving all predictor variables.

	Coef Estimates	P-Value
(Intercept)	-300.0848039	0.0004652
bedrooms	-58.3531453	0.0000065
bathrooms	68.2541014	0.0012979
sqft_living	0.2609683	0.0000000
condition	36.6402055	0.0231854
if_basement1	-58.8254709	0.0091500
house_age	1.0007524	0.0342776
cityBellevue	402.9644709	0.0000000
cityIssaquah	192.8171552	0.0023546
cityKent	192.0829810	0.0023943
cityKirkland	286.7290160	0.0000059
cityMedina	1191.9241550	0.0000000
cityMercerisland	529.6076728	0.0000000
cityRedmond	243.3809709	0.0000647
citySammamish	217.8271899	0.0008843
citySeattle	313.5117092	0.0000000
cityShoreline	158.5865198	0.0215383
cityWoodinville	143.9101433	0.0460584

It should be noted that *if\_basement*, *if\_renovated* and *city* were all factor variables, and so when they were fit into a model, they were converted into dummy variables, with one variable created for each factor level. This is why some of the variables selected above are not the same as those variables shown in the cleaned data set (Table 1). This also raises the idea that location may have a large influence on house price as 11 of the variables shown above are all dummy variables originating from *city*.

Multicollinearity was explored in the multiple linear model. The variance inflation factors (VIF) for each variable was calculated which shows how much of the variance of the regression coefficient is inflated due to any multicollinearity in the model. None of the VIF scores were above 5 wh, with the highest being bathrooms at 3.3, and so there was no problematic collinearity indicated. This was carried out using the *vif()* function in the *car* package.

Polynomial models of regression were trialed at this point but they did not improve the MSE results and so this approach was not looked into further.

#### 3.2 Variable Selection Methods

To look further into which variables were most influential on price, three variable selection methods were explored. Firstly best-subset selection, which is a method that finds the best combinations of predictors for models of each size that produce the best fit in terms of mean squared error (MSE). The validation set approach and cross-validation are direct methods of test error estimation that were used. The validation set approach produced a model containing a high number of variables and it was decided that cross-validation was the most appropriate method to use to help narrow down the variables needed to predict house price. Cross-validation showed that a model containing 15 variables had the lowest cross-validation error. These variables were extracted and a linear model created containing only them. This linear model had a lower MSE than the simple linear model, but a higher MSE than the linear model containing all of the available variables. This suggested that the model chosen by best-subset selection was less accurate than a multiple linear regression model.

If R2 statistics were used to choose among models instead of cross validation, the model containing all of

variables would always be considered the 'best' one with the lowest error rate. Indirect methods of test error estimation are adjusted R2, CP or BIC criterion.

Forward stepwise selection is slightly different to best-subset selection as it starts with zero variables and one by one adds the variable which gives the smallest increase in squared error. Backward stepwise selection follows the same idea as forward selection but it starts with a full model, and iteratively removes variables until it leaves a one variable model with the lowest mean squared error.

The validation error at different model sizes for the three kinds of variable selection are shown in Figure 2, this also includes the cross-validation error for best-subset selection. Forward and backward selection yielded almost identical results to each other with only a one variable difference to best-subset selection. The specific variables selected from best-subset selection were also very similar to the ones that showed a significant effect in the multiple linear model, with only one variable different. Forward and backward subset selection methods gave lower MSE results than best-subset selection. Figure 2 shows that all of these methods produce extremely similar results, it is also noticeable how there may be some overfitting in these models as the model size increases.

