PALISADE Lattice Cryptography Library User Manual (v1.10.5)

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Abstract

This document is the manual for the PALISADE lattice cryptography library. This manual provides an introduction to the library by describing the library architecture and cataloging its capabilities. We focus on the PALISADE library's ability to support homomorphic encryption capabilities to evaluate arithmetic operations on data while encrypted. We do not explicitly provide an introduction to lattice cryptography, but we provide an overview of notation and terminology necessary to use the PALISADE library. In addition to providing code samples for the use of the PALISADE library, we also discuss the library programming style for developers who wish to read library code or even add to the library. We also provide an overview of common pitfalls in the use of PALISADE.

Contents

1	Document Overview	5
2	Introduction	6
3	A Brief Overview of Lattice Cryptography	8
4	Library Architecture 4.1 Application Layer	10 10 11 11 11 12 12
5	Capabilities	13
6	PALISADE Directory Structure	20
7	Terminology and Notation 7.1 Typing 7.2 CryptoContext 7.3 BinFHEContext 7.4 ABEContext 7.5 SignatureContext 7.6 Plaintext 7.7 Ciphertext 7.8 Access Policy 7.9 Signature 7.10 Keys 7.11 Capability 7.12 Scheme 7.13 Element 7.13.1 Poly 7.13.2 NativePoly 7.13.2 NativePoly 7.14 ElementParams 7.15 EncodingParams 7.15 EncodingParams 7.16 Matrix	222 233 244 245 266 277 277 277 288 299 299 299 299 300 300
8	Sample Implementations: PKE Module 8.1 Creating a CryptoContext	31 31 36 40

	8.4	Decryption	40
	8.5	Re-Encryption	41
	8.6		42
	8.7	1	43
	8.8	Homomorphic Multiplication of Ciphertexts	45
9	Sam	ple Implementations: FHE	47
	9.1	Integer arithmetic	47
	9.2	Real-number arithmetic	47
	9.3	Boolean Circuit Arithmetic	49
10	Sam	ple Implementations: ABE	50
	10.1	Creating an ABEContext	50
	10.2	Generating Master Keys	50
	10.3	Creating Access Policies	50
	10.4	Key Generation	51
	10.5	Encryption	52
	10.6	Decryption	52
11	Sam	ple Implementations: Digital Signature	53
	11.1	Creating a SignatureContext	53
	11.2	Key Generation	53
	11.3	Signing	53
	11.4	Verification	54
12	Buil	ding and Installing PALISADE	55
13	Pros	gramming Style	56
Αį	ppen	dix A PALISADE License	57
Aı	ppen	dix B Support	58
\mathbf{L}^{i}	istir	ngs	
	1	Directory structure for PALISADE source code	20
	2		$\frac{20}{26}$
	3		$\frac{20}{32}$
	3 4		34
	5		$\frac{34}{34}$
	6		36
	7		36
	8		37
	9		37 37
	10		31 38

11	Creating a CoefPackedEncoding Plaintext	38
12	Creating a PackedEncoding Plaintext	39
13	Creating a CKKSPackedEncoding Plaintext	39
14	Creating a String Plaintext	39
15	Encrypting	40
16	Decrypting	40
17	Re-Encrypting	42
18	Adding Ciphertexts	44
19	Multiplying Ciphertexts	46
20	List of arguments of CKKS context generation method	48
21	Creating a CKKS plaintext	48
22	Creating a ABEContext with Security Level	50
23	Creating a ABEContext with Parameters	50
24	Generating Master Public Key Pair with ABEContext	50
25	Creating a User Identifier with GPV IBE ABEContext	51
26	Creating a User Attribute Set/Access Policy with CP-ABE ABEContext $$	51
27	Generating a Secret Key with ABEContext	51
28	Generating a Secret Key with ABEContext (Offline Phase - Perturbation Gen-	
	eration) \dots	51
29	Generating a Secret Key with ABEContext (Online Phase - Key Generation)	52
30	Encryption with CP-ABE ABEContext	52
31	Decryption with CP-ABE ABEContext	52
32	Decryption with GPV IBE ABEContext	53
33	Creating a SignatureContext with Parameters	53
34	Key Generation with SignatureContext	53
35	Signing with SignatureContext	54
36	Signing with Signature Context (Offline Phase - Perturbation Generation)	54
37	Signing with SignatureContext (Online Phase - Signing)	54
38	Verification with SignatureContext	55

1 Document Overview

This manuscript is a working document to introduce users to the PALISADE lattice cryptography library. The most recent copy of this document is available for download from the PALISADE library website. Copies of this document may be available for download from PALISADE contributors' websites, but the version available for download on the PALISADE library website should be considered authoritative.

The manual is organized as follows;

- An introduction to the library is provided in Section 2.
- Section 3 provides a basic introduction to lattice cryptography.
- The library architecture is discussed in Section 4.
- The library capabilities are discussed in Section 5.
- Section 6 provides an overview of the PALISADE library directory structure.
- Section 7 provides an overview of notation and terminology used in the library and this manual.
- Section 8 provides codes samples for the Public Key Encryption (PKE) module.
- Section 9 provides codes samples covering FHE for integer arithmetic, real-number arithmetic, and Boolean circuits.
- Section 10 provides codes samples for Attribute-based Encryption (ABE).
- Section 11 provides codes samples for Digital Signatures (Signature).
- Section 12 describes how to build the library in a generic Linux environment.
- Section 13 describes the programming style we maintain in the library for those users who wish to contribute code to the library.

In addition, we provide the following appendices:

- Appendix A reproduces the library's BSD 2-clause license.
- The PALISADE library has been made possible by the generous support of our sponsors. A listing of the PALISADE library sponsors can been seen in Appendix B.

The public version of the PALISADE Lattice Cryptography library can be found on The PALISADE Git Repository.

The listed authors of this document are the current primary maintainers of the PALISADE library repository.

2 Introduction

Lattice cryptography has received considerable attention because of its capability to support both post-quantum public-key encryption and the ability to compute on data while encrypted via homomorphic encryption. Lattice cryptography also provides other powerful capabilities such as proxy re-encryption and attribute-based encryption. The PALISADE library provides implementations of the building blocks for lattice cryptography capabilities along with end-to-end implementations of advanced lattice cryptography protocols for public-key encryption, proxy re-encryption, homomorphic encryption and others. PALISADE provides both an experimental platform for researchers to design and evaluate new lattice cryptography capabilities, while at the same time providing implementations of known protocols that can be integrated into applications. In this manual we describe PALISADE and discuss how it can be used.

The PALISADE library is designed to address the following inherent challenges of lattice cryptography implementation:

- The complexity of algebraic constructions makes it hard for non-experts to leverage, let alone implement, algebraic constructions used as the building blocks of lattice cryptography.
- Lattice cryptography implementations are often purpose-built. Rapid deployment on new hardware systems is difficult to support with these existing implementations.
- Parameter selection for security and performance takes very sophisticated understanding, and this is nontrivial even for experts up to a dozen parameters may be needed to be set for some schemes.
- Security assumptions are evolving, and it has been difficult to adapt prior implementations. See for example the recent sub-field lattice attacks against LTV which required re-design of libraries that previously used this scheme.
- Application integration has been challenging, without easy methods to efficiently perform operations on non-trivial data types, such as rationals, complex numbers, etc.

As a result of these identified challenges, we design PALISADE to achieve the following design goals:

- Create an extensible and adaptable library for lattice cryptography. Lattice crypto uses several computational primitives. We allow for new protocols that mix-and-match these primitives to avoid the need for expert low-level knowledge. This has been a major advance in the PALISADE library, and we are still refining these features of PALISADE as we support more capabilities.
- Provide a modular structure to mix and match components. This allows for systemoptimized arithmetic and lattice "back-ends"/plugins. We currently support multiple implementations of big integer math that have various performance trade offs and bit length limitations. Multiple sets of math back-ends can be selected at compile

time. The PALISADE library is thus designed to be highly portable into commodity computing and hardware environments, including Windows, Linux, MacOS and Android environments (though Android it experimental). The ability to support multiple hardware accelerators is a work in progress in PALISADE.

- Offer (semi-)automated parameter selection. This reduces the need to tune an overwhelming number of parameters. This is still a major research topic and is a work in progress in PALISADE.
- Develop common crypto APIs. Common crypto APIs across multiple schemes and back-ends "hide" complex details of lattice constructions / parameterization from application developers, allowing developers to focus on their areas of interest while integrating and replacing components to maintain security and performance. This is another major feature of PALISADE that we continue to refine.
- Deliver good software engineering with focus on usability. This permits standards-based design and style. Unit tests and bench-marking environments are supported for evaluation and tuning of integrated applications. We aim to provide documentation, clean code and useful examples that reduce effort for new developers.

Our identification of these goals in PALISADE is informed by industry experience integrating PALISADE into multi-organizational large software engineering projects. As a result of these identified challenges and the resulting engineering goals we set for ourselves in the design of PALISADE, we designed PALISADE to be highly modular, with a core library of lattice cryptography primitives that support multiple protocols for public-key encryption, homomorphic encryption, digital signature schemes, proxy re-encryption and program obfuscation.

3 A Brief Overview of Lattice Cryptography

In the following discussion, objects and functions that are directly supported by PALISADE are printed in this type.

At a high intuitive level, encryption is a computational process wherein Data is Encoded as Plaintext and then encrypted into Ciphertext according to some Encryption algorithm. Conversely, Decryption is a corresponding computational process wherein the Plaintext can be recovered from the Ciphertext through the use of a corresponding Decryption algorithm.

These algorithms use cryptographic Keys to perform the Encryption and Decryption operations. Intuitively, an encryption scheme is secure if it prevents an adversary from recovering Plaintext (or information about a Plaintext) from Ciphertext when the adversary does not have the corresponding decryption key.

