PALISADE Lattice Cryptography Library User Manual (v1.6.0)

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Abstract

This document is the manual for the PALISADE lattice cryptography library. This manual provides an introduction to the library by describing the library architecture and cataloging its capabilities. We focus on the PALISADE library's ability to support public-key homomorphic encryption capabilities to evaluate arithmetic operations on data while encrypted. We do not explicitly provide an introduction to lattice cryptography, but we provide an overview of notation and terminology necessary to use the PALISADE library. In addition to providing code samples for the use of the PALISADE library, we also discuss the library programming style for developers who wish to read library code or even add to the library. We also provide an overview of common pitfalls in the use of PALISADE.

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Listings

1 Document Overview

This manuscript is a working document to introduce users to the PALISADE lattice cryptography library. The most recent copy of this document is available for download from the PALISADE library website. This document will be updated as the public version of the PALISADE library repo is updated. Copies of this document may be available for download from PALISADE contributors' websites, but the version available for download on the PALISADE library website should be considered authoritative.

The manual is organized as follows.

- An introduction to the library is provided in Section 2.

- Section 3 provides a basic introduction to lattice cryptography.

- The library architecture is discussed in Section 4.

- The library capabilities are discussed in Section 5.

- Section 6 provides an overview of the PALISADE library directory structure.

- Section 7 provides an overview of notation and terminology used in the library and this manual.

- This document is intended to be driven by code samples which show the library being used for specific needs.

- Section 8 provides these code samples, with a focus on homomorphic encryption applications.

- Section 9 describes how the library can be built in a generic Linux environment.

- Section 10 describes the programming style we maintain in the library for those users who wish to contribute code to the library.

In addition to the primary manual content discussed above, we provide the following appendices.

- Appendix A reproduces the library's BSD 2-clause license.

- The PALISADE library has been made possible by the generous support of our sponsors. A listing of the PALISADE library sponsors can been seen in Appendix B.

The public version of the PALISADE Lattice Cryptography library can be found on The PALISADE Git Repo.

The listed authors of this document are the current primary maintainers of the PALISADE library repo.

2 Introduction

Lattice cryptography has received considerable attention because of its capability to support both post-quantum public-key encryption and the ability to compute on data while encrypted via homomorphic encryption. Lattice cryptography also provides other powerful capabilities such as proxy re-encryption and attribute-based encryption. The PALISADE library provides implementations of the building blocks for lattice cryptography capabilities along with end-to-end implementations of advanced lattice cryptography protocols for public-key encryption, proxy re-encryption, homomorphic encryption and others. PALISADE provides both an experimental platform for researchers to design and evaluate new lattice cryptography capabilities, while at the same time providing implementations of known protocols that can be integrated into applications. In this manual we describe PALISADE and discuss how it can be used.

The PALISADE library is designed to address the following inherent challenges of lattice cryptography implementation:

- The complexity of algebraic constructions makes it hard for non-experts to leverage, let alone implement, algebraic constructions used as the building blocks of lattice cryptography.

- Lattice cryptography implementations are often purpose-built. Rapid deployment on new hardware systems is difficult to support with these existing implementations.

- Parameter selection for security and performance takes very sophisticated understanding, and this is nontrivial even for experts - up to a dozen parameters may be needed to be set for some schemes.

- Security assumptions are evolving, and it has been difficult to adapt prior implementations. See for example the recent subfield lattice attacks against LTV which required re-design of libraries that previously used this scheme.

- Application integration has been challenging, without easy methods to efficiently perform operations on non-trivial data types, such as rationals, complex numbers, etc.

As a result of these identified challenges, we design PALISADE to achieve the following design goals:

- *Create an extendible and adaptable library for lattice cryptography.* Lattice crypto uses few computational primitives. We allow for new protocols that mix-and-match these primitives to avoid the need for expert low-level knowledge. This has been a major advance in the PALISADE library, and we are still refining these features of PALISADE as we support more capabilities.

- *Provide a modular structure to mix and match components.* This allows for system-optimized arithmetic and lattice "backends"/plugins. We currently support multiple math backends which can be selected at compile time. The PALISADE library is thus designed to be highly portable into commodity computing and hardware environments, including Windows, Linux, MacOS and Android environments. The ability to support multiple hardware accelerators is a work in progress in PALISADE.

- *Offer (semi-)automated parameter selection.* This reduces the need to tune an overwhelming number of parameters. This is still a major research topic and is a work in progress in PALISADE.

- *Develop common crypto APIs.* Common crypto APIs across multiple schemes and backends "hide" complex details of lattice constructions / parameterization from application developers, allowing developers to focus on their areas of interest while integrating and replacing components to maintain security and performance. This is another major feature of PALISADE that we continue to refine.

- *Deliver good software engineering with focus on usability.* This permits standards-based design and style. Unit tests and benchmarking environments are supported for evaluation and tuning of integrated applications. We aim to provide documentation, clean code and code samples that reduce effort for new developers.

Our identification of these goals in PALISADE is informed by industry experience integrating PALISADE into multi-organizational large software engineering projects. As a result of these identified challenges and the resulting engineering goals we set for ourselves in the design of PALISADE, we design PALISADE to be highly modular, with a core library of lattice cryptography primitives that support multiple protocols for public-key encryption, homomorphic encryption, digital signature schemes, proxy re-encryption and program obfuscation.

3 A Brief Overview of Lattice Cryptography

At a high intuitive level, encryption is a computational process wherein **Data** is **Encoded** as **Plaintext** and then encrypted into **Ciphertext** according to some **Encryption** algorithm. Conversely, decryption is a corresponding computational process wherein the **Plaintext** can be recovered from the **Ciphertext** through the use of a correspoding **Decryption** algorithm.

These algorithms use cryptographic **Keys** to perform the **Encryption** and **Decryption** operations. Intuitively, an encryption scheme is secure if it prevents an adversary from recovering **Plaintext** (or information about a **Plaintext**) from **Ciphertext** when the adversary does not have the corresponding decryption key.

A "symmetric key" protocol uses the same key to perform both encryption and decryption. A "public key" or "assymmetric" protocol uses a pair of **Public** and **Secret** keys, respectively, for encryption and decryption. A **Secret** key is sometimes called a **Private** key.

In practice symmetric keys and secret keys are kept secret because they can be used to access protected information. Public keys are often widely distributed and often published on the open Internet. The intended use of a public key is that one can encrypt data with a downloaded public key corresponding to an intended recipient, encrypt sensitive information for the recipient with the public key, and send that encrypted sensitive information to the recipient. The recipient can use her secret key to decrypt and recover the protected information encoded in the plaintext.

Cryptographic algorithms are designed around computational hardness assumptions so that the difficulty of recovering information about plaintext is at least as hard as some computationally hard problem. Thus, it is theoretically possible to break such a system, but it is assumed infeasible to do so by any known practical means. Different computationally hard problems define different classes of encryption systems. PALISADE focuses on lattice-based cryptography. The security of lattice cryptography is based on the hardness of variants of the Shortest Vector Problem (SVP), Learning With Errors (LWE), and other hard problems. Lattice cryptography has both symmetric and public key variants, but we generally focus on the public key lattice cryptography variants in this manual and in the PALISADE library.

Homomorphic Encryption (HE) or Fully Homomorphic Encryption (FHE) refer to a class of encryption methods envisioned by Rivest, Adleman, and Dertouzos in 1978. Homomorphic encryption differs from basic encryption methods in that it allows computation to be performed directly on encrypted data without requiring access to a secret key. The result of such a computation remains in an encrypted form, and can at a later point be revealed by the owner of the secret key by decrypting the result.

In 2009 Craig Gentry showed the existence of lattice-based FHE capabilities. Since this initial discovery of a lattice-based FHE protocol, there has been a Renaissance in lattice cryptography, with the discovery of several other

increasingly practical homomorphic encryption schemes and variations of homomorphic encryption protocols. Some of the common homomorphic encryption schemes include the Brakerski-Fan-Vercauteren (BFV)[1], Brakerski-Gentry-Vaikuntanathan (BGV), and Stehle-Steinfeld (StSt) schemes. Other related protocols include:

- Proxy Re-Encryption (PRE), which permits delegation of ciphertext decryption, thus allowing a host to delegate access to encrypted data.

