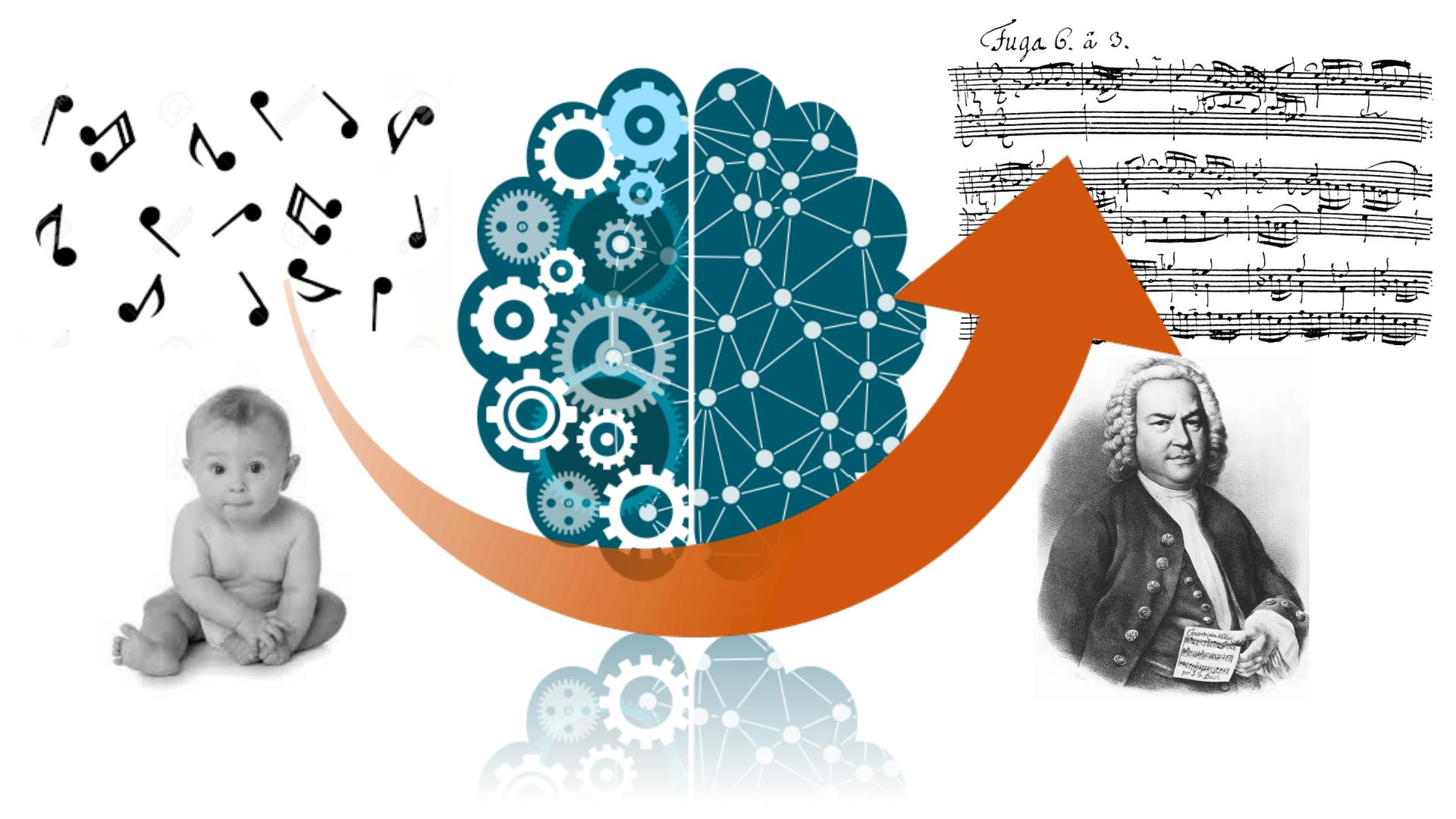


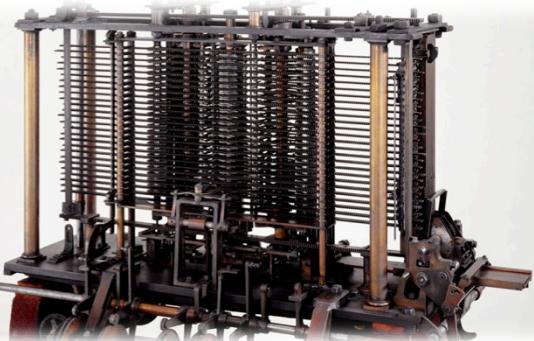
# LEARNING TO GENERATE MUSIC WITH BACHPROP

Magliaso Sommer Akademie | Florian Colombo



# Ada Lovelace | First Programmer

"Supposing, for instance, that the fundamental relations of pitched sounds in the science of harmony and of musical composition were susceptible of such expression and adaptations, the engine might **compose elaborate and scientific pieces of music** of any degree of complexity or extent."