A "symmetric key" protocol uses the same key to perform both encryption and decryption. A "public key" or "assymmetric" protocol uses a pair of Public and Secret keys, respectively, for encryption and decryption. A Secret key is sometimes called a Private key.

In practice symmetric keys and secret keys are kept secret because they can be used to access protected information. Public keys are often widely distributed and often published on the open Internet. The intended use of a public key is that one can encrypt data with a downloaded public key corresponding to an intended recipient, encrypt sensitive information for the recipient with the public key, and send that encrypted sensitive information to the recipient. The recipient can use her secret key to decrypt and recover the protected information encoded in the plaintext.

Cryptographic algorithms are designed around computational hardness assumptions so that the difficulty of recovering information about plaintext is at least as hard as some provable computationally hard problem. Thus, it is theoretically possible to break such a system, but it is assumed infeasible to do so by any known practical means. Different computationally hard problems define different classes of encryption systems. PALISADE focuses on lattice-based cryptography. The security of lattice cryptography is based on the hardness of variants of the Shortest Vector Problem (SVP), Learning With Errors (LWE), and other hard problems. Lattice cryptography has both symmetric and public key variants, but we generally focus on the public key lattice cryptography variants in the PALISADE library and this manual.

Homomorphic Encryption (HE) or Fully Homomorphic Encryption (FHE) refer to a class of encryption methods envisioned by Rivest, Adleman, and Dertouzos in 1978. HE differs from basic encryption methods in that it allows computation to be performed directly on encrypted data without requiring access to a secret key. The result of such a computation remains in an encrypted form, and can at a later point be revealed by the owner of the secret key by decrypting the result.

In 2009 Craig Gentry showed the existence of lattice-based FHE capabilities. Since this initial discovery of a lattice-based FHE protocol, there has been a Renaissance in lattice cryptography, with the discovery of several other increasingly practical HE schemes and variations of HE protocols. Some of the common HE schemes include the Brakerski-Fan-Vercauteren (BFV)¹, Brakerski-Gentry-Vaikuntanathan (BGV), Cheon-Kim-Kim-Song (CKKS), FHEW, TFHE and Stehle-Steinfeld (StSt) schemes. Other related protocols include:

- Proxy Re-Encryption (PRE), which permits delegation of ciphertext decryption, thus allowing a host to delegate access to encrypted data.
- Somewhat Homomomorphic Encryption (SHE), which permits a limited amount of computation on encrypted data.
- Leveled Somewhat Homomorphic Encryption (Leveled SHE), which permits at least a fixed depth of computation to be performed on encrypted data by using a decreasing ladder (set) of ciphertext moduli.
- Multiparty Homomorphic Encryption, which enables multiple participants to contribute data to a joint computation, without sharing access to the actual data.

The public version of PALISADE supports all of the protocols discussed above, and we are in the process of adding support for more protocols and schemes. From v1.4 and onwards, PALISADE also supports a selection of trapdoor-based schemes: a Gentry-Peikert-Vaikuntanathan (GPV) digital signature scheme, a GPV identity-based encryption (IBE) scheme, and a Zhang-Zhang ciphertext-policy attribute-based encryption (CP-ABE) scheme.

An inherent property of encrypted computing technologies, including the various protocols supported by PALISADE, is that computing on encrypted data is significantly slower and more compute-intensive than computing on plaintext data. As such, debugging the applications of encrypted computing technologies can be a frustrating, slow process. To aid developers in integrating PALISADE implementations of encrypted computing technologies, we also provide in PALISADE a "Null" scheme which supports the same API as the BFV, BGV, and StSt implementations, but which does not encrypt data and performs all operations on unencrypted plaintext. The Null scheme implementation operates as a light-duty no-security equivalent of the encrypted computing protocols supported by PALISADE. We provide the Null scheme so developers can test the correctness their PALISADE program more easily without the overhead or frustration of testing operations with slower more compute-intensive workloads engendered by encrypted computing capabilities.

¹This scheme is also frequently denoted as the FV scheme, but we choose to call it the BFV scheme.

4 Library Architecture

The PALISADE library implements lattice cryptography in C++. The objects that are created by and manipulated within PALISADE are instances of C++ classes.

PALISADE is designed as a layered architecture where each layer provides a set of services to the layer "above" it in the stack, and makes use of services in the layer "below" it in the stack. The interfaces between each of the layers are designed to implement a common API. This permits substituting multiple implementations at any layer for experimental purposes.

The high-level architecture of PALISADE is illustrated in Figure 1.

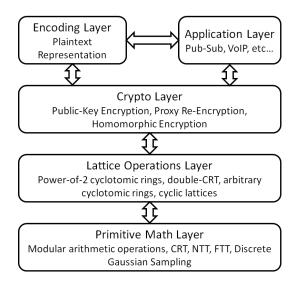


Figure 1: High-level PALISADE architecture

The layers in PALISADE are as follows:

- 1. **Application**: All programs that call the PALISADE library services are in this layer.
- 2. **Encoding**: All implementations of methods to encode data are at this layer.
- 3. Crypto: All implementation of cryptographic protocols are at this layer.
- 4. Lattice Operations: All higher-level lattice-crypto mathematical building blocks are in this layer.
- 5. **Primitive Math**: All low-level generic mathematical operations, such as multi-precision arithmetic implementations, are at this layer.

4.1 Application Layer

All programs that make use of the PALISADE library are said to be in the Application layer.

All programs at the Application layer make calls to services exposed in the PALISADE Crypto layer to gain access to PALISADE lattice cryptography functionality. The Application layer also makes use of service at the Encoding layer.

4.2 Encoding Layer

The Encoding layer contains all classes needed to provide for the encoding of any supported raw plaintext message data into a Plaintext object, and for decoding back to raw plaintext messages whenever necessary.

The Encoding layer is used to create Plaintext objects. These objects are sometimes created at the request of the Application layer, in which case Crypto layer methods act as a proxy for the Application layer, sometimes at the request of the Crypto layer itself. The interface for Encoding functionality is C++ methods provided by Plaintext.

4.3 Crypto Layer

The Crypto layer contains all classes needed to provide all available lattice cryptography functionality for specific cryptographic protocols such as public-key encryption, PRE and SHE schemes, and all included methods such as encryption and decryption, proxy re-encryption and container classes for parameters specific to those schemes.

The interface for Crypto functionality is C++ methods provided by CryptoContext. Therefore the Crypto layer provides various factory methods for creating a CryptoContext along with the context itself. The Crypto layer manipulates Plaintext and Ciphertext objects that are passed to it by the Application layer, and returns the appropriate Plaintext and Ciphertext objects to the Application. Operations on a Matrix of such objects is also provided.

Similar to CryptoContext, the library also provides BinFHEContext, SignatureContext and ABEContext for Boolean-circuit FHE, digital signature and GPV IBE/CP-ABE operations, respectively. However, unlike CryptoContext these contexts have their own implementation of ciphertexts. SignatureContext and BinFHEContext also use their own implementation of plaintexts. The Crypto layer makes use of services provided by the Lattice Operations layer.

4.4 Lattice Operations Layer

The Lattice Operations layer provides support for all lattice constructs, including power-of-two cyclotomic rings and arbitrary cyclotomic rings. The Double Chinese Remainder Theorem (Double-CRT) representation of cyclotomic rings is also implemented in the Lattice layer.

With the release of version 1.4.0, the lattice layer also hosts trapdoors and trapdoor sampling. Trapdoors are lattice constructs consisting of two vectors of polynomials. These structures are key parts of the newly added digital signature, identity-based encryption and ciphertext-policy attribute-based encryption schemes. These algorithms require a preimage of the information to be sampled from a discrete Gaussian over a lattice, which is done using the trapdoor sampling algorithms.

The Lattice layer is used to provide an implementation of the various Poly classes, including Poly, NativePoly, and DCRTPoly. These objects are used as building blocks in Plaintext and Ciphertext. The interface for Lattice functionality is the C++ methods provided by the Poly classes.

The Lattice layer performs lattice operations by decomposing operations into primitive arithmetic operations on integers, vectors, and matrices. The Lattice layer makes use of the Primitive Math layer to perform these operations.

4.5 Primitive Math Layer

The Primitive Math layer provides support for basic modular arithmetic operations, including multi-precision arithmetic. This layer also includes efficient algorithms for Number-Theoretic Transform (NTT), Fermat-Theoretic Transform (FTT), and discrete Gaussian samplers, among others. The interface for Math functionality is the C++ methods provided by both custom multi-precision libraries, and external imported libraries such as NTL.

4.6 Utilities

PALISADE also provides a cross-cutting Utilities module for common utility functions used by all the layers. The primary contents of this layer are tools for basic hashing, serialization and deserialization of objects, efficient memory allocation, debugging, and exception handling.

5 Capabilities

One of the goals of PALISADE is to provide straightforward mechanisms to select 1) an encryption protocol, 2) an encryption scheme to support that protocol, 3) encoding mechanisms to represent data with that scheme, 4) math back-ends to support efficient computational operations over that data for the scheme and 5) configuration parameters for that protocol, encoding mechanisms and math back-end. PALISADE provides a broad set of selections for each of these choices, and provides the user with the ability to add their own schemes, encodings, operations, etc. Furthermore, the user of PALISADE can select from multiple lattice layer implementations and math layer implementations, can easily mix-and-match, and can even provide their own implementations at different layers. In this section we describe these choices we make available in PALISADE.

At the highest level, the PALISADE library groups encryption protocols into a set of capabilities that can be selectively enabled by the user at run time. Enabling a particular capability turns on several functions in support that capability. Some capabilities imply other capabilities, such as how SHE, for example, implies PKE capabilities. Thus, in these scenarios, some capabilities are turned "on" automatically.