- Somewhat Homomomorphic Encryption (SHE), which permits a limited amount of computation on encrypted data.

- Leveled Somewhat Homomorphic Encryption (Leveled SHE), which permits at least a fixed depth of computation to be performed on encrypted data by using a decreasing ladder of ciphertext moduli.

- Multiparty Homomorphic Encryption, which enables multiple participants to contribute data to a joint computation, without sharing access to the actual data.

The public version of PALISADE supports all of the protocols discussed above, and we are in the process of adding support for more protocols and schemes. From v1.4 and onwards, PALISADE also supports a selection of trapdoor-based schemes: a Gentry-Peikert-Vaikuntanathan (GPV) digital signature scheme, a GPV identity-based encryption (IBE) scheme, and a Zhang-Zhang ciphertext-policy attribute-based encryption (CP-ABE) scheme.

An inherent property of encrypted computing technologies, including the various protocols supported by PALISADE, is that computing on encrypted data is significantly slower and more compute-intensive than computing on plaintext data. As such, debugging the applications of encrypted computing technologies can be a frustrating, slow process. To aid developers in integrating PALISADE implementations of encrypted computing technoligies, we also provide in PALISADE a "Null" scheme which supports the same API as the BFV, BGV, and StSt implementations, but which does not encrypt data and performs all operations on unencrypted plaintext. The Null scheme implementation operates as a light-duty no-security equivalent of the encrypted computing protocols supported by PALISADE. Thus, we provide the Null scheme so developers can test their PALISADE integrations more easily without the overhead or frustration of testing operations with slower more compute-intensive workloads engendered by encrypted computing capabilities.

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[1]This scheme is also frequently denoted as the FV scheme, but we choose to call it the BFV scheme.

4   Library Architecture

The PALISADE library implements lattice cryptography in C++. The objects that are created by and manipulated within PALISADE are instances of C++ classes.

PALISADE is designed as a layered architecture where each layer provides a set of services to the layer "above" it in the stack, and makes use of services in the layer "below" it in the stack. The interfaces between each of the layers are designed to implement a common API. This permits substituting multiple implementations at any layer for experimental purposes.

The high-level architecture of PALISADE is illustrated in Figure 1.
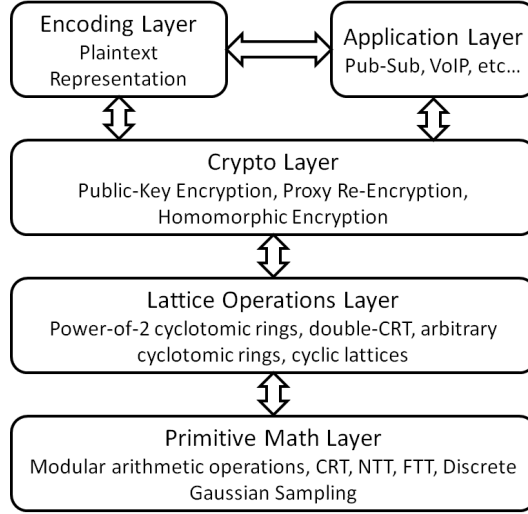
Figure 1: High-level PALISADE architecture

The layers in PALISADE are as follows:

1. **Application**: All programs that call the PALISADE library services are in this layer.

2. **Encoding**: All implementations of methods to encode data are at this layer.

3. **Crypto**: All implementation of cryptographic protocols are at this layer.

4. **Lattice Operations**: All higher-level lattice-crypto mathematical building blocks are in this layer.

5. **Primitive Math**: All low-level generic mathematical operations, such as multi-precision arithmetic implementations, are at this layer.

4.1 Application Layer

All programs that make use of the PALISADE library are said to be in the Application layer.

All programs at the Application layer make calls to services exposed in the PALISADE Crypto layer to gain access to PALISADE lattice cryptography functionality. The Application layer also makes use of service at the Encoding layer.

4.2 Encoding Layer

The Encoding layer contains all classes needed to provide for the encoding of any supported raw plaintext message data into a **Plaintext** object, and for decoding back to raw plaintext messages whenever necessary.

The Encoding layer is used to create **Plaintext** objects. These objects are sometimes created at the request of the Application layer, in which case Crypto layer methods act as a proxy for the Application layer, sometimes at the request of the Crypto layer itself. The interface for Encoding functionality is C++ methods provided by **Plaintext**.

4.3 Crypto Layer

The Crypto layer contains all classes needed to provide all available lattice cryptography functionality for specific cryptographic protocols such as public-key encryption, PRE and SHE schemes, and all included methods such as encryption and decryption, proxy re-encryption and container classes for parameters specific to those schemes.

The interface for Crypto functionality is C++ methods provided by **CryptoContext**. Therefore the Crypto layer provides various factory methods for creating a **CryptoContext** along with the context itself. The Crypto layer manipulates **Plaintext** and **Ciphertext** objects that are passed to it by the Application layer, and returns the appropriate **Plaintext** and **Ciphertext** objects to the Application. Operations on a **Matrix** of such objects is also provided.

Similar to **CryptoContext**, library also provides **SignatureContext** and **ABEContext** for the digital signature and GPV IBE/CP-ABE operations, respectively. However, unlike **CryptoContext** these contextes have their own implementation of ciphertexts. **SignatureContext** also uses its own implementation of plaintexts. The Crypto layer makes use of services provided by the Lattice Operations layer.

4.4 Lattice Operations Layer

The Lattice Operations layer provides support for all lattice constructs, including power-of-two cyclotomic rings and arbitrary cyclotomic rings. The Double Chinese Remainder Theorem (Double-CRT) representation of cyclotomic rings is also implemented in the Lattice layer.

With the release of version 1.4.0, the lattice layer also hosts trapdoors and trapdoor sampling. Trapdoors are lattice constructs consisting of two vectors of polynomials. These structures are key parts of the newly added digital signature, identity-based encryption and ciphertext-policy attribute-based encryption schemes. These algorithms require a preimage of the information to be sampled from a discrete Gaussian over a lattice, which is done using the trapdoor sampling algorithms.

The Lattice layer is used to provide an implementation of the various **Poly** classes, including **Poly**, **NativePoly**, and **DCRTPoly**. These objects are used as building blocks in **Plaintext** and **Ciphertext**. The interface for Lattice functionality is the C++ methods provided by the **Poly** classes.

The Lattice layer performs lattice operations by decomposing operations into primitive arithmetic operations on integers, vectors, and matrices. The Lattice layer makes use of the Primitive Math layer to perform these operations.

4.5   Primitive Math Layer

The Primitive Math layer provides support for basic modular arithmetic operations, including multi-precision arithmetic. This layer also includes efficient algorithms for Number-Theoretic Transform (NTT), Fermat-Theoretic Transform (FTT), and discrete Gaussian samplers, among others. The interface for Math functionality is the C++ methods provided by both custom multi-precision libraries, and external imported libraries such as NTL.

4.6   Utilities

PALISADE also provides a cross-cutting Utilities module for common utility functions used by all the layers. The primary use of this layer is for serialization and deserialization of objects, and for creation of exceptions.

5 Capabilities

One of the goals of PALISADE is to provide straightforward mechanisms to select 1) an encryption protocol, 2) an encryption scheme to support that protocol, 3) encoding mechanisms to represent data with that scheme, 4) a math back-end to support computational operations over that data for the scheme and 5) configuration parameters for that protocol, encoding mecahnisms and math back-end. PALISADE provides a broad set of selections for each of these choices, and provides the user with the ability to add their own schemes, encodings, operations, etc. Furthermore, the user of PALISADE can select from multiple lattice layer implementations and math layer implementations, can easily mix-and-match, and can even provide their own implementations at different layers. In this section we describe these choices we make available in PALISADE.

At the highest level, the PALISADE library groups encryption protocols into a set of capabilities that can be selectively enabled by the user at run time. Table 1 shows which functions are supported by which capabilities. Enabling a particular capability turns on several functions in support that capability. Some capabilities implies other capabilities, such as how SHE for example implies PKE capabilities. Thus, in these scenarioes, some capabilities are turned "on" automatically.