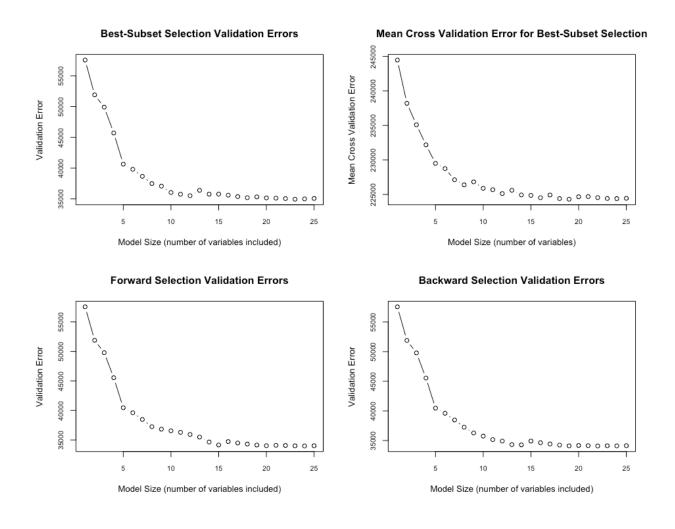


Figure 2: The Validation and Cross Validation Error plots for best-subset, forward and backward selection.

# 3.3 Ridge Regression and LASSO

Ridge Regression and the LASSO are both shrinkage methods. In the above variable selection methods, only a subset of predictors are used. In shrinkage methods all of the predictors are included in the model but the coefficient estimates are constrained towards zero, this can help to reduce variance.

Ridge Regression utilises L2 regularisation, this adds a penalty to the coefficients that is equal to the square of the coefficients. Lambda is a tuning parameter, as its magnitude increases, the shrinkage penalty has more of an impact and the coefficient estimates will be closer to zero. Selecting the right value of lambda is very important, in this analysis it was selected using cross-validation. If lambda = 0, this method would be identical to ordinary least squares. Ridge regression does however always include all of the variables in the data set, this can lead to problems with interpretation.

LASSO is another coefficient shrinkage technique in which the L0 norm is replaced with the L1 norm. LASSO stands for Least Absolute Shrinkage and Selection Operator. The L1 norm applies a penalty to the coefficients equal to the absolute value of the coefficients. In this method, lambda allows some coefficients to be set equal to 0, in which case they are dropped out of the regression model. In this way it acts as a selection method for choosing the variables with the most influence. This decreases the variance of the model but increases the bias. We can change lambda to any value, but in this analysis cross-validation was used to select the best value of lambda. This method suggested a model containing 34 variables led to the lowest RMSE. A model was also created using an alternative value of lambda. This alternative model only contained 15 variables and is therefore more easily interpretable, the RMSE was only increased slightly but was still lower than any of the other models tried in this analysis.

#### 3.4 Tree Based Methods

A few tree based methods were explored in this analysis, starting with a simple decision tree, moving through bagging, randomForests and boosting. Tree based methods are easy to interpret but can sometimes oversimplify things. Trees are grown using branches which split due to conditions, eventually reaching an end node that gives the outcome, in this case the outcome is House Price. Tree methods have a limit on the number of variables, so the reduced data set from forward selection was used throughout the tree methods.

Using just one decision tree gave a MSE higher than using just ordinary least squares, the pruned tree with the lowest cross validation error had the same number of branches as the original decision tree. This simple decision tree only used one variable - sqft\_living, suggesting this has largest influence on house price.

#### 3.4.1 Random Forests and Bagging

RandomForest is a method that combines together multiple decision trees, this can help to improve prediction accuracy. Bagging is a type of randomForest, also known as Bootstrap Aggregation, in which the number of predictors (m) that is considered at each split of the tree is equal to the total number of predictors (p) in the data set. Random Forests only considers a subset of the predictors, usually sqrt(p) which in this case was around 3, at each split. Lowering the number of predictors considered at each split of the tree reduces variance and in this analysis led to a much improved model compared to randomForest where m = p.

#### 3.4.2 Boosting

Boosting is another tree based method in which trees are grown sequentially, with each tree 'learning' from the last. It learns more slowly than other approaches and can reduce overfitting. Two different variations of a boosted model were created, with different values of lambda, the tuning parameter, and although reducing lambda improved MSE, it was not competitive with the multiple linear regression.

The tree based methods, although more easily interpretable, produced some high RMSE results. The best of these models were the randomForests with *mtry=3* and a smaller number of trees, the RMSE of these was similar to the simple linear model containing only one variable.