Capabilities and functions currently supported by PALISADE are listed in Tables 1–5. More detailed information on each function can be found in the PALISADE API specifications published in the gitlab repository (the API specifications are generated using Doxygen).

Table 1: Non-FHE PALISADE Capabilities and Functions

Capability	apability Description Functions Supp		Also Enabled
	Public/Symmetric Key Encryption	KeyGen	
ENCRYPTION		Encrypt	
		Decrypt	
PRE	Proxy Re-Encryption	ReKeyGen	PKE
1 1111		ReEncrypt	1 IXE

Once an encryption protocol is selected, a user of PALISADE can select from one of multiple schemes:

- BFV variants
 - BFV: "textbook" Fan-Vercauteren variant of Brakerski's scale invariant scheme [Bra12, FV12, LN14]
 - BFVrns: Halevi-Polyakov-Shoup full RNS variant of the BFV scheme [HPS18, BPA+18]
 - BFVrnsB: Bajard-Eynard-Hasan-Zucca full RNS variant of the BFV scheme [BEHZ16, BPA+18]
- BGV variants
 - BGV: Brakerski-Gentry-Vaikuntanathan scheme [BGV14, GHS12]
 - BGVrns: A full RNS variant of the BGV scheme [KPZ20]
- CKKS: 2 full RNS variants of the Cheon-Kim-Kim-Song scheme [CKKS16] with various RNS optimizations from [CHK⁺18, BGP⁺19, HK19, KPP20]
- StSt: Stehle-Steinfeld scheme [SS11]
- FHEW: FHEW and extended TFHE schemes [DM14, CGGI18, MP20]
- Null: A system with all encryptions removed and all math operations done on Plaintext for development. Emulates BFV* and BGV* schemes (integer arithmetic operations).

Table 6 maps which schemes support which capabilities.

Starting with version 1.7, PALISADE also supports FHEW [DM14, MP20], a scheme for evaluating arbitrary Boolean circuits that runs bootstrapping for each binary gate evaluation. This scheme has very specialized functionality for working with boolean operations. Details on FHEW capabilities are provided in Table 5. Starting with release 1.8, PALISADE also supports FHEW with Gama-Izabachene-Nguyen-Xie (GINX) bootstrapping [GINX16], which is considered as an extended version of the TFHE scheme [MP20].

In addition to the homomorphic encryption schemes, PALISADE supports the following trapdoor-based schemes

- GPV Signature: Gentry-Peikert-Vaikuntanathan Digital Signature Scheme [GPV08, GPR+17]
- GPV IBE: Gentry-Peikert-Vaikuntanathan Identity-based Encryption Scheme [GPV08, GPR+17]
- CP-ABE: Zhang-Zhang Ciphertext-policy Attribute-based Encryption Scheme [ZZG12, GPR+17]

The functions for these schemes are listed in Table 7.

Table 2: PALISADE Operations/Functions included in the SHE capability (the Stehle-Steinfeld scheme is not included here as it supports only very limited/shallow computations). Note: BFV* and BGV* indicate all variants of BFV and BGV, respectively.

Functions Supported	Schemes Supported
EvalAdd	BGV*, BFV*, CKKS
EvalAdd (Scalar)	CKKS
EvalAdd (Plaintext)	BGV*, BFV*, CKKS
EvalAddMutable(All)	CKKS, BGVrns
EvalMult	BGV*, BFV*, CKKS
EvalMult (Scalar)	CKKS, BGVrns
EvalMult (Plaintext)	BGV*, BFV*, CKKS
EvalMultMutable (All)	CKKS, BGVrns
EvalMultAndRelinearize	BFV*, BGVrns, CKKS
EvalSub	BGV*, BFV*, CKKS
EvalSub (Scalar)	CKKS
EvalSub (Plaintext)	BGV*, BFV*, CKKS
EvalSubMutable (All)	CKKS, BGVrns
EvalNegate	BGV*, BFV*, CKKS
EvalLinearWSum(Mutable)	CKKS, BGVrns
EvalAutomorphism	BGV*, BFV*, CKKS
EvalAtIndex	BGV*, BFV*, CKKS
EvalFastRotation	CKKS, BGVrns
EvalSumRows	CKKS
EvalSumCols	CKKS
EvalSum	BGV*, BFV*, CKKS
EvalMerge	BGV*, BFV*, CKKS
EvalAddMany(InPlace)	BGV*, BFV*, CKKS
EvalMultMany	BGV*, BFV*, CKKS
EvalInnerProduct	BGV*, BFV*, CKKS
EvalLinRegression	BGV*, BFV*, CKKS
EvalLinRegressBatched	BGV*, BFV*, CKKS
EvalCrossCorrelation	BGV*, BFV*, CKKS
EvalRightShift	BGV*, BFV*, StSt
	DOINT DELLA CHILLS
KeySwitch	BGV*, BFV*, CKKS
Relinearize	CKKS, BGVrns
KeySwitchGen	BGV*, BFV*, CKKS
EvalMultKeyGen	BGV*, BFV*, CKKS
EvalAutomorphismKeyGen	BGV*, BFV*, CKKS
EvalAtIndexKeyGen	BGV*, BFV*, CKKSl
EvalSumKeyGen	BGV*, BFV*, CKKS
EvalSumRowsKeyGen	CKKS
EvalSumColsKeyGen	CKKS
AdjustLevelWithRescale	CKKS
EvalFastRotationPrecompute	CKKS, BGVrns
AddRandomNoise 15	BGV*, BFV*, CKKS

Table 3: PALISADE Operations/Functions included in the LeveledSHE capability. Note: BGV^* indicates all variants of BGV

Functions Supported	Schemes Supported
ModReduce	BGV*
Rescale	CKKS
LevelReduce	CKKS
Compress	BGVrns, CKKS
EvalPoly	CKKS

Table 4: PALISADE Operations/Functions included in the MULTIPARTY (Threshold FHE) capability. Note: BFV^* and BGV^* indicate all variants of BFV and BGV, respectively

Functions Supported	Schemes Supported
MultiKeySwitchGen	BGV*, BFV*, CKKS
MultiEvalAutomorphismKeyGen	BGV*, BFV*, CKKS
MultiEvalSumKeyGen	BGV*, BFV*, CKKS
MultiEvalAtIndexKeyGen	BGV*, BFV*, CKKS
MultiAddPubKeys	BGV*, BFV*, CKKS
MultiAddEvalKeys	BGV*, BFV*, CKKS
MultiMultEvalKey	BGV*, BFV*, CKKS
MultAddEvalSumKeys	BGV*, BFV*, CKKS
MultiAddEvalAutomorphismKeys	BGV*, BFV*, CKKS
MultiAddEvalMultKeys	
	BGV*, BFV*, CKKS
MultipartyDecryptLead	BGV*, BFV*, CKKS
MultipartyDecryptMain	BGV*, BFV*, CKKS
MultipartyDecryptionFusion	BGV*, BFV*, CKKS

Table 5: PALISADE Capabilities and Functions for Boolean-Circuit FHE (performs bootstrapping for each binary gate evaluation)

Capability	Description	Functions Supported
		KeyGen
		BTKeyKeyGen
		Encrypt
		Decrypt
		Bootstrap
	FHE Scheme for	EvalNOT
		EvalBinGate(OR)
FHEW	Arbitrary Boolean Circuits	EvalBinGate(AND)
		EvalBinGate(NOR)
		EvalBinGate(NAND)
		EvalBinGate(XOR)
		EvalBinGate(NXOR)
		EvalBinGate(XOR_FAST)
		EvalBinGate(NXOR_FAST)

Table 6: PALISADE Implemented Capabilities Matrix

Function/Scheme	CKKS	\mathbf{StSt}	BGV*	BFV^*	Null
ENCRYPTION	Y	Y	Y	Y	Y
PRE	Y	Up to 2 hops	Y	Y	Y
SHE	Y	Up to 2 levels	Y	Y	Y
LeveledSHE	Y		Y		Y
Multiparty	Y	Limited	Y	Y	Y

Table 7: Other PALISADE Capabilities and Functions

Capability	Description	Functions Supported	Also Enabled
		Setup	
		KeyGen	
CP-ABE	Ciphertext-Policy	KeyGenOfflinePhase	
CP-ADE	Attribute-Based Encryption	KeyGenOnlinePhase	
		Encrypt	
		Decrypt	
	Digital Signature	KeyGen	
		Sign	
GPV Signature		SignOfflinePhase	
		SignOnlinePhase	
		Verify	
		Setup	
	Identity-Based Encryption	KeyGen	
CDV IDE		KeyGenOfflinePhase	
GPV IBE		KeyGenOnlinePhase	
		Encrypt	
		Decrypt	

After the selection of the scheme, a user can then select how to represent polynomials, among the following polynomial types:

- Poly, which corresponds to representing polynomial coefficients in a multiprecision integer format.
- DCRTPoly, which corresponds to representing polynomial coefficients in a Residue Number System (RNS), a.k.a. Chinese Remainder Theorem (CRT), format using single-precision integers.
- NativePoly, which corresponds to representing polynomial coefficients in a single-precision format (only works up to the word size of 60 bits).

We generally recommend using the DCRTPoly representation of polynomials for performance on commodity computing environments. We include the multiprecision polynomial representation Poly primarily for advanced users and implementers of new schemes who wish to do an initial implementation using the simpler, less efficient Poly representation.