Capabilities currently supported PALISADE are listed in Table 1.

Table 1: PALISADE Capabilities and Functions

Capability	Description	Functions Supported	Also Enabled
ENCRYPTION	Public-Key Encryption	KeyGen Encrypt Decrypt	
PRE	Proxy Re-Encryption	ReKeyGen ReEncrypt	PKE
SHE	Somewhat Homomorphic Encryption	EvalAdd EvalMult EvalSub EvalNegate EvalAutomorphism EvalAtIndex EvalMerge EvalMultMany EvalSum EvalInnerProduct EvalLinRegression EvalLinRegressBatched EvalCrossCorrelation EvalRightShift ——— KeySwitch KeySwitchGen EvalMultKeyGen EvalAutomorphismKeyGen EvalAtIndexKeyGen EvalSumKeyGen	PKE
LeveledSHE	Leveled SHE with Modulus Switching	ModReduce RingReduce LevelReduce ComposedEvalMult	PKE SHE
Multiparty	Multiparty Capabilities	MultipartyKeyGen MultiPartyDecrypt	PKE
CP-ABE	Ciphertext-Policy Attribute-Based Encryption	Setup KeyGen KeyGenOfflinePhase KeyGenOnlinePhase Encrypt Decrypt	
GPV Signature	Digital Signature	KeyGen Sign SignOfflinePhase SignOnlinePhase Verify	
GPV IBE	Identity-Based Encryption	Setup KeyGen KeyGenOfflinePhase KeyGenOnlinePhase Encrypt Decrypt	

Once an encryption protocol is selected, a user of PALISADE can select from one of multiple schemes, each of which supports some or all of the above protocols

- BFV variants

  - BFV: "textbook" Fan-Vercauteren variant of Brakerski's scale invariant scheme [2, 5, 9]

  - BFVrns: Halevi-Polyakov-Shoup RNS variant of the BFV scheme [8]

– BFVrnsB: Bajard-Eynard-Hasan-Zucca RNS variant of the BFV scheme [1]

- BGV: Brakerski-Gentry-Vaikuntanathan scheme [3, 6]

- StSt: Stehele-Steinfeld scheme [11]

- Null

Table 2 maps which schemes support which capabilities.

In addition to the homomorphic encryption schemes, PALISADE supports the following trapdoor based schemes

- GPV Signature: Gentry-Peikert-Vaikuntanathan Digital Signature Scheme [7]

- GPV IBE: Gentry-Peikert-Vaikuntanathan Identity-based Encryption Scheme [7]

- CP-ABE: Zhang-Zhang Ciphertext-policy Attribute-based Encryption Scheme [12]

Table 2: PALISADE Implemented Capabilities Matrix

Function/Scheme	LTV	StSt	BGV	BFV*	Null
ENCRYPTION	Y	Y	Y	Y	Y
PRE	Y	Up to 2 Hops	Y	Y	Y
SHE	Y	Y	Y	Y	Y
LeveledSHE	Y		Y		Y
Multiparty	Y	Y	Y	Y	Y

After the selection of the scheme, a user can then select how to represent polynomials, among the following polynomial types:

- **Poly**, which corresponds to representing polynomial coefficients in a multiprecision integer format.

- **DCRTPoly**, which corresponds to representing polynomial coefficients in a Residue Number System (RNS), a.k.a. Chinese Remainder Theorem (CRT), format using single-precision integers.

- **NativePoly**, which corresponds to representing polynomial coefficents in a single-precision format (only works up to the word size of 64 bits).

We generally recommend using the **DCRTPoly** representation of polynomials for performance on commodity computing environments, although we include the multiprecision polynomial representation **Poly** for advanced users and implementers of new schemes who which to initially implement using the simpler **Poly** representation.

Similar to the polynomial representations, PALISADE also supports multiple math back-ends. The current implementation of PALISADE selects the math back end at compile time. Supported multi-precision math backends include:

- Multi-precision with fixed sizing (BACKEND 2) supporting bit widths up to 3000 by default (this value can be changed)

- Multi-precision with variable sizing (BACKEND 4)

- NTL (BACKEND 6)

Native data types are always available, and we require that native 64-bit operations be supported in order to use PALISADE.

6 PALISADE Directory Structure

The directory structure of the PALISADE source code is shown in Table 3

Table 3: PALISADE Library File Structure

Directory	Description
benchmark	Code for benchmarking PALISADE library components.
build	Binaries and build scripts (this folder is created by the user).
doc	Documentation of library components, including doxygen.
src	Library source code.
test	Google unit test code.
third-party	Code provided by an external third party.

Within the PALISADE library: the src/core/lib directory contains subdirectories for the Math, Lattice, Encoding and Utils layers; and the src/pke/lib, src/abe/lib and src/signature/lib directories contain the Crypto layer source code for PKE, ABE and signatures, respectively.

All of the src/core, src/pke. src/abe and src/signature contain a subdirectory for unit tests as well as a subdirectory for demo applications that exercise the capabilities of PALISADE.

7   Terminology and Notation

In this section we provide a glossary of terminology that we use in PALISADE.

PALISADE provides a framework for using lattice cryptography.

If a **Scheme** supports the ENCRYPTION **Capability**, encrypt and decrypt methods are available for use. The encrypt and decrypt methods are provided as part of the implementation of the ENCRYPTION **Capability** in the **Scheme** being used. A **Plaintext** can be encrypted into a **Ciphertext** through the use of an encrypt method. A **Ciphertext** can be used to generate a **Plaintext** through the use of a decrypt method. The library supports several formats of **Plaintext** and methods to create a **Plaintext** for use in PALISADE.

If a **Scheme** supports the PRE **Capability**, a re-encrypt method is available.

If a **Scheme** supports the SHE and/or LeveledSHE **Capability**, then there is support for homomorphic operations on pairs of **Ciphertext** as well as mixed-mode operations between a **Ciphertext** and a **Plaintext**. These operations are supported by using C++ operator overloading. For example, multiplication of two instances of a **Ciphertext**, A and B, can be simply written as A * B.

PALISADE also includes support for several **Matrix** operations. It is possible to create several **Matrix** of **Plaintext**, encrypt them, perform operations on them, and then decrypt back into a **Matrix** of **Plaintext**.

7.1   Typing

All PALISADE operations are strongly typed. A **Plaintext** that is passed to encrypt will create a **Ciphertext** that is aware of the underlying format of the **Plaintext**, as well as the particular key that was used to encrypt the **Plaintext**. The decrypt operation will fail in cases where an improper key is used. A successful decrypt will produce a new **Plaintext** whose underlying format matches the initial **Plaintext** that was passed to encrypt. Homomorphic operations between **Ciphertext**, and mixed-mode operations between a **Ciphertext** and a **Plaintext** will only be permitted for operands with formats and keys that match.

The underlying data inside of PALISADE is an **Element** in lattice space. Within PALISADE, all **Plaintext** are encoded into an **Element**. Every **Ciphertext** contains one or more **Element** objects, and all operations are mathematical operations on these **Elements**.

There are several formats of **Element** available: a **Poly**, which represents the encoded **Plaintext** as a polynomial; a **NativePoly**, which uses a polynomial with coefficients with a maximum size of 64 bits; and a **DCRTPoly**, which represents the encoded **Plaintext** as a stack of decomposed **MativePoly** polynomials using the Double Chinese Remainder Transform.

7.2 CryptoContext

A **CryptoContext** in PALISADE is the class that provides all PALISADE encryption functionality. All objects used in a PALISADE implementation are created by a **CryptoContext** and can be considered to "belong to" the **CryptoContext** that they were created with.

Any and all operations on PALISADE objects must be on objects that belong to the same **CryptoContext**. The high-level use of the **CryptoContext** to encrypt a **Plaintext** to generate a **Ciphertext** is as follows:

1. Choose a set of **ElementParams** to define parameters for the **Element** to be used.

2. Choose a set of **EncodingParams** to define parameters for encoding.

3. Select a **Scheme** that you wish to use for lattice cryptography.

4. Construct a **CryptoContext** for your selected scheme, **ElementParams** and **EncodingParams**, in which all operations shall take place. The construction of a **CryptoContext** involves selecting parameters for security and performance. There are potentially multiple mechanisms to generate the Scheme parameters needed for this construction.