### 4 Results:

Link to Github repository containing fully reproducible methods script.

The objectives of this analysis were to understand which attributes of the houses can be used to most effectively construct a prediction model for house price, and to then minimise the differences between predicted and actual house price using model selection.

For regression problems the most common way to measure accuracy of a model is by minimising test error. The RMSE scores of all approaches considered in this analysis are shown in Table 3. The model that gave the lowest RMSE was a LASSO regression model, however ridge regression and multiple linear regression also gave similarly low RMSE results. Ridge regression produced a more complicated model than the LASSO due to the fact that it does not drop out any predictor variables. For the sake of interpretability, the ridge regression model will not be further analysed here. In general the LASSO performs well when there is a few variables with a large influence on response, and a number of variables with a lesser influence, which seems to be the case in this dataset.

Table 3: Results of each model attempted, with error shown as RMSE = Root Mean Squared Error.

Model	RMSE
Simple Linear Model	239.9351
Multiple Linear Model with all availanle	187.2485
predictors	
Mutiple Linear Model with only 15 predictors	187.8978
Linear Model, variables selected by	218.6456
best-subset selection	
Linear Model, variables selected by	215.3550
backward stepwise selection	
Linear Model, variables selected by forward	214.3310
stepwise selection	
LASSO Regression Model	186.8578
LASSO Regression Model with increased	195.5521
lambda	
LASSO Regression Model only using	119.9332
observations with price under \$1m	
Ridge Regression Model	187.5832
Basic Decision Tree	255.7033
Bagging Model of randomForest, m = p	306.8430
Bagging Model, reduced to 100 trees	296.0593
randomForest, m = 3	234.2084
randomForest, m = 30, reduced to 30 trees	233.3519
Boosting with lambda = 0.1	647.3418
Boosting with lambda = 0.001	245.5804

It is clear that location has a large influence on house price as out of the 34 variables that has coefficients not equal to zero in the LASSO model, 26 of them were location dummy variables. The size of the house (sqft\_living) was a non-location variable that had the largest influence on house prices. To consider which of the other variables had the largest influence on price, a linear model was constructed without the *city* variable. The *sqft\_living* variable was found to be most significant, followed by *bedrooms*, *bathrooms* and *house\_age*. This agrees with the plots of influence seen from the randomForest plots that showed these variables to be most influential. *sqft\_living* was included in every model created by variable selection and was not dropped out of the LASSO, suggesting it is one of the most influential variables towards house price in this dataset.

The LASSO model with the lowest RMSE contained 34 variables, however by increasing the lambda value from the value chosen as best by cross-validation to one slightly higher, the number of variables in the model

can be dropped down to 15, with only a slight increase in RMSE to 195.55. The 15 variables that remain in this LASSO model are very similar to those that showed significance in the multiple linear regression model.

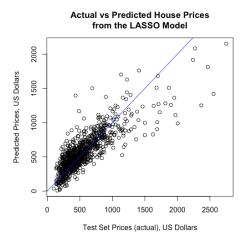


Figure 3: Actual house prices (from test set) vs predicted house prices (from LASSO model), containing 34 variables, trained on all available data

Figure 3 shows the plot of predicted vs actual values for the LASSO model that produced the lowest RMSE score. We can see that they are less accurate for houses that are more expensive. As the test set price is increased, a number of the predicted prices are falling much lower on the y axis. This suggests that the model produced is less accurate for more expensive houses. A possible explanation for this is that there were less observations for more expensive homes which led to fewer training observations. The model seems to be more accurate at predicting price up until around \$1,000,000. To investigate this further, a LASSO model was recreated using only those observations with price under 1,000,000 dollars, the RMSE was drastically improved to 119.93, by far the best seen in this analysis. This suggests that these larger prices were having an impact on prediction accuracy of the model. From figure 4 it is clear that the actual vs predicted prices have a closer relationship to the line throughout the whole axis range. However restricting the prices to train the model means that it would be useless for predicting more expensive homes.