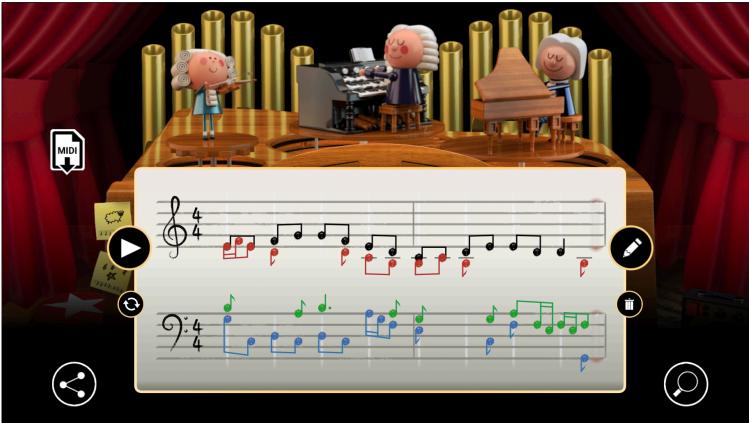
# Deep Generative Models | Images



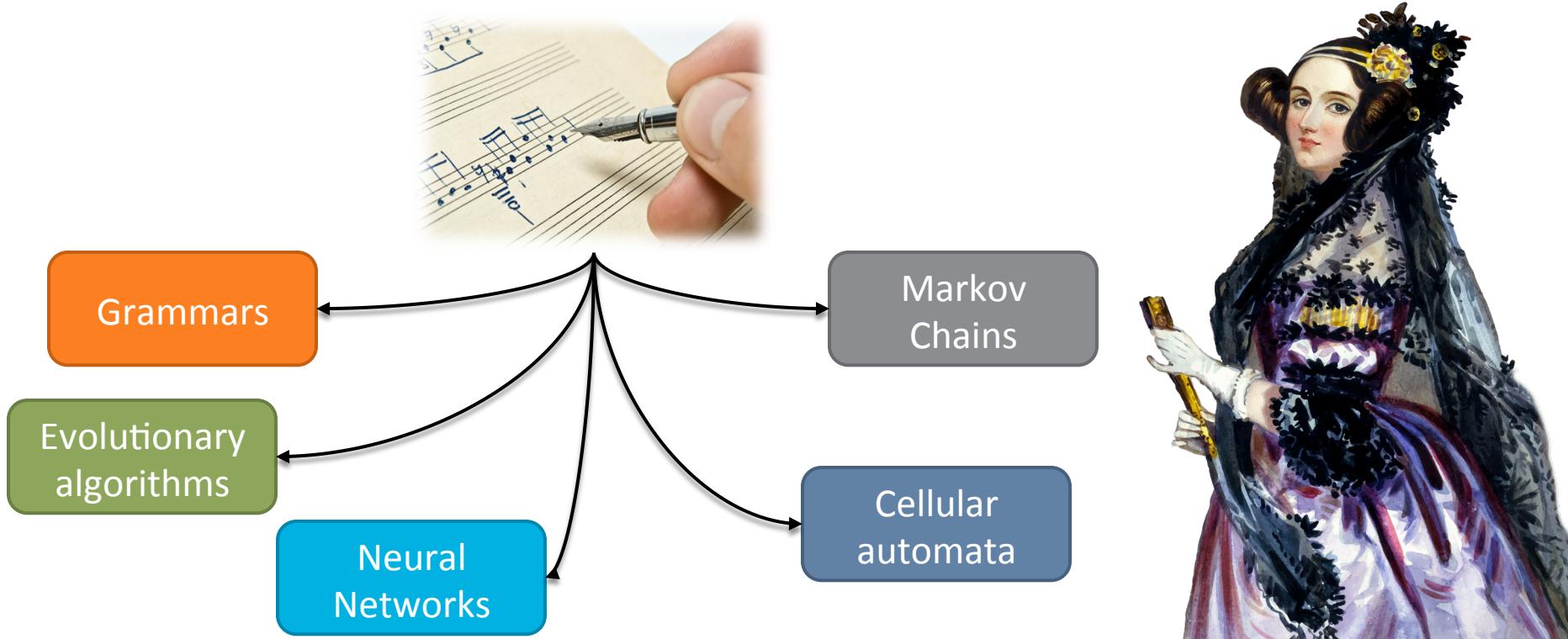
Karras et al. ICLR18



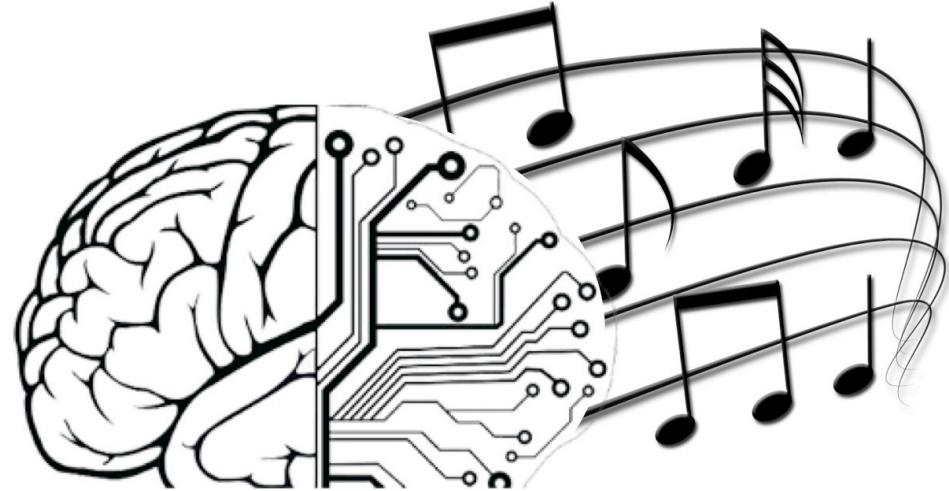