5. Select which **Capability** are used with the **CryptoContext**. Note that not every **Scheme** will support every possible **Capability**.

6. Use CryptoContext methods to create **Keys**.

7. The user may also perform homomorphic operations on **Ciphertext** and **Plaintext** objects if that **Capability** has been enabled and if the **Scheme** supports the operations.

8. Encrypt a **Plaintext** into a **Ciphertext**.

9. Decrypt a **Ciphertext** back to a **Plaintext**.

Each **CryptoContext** is uniquely identified by its **Scheme**, **Element** type, **ElementParams** and **EncodingParams**. When we say that an object "belongs to" a **CryptoContext**, we are actually saying that it is associated with a **CryptoContext** with a particular **Scheme**, **Element** type, **ElementParams** and **EncodingParams**.

PALISADE incorporates the standard security tables developed during the Homomorphic Encryption standardization process described at
`http://homomorphicencryption.org`. Users of the library can construct a **CryptoContext** by specifying the parameter sets defined in the standard.

It follows that if one creates a **CryptoContext** on two different computers, each with the same **Scheme**, **Element** type, **ElementParams** and **EncodingParams**, then those two **CryptoContext**s are the same, and objects created on one machine can be transferred to and used on the other machine.

7.3 ABEContext

An **ABEContext** is the equivalent of a **CryptoContext** for attribute-based and identity-based encrpytion functionality. All CP-ABE and GPV IBE related operations are done using an **ABEContext**. The high-level use of an **ABEContext** to encrypt a **Palintext** is as follows:

1. Choose a set of parameters to create appropriate set of **ElementParams** for the **Element** to be used.

2. Select a **Scheme** to use (GPV IBE or CP-ABE).

3. Construct a **ABEContext** for your selected scheme and parameters. Note that the steps up to this point are similar to **CryptoContext**, with the exception of **EncodingParams**. This is due to the fact that **ABEContext** at its current implementation only supports the plaintext modulus of 2 for encoding, hence it is done internally.

4. Create an **AccessPolicy** for the parties that will be able to decrypt.

5. Use ABEContext methods to create **Keys**.

6. Encrypt a **Plaintext** under an **AccessPolicy** into a **Ciphertext**.

7. Decrypt a **Ciphertext** back to a **Plaintext**.

   The standard security tables developed during the Homomorphic Encryption standardization process described at `http://homomorphicencryption.org` also apply to **ABEContext**.

   It is also worth to mention that **ABEContext** does not support **DCRT-Poly** at its current state. However, for most cases **NativePoly** is enough. The ABE does not have homomorphic operations within ciphertexts defined for the time being, which means there is no need for moduli larger than 64 bits. The ciphertext modulus required for the security/correctness of regular encryption functionality is below 64 bits.

7.4 SignatureContext

A **SignatureContext** is the equivalent of a **CryptoContext** for digital signature schemes. All GPV signature scheme-related operations are done using a **SignatureContext**. The high-level use of a **SignatureContext** to sign a **Plaintext** is as follows:

1. Choose a set of parameters to create appropriate set of **ElementParams** for the **Element** to be used.

2. Select a **Scheme** to use (GPV only for the time being).

3. Construct a **SignatureContext** for your selected scheme and parameters. Note that the steps up to this point are similar to **CryptoContext**, with the exception of **EncodingParams**. This is due to the fact that the encoding is handled internally.

4. Use SignatureContext methods to create **Keys**.

5. Sign a **Plaintext** into a **Signature**.

6. Verify a **Signature**with a **Plaintext**.

It is also worth to mention that just like **ABEContext**, **SignatureContext** does not support **DCRTPoly** at its current state and **NativePoly** is enough for all cases. Homomorphic operations are not defined for signatures, which means there is no need for moduli larger than 64 bits.

7.5   Plaintext

A **Plaintext** is used in PALISADE to represent something that has not been encrypted. It is actually the base class for each of the possible plaintext encodings that are supported in PALISADE:

- ScalarEncoding

- IntegerEncoding

- FractionalEncoding

- PackedEncoding

- CoefPackedEncoding

- StringEncoding

A **Plaintext** is created by invoking the appropriate **CryptoContext** method, passing it the unencrypted information as a parameter.

Once created, a **Plaintext** can be encrypted into a **Ciphertext** using the **CryptoContext** Encrypt routine.

A **Plaintext** can also be used as a parameter to several of the **CryptoContext** homomorphic operations.

When a **Ciphertext** is decrypted, the decryption method creates a new **Plaintext** to contain the decryption.

The **Plaintext** has several methods that provide access to the information in the **Plaintext**, as shown in listing 1:

Note that the only one of these **Plaintext** methods that will return a value is the one that corresponds to the actual type of the **Plaintext**. For example, GetStringValue() will return a std::string if the **Plaintext** is actually a **StringEncoding**, and will throw an exception otherwise.

While **ABEContext** also uses **Plaintext** for unencrypted information, **SignatureContext** uses its own plaintext definition.

```
const std::string&      GetStringValue();
const int64_t           GetIntegerValue();
const int64_t           GetScalarValue();
const vector<int64_t>&  GetCoefPackedValue();
const vector<uint64_t>& GetPackedValue();
```

Listing 1: Values in Plaintext

7.6   Ciphertext

A **Ciphertext** is used in PALISADE to represent encrypted information. A **Ciphertext** is created from a **Plaintext** by an encrypt method, and is converted back to a **Plaintext** by a decrypt method. The encrypt and decrypt methods also require **Keys** that have been generated by the **CryptoContext**.

Homomorphic operations between pairs of **Ciphertext**, or between a **Ciphertext** and a **Plaintext**, are supported, provided that the encodings of the operands match, and provided that those encodings support homomorphic operations (for example, homomorphic operations are not supported for string encodings, and will be rejected if attempted).

The CP-ABE/GPV IBE schemes utilizing **ABEContext** have their own unique classes for ciphertext implementations, which do not have homomorphic operations supported at this time.

7.7   Access Policy

An **Access Policy** is a rule/set of rules dictating the decrypting party of the communication. User holding the appropriate rights can generate the relevant **Keys** for decryption and decrypt the information encrypted under an **Access Policy**.

In the context of GPV IBE, **Access Policy** refers to the unique user identifier.

In the context of CP-ABE, **Access Policy** can refer to both attributes defined for the access policy as well as user's own attribute set.

7.8   Signature

A **Signature** is used in PALISADE for authentication. A **Signature** is created from a **Plaintext** by a sign method, and used in conjunction with the **Plaintext** for verification. The sign and verify methods also require **Keys** that have been generated by the **SignatureContext**.

7.9   Keys

Many PALISADE functions make use of **Keys**. These objects are created using **CryptoContext**, **ABEContext** or **SignatureContext** methods.

Encryption and decryption functionality requires a public key/private key pair. The **CryptoContext** KeyGen method generates this key pair and returns it to the caller.

CP-ABE and GPV IBE operations require a master public key/private key pair for the encryption and derivation of personal secret keys. This is done using Setup method of **ABEContext**. For decryption, a secret key corresponding to an access policy/user is required, which is done using the **ABEContext** KeyGen method.

Signing and verification operations for digital signature schemes require a sign(private)/verify(public) key pair. This pair can be generated using the **SignatureContext** KeyGen method.

Re-Encryption requires an Evaluation key. This key is generated using the ReKeyGen method.

Certain homomorphic operations may require the application of evaluation keys to complete the operation. The **CryptoContext** EvalMultKeyGen and EvalAddKeyGen methods are used to generate the requisite keys needed for the EvalMult and EvalAdd operations, respectively.

7.10 Capability

A **Capability** refers to sets of **CryptoContext** methods that must be enabled before they can be used. A **Capability** must be enabled by calling the **CryptoContext** Enable method and passing it the name of the **Capability** as an argument. Multiple values for **Capability** can be or-ed together and passed as a single argument to Enable.

Table 1 lists the available choices for **Capability**, and the functionality enabled when a particular **Capability** is Enabled.