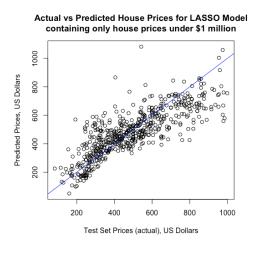


Figure 4: Actual house prices (from test set) vs predicted house prices (from LASSO model), only trained with observations with house prices under one million dollars

The multiple linear regression containing only 15 variables (those that were significant in the multiple linear regression containing all predictors) has a lower RMSE result than the LASSO model with only 15 variables. The multiple linear regression is arguably more easily interpreted than the LASSO. The diagnostic plots of this model are shown in Figure 5 From the first of the diagnostic plots it is clear that the assumption of linear regression holds true due to the straight horizontal line at 0 we can see. The points follow the QQ plot line, but there are some tails at either ends, this may suggest that the residuals are not normally distributed. The third plot checks for homogenity of variance of the residuals, it is clear that the red line is not horizontal. A Breusch Pagen Test was carried on this linear regression model (P = 0.1304, df = 17) leading to the the null hypothesis being accepted, concluding there is homoscedasticity in the residuals. This is good as it meant no further transformations were needed on this model. The final graph checks for any points with high leverage using Cook's distance. None of the points in this data set lie outside of this distance, although a few are near the border.

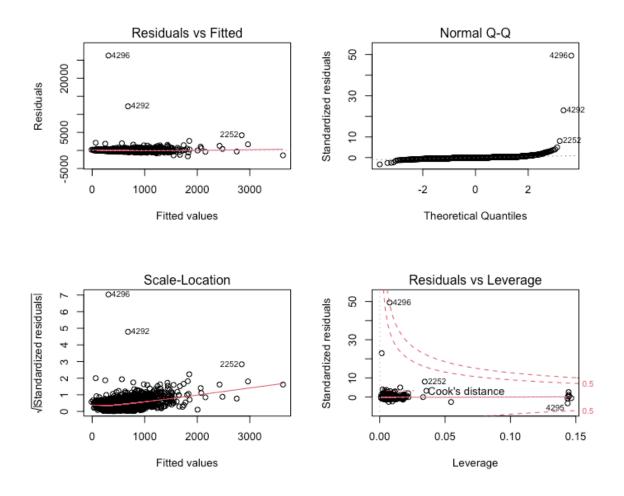


Figure 5: The diagnostic plots for a multiple linear model containing 15 varibles, RMSE = 187.90

#### 4.1 Conclusions:

In the case of this dataset, a LASSO model containing 34 gave the lowest RMSE. However a similarly acceptable low score was given by a multiple linear regression containing only 15 variables which is much easier to interpret due to it containing a lower number of variables. The predictor variables that had the largest influence on House Price in this dataset were house size (sqft living), number of bedrooms and bathrooms and house age. Increases in each of these led to increases in house price. By looking at the coefficients produced by the various models it is clear that some of the location dummy variables had large impacts, in particular houses in Seattle, Mercer Island, Medina and Bellevue had more expensive homes, and those in Federal Way had less expensive homes. Seattle is the capital city of Washington and so this may be an explanation of the higher house prices, it presumably being a more popular place to live. By using a larger data set, more accurate models may be possible. It was clear location had a large impact, so potentially by focusing on one smaller area the model could be refined for the other non-location variables. Some of the city factor levels only contained information for a small number of houses, and others (e.g. Seattle) contained over 1,000, this may have impacted their influence on the price variable in this dataset. Overall, the linear regression model containing only 15 variables proved to be easily interpretable and gave one of the lowest RMSE scores. RandomForests produced RMSE scores in the same region as a linear model containing only one variable, this suggests that they can be useful if there are fewer variables. Finally, it was clear that by restricting the data set to only contain less expensive houses, the prediction accuracy of the LASSO model could be greatly improved, this suggests that a larger, more complete data set may have yielded improved results.

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