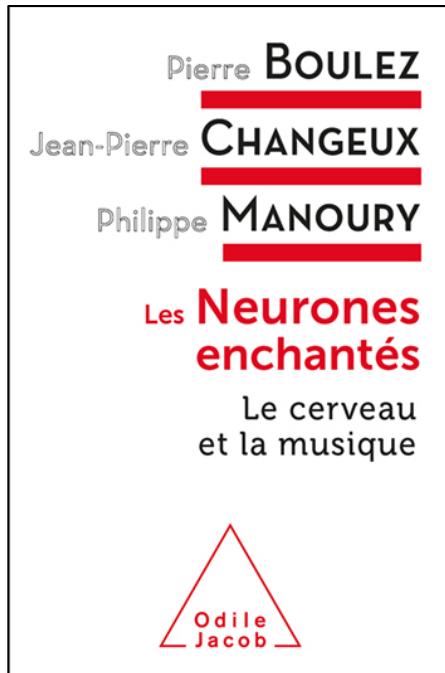
# Deep Generative Models | Music



# Music Composition | Automated approaches

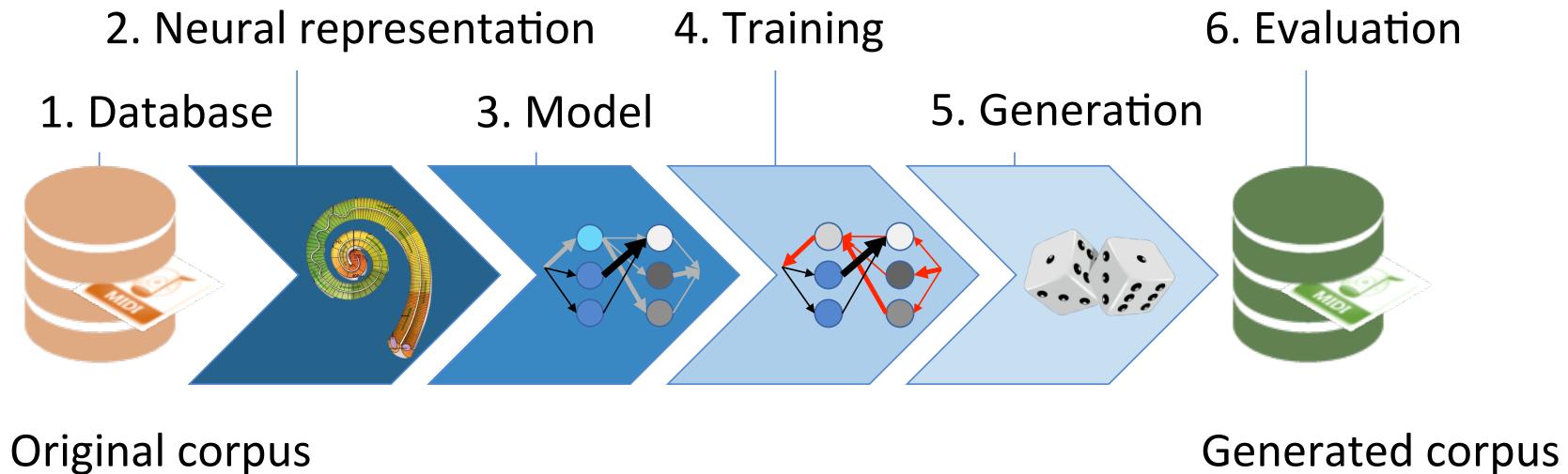
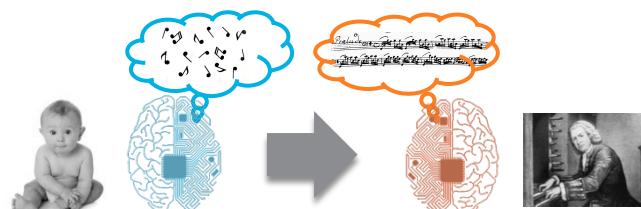