7.11 Scheme

A **Scheme** is the algorithms used for key generation, encryption/decryption, and homomorphic operations.

Table 2 outlines the different supported schemes in PALISADE.

In order to use a particular **Scheme**, its configuration parameters must be specified. The particular configuration parameters for each scheme are stored in a CryptoParameters class that is particular for that scheme. The classes for CryptoParameters for each scheme are unique, but they all share several characteristics:

1. Each CryptoParameter class has a constructor that allows for the specification of all configuration parameters.

2. The CryptoParameter may have a ParamsGen feature that generates a full set of configuration parameters from a small specification as to how many homomorphic operations will be performed.

3. The CryptoParameter class is part of the CryptoContext

ABEContext and **SignatureContext** also use their equivalent parameter classes like CryptoParameters.

7.12 Element

The math layer performs operations on different kinds of **Element**. This is a representation of a vector in lattice space.

7.12.1 Poly

A **Poly** is a vector of polynomial coefficients. The coefficients are whatever the BigInteger is for the selected math backend, and the vector is simply a vector of these BigInteger, and an associated modulus. All operations on a Poly are done modulo the modulus.

7.12.2 NativePoly

A **NativePoly** is a vector of polynomial coefficients where each of the coefficients is at most a 64-bit unsigned integer. The NativePoly also has a modulus of at most 64 bits, and all operations are done modulo the modulus.

7.12.3 DCRTPoly

A **DCRTPoly** implements a large Poly decomposed into a tower of **NativePoly** elements.

7.13 ElementParams

An **ElementParams** is a container for the configuration parameters of whatever Element is being used. The configuration parameters include the ring dimension, cyclotomic order, and primitive root of unity.

7.14 EncodingParams

An **EncodingParams** is a container for all of the parameters needed to encode a **Plaintext**. In most cases, this consists solely of a plaintext modulus; however, some encodings require more detailed parameters.

7.15 Matrix

PALISADE supports general operations **Matrix** objects with elements of the types described above in this section, as well as operations on these matrices. A user can create a matrix of **Plaintext**, encrypt it into a matrix of **Ciphertext**, and perform operations on matrices.

In addition to homomorphic matrix multiplication, higher level statistical operations such as inner product and linear regression are available. Some operations result in a matrix of **RationalCiphertext**, where each entry in

the matrix is a rational number such that the numerator and denominator of the entry is a **Ciphertext**. For matrices of **RationalCiphertext**, separate decryption of the numerators and denominators of each entry are provided.

8 Sample Implementations

8.1 PKE

8.1.1 Creating a CryptoContext

All PALISADE operations are associated with a CryptoContext; therefore, the first step in using PALISADE is to acquire a CryptoContext. A CryptoContext can be created in a number of different ways through the use of static CryptoContextFactory methods. The factory methods return a shared_ptr to a CryptoContext.

It is useful to note that PALISADE keeps track all of the CryptoContexts that have been created, and will not create duplicate contexts. If a user requests that the factory create a context that already exists, the factory simply returns a shared_ptr to the existing context rather than creating a duplicate of that existing context.

A CryptoContext is uniquely identified by the parameters for the underlying lattice layer element that is to be used, the encoding parameters to be used with Plaintext, and the Scheme (and any associated configuration parameters for the Scheme).

The underlying lattice layer element is either a Poly, a NativePoly, or a DCRTPoly. These type names are used as template parameters with the CryptoContext and its methods. The lattice layer elements share a set of element parameters that are given to the CryptoContextFactory methods.

Encoding parameters may be a simple Plaintext modulus, or they may be a broader set of EncodingParms that are used. Encoding parameters are passed to the CryptoContextFactory methods.

Different Schemes have wildly different configuration parameters, and so the Scheme is selected by calling a CryptoContextFactory method for the desired Scheme.

Each Scheme actually has several factory methods:

- A method that accepts values for all configuration parameters for the scheme.

- A method that accepts some values for configuration parameters, and that invokes a scheme-specific parameter generation operation.

There are two other mechanisms available for creating a CryptoContext:

- Deserialize a previously serialized CryptoContext.

- Construct a CryptoContext from one of the set of predefined scheme parameters.

Once a CryptoContext has been created, the appropriate capabilities should be enabled. Once this is complete, the CryptoContext is ready for use.

Below are some code samples for creating contexts. Listing 2 demonstrates creating a CryptoContext by specifying all of the scheme's parameters.

```cpp
/// Example showing creating a BGV CryptoContext
/// By specifying all Scheme parameters
/// Element is Poly with non power-of-two cyclotomics

usint m = 22;
PlaintextModulus p = 2333;
BigInteger ptm(p);

BigInteger ctm("955263939794561");
BigInteger srr("941018665059848");
BigInteger bigmod("80899135611688102162227204937217");
BigInteger bigroot("77936753846653065954043047918387");

auto cycloPoly = GetCyclotomicPolynomial<BigVector>(m,
    ctm);
ChineseRemainderTransformArb<BigInteger, BigVector>::
    SetCylotomicPolynomial(cycloPoly, ctm);

float stdDev = 3.19;
usint bSize = 8;

shared_ptr<Poly::Params> params(new ILParams(m, ctm, srr,
     bigmod, bigroot));

EncodingParams ep(new EncodingParamsImpl(p,
    PackedEncoding::GetAutomorphismGenerator(p), bSize));

CryptoContext<Poly> cc = CryptoContextFactory<Poly>::
    genCryptoContextLTV(params, ep, bSize, stdDev);

cc->Enable(ENCRYPTION);
cc->Enable(SHE);
```

Listing 2: Creating a CryptoContext with parameters

Listing 3 demonstrates the use of the factory method that uses parameter generation.

Listing 4 shows the use of preconfigured parameter sets.

```
/// Example showing creating a BFV Cryptocontext
/// using parameter generation
/// Element is DCRTPoly (configured by ParamsGen)

int relWindow = 1;
PlaintextModulus ptm = 256;
double sigma = 4;
double rootHermiteFactor = 1.006;

//Set Crypto Parameters
CryptoContext<Poly> cryptoContext =
        CryptoContextFactory<Poly>::genCryptoContextBFV(
                ptr, rootHermiteFactor, relWindow, sigma,
                    0, 5, 0, OPTIMIZED, 6);

// enable features that you wish to use
cryptoContext->Enable(ENCRYPTION);
cryptoContext->Enable(SHE);
```

Listing 3: Creating a CryptoContext with parameter generation

```
/// Example showing CryptoContext generation
// from a preconfigured parameter set

CryptoContext<Poly> cryptoContext =
        CryptoContextHelper::getNewContext("BGV3");

if( !cryptoContext ) {
        cout << "Error creating CryptoContext" << endl;
        return 0;
}

cryptoContext->Enable(ENCRYPTION);
```

Listing 4: Creating a preconfigured CryptoContext

Listing 5 shows the use of parameter sets defined by the Homomorphic Encryption standardization process, as defined in `http://homomorphicencryption.org`.

```cpp
/// Example showing CryptoContext generation
// using standard tables from the homomorphic encryption
   standardization project


PlaintextModulus ptm = 536903681;
double sigma = 3.2;
SecurityLevel securityLevel = HEStd_128_classic;

// support 7 multiplies (ciel(log2(7)))
usint nMults = 3;

// generate keys for s^2 and s^3
usint maxDepth = 3;

CryptoContext<DCRTPoly> cryptoContext =
    CryptoContextFactory<DCRTPoly>::
        genCryptoContextBFVrns(
          ptm, securityLevel, sigma, 0, nMults, 0,
             OPTIMIZED, maxDepth);

if( !cryptoContext ) {
        cout << "Error creating CryptoContext" << endl;
        return 0;
}

cryptoContext->Enable(ENCRYPTION);
```

Listing 5: Creating a CryptoContext using standard paranerers

Listing 6 shows creation from a serialization.

```
/// Example showing CryptoContext generation
/// from a serialization

// Deserialize the crypto context
CryptoContext<DCRTPoly> cc;
if ( !Serial::DeserializeFromFile(DATAFOLDER + "/
    cryptocontext.txt", cc, SerType::BINARY) ) {
        cerr << "I cannot read serialization from " <<
            DATAFOLDER + "/cryptocontext.txt" << endl;
}
else
        cout << "The cryptocontext has been deserialized.
            " << std::endl;
```

Listing 6: Creating a CryptoContext from a serialization

8.1.2   Creating A Plaintext

PALISADE users are able to convert integers, vectors of integers, and strings into Plaintext objects.