Similar to the polynomial representations, PALISADE also supports multiple big integer math back-ends. The user selects which of the various math back-ends are included at build or compile time ². Currently supported multi-precision math back-ends include:

- Multi-precision with fixed bitwidth sizing (MATHBACKEND 2) supporting bit widths up to 3500 by default (this limit can be changed in a header file). This is the default back-end.
- Multi-precision with dynamic bitwidth sizing (MATHBACKEND 4). This back-end is slightly slower than MATHBACKEND 2, but allows for extremely large integers.
- \bullet NTL and GMP based multi-precision with variable sizing and optimization for various platforms (MATHBACKEND 6) 3

Note the numbering of back-ends is due to historical reasons, as various back-ends have been deprecated over time.

Native data types are always available (and used for NativePoly and single-precision integers in DCRTPoly), and we currently support native 64-bit and 128-bit word sizes. This limitation may be lifted in future releases, allowing PALISADE to be used on 32-bit architectures.

 $^{^2}$ Math back-end selection is controlled at build setup time by adding a cmake flag, e.g., -DMATHBACKEND=4, or at compile time by editing src/core/lib/math/backend.h.

³We include the minimum required version of the GMP and NTL distribution with our release.

6 PALISADE Directory Structure

The directory structure of the PALISADE source code is shown in Listing 1 and Table 8.

```
|- benchmark
|- build
|- doc
|- src
    |- core
    |- include
               -- PALISADE core header files
 |- math
       |- lattice
       |- encoding
 |- util
| |- lib
            -- PALISADE core source files
|- math
      |- lattice
      |- encoding
| | |- util
| |- abe
| |- include -- Attribute-based encryption crypto layer header files
 |- pke
               -- Homomorphic scheme header files
 |- include
       |- scheme
          |- bfv -- Original BFV (integ. arithm. - slower than RNS variants)
         |- bfvrns -- HPS RNS variant of BFV scheme (integer arithmetic)
         |- bfvrnsb -- BEHZ RNS variant of BFV scheme (integer arithmetic)
         |- bgv -- BGV scheme (integer arithmetic)
         |- bgvrns -- full RNS variant of BGV scheme (integer arithmetic)
         |- ckks -- CKKS scheme (real-number arithmetic)
         |- null -- NULL scheme (integer arithemtic)
         |- stst -- Stehle-Steinfeld scheme (limited HE operations)
            -- Public key encryption crypto layer source files
    |- lib
       |- scheme
         |- bfv -- Original BFV (integ. arithm. - slower than RNS variants)
         |- bfvrns -- HPS RNS variant of BFV scheme (integer arithmetic)
         |- bfvrnsb -- BEHZ RNS variant of BFV scheme (integer arithmetic)
         |- bgv -- BGV scheme (integer arithmetic)
         |- bgvrns -- full RNS variant of BGV scheme (integer arithmetic)
         |- ckks -- CKKS scheme (real-number arithmetic)
         |- null -- NULL scheme (integer arithemtic)
          |- stst -- Stehle-Steinfeld scheme (limited HE operations)
 |- signature
    |- include
               -- Signature crypto layer header files
    -- Test software scripts
|- test
|- third-party -- External third-party software
```

Listing 1: Directory structure for PALISADE source code

All of the src/core, src/pke. src/binfhe, src/abe and src/signature contain subdirectories for header files (include), library source files (lib), unit tests (unittest) as well as

Table 8: PALISADE Library File Structure

Directory	Description
benchmark	Code for benchmarking PALISADE library components.
build	Binaries and build scripts (this folder is created by the user).
doc	Documentation of library components, including doxygen.
src	Library source code.
test	Google unit test code.
third-party	Code provided by an external third party.

subdirectories for main examples (examples) that exercise most common capabilities of PALISADE and additional examples (extras) for less common scenarios.

7 Terminology and Notation

In this section we provide a glossary of terminology that we use in PALISADE.

PALISADE provides a framework for using lattice cryptography.

If a Scheme supports the ENCRYPTION Capability, encrypt and decrypt methods are available for use. The encrypt and decrypt methods are provided as part of the implementation of the ENCRYPTION Capability in the Scheme being used. A Plaintext can be encrypted into a Ciphertext through the use of an encrypt method. A Ciphertext can be used to generate a Plaintext through the use of a decrypt method. The library supports several formats of Plaintext and methods to create a Plaintext for use in PALISADE.

If a Scheme supports the PRE Capability, a re-encrypt method is available.

If a Scheme supports the SHE and/or LeveledSHE Capability, then there is support for homomorphic operations on pairs of Ciphertext as well as mixed-mode operations between a Ciphertext and a Plaintext. These operations are supported by using C++ operator overloading. For example, multiplication of two instances of a Ciphertext, A and B, can be simply written as A \star B.

PALISADE also includes support for several Matrix operations. It is possible to create several Matrix of Plaintext, encrypt them, perform operations on them, and then decrypt back into a Matrix of Plaintext.

7.1 Typing

All PALISADE operations are strongly typed. A Plaintext that is passed to encrypt will create a Ciphertext that is aware of the underlying format of the Plaintext, as well as the particular key that was used to encrypt the Plaintext. The decrypt operation will fail in cases where an improper key is used. A successful decrypt will produce a new Plaintext whose underlying format matches the initial Plaintext that was passed to encrypt. Homomorphic operations between Ciphertexts, and mixed-mode operations between a Ciphertext and a Plaintext will only be permitted for operands with formats and keys that match.

The underlying data inside of PALISADE is an Element in lattice space. Within PALISADE, all Plaintexts are encoded into an Element. Every Ciphertext contains one or more Element objects, and all operations are mathematical operations on these Elements.

There are several formats of Element available: a Poly, which represents the encoded Plaintext as a polynomial; a NativePoly, which uses a polynomial with coefficients with a maximum size of 64 bits (when the native backend is set to use 64-bit integers); and a DCRTPoly, which represents the encoded Plaintext as a stack of decomposed NativePoly polynomials using the Double Chinese Remainder Theorem.

7.2 CryptoContext

A CryptoContext in PALISADE is the class that provides all PALISADE encryption functionality. All objects used in a PALISADE implementation are created by a CryptoContext and can be considered to "belong to" the CryptoContext that they were created with.

Any and all operations on PALISADE objects must be on objects that belong to the same CryptoContext. The high-level use of the CryptoContext to encrypt a Plaintext to generate a Ciphertext is as follows:

- 1. Choose a set of ElementParams to define parameters for the Element to be used.
- 2. Choose a set of EncodingParams to define parameters for encoding.
- 3. Select a Scheme that you wish to use for lattice cryptography.
- 4. Construct a CryptoContext for your selected scheme, ElementParams and EncodingParams, in which all operations shall take place. The construction of a CryptoContext involves selecting parameters for security and performance. There are potentially multiple mechanisms to generate the Scheme parameters needed for this construction.
- 5. Select which Capability are used with the CryptoContext. Note that not every Scheme will support every possible Capability.
- 6. Use CryptoContext methods to create Keys.
- 7. The user may also perform homomorphic operations on Ciphertext and Plaintext objects if that Capability has been enabled and if the Scheme supports the operations.
- 8. Encrypt a Plaintext into a Ciphertext.
- 9. Decrypt a Ciphertext back to a Plaintext.

Each CryptoContext is uniquely identified by its Scheme, Element type, ElementParams and EncodingParams. When we say that an object "belongs to" a CryptoContext, we are actually saying that it is associated with a CryptoContext with a particular Scheme, Element type, ElementParams and EncodingParams.

PALISADE incorporates the standard security tables developed during the Homomorphic Encryption standardization process described at

http://homomorphicencryption.org. Users of the library can construct a CryptoContext by specifying the parameter sets defined in the standard.

It follows that if one creates a CryptoContext on two different computers, each with the same Scheme, Element type, ElementParams and EncodingParams, then those two CryptoContexts are the same, and objects created on one machine can be transferred to and used on the other machine.

7.3 BinFHEContext

A Binfhecontext is the equivalent of a CryptoContext for Boolean-circuit FHE. All operations are performed using an instance of the Binfhecontext class. The high-level use of an Binfhecontext to perform FHE operations is as follows:

- 1. Choose a predefined configuration to instantiate the context. The options are:
 - TOY (Toy parameter set for unit tests and debugging),
 - MEDIUM (≥ 100 bits of security for both classical and quantum computer attacks),
 - STD128 (HE standard set with more than 128 bits of security w.r.t. classical computer attacks),
 - STD192 (HE standard set with more than 192 bits of security w.r.t. classical computer attacks),
 - STD256 (HE standard set with more than 256 bits of security w.r.t. classical computer attacks),
 - STD128Q (HE standard set with more than 128 bits of security w.r.t. quantum computer attacks),
 - STD192Q (HE standard set with more than 192 bits of security w.r.t. quantum computer attacks),
 - STD256Q (HE standard set with more than 256 bits of security w.r.t. quantum computer attacks).
- 2. Generate a secret key (an instance of LWEPrivateKey).
- 3. Generate the bootstrapping keys, including a refreshing and switching keys. The bootstrapping keys are stored inside the context.
- 4. Encrypt a plaintext (LWEPlaintext) to form a ciphertext (an instance of LWECiphertext).
- 5. Perform any of the following operations as many times as needed: NOT (no boostrapping), OR, AND, NAND, NOR, XOR, or XNOR. The last six require bootstrapping and take the same time to execute.
- 6. Decrypt the result using the secret key.

7.4 ABEContext

An ABEContext is the equivalent of a CryptoContext for attribute-based and identity-based encryption functionality. All CP-ABE and GPV IBE related operations are done using an ABEContext. The high-level use of an ABEContext to encrypt a Plaintext is as follows:

- 1. Choose a set of parameters to create appropriate set of ElementParams for the Element to be used.
- 2. Select a Scheme to use (GPV IBE or CP-ABE).
- 3. Construct a ABEContext for your selected scheme and parameters. Note that the steps up to this point are similar to CryptoContext, with the exception of EncodingParams. This is due to the fact that ABEContext at its current implementation only supports the plaintext modulus of 2 for encoding, hence it is done internally.
- 4. Create an AccessPolicy for the parties that will be able to decrypt.
- 5. Use ABEContext methods to create Keys.
- 6. Encrypt a Plaintext under an AccessPolicy into a Ciphertext.
- 7. Decrypt a Ciphertext back to a Plaintext.

The standard security tables developed during the Homomorphic Encryption standardization process described at http://homomorphicencryption.org also apply to ABEContext.

It is also worth to mention that ABEContext does not support DCRTPoly at its current state. However, for most cases NativePoly is enough. For the time being, ABE does not have homomorphic operations within ciphertexts defined. Because of this the ciphertext modulus required for the security/correctness of regular encryption functionality is below 64 bits.

7.5 SignatureContext

A SignatureContext is the equivalent of a CryptoContext for digital signature schemes. All GPV signature scheme-related operations are done using a SignatureContext. The high-level use of a SignatureContext to sign a Plaintext is as follows:

- 1. Choose a set of parameters to create appropriate set of ElementParams for the Element to be used.
- 2. Select a Scheme to use (GPV only for the time being).
- 3. Construct a SignatureContext for your selected scheme and parameters. Note that the steps up to this point are similar to CryptoContext, with the exception of EncodingParams. This is due to the fact that the encoding is handled internally.
- 4. Use SignatureContext methods to create Keys.
- 5. Sign a Plaintext into a Signature.
- 6. Verify a Signature with a Plaintext.

It is also worth to mention that just like ABEContext, SignatureContext does not support DCRTPoly at its current state and NativePoly is enough for all cases. Homomorphic

operations are not defined for signatures, which means there is no need for moduli larger than 64 bits.

7.6 Plaintext

A Plaintext is used in PALISADE to represent something that has not been encrypted. It is actually the base class for each of the possible plaintext encodings that are supported in PALISADE:

- ScalarEncoding
- IntegerEncoding
- FractionalEncoding
- PackedEncoding
- CKKSPackedEncoding
- CoefPackedEncoding
- StringEncoding

A Plaintext is created by invoking the appropriate CryptoContext method, passing it the unencrypted information as a parameter.

Once created, a Plaintext can be encrypted into a Ciphertext using the CryptoContext Encrypt routine.

A Plaintext can also be used as a parameter to several of the CryptoContext homomorphic operations.

When a Ciphertext is decrypted, the decryption method creates a new Plaintext to contain the decryption.

The Plaintext has several methods that provide access to the information in the Plaintext, as shown in listing 2:

```
const std::string& GetStringValue();
const int64_t GetIntegerValue();
const int64_t GetScalarValue();
const vector<int64_t>& GetCoefPackedValue();
const vector<uint64_t>& GetPackedValue();
const vector<complex<double>>& GetCKKSPackedValue();
```

Listing 2: Values in Plaintext

Note that the only one of these Plaintext methods that will return a value is the one that corresponds to the actual type of the Plaintext. For example, GetStringValue() will return a std::string if the Plaintext is actually a StringEncoding, and will throw an exception otherwise.

While ABEContext also uses Plaintext for unencrypted information, SignatureContext uses its own plaintext definition.

7.7 Ciphertext

A Ciphertext is used in PALISADE to represent encrypted information. A Ciphertext is created from a Plaintext by an encrypt method, and is converted back to a Plaintext by a decrypt method. The encrypt and decrypt methods also require Keys that have been generated by the CryptoContext.

Homomorphic operations between pairs of Ciphertext, or between a Ciphertext and a Plaintext, are supported, provided that the encodings of the operands match, and provided that those encodings support homomorphic operations (for example, homomorphic operations are not supported for string encodings, and will be rejected if attempted).

The CP-ABE/GPV IBE schemes utilizing ABEContext have their own unique classes for ciphertext implementations, which do not have homomorphic operations supported at this time.

7.8 Access Policy

An AccessPolicy is a rule/set of rules dictating the decrypting party of the communication. User holding the appropriate rights can generate the relevant Keys for decryption and decrypt the information encrypted under an AccessPolicy.

In the context of GPV IBE, AccessPolicy refers to the unique user identifier.

In the context of CP-ABE, AccessPolicy can refer to both attributes defined for the access policy as well as user's own attribute set.

7.9 Signature

A Signature is used in PALISADE for authentication. A Signature is created from a Plaintext by a sign method, and used in conjunction with the Plaintext for verification. The sign and verify methods also require Keys that have been generated by the SignatureContext.

7.10 Keys

Many PALISADE functions make use of Keys. These objects are created using CryptoContext, ABEContext or SignatureContext methods.

Encryption and decryption functionality requires a public key/private key pair. The CryptoContext KeyGen method generates this key pair and returns it to the caller.

CP-ABE and GPV IBE operations require a master public key/private key pair for the encryption and derivation of personal secret keys. This is done using Setup method of ABEContext. For decryption, a secret key corresponding to an access policy/user is required, which is done using the ABEContext KeyGen method.

Signing and verification operations for digital signature schemes require a sign(private)/verify(public) key pair. This pair can be generated using the SignatureContext KeyGen method.

Re-Encryption requires an Evaluation key. This key is generated using the ReKeyGen method.

Certain homomorphic operations may require the application of evaluation keys to complete the operation. The CryptoContext EvalMultKeyGen and EvalAddKeyGen methods are used to generate the requisite keys needed for the EvalMult and EvalAdd operations, respectively.

7.11 Capability

A Capability refers to sets of CryptoContext methods that must be enabled before they can be used. A Capability must be enabled by calling the CryptoContext Enable method and passing it the name of the Capability as an argument. Multiple values for Capability can be or-ed together and passed as a single argument to Enable.

Section 5 discusses in the detail the available choices for Capability, and the functionality enabled when a particular Capability is Enabled.

7.12 Scheme

A Scheme (the full class name is LPPublicKeyEncryptionScheme) contains the algorithms used for key generation, encryption/decryption, and homomorphic operations.

Table 6 outlines the different supported schemes in PALISADE.

In order to use a particular Scheme, its configuration parameters must be specified. The particular configuration parameters for each scheme are stored in a CryptoParameters class (the full class name is LPCryptoParameters) that is particular for that scheme. The classes for CryptoParameters for each scheme are unique, but they all share several characteristics:

1. Each CryptoParameters class has a constructor that allows for the specification of all configuration parameters.

- 2. The CryptoParameters may have a ParamsGen feature that generates a full set of configuration parameters from a small specification as to how many homomorphic operations will be performed.
- 3. The CryptoParameters class is part of the CryptoContext

ABEContext and SignatureContext also use their equivalent parameter classes like CryptoParameters.

7.13 Element

The math layer performs operations on different kinds of Element. This is a representation of a vector in lattice space.

7.13.1 Poly

A Poly is a vector of polynomial coefficients. The coefficients are whatever the BigInteger type is for the selected math back-end, and the vector is simply a vector of these BigInteger, and an associated modulus. All operations on a Poly are done modulo this modulus.

7.13.2 NativePoly

A NativePoly is a vector of polynomial coefficients where each of the coefficients is of type 64-bit unsigned integer. The NativePoly also has a modulus of at most 64 bits (though our math implementations are most efficient for moduli of 60 bits or less). Again, all operations are done modulo the modulus.

7.13.3 DCRTPoly

A DCRTPoly implements a large Poly decomposed via residue arithmetic into a tower (set) of NativePoly elements.

7.14 ElementParams

An ElementParams is a container for the configuration parameters of whatever Element is being used. The configuration parameters include the ring dimension, cyclotomic order, and primitive root of unity.

7.15 EncodingParams

An EncodingParams is a container for all of the parameters needed to encode a Plaintext. In most cases, this consists solely of a plaintext modulus; however, some encodings require more detailed parameters.

7.16 Matrix

PALISADE supports general operations Matrix objects with elements of the types described above in this section, as well as operations on these matrices. A user can create a matrix of Plaintext, encrypt it into a matrix of Ciphertext, and perform operations on matrices.

In addition to homomorphic matrix multiplication, higher level statistical operations such as inner product and linear regression are available. Some operations result in a matrix of RationalCiphertext, where each entry in the matrix is a rational number such that the numerator and denominator of the entry is a Ciphertext. For matrices of RationalCiphertext, separate decryption of the numerators and denominators of each entry are provided.

8 Sample Implementations: PKE Module

8.1 Creating a CryptoContext

All PALISADE operations in the PKE module are associated with a CryptoContext; therefore, the first step in using PALISADE is to acquire a CryptoContext. A CryptoContext can be created in a number of different ways through the use of static CryptoContextFactory methods. The factory methods return a shared_ptr to a CryptoContext.

It is useful to note that PALISADE keeps track all of the CryptoContexts that have been created, and will not create duplicate contexts. If a user requests that the factory create a context that already exists, the factory simply returns a shared_ptr to the existing context rather than creating a duplicate of that existing context.

A CryptoContext is uniquely identified by the parameters for the underlying lattice layer element that is to be used, the encoding parameters to be used with Plaintext, and the Scheme (and any associated configuration parameters for the Scheme).

The underlying lattice layer element is either a Poly, a NativePoly, or a DCRTPoly. These type names are used as template parameters with the CryptoContext and its methods. The lattice layer elements share a set of element parameters that are given to the CryptoContextFactory methods.

Encoding parameters may be a simple Plaintext modulus, or they may be a broader set of EncodingParms that are used. Encoding parameters are passed to the CryptoContextFactory methods.

Different Schemes have wildly different configuration parameters, and so the Scheme is selected by calling a CryptoContextFactory method for the desired Scheme.

Each Scheme actually has several factory methods:

- A method that accepts values for all configuration parameters for the scheme.
- A method that accepts some values for configuration parameters, and that invokes a scheme-specific parameter generation operation.