Plaintext objects can be used as input to Encryption, can be used as part of homomorphic operations, and are produced as a result of decryption.

All Plaintexts are created by static factory methods within the CryptoContext. Each style of Plaintext encoding has its own factory method.

The Plaintexts are all type safe. A Ciphertext knows the encoding used by the original Plaintext that it came from. Decryption creates a Plaintext with the proper encoding. All homomorphic operations check types before performing the operation, and will fail if either the encodings do not match, or if a particular encoding does not support homomorphic operations.

8.1.2.1   ScalarEncoding

ScalarEncoding is used to encode a single integer by simply copying the integer into the polynomial starting at index 0 and zero-filling remaining unused indices of the polynomial. Listing 7 shows an example of creating a Scalar Plaintext.

```
int64_t val = 12;

Plaintext sPtx = ctx->MakeScalarPlaintext(val);

Plaintext sPtx2 = ctx->MakeScalarPlaintext(-val);
```

Listing 7: Creating a Scalar Plaintext

8.1.2.2 IntegerEncoding

IntegerEncoding is used to encode a single unsigned integer into a polynomial such that each bit (0 or 1) in the integer is copied into its corresponding slot in the polynomial. For example, the integer 14, which is binary 1110, is encoded by emplacing 1, 1, 1 and 0 into the first four positions of the polynomial. This is shown in listing 8.

```
Plaintext intPtx = ctx->MakeIntegerPlaintext(14);
```

Listing 8: Creating an Integer Plaintext

Important Note: IntegerEncoding encodes each bit of the integer into a separate coefficient of the polynomial. This implies that the ring dimension (degree of polynomial) should be large enough to store all bits, especially in scenarios where each homomorphic multiplication doubles the number of polynomial coefficients with each multiplication. This is typically a non-issue for secure schemes/settings (as the ring dimension is already large enough) but can be an issue for the Null scheme, where the cyclotomic order is provided as an input argument.

8.1.2.3 FractionalEncoding

FractionalEncoding is a generalization of IntegerEncoding that can encode both integers and fractions. Currently it is limited in its functionaly and is only used to add support for right shifting (moving least significant bits to the fractional part). Examples of FractionalEncoding for encoding an integer 3 and a fraction 1/8 are shown in listing 9.

```
Plaintext intPtx = ctx->MakeFractionalPlaintext(3);
Plaintext intPtx = ctx->MakeFractionalPlaintext(0,3);
```

Listing 9: Creating a Fractional Plaintext

Important Note: FractionalEncoding encodes each bit of the integer into a separate coefficient of the polynomial. This implies that the ring dimension (degree of polynomial) should be large enough to store all bits, especially in

scenarios where each homomorphic multiplication doubles the number of polynomial coefficients with each multiplication. This is typically a non-issue for secure schemes/settings (as the ring dimension is already large enough) but can be an issue for the Null scheme, where the cyclotomic order is provided as an input argument.

8.1.2.4 CoefPackedEncoding

CoefPackedEncoding is used to encode a vector of integers, or an initializer list of integers, into a polynomial such that each integer is emplaced into a coefficient of the polynomial. This is illustrated in listing 10.

```
std::vector<int64_t> inputs( { 2, 3, 5, 7} );

// construction from vector
Plaintext c1 = ctx->MakeCoefPackedPlaintext(inputs);

// construction from initializer list
Plaintext c2 = ctx->MakeCoefPackedPlaintext({-6,1,4,8});
```

Listing 10: Creating a CoefPackedEncoding Plaintext

8.1.2.5 PackedEncoding

PackedEncoding is an implementation of an efficient encoder packing multiple integers into a single plaintext polynomial (single ciphertext) that enables SIMD (Single Instruction, Mutiple Data) operations on these integers. Currently PALISADE supports addition, multiplication, and rotation capabilities for packed ciphertexts. The cyclotomic order m has to divide $p-1$, where p is the plaintext modulus. This is shown in listing 11.

```
std::vector<int64_t> val( {37, 22, 18, 4, 3, 2, 1, 9} );

Plaintext packedPtx = ctx->MakePackedPlaintext(val);
```

Listing 11: Creating a PackedEncoding Plaintext

8.1.2.6 StringEncoding

StringEncoding is used to encode a string into a polynomial. For this encoding, each 8-bit character in the input is encoded directly into a coefficient of the polynomial. This encoding is constrained to only use 256 as a plaintext modulus. Listing 12 shows the use of this encoding.

Future implementations that support other character encodings, such as Unicode, are possible but are not currently supported.

Homomorphic operations will NOT work with this encoding.

```
string s("Here is my string!");

Plaintext stringPtx = ctx->MakeStringPlaintext(s);
```

<div align="center">Listing 12: Creating a String Plaintext</div>

8.1.3 Encryption

In order to encrypt a Plaintext into a Ciphertext, create a CryptoContext and a Plaintext as illustrated above.

The code in listing 13 illustrates this. It assumes that you have created a CryptoContext named "cc" and have created a Plaintext named ptxt within cc.

Observe that the code uses the KeyGen method to create a key pair, and uses the publicKey portion of that key pair for the encryption. The encryption will fail if the keys were generated in a different CryptoContext than cc.

```
/////////////////////////////////////////////////////
// Perform Key Generation Operation
/////////////////////////////////////////////////////

LPKeyPair<Poly> keyPair = cc->KeyGen();

if( !keyPair.good() ) {
        cout << "Key generation failed!" << endl;
        exit(1);
}

/////////////////////////////////////////////////////
// Encryption
/////////////////////////////////////////////////////

Ciphertext<Poly> ciphertext;

ciphertext = cc->Encrypt(keyPair.publicKey, ptxt);
```

<div align="center">Listing 13: Encrypting</div>

8.1.4 Decryption

In order to decrypt a Ciphertext into a Plaintext, a CryptoContext, Ciphertext and KeyPair must exist. The keys and the Ciphertext must have been created within the CryptoContext. An example is shown in listing 14.

```
/////////////////////////////////////////////////////
//Decryption of Ciphertext
/////////////////////////////////////////////////////

Plaintext decrypted;

cc->Decrypt(keyPair.secretKey, ciphertext, &decrypted);
```

Listing 14: Decrypting

8.1.5 Re-Encryption

Re-Encryption involves converting a Ciphertext that is decryptable with key "A" into a Ciphertext that is decryptable with key "B" by creating a re-encryption key and using it to re-encrypt the ciphertext.

The code sample in listing 15 illustrates this capability. It assumes a CryptoContext cc, an initial keypair A, and a Ciphertext cipher that has been created using A. We show the generation of key pair B, the generation of the re-encryption key, the re-encryption operation, and the subsequent decryption of the re-encrypted Ciphertext with B's secret key.

Two variants of re-encryptions are shown. The first one corresponds to the Chosen Plaintext Attack (CPA) model. The second variant corresponds to the model secure under Honest Re-encryption Attacks (HRA) [4]. We recommend the HRA model for practical use.