There are two other mechanisms available for creating a CryptoContext:

- Deserialize a previously serialized CryptoContext.
- Construct a CryptoContext from one of the set of predefined scheme parameters.

Once a CryptoContext has been created, the appropriate capabilities should be enabled. Once this is complete, the CryptoContext is ready for use.

Below are some code samples for creating contexts. Listing 3 demonstrates creating a CryptoContext by specifying all of the scheme's parameters.

```
/// Example showing creating a BGV CryptoContext
/// By specifying all Scheme parameters
/// Element is Poly with non power-of-two cyclotomics
usint m = 22;
PlaintextModulus p = 2333;
BigInteger ptm(p);
BigInteger ctm("955263939794561");
BigInteger srr("941018665059848");
BigInteger bigmod("80899135611688102162227204937217");
BigInteger bigroot ("77936753846653065954043047918387");
auto cycloPoly = GetCyclotomicPolynomial<BigVector>(m, ctm);
ChineseRemainderTransformArb<BigInteger, BigVector>::SetCylotomicPolynomial(
   cycloPoly, ctm);
float stdDev = 3.19;
usint bSize = 8:
shared_ptr<Poly::Params> params(new ILParams(m, ctm, srr, bigmod, bigroot));
EncodingParams ep(new EncodingParamsImpl(p, PackedEncoding::
   GetAutomorphismGenerator(p), bSize));
CryptoContext<Poly> cc = CryptoContextFactory<Poly>::genCryptoContextLTV(
   params, ep, bSize, stdDev);
cc->Enable(ENCRYPTION);
cc->Enable(SHE);
```

Listing 3: Creating a CryptoContext with parameters

Listing 4 demonstrates the use of the factory method that uses parameter generation. Listing 5 shows the use of preconfigured parameter sets.

Listing 4: Creating a CryptoContext with parameter generation

Listing 5: Creating a preconfigured CryptoContext

Listing 6 shows the use of parameter sets defined by the Homomorphic Encryption standardization process, as defined in http://homomorphicencryption.org.

```
/// Example showing CryptoContext generation
// using standard tables from the homomorphic encryption standardization
   project
PlaintextModulus ptm = 536903681;
double sigma = 3.2;
SecurityLevel securityLevel = HEStd 128 classic;
// support 7 multiplies (ciel(log2(7)))
usint nMults = 3;
// generate keys for s^2 and s^3
usint maxDepth = 3;
CryptoContext<DCRTPoly> cryptoContext =
     CryptoContextFactory<DCRTPoly>::genCryptoContextBFVrns(
          ptm, securityLevel, sigma, 0, nMults, 0, OPTIMIZED, maxDepth);
if( !crvptoContext ) {
        cout << "Error creating CryptoContext" << endl;</pre>
        return 0;
cryptoContext->Enable (ENCRYPTION);
```

Listing 6: Creating a CryptoContext using standard parameters

Listing 7 shows creation from a serialization.

Listing 7: Creating a CryptoContext from a serialization

8.2 Creating A Plaintext

PALISADE users are able to convert integers, vectors of integers, vectors of complex numbers, and strings into Plaintext objects.

Plaintext objects can be used as input to Encryption, can be used as part of homomorphic operations, and are produced as a result of decryption.

All Plaintexts are created by static factory methods within the CryptoContext. Each style of Plaintext encoding has its own factory method.

The Plaintexts are all type safe. A Ciphertext knows the encoding used by the original Plaintext that it came from. Decryption creates a Plaintext with the proper encoding. All homomorphic operations check types before performing the operation, and will fail if either the encodings do not match, or if a particular encoding does not support homomorphic operations.

8.2.0.1 Scalar Encoding

ScalarEncoding is used to encode a single integer by simply copying the integer into the polynomial starting at index 0 and zero-filling remaining unused indices of the polynomial. Listing 8 shows an example of creating a Scalar Plaintext.

```
int64_t val = 12;
Plaintext sPtx = ctx->MakeScalarPlaintext(val);
Plaintext sPtx2 = ctx->MakeScalarPlaintext(-val);
```

Listing 8: Creating a Scalar Plaintext

8.2.0.2 IntegerEncoding

IntegerEncoding is used to encode a single unsigned integer into a polynomial such that each bit (0 or 1) in the integer is copied into its corresponding slot in the polynomial. For example, the integer 14, which is binary 1110, is encoded by emplacing 1, 1, 1 and 0 into the first four positions of the polynomial. This is shown in listing 9.

```
Plaintext intPtx = ctx->MakeIntegerPlaintext(14);
```

Listing 9: Creating an Integer Plaintext

Important Note: IntegerEncoding encodes each bit of the integer into a separate coefficient of the polynomial. This implies that the ring dimension (degree of polynomial) should be large enough to store all bits, especially in scenarios where each homomorphic multiplication doubles the number of polynomial coefficients with each multiplication. This is typically a non-issue for secure schemes/settings (as the ring dimension is already large enough) but can be an issue for the Null scheme, where the cyclotomic order is provided as an input argument.

8.2.0.3 FractionalEncoding

FractionalEncoding is a generalization of IntegerEncoding that can encode both integers and fractions. Currently it is limited in its functionaly and is only used to add support for right shifting (moving least significant bits to the fractional part). Examples of FractionalEncoding for encoding an integer 3 and a fraction 1/8 are shown in listing 10.

```
Plaintext intPtx = ctx->MakeFractionalPlaintext(3);
Plaintext intPtx = ctx->MakeFractionalPlaintext(0,3);
```

Listing 10: Creating a Fractional Plaintext

Important Note: FractionalEncoding encodes each bit of the integer into a separate coefficient of the polynomial. This implies that the ring dimension (degree of polynomial) should be large enough to store all bits, especially in scenarios where each homomorphic multiplication doubles the number of polynomial coefficients with each multiplication. This is typically a non-issue for secure schemes/settings (as the ring dimension is already large enough) but can be an issue for the Null scheme, where the cyclotomic order is provided as an input argument.

8.2.0.4 CoefPackedEncoding

CoefPackedEncoding is used to encode a vector of integers, or an initializer list of integers, into a polynomial such that each integer is emplaced into a coefficient of the polynomial. This is illustrated in listing 11.

```
std::vector<int64_t> inputs( { 2, 3, 5, 7} );

// construction from vector
Plaintext c1 = ctx->MakeCoefPackedPlaintext(inputs);

// construction from initializer list
Plaintext c2 = ctx->MakeCoefPackedPlaintext({-6,1,4,8});
```

Listing 11: Creating a CoefPackedEncoding Plaintext

8.2.0.5 PackedEncoding

PackedEncoding is an implementation of an efficient encoder packing multiple integers into a single plaintext polynomial (single ciphertext) that enables SIMD (Single Instruction, Mutiple Data) operations on these integers. Currently PALISADE supports addition, multiplication, and rotation capabilities for packed ciphertexts. The cyclotomic order m has to divide p-1, where p is the plaintext modulus. This is shown in listing 12.

```
std::vector<int64_t> val( {37, 22, 18, 4, 3, 2, 1, 9} );
Plaintext packedPtx = ctx->MakePackedPlaintext(val);
```

Listing 12: Creating a PackedEncoding Plaintext

8.2.0.6 CKKSPackedEncoding

CKKSPackedEncoding is an implementation of an efficient encoder packing multiple complex/real numbers into a single plaintext polynomial (single ciphertext) that enables SIMD (Single Instruction, Mutiple Data) operations on these complex/real numbers. Currently PALISADE supports addition, multiplication, and rotation capabilities for packed ciphertexts. An exampple is shown in listing 13.

Listing 13: Creating a CKKSPackedEncoding Plaintext

8.2.0.7 StringEncoding

StringEncoding is used to encode a string into a polynomial. For this encoding, each 8-bit character in the input is encoded directly into a coefficient of the polynomial. This encoding is constrained to only use 256 as a plaintext modulus. Listing 14 shows the use of this encoding.

Future implementations that support other character encodings, such as Unicode, are possible but are not currently supported.

Homomorphic operations will NOT work with this encoding.

```
string s("Here is my string!");
Plaintext stringPtx = ctx->MakeStringPlaintext(s);
```

Listing 14: Creating a String Plaintext

8.3 Encryption

In order to encrypt a Plaintext into a Ciphertext, create a CryptoContext and a Plaintext as illustrated above.

The code in listing 15 illustrates this. It assumes that you have created a CryptoContext named "cc" and have created a Plaintext named ptxt within cc.

Observe that the code uses the KeyGen method to create a key pair, and uses the publicKey portion of that key pair for the encryption. The encryption will fail if the keys were generated in a different CryptoContext than cc.

Listing 15: Encrypting

8.4 Decryption

In order to decrypt a Ciphertext into a Plaintext, a CryptoContext, Ciphertext and KeyPair must exist. The keys and the Ciphertext must have been created within the CryptoContext. An example is shown in listing 16.

Listing 16: Decrypting

8.5 Re-Encryption

Re-Encryption involves converting a Ciphertext that is decryptable with key "A" into a Ciphertext that is decryptable with key "B" by creating a re-encryption key and using it to re-encrypt the ciphertext.

The code sample in listing 17 illustrates this capability. It assumes a CryptoContext cc, an initial keypair A, and a Ciphertext cipher that has been created using A. We show the generation of key pair B, the generation of the re-encryption key, the re-encryption operation, and the subsequent decryption of the re-encrypted Ciphertext with B's secret key.

Two variants of re-encryptions are shown. The first one corresponds to the Chosen Plaintext Attack (CPA) model. The second variant corresponds to the model secure under Honest Re-encryption Attacks (HRA) [Coh17]. We recommend the HRA model for practical use.

Note that in order to use Re-Encryption, the PRE capability must be enabled for the CryptoContext.

```
// Perform Key Generation Operation
// Initialize Key Pair Containers
LPKeyPair<Poly> B = cc->KeyGen();
if( !B.good() ) {
   cout << "Key generation failed!" << endl;</pre>
   exit(1);
//Perform Re-encryption key generation operation.
LPEvalKey<Poly> rekey =
   cc->ReKeyGen(B.publicKey, A.secretKey);
// Re-Encryption
// CPA-secure variant
auto re_cipher = cc->ReEncrypt(rekey, cipher);
//Decryption of Ciphertext
// Re-Encryption with Ciphertext Re-randomization
// HRA-secure variant
auto re_cipherHRA = cc->ReEncrypt(rekey, cipher, A.publicKey);
//Decryption of Ciphertext
Plaintext ptxtHRA;
cc->Decrypt (B.secretKey, re_cipherHRA, &ptxtHRA);
```

Listing 17: Re-Encrypting

8.6 Serialization and Description

When used in client/server and other distributed application settings, PALISADE objects need to be saved to persistent storage or streams, and then loaded back to instantiate the PALISADE objects in memory. PALISADE provides a serialization capability based on the industry-standard C++ **cereal** library (see https://github.com/USCiLab/cereal). The objects can be serialized either as binary objects (fastest option) or as JSON files (in cross-platform scenarios).

PALISADE objects can be serialized to streams (**Serialize/Deserialize** methods) or files (**SerializeToFile/DeserializeFromFile** methods).

Many of the objects to be serialized are associated with a particular CryptoContext. In order for such objects to be correctly serialized and deserialized, the serialization saves the CryptoContext that the object belongs to as part of the serialization, and the deserialization makes sure that the CryptoContext for the object being deserialized matches the CryptoContext in the serialization.

A simple of example of serialization to files is provided in src/pke/examples/simple-integers-serial.cpp. A simple example of serialization to streams is provided in pke/u-nittest/UnitTestSer.h.

8.7 Homomorphic Addition of Ciphertexts

Homomorphic addition of two **Ciphertext** is performed by invoking the EvalAdd method of the **CryptoContext**. Both of the operands to the EvalAdd must have been created in the same **CryptoContext**, encrypted with the same **Key**, and encoded in the same way for this operation to work.

The code sample in listing 18 illustrates how to encode two vectors of integers into **Plaintext**, encrypt them into **Ciphertext**, perform homomorphic addition, and decrypt the result back into a **Plaintext**.

This code assumes a **CryptoContext** named cc and a keypair named kp.

```
// Encode source data
std::vector<int64_t> v1 = \{3,2,1,3,2,1,0,0,0,0,0,0,0\};
Plaintext p1 = cc->MakeCoefPackedPlaintext(v1);
Plaintext p2 = cc->MakeCoefPackedPlaintext(v2);
Plaintext p3 = cc->MakeCoefPackedPlaintext(v3);
// Encryption
auto c1 = cc->Encrypt(kp.publicKey, p1);
auto c2 = cc->Encrypt(kp.publicKey, p2);
auto c3 = cc->Encrypt(kp.publicKey, p3);
// EvalAdd Operation
auto c12 = cc\rightarrowEvalAdd(c1,c2);
auto csum = cc->EvalAdd(c12,c3);
//Decryption after Accumulation Operation
Plaintext plaintextAdd;
cc->Decrypt(kp.secretKey, csum, &plaintextAdd);
plaintextAdd->SetLength(p1->GetLength());
cout << "Original Plaintext:" << endl;</pre>
cout << p1 << endl;</pre>
cout << p2 << endl;
cout << p3 << endl;
cout << "Resulting Added Plaintext:" << endl;</pre>
cout << plaintextAdd << endl;</pre>
```

Listing 18: Adding Ciphertexts

8.8 Homomorphic Multiplication of Ciphertexts

Homomorphic multiplication of two **Ciphertext** is performed by invoking the EvalMult method of the **CryptoContext**. Both of the operands to the EvalMult must have been created in the same **CryptoContext**, encrypted with the same **Key**, and encoded in the same way for this operation to work.

The code sample in listing 19 illustrates how to encode two vectors of integers into **Plaintext**, encrypt them into **Ciphertext**, perform homomorphic multiplication, and decrypt the result back into a **Plaintext**.

This code assumes a **CryptoContext** named cc and a keypair named kp.

Note the creation of an EvalMult key using EvalMultKeyGen at the beginning of the sample.

```
cc->EvalMultKeyGen(kp.secretKey);
// Encode source data
std::vector<int64_t> v1 = \{3, 2, 1, 3, 2, 1, 0, 0, 0, 0, 0, 0\};
Plaintext p1 = cc->MakeCoefPackedPlaintext(v1);
Plaintext p2 = cc->MakeCoefPackedPlaintext(v2);
Plaintext p3 = cc->MakeCoefPackedPlaintext(v3);
// Encryption
auto c1 = cc->Encrypt(kp.publicKey, p1);
auto c2 = cc->Encrypt(kp.publicKey, p2);
auto c3 = cc->Encrypt(kp.publicKey, p2);
// EvalMult Operation
auto m12 = cc->EvalMult(c1,c2);
auto cprod = cc->EvalMult(m12,c3);
//Decryption after Multiplication Operation
Plaintext plaintextMul;
cc->Decrypt(kp.secretKey, cprod, &plaintextMul);
plaintextMul->SetLength(p1->GetLength());
cout << "Original Plaintext:" << endl;</pre>
cout << p1 << endl;
cout << p2 << endl;
cout << p3 << endl;
cout << "Resulting Plaintext:" << endl;</pre>
cout << plaintextMul << endl;</pre>
```

Listing 19: Multiplying Ciphertexts

9 Sample Implementations: FHE

PALISADE implements several fully homomorphic encryption schemes. Different schemes work with different input data types, and this is why this Section is organized based on three data types: integer numbers, real numbers, and binary bits (i.e., Boolean circuits). Each subsection describes which cryptographic schemes are appropriate for the respective data type, and how to start using the schemes in PALISADE.

9.1 Integer arithmetic

PALISADE provides two schemes that work with integer numbers, namely BFV and BGV. PALISADE includes RNS variants for both schemes. Here, we discuss BFV as an example.

In order to use BFV, users need to create a **CryptoContext** through the static factory method called **genCryptoContextBFV**. Among other arguments, this factory method takes the plaintext modulus, the security level, and the additive, multiplicative, and keyswitching depths of the computation. The plaintext modulus determines an upper bound for the integer inputs in the BFV scheme. The security level is a parameter whose possible values correspond to 128-, 192-, or 256-bit security; PALISADE picks the appropriate underlying security parameters by consulting the relevant tables of the current FHE standard. Depending on the computation the user wants to carry out, she can set either the additive, multiplicative, or key-switching depth, and set all others to 0. Users who want to start using BFV can try running the examples at the following locations:

- 1. src/pke/examples/simple-integers.cpp simple example showing how to instantiate the BFV scheme, generate keys, encrypt the data, perform homomorphic operations, and decrypt the result.
- 2. src/pke/examples/simple-integers-serial.cpp shows how to serialize/deserialize objects when using the BFV scheme.

9.2 Real-number arithmetic

PALISADE supports real- and complex-number arithmetic through the use of the CKKS scheme. CKKS is implemented in RNS for better performance, so its **CryptoContext** can only be created with **DCRTPoly** as the template argument.

Creating a **CryptoContext** is done by an invocation of the static factory method **gen-CryptoContextCKKS**. Listing 20 shows all different arguments for **genCryptoContextCKKS**.

Listing 20: List of arguments of CKKS context generation method.

The CKKS scheme supports three different key switching algorithms, specifically digit decomposition by Brakerski and Vaikuntanathan (**BV**) [BV14], ciphertext modulus doubling by Gentry, Halevi and Smart (**GHS**) [GHS12], and the hybrid technique (**HYBRID**) [HK19] which combines ideas from the other two. Users can choose which algorithm the CKKS scheme will use by specifying the corresponding argument when creating the **CryptoContext**.

Besides choosing key switching algorithms, users can also choose between three variants called **EXACTRESCALE**, **APPROXRESCALE**, and **APPROXAUTO**. The former is simplest to use because it performs automatic rescaling, and introduces smaller rescaling error to computations of high multiplicative depth. This comes at a moderate performance cost of about 5-30% compared to **APPROXRESCALE**, which requires the user to track the depth of different ciphertexts and call **Rescale()** appropriately. The **APPROXAUTO** mode has the same rescaling approximation error as **APPROXRESCALE** but does the rescaling automatically.

CKKS provides proxy re-encryption and multiparty capabilities, but for PRE only the **BV** key switching algorithm is available. The multiparty capability supports all three key switching techniques.

Because of the way CKKS works, inputs have to be complex double numbers. CKKS also supports SIMD-like operations on packed data. Listing 21 shows how to create CKKS plaintexts. Users can also specify the depth and level of the plaintexts they want to create, by supplying these arguments to MakeCKKSPackedPlaintext().

```
vector<complex<double>> x2 = { 5.0, 4.0, 3.0, 2.0, 1.0, 0.75, 0.5, 0.25 };
Plaintext ptxt1 = cc->MakeCKKSPackedPlaintext(x1);
```

Listing 21: Creating a CKKS plaintext.

The best way to start working with encrypted real numbers is to read the source code and

related comments of the following examples:

- 1. src/pke/examples/simple-real-numbers.cpp Simple example showing how to instantiate the CKKS scheme and perform basic homomorphic operations (addition, subtraction, multiplication, rotation).
- 2. src/pke/examples/advanced-real-numbers.cpp Advanced examples illustrating usage of HYBRID key switching, EXACTRESCALE versus APPROXRESCALE, and hoisted rotations.