Note that in order to use Re-Encryption, the PRE capability must be enabled for the CryptoContext.

```cpp
////////////////////////////////////////////////////
// Perform Key Generation Operation
////////////////////////////////////////////////////

// Initialize Key Pair Containers
LPKeyPair<Poly> B = cc->KeyGen();

if( !B.good() ) {
        cout << "Key generation failed!" << endl;
        exit(1);
}

////////////////////////////////////////////////////
//Perform Re-encryption key generation operation.
////////////////////////////////////////////////////

LPEvalKey<Poly> rekey =
        cc->ReKeyGen(B.publicKey, A.secretKey);

////////////////////////////////////////////////////
// Re-Encryption
// CPA-secure variant
////////////////////////////////////////////////////

auto re_cipher = cc->ReEncrypt(rekey, cipher);

////////////////////////////////////////////////////
//Decryption of Ciphertext
////////////////////////////////////////////////////

////////////////////////////////////////////////////
// Re-Encryption with Ciphertext Re-randomization
// HRA-secure variant
////////////////////////////////////////////////////

auto re_cipherHRA = cc->ReEncrypt(rekey, cipher,B.
    publicKey);

////////////////////////////////////////////////////
//Decryption of Ciphertext
////////////////////////////////////////////////////

Plaintext ptxtHRA;

cc->Decrypt(B.secretKey, re_cipherHRA, &ptxtHRA);
```

Listing 15: Re-Encrypting

8.1.6 Serialization and Deserialization

When used in client/server and other distributed application settings, PALISADE objects need to be saved to persistent storage or streams, and then loaded back to instantiate the PALISADE objects in memory. PALISADE provides a serialization capability based on the industry-standard C++ **cereal** library (see https://github.com/USCiLab/cereal). The objects can be serialized either as binary objects (fastest option) or as JSON files (in cross-platform scenarios).

PALISADE objects can be serialized to streams (**Serialize**/**Deserialize** methods) or files (**SerializeToFile**/**DeserializeFromFile** methods).

Many of the objects to be serialized are associated with a particular CryptoContext. In order for such objects to be correctly serialized and deserialized, the serialization saves the CryptoContext that the object belongs to as part of the serialization, and the deserialization makes sure that the CryptoContext for the object being deserialized matches the CryptoContext in the serialization.

A simple of example of serialization to files is provided in **src/pke/demo/demo-simple-example-sereal.cpp**. A simple example of serialization to streams is provided in **pke/unittest/UnitTestSer.h**.

8.1.7 Homomorphic Addition of Ciphertexts

Homomorphic addition of two **Ciphertext** is performed by invoking the EvalAdd method of the **CryptoContext**. Both of the operands to the EvalAdd must have been created in the same **CryptoContext**, encrypted with the same **Key**, and encoded in the same way for this operation to work.

The code sample in listing 16 illustrates how to encode two vectors of integers into **Plaintext**, encrypt them into **Ciphertext**, perform homomorphic addition, and decrypt the result back into a **Plaintext**.

This code assumes a **CryptoContext** named cc and a keypair named kp.

```cpp
// Encode source data

std::vector<int64_t> v1 = {3,2,1,3,2,1,0,0,0,0,0,0};
std::vector<int64_t> v2 = {2,0,0,0,0,0,0,0,0,0,0,0};
std::vector<int64_t> v3 = {1,0,0,0,0,0,0,0,0,0,0,0};
Plaintext p1 = cc->MakeCoefPackedPlaintext(v1);
Plaintext p2 = cc->MakeCoefPackedPlaintext(v2);
Plaintext p3 = cc->MakeCoefPackedPlaintext(v3);

// Encryption

auto c1 = cc->Encrypt(kp.publicKey, p1);
auto c2 = cc->Encrypt(kp.publicKey, p2);
auto c3 = cc->Encrypt(kp.publicKey, p3);

// EvalAdd Operation

auto c12 = cc->EvalAdd(c1,c2);
auto csum = cc->EvalAdd(c12,c3);

//Decryption after Accumulation Operation

Plaintext plaintextAdd;

cc->Decrypt(kp.secretKey, csum, &plaintextAdd);

plaintextAdd->SetLength(p1->GetLength());

cout << "Original Plaintext:" << endl;
cout << p1 << endl;
cout << p2 << endl;
cout << p3 << endl;

cout << "Resulting Added Plaintext:" << endl;
cout << plaintextAdd << endl;
```

Listing 16: Adding Ciphertexts

8.1.8 Homomorphic Multiplication of Ciphertexts

Homomorphic multiplication of two **Ciphertext** is performed by invoking the EvalMult method of the **CryptoContext**. Both of the operands to the EvalMult must have been created in the same **CryptoContext**, encrypted with the same **Key**, and encoded in the same way for this operation to work.

The code sample in listing 17 illustrates how to encode two vectors of integers into **Plaintext**, encrypt them into **Ciphertext**, perform homomorphic multiplication, and decrypt the result back into a **Plaintext**.

This code assumes a **CryptoContext** named cc and a keypair named kp.

Note the creation of an EvalMult key using EvalMultKeyGen at the beginning of the sample.

```
cc->EvalMultKeyGen(kp.secretKey);

// Encode source data

std::vector<int64_t> v1 = {3,2,1,3,2,1,0,0,0,0,0,0};
std::vector<int64_t> v2 = {2,0,0,0,0,0,0,0,0,0,0,0};
std::vector<int64_t> v3 = {1,0,0,0,0,0,0,0,0,0,0,0};
Plaintext p1 = cc->MakeCoefPackedPlaintext(v1);
Plaintext p2 = cc->MakeCoefPackedPlaintext(v2);
Plaintext p3 = cc->MakeCoefPackedPlaintext(v3);

// Encryption

auto c1 = cc->Encrypt(kp.publicKey, p1);
auto c2 = cc->Encrypt(kp.publicKey, p2);
auto c3 = cc->Encrypt(kp.publicKey, p2);

// EvalMult Operation

auto m12 = cc->EvalMult(c1,c2);
auto cprod = cc->EvalMult(m12,c3);

//Decryption after Multiplication Operation

Plaintext plaintextMul;

cc->Decrypt(kp.secretKey, cprod, &plaintextMul);

plaintextMul->SetLength(p1->GetLength());

cout << "Original Plaintext:" << endl;
cout << p1 << endl;
cout << p2 << endl;
cout << p3 << endl;

cout << "Resulting Plaintext:" << endl;
cout << plaintextMul << endl;
```

Listing 17: Multiplying Ciphertexts

8.2 ABE

8.2.1 Creating an ABEContext

An **ABEContext** can be created by either choosing the relevant security level or basic parameters related to security level.

```
/// Example showing creating an CP-ABE ABEContext
/// By specifying security level and number of attributes
    only
/// Element is NativePoly
/// First parameter is for security level, next parameter
    is the number of attributes

 ABEContext<NativePoly> context;
 context.GenerateCPABEContext(HEStd_192_classic,6);
```

Listing 18: Creating a ABEContext with Security Level

```
/// Example showing creating a GPV IBE ABEContext
/// By specifying relevant parameters: ring size and base
    of the gadget matrix
/// Element is NativePoly
/// First parameter is for ring size, second one is for
   base

 ABEContext<NativePoly> context;
 context.GenerateIBEContext(1024,64);
```

Listing 19: Creating a ABEContext with Parameters

8.2.2 Generating Master Keys

```
/// Example showing master key pair generation for GPV
    IBE ABEContext
/// Element is NativePoly

IBEMasterPublicKey<NativePoly> mpk;
IBEMasterSecretKey<NativePoly> msk;
context.Setup(&mpk,&msk);
```

Listing 20: Generating Master Public Key Pair with ABEContext

8.2.3 Creating Access Policies

```
/// Example showing user identifier generation for GPV
    IBE ABEContext
/// Element is NativePoly

IBEUserIdentifier<NativePoly> id(context.
    GenerateRandomElement());
```

Listing 21: Creating a User Identifier with GPV IBE ABEContext

```
/// Example showing user attribute set/access policy
    creating for CP-ABE ABEContext
/// Element is NativePoly

std::vector<unsigned int> userattributes = {1,0,1,0,1,1};
std::vector <int> accesspolicy = {0,-1,1,0,1,0);

CPABEUserAccess<NativePoly> ua(userattributes);
CPABEAccessPolicy<NativePoly> ap(accesspolicy);
```

Listing 22: Creating a User Attribute Set/Access Policy with CP-ABE ABEContext

8.2.4 Key Generation

The secret key generated is tailored to the identifier or attribute set of the user

```
/// Example showing secret key generation for GPV IBE
   ABEContext
/// Element is NativePoly
/// msk is the master secret key, mpk is the master
   public key, id is the user identifier

IBESecretKey<NativePoly> sk;
context.KeyGen(msk,mpk,id,&sk);
```