9.3 Boolean Circuit Arithmetic

PALISADE provides an implementation of FHEW to evaluate homorphically arbitrary Boolean circuits. Currently, PALISADE supports only the symmetric key encryption. The binary gates that are currently supported are OR, AND, NOR, NAND, XOR, and XNOR. All these gates take the same time, and internally call bootstrapping. The unary gate NOT is also supported; it's very fast (negligibly fast as compared to binary gate operations) and does not require any bootstrapping.

The following code samples are provided in the examples folder of the **binfhe** module:

- 1. **src/binfhe/examples/boolean.cpp** simple example showing how to instantiate a **BinFHEContext**, generate keys, encrypt the data, evaluate a Boolean circuit, and decrypt the result.
- 2. src/binfhe/examples/boolean-serial-json.cpp shows how to serialize a crypto context, ciphertext, and keys in JSON representation. This representation is about one order of magnitude slower than the binary representation, and is typically useful only during debugging (or in special cross-platform scenarios).
- 3. src/binfhe/examples/boolean-serial-binary.cpp shows how to serialize/deserialize a crypto context, ciphertext, and keys in the binary representation. This representation is recommeded for most practical scenarios.

10 Sample Implementations: ABE

10.1 Creating an ABEContext

An **ABEContext** can be created by either choosing the relevant security level or basic parameters related to security level.

```
/// Example showing creating an CP-ABE ABEContext
/// By specifying security level and number of attributes only
/// Element is NativePoly
/// First parameter is for security level, next parameter is the number of attributes

ABEContext<NativePoly> context;
context.GenerateCPABEContext(HEStd_192_classic,6);
```

Listing 22: Creating a ABEContext with Security Level

```
/// Example showing creating a GPV IBE ABEContext
/// By specifying relevant parameters: ring size and base of the gadget matrix
/// Element is NativePoly
/// First parameter is for ring size, second one is for base

ABEContext<NativePoly> context;
context.GenerateIBEContext(1024,64);
```

Listing 23: Creating a ABEContext with Parameters

10.2 Generating Master Keys

```
/// Example showing master key pair generation for GPV IBE ABEContext
/// Element is NativePoly

IBEMasterPublicKey<NativePoly> mpk;
IBEMasterSecretKey<NativePoly> msk;
context.Setup(&mpk,&msk);
```

Listing 24: Generating Master Public Key Pair with ABEContext

10.3 Creating Access Policies

```
/// Example showing user identifier generation for GPV IBE ABEContext
/// Element is NativePoly

IBEUserIdentifier<NativePoly> id(context.GenerateRandomElement());
```

Listing 25: Creating a User Identifier with GPV IBE ABEContext

```
/// Example showing user attribute set/access policy creating for CP-ABE
   ABEContext
/// Element is NativePoly

std::vector<unsigned int> userattributes = {1,0,1,0,1,1};

std::vector <int> accesspolicy = {0,-1,1,0,1,0);

CPABEUserAccess<NativePoly> ua(userattributes);
CPABEAccessPolicy<NativePoly> ap(accesspolicy);
```

Listing 26: Creating a User Attribute Set/Access Policy with CP-ABE ABEContext

10.4 Key Generation

The secret key generated is tailored to the identifier or attribute set of the user

```
/// Example showing secret key generation for GPV IBE ABEContext
/// Element is NativePoly
/// msk is the master secret key, mpk is the master public key, id is the user identifier

IBESecretKey<NativePoly> sk;
context.KeyGen(msk,mpk,id,&sk);
```

Listing 27: Generating a Secret Key with ABEContext

Additionally, it is possible to split the key generation process into two phases: Online and offline. Offline phase consists of creation of perturbation vector which is independent from the user's id or attribute set.

```
/// Example showing the offline phase of secret key generation for GPV IBE
   ABEContext
/// Element is NativePoly
/// msk is the master secret key

PerturbationVector<NativePoly> pv;
context.KeyGenOfflinePhase(msk,pv);
```

Listing 28: Generating a Secret Key with ABEContext (Offline Phase - Perturbation Generation)

The online phase in this scenario consists of actual key generation based on user's id or attribute set without the perturbation subroutine.

```
/// Example showing the online phase of secret key generation for GPV IBE
   ABEContext
/// Element is NativePoly
/// msk is the master secret key, mpk is the master public key, id is the user
   's identifier and pv is the perturbation vector

IBESecretKey<NativePoly> sk;
context.KeyGenOnlinePhase(msk,mpk,id,pv,&sk);
```

Listing 29: Generating a Secret Key with ABEContext (Online Phase - Key Generation)

10.5 Encryption

A **Plaintext** is encrypted with a target party, which means the target user's identifier in GPV IBE or access policy for CP-ABE.

```
/// Example showing encryption for CP-ABE ABECOntext
/// Element is NativePoly
///mpk is the master public key, ap is the access policy

///Creation of plaintext. The format is intentionally used for support
std::vector<int64_t> vectorOfInts = { 1,0,0,1,1,0,1,0, 1, 0 };
Plaintext pt = context.MakeCoefPackedPlaintext(vectorOfInts);

///Actual encryption
CPABECiphertext<NativePoly> ct;
context.Encrypt(mpk,ap,pt,&ct);
```

Listing 30: Encryption with CP-ABE ABEContext

10.6 Decryption

```
/// Example showing decryption for CP-ABE ABEContext
/// Element is NativePoly
///sk is the secret key of the user, ua is the user's attributes, ap is the access policy defined and ct is the ciphertext
Plaintext dt = context.Decrypt(ap,ua,sk,ct);
```

Listing 31: Decryption with CP-ABE ABEContext

```
/// Example showing decryption for GPV IBE ABEContext
/// Element is NativePoly
///sk is the secret key of the user and ct is the ciphertext
Plaintext dt = context.Decrypt(sk,ct);
```

Listing 32: Decryption with GPV IBE ABEContext

11 Sample Implementations: Digital Signature

11.1 Creating a SignatureContext

A **SignatureContext** can be created by either choosing one of the predefined ring sizes or a set of parameters.

```
/// Example showing creating a GPV SignatureContext
/// By specifying some specific parameters
/// First parameter is the ring size, second parameter is the bit width of
   modulus and third one is the base of the gadget matrix
/// Element is NativePoly
SignatureContext<NativePoly> context;
context.GenerateGPVContext(1024,61,64);
```

Listing 33: Creating a SignatureContext with Parameters

11.2 Key Generation

```
/// Example showing creating sign/verification keys with a GPV
    SignatureContext
/// Element is NativePoly

GPVVerificationKey<NativePoly> vk;
GPVSignKey<NativePoly> sk;
context.KeyGen(&sk,&vk);
```

Listing 34: Key Generation with SignatureContext

11.3 Signing

```
/// Example showing signing with a GPV SignatureContext
/// Element is NativePoly
///sk is the signing key and vk is the verification key

///Creation of plaintext
string pt = "This is a test";
GPVPlaintext<NativePoly> plaintext(pt);

///Actual signing
GPVSignature<NativePoly> signature;
context.Sign(plaintext,sk,vk,&signature);
```

Listing 35: Signing with SignatureContext

Additionally, it is possible to split the signing process into two phases: Online and offline. Offline phase consists of creation of perturbation vector which is independent from message to be signed.

```
/// Example showing offline phase of signing with a GPV SignatureContext
/// Element is NativePoly
///sk is the signing key

PerturbationVector<NativePoly> pv;
context.SignOfflinePhase(sk,pv);
```

Listing 36: Signing with SignatureContext (Offline Phase - Perturbation Generation)

The online phase in this scenario consists of actual signing process without the perturbation subroutine.

```
/// Example showing online phase of signing with a GPV SignatureContext
/// Element is NativePoly
///sk is the signing key, vk is the verification key and pv is the
    perturbation vector generated in offline phase

///Creation of plaintext
string pt = "This is a test";
GPVPlaintext<NativePoly> plaintext(pt);

///Actual signing
GPVSignature<NativePoly> signature;
context.SignOnlinePhase(plaintext,sk,vk,pv,&signature);
```

Listing 37: Signing with SignatureContext (Online Phase - Signing)

11.4 Verification

```
/// Example showing verification with a GPV SignatureContext
/// Element is NativePoly
/// vk is the verification key
bool verificationResult = context.Verify(plaintext, signature, vk);
```

Listing 38: Verification with SignatureContext

12 Building and Installing PALISADE

PALISADE git repository includes an up-to-date wiki with detailed instructions on building and running PALISADE on various platforms. We use CMake to build PALISADE, and support Linux, Windows, and macOS. The library requires a C++ compiler that implements the C++11 standard, with support for the OpenMP library. Make, cmake, and autoconf also need to be installed. While not required, it is also recommended that you install and use doxygen.

13 Programming Style

PALISADE coding style is based on the official Google C++ coding style.

Of particular note on the documentation style:

- We use doxygen commenting style on classes, methods and constants.
- We given meaningful variable names to all variables.
- Every reused discrete block of code has its own method.
- Every discrete line or code or discrete group of code lines for each task has its own comment.

With regards to naming conventions:

- Variable names: camelCase.
- Class, struct, typedef, and enum names: CamelCase.
- Class data members: m camelCase.
- Class accessor names: GetProperty() and SetProperty().
- Class method names: CamelCase.
- Global variable names: g_camelCase.
- Constant names and macros: UPPER_CASE_WITH_UNDERSCORES (example: BIT_LENGTH).
- Operator overloading is used for binary operations.

We also follow the additional design principles that:

- cout should never be used for exception handling and should never be used in committed code in the core PALISADE library.
- a set of PALISADE exceptions is defined in utils/exception.h. The library is being migrated to throw only these exceptions.

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