Listing 23: Generating a Secret Key with ABEContext

Additionally, it is possible to split the key generation process into two phases: Online and offline. Offline phase consists of creation of perturbation vector which is independent from the user's id or attribute set.

```
/// Example showing the offline phase of secret key
   generation for GPV IBE ABEContext
/// Element is NativePoly
/// msk is the master secret key

PerturbationVector<NativePoly> pv;
context.KeyGenOfflinePhase(msk,pv);
```

Listing 24: Generating a Secret Key with ABEContext (Offline Phase - Perturbation Generation)

The online phase in this scenario consists of actual key generation based on user's id or attribute set without the perturbation subroutine.

```
/// Example showing the online phase of secret key
   generation for GPV IBE ABEContext
/// Element is NativePoly
/// msk is the master secret key, mpk is the master
   public key, id is the user's identifier and pv is the
   perturbation vector

IBESecretKey<NativePoly> sk;
context.KeyGenOnlinePhase(msk,mpk,id,pv,&sk);
```

Listing 25: Generating a Secret Key with ABEContext (Online Phase - Key Generation)

8.2.5 Encryption

A **Plaintext** is encrypted with a target party, which means the target user's identifier in GPV IBE or access policy for CP-ABE.

```
/// Example showing encryption for CP-ABE ABEContext
/// Element is NativePoly
///mpk is the master public key, ap is the access policy

///Creation of plaintext. The format is intentionally
    used for support
 std::vector<int64_t> vectorOfInts = { 1,0,0,1,1,0,1,0,
    1, 0};
 Plaintext pt = context.MakeCoefPackedPlaintext(
    vectorOfInts);

///Actual encryption
 CPABECiphertext<NativePoly> ct;
context.Encrypt(mpk,ap,pt,&ct);
```

Listing 26: Encryption with CP-ABE ABEContext

8.2.6 Decryption

```
/// Example showing decryption for CP-ABE ABEContext
/// Element is NativePoly
///sk is the secret key of the user, ua is the user's
    attributes, ap is the access policy defined and ct is
    the ciphertext

Plaintext dt = context.Decrypt(ap,ua,sk,ct);
```

Listing 27: Decryption with CP-ABE ABEContext

```
/// Example showing decryption for GPV IBE ABEContext
/// Element is NativePoly
///sk is the secret key of the user and ct is the
   ciphertext

Plaintext dt = context.Decrypt(sk,ct);
```

Listing 28: Decryption with GPV IBE ABEContext

8.3 Signature

8.3.1 Creating a SignatureContext

A **SignatureContext** can be created by either choosing one of the predefined ring sizes or a set of parameters.

```
/// Example showing creating a GPV SignatureContext
/// By specifying some specific parameters
/// First parameter is the ring size, second parameter is
    the bit width of modulus and third one is the base of
    the gadget matrix
/// Element is NativePoly

SignatureContext<NativePoly> context;
context.GenerateGPVContext(1024,61,64);
```

Listing 29: Creating a SignatureContext with Parameters

8.3.2 Key Generation

```
/// Example showing creating sign/verification keys  with
    a GPV SignatureContext
/// Element is NativePoly

GPVVerificationKey<NativePoly> vk;
GPVSignKey<NativePoly> sk;
context.KeyGen(&sk,&vk);
```

Listing 30: Key Generation with SignatureContext

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8.3.3 Signing

```
/// Example showing signing  with a GPV SignatureContext
/// Element is NativePoly
///sk is the signing key and vk is the verification key

///Creation of plaintext
string pt = "This is a test";
GPVPlaintext<NativePoly> plaintext(pt);

///Actual signing
GPVSignature<NativePoly> signature;
context.Sign(plaintext,sk,vk,&signature);
```

Listing 31: Signing with SignatureContext

Additionally, it is possible to split the signing process into two phases: Online and offline. Offline phase consists of creation of perturbation vector which is independent from message to be signed.

```
/// Example showing offline phase of signing  with a GPV
    SignatureContext
/// Element is NativePoly
///sk is the signing key

PerturbationVector<NativePoly> pv;
context.SignOfflinePhase(sk,pv);
```

Listing 32: Signing with SignatureContext (Offline Phase - Perturbation Generation)

The online phase in this scenario consists of actual signing process without the perturbation subroutine.

```
/// Example showing online phase of signing  with a GPV
    SignatureContext
/// Element is NativePoly
///sk is the signing key, vk is the verification key and
    pv is the perturbation vector generated in offline
    phase

///Creation of plaintext
string pt = "This is a test";
GPVPlaintext<NativePoly> plaintext(pt);

///Actual signing
GPVSignature<NativePoly> signature;
context.SignOnlinePhase(plaintext,sk,vk,pv,&signature);
```

Listing 33: Signing with SignatureContext (Online Phase - Signing)

8.3.4 Verification

```
/// Example showing verification  with a GPV
    SignatureContext
/// Element is NativePoly
/// vk is the verification key

bool verificationResult = context.Verify(plaintext,
    signature,vk);
```

Listing 34: Verification with SignatureContext

8.4 Matrix Operations

A large number of matrix operations are available in PALISADE.

In the example in Listing 35, we illustrate performing a linear regression on two encrypted matrices. The code assumes a CryptoContext named cc.

```
auto zA = [=]() { return
make_unique<Plaintext>(cc->MakeCoefPackedPlaintext(
                    {int64_t(0)} ));
};

Matrix<Plaintext> xP = Matrix<Plaintext>(zA, 2, 2);
xP(0,0) = cc->MakeCoefPackedPlaintext({1,0,1,1,0,1,0,1});
xP(0,1) = cc->MakeCoefPackedPlaintext({1,1,0,1,0,1,1,0});
xP(1,0) = cc->MakeCoefPackedPlaintext({1,1,1,1,0,1,0,1});
xP(1,1) = cc->MakeCoefPackedPlaintext({1,0,0,1,0,1,1,0});

Matrix<Plaintext> yP = Matrix<Plaintext>(zA, 2, 1);
yP(0,0) = cc->MakeCoefPackedPlaintext({1,1,1,0,0,1,0,1});
yP(1,0) = cc->MakeCoefPackedPlaintext({1,0,0,1,0,1,1,0});

//Perform the key generation operations.
LPKeyPair<Poly> kp = cc->KeyGen();
cc->EvalMultKeyGen(kp.secretKey);

//Encryption
shared_ptr<Matrix<RationalCiphertext<Poly>>> x =
  cc->EncryptMatrix(kp.publicKey, xP);
shared_ptr<Matrix<RationalCiphertext<Poly>>> y =
  cc->EncryptMatrix(kp.publicKey, yP);

//Linear Regression
auto result = cc->EvalLinRegression(x, y);

//Decryption into num and denom matrices
shared_ptr<Matrix<Plaintext>> num;
shared_ptr<Matrix<Plaintext>> denom;
cc->DecryptMatrix(kp.secretKey, result, &num, &denom);
```

Listing 35: Calculating Linear Regression

9 Building and Installing PALISADE

PALISADE git repository includes an up-to-date wiki with detailed instructions on building and running PALISADE on various platforms. We use CMake to build PALISADE, and support Linux, Windows, and macOS. The library requires a C++ compiler that implements the C++11 standard, with support for the OpenMP library. Make, cmake, and autoconf also need to be installed. While not required, it is also recommended that you install and use doxygen.

10   Programming Style

PALISADE coding style is based on the official Google C++ coding style.
Of particular note on the documentation style:

- We use doxygen commenting style on classes, methods and constants.

- We given meaningful variable names to all variables.

- Every reused discrete block of code has its own method.

- Every discrete line or code or discrete group of code lines for each task has its own comment.

With regards to naming conventions:

- Variable names: camelCase.

- Class, struct, typedef, and enum names: CamelCase.

- Class data members: m_camelCase.

- Class accessor names: GetProperty() and SetProperty().

- Class method names: CamelCase.

- Global variable names: g_camelCase.

- Constant names and macros: UPPER_CASE_WITH_UNDERSCORES (example: BIT_LENGTH).

- Operator overloading is used for binary operations.

We also follow the additional design principles that:

- cout should never be used for exception handling and should never be used in committed code in the core PALISADE library.

- a set of PALISADE exceptions is defined in utils/exception.h. The library is being migrated to throw only these exceptions.

A PALISADE License

PALISADE is available under the following license:

B Support

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