# What is the next note?

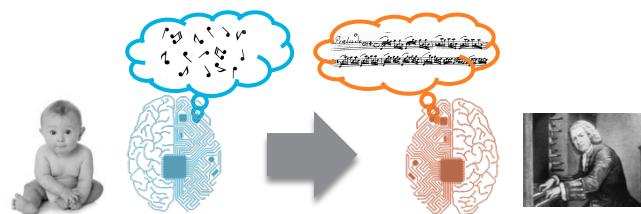


**BachProp**

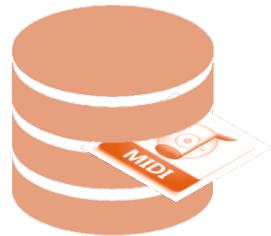
# BachProp | Algorithm



# Datasets



- **Nottingham**
  - ▣ 1035 folk tunes with homogeneous structure
- **Chorales**
  - ▣ 381 4-voices chorales harmonized by J.S. Bach
- **John Sankey**
  - ▣ 135 keyboard pieces from J.S. Bach recorded live by John Sankey
- **String quartets**
  - ▣ 215 Haydn and Mozart string quartets

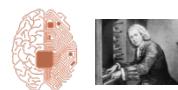


Original corpus

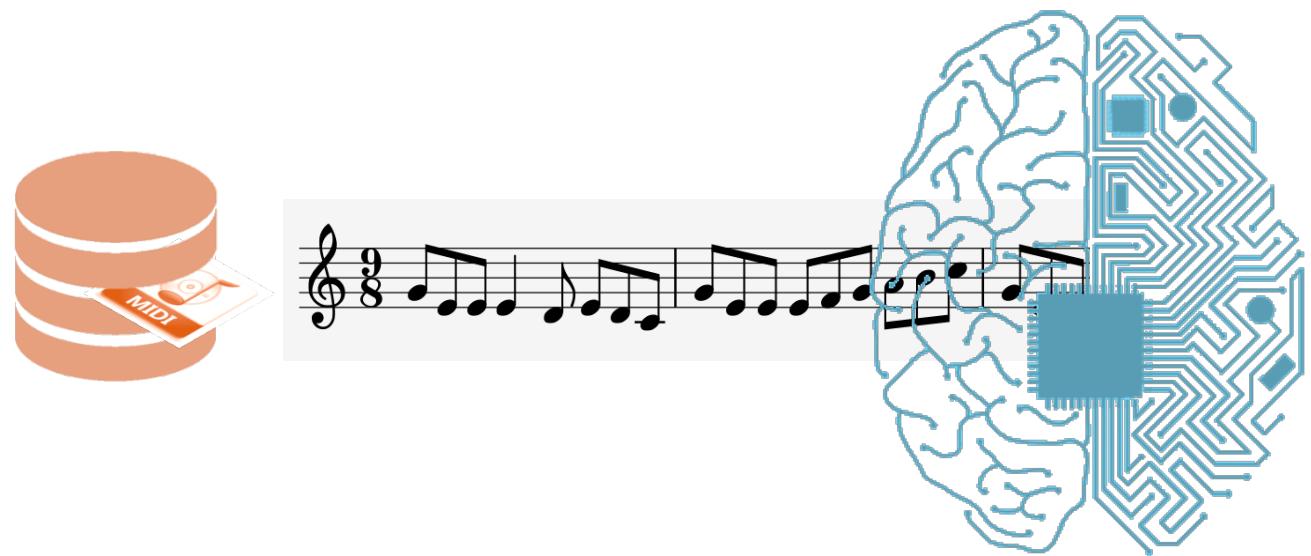


Original and generated examples | BachProp

[sites.google.com/view/bachprop/](http://sites.google.com/view/bachprop/)



# Neural representation | Ear of an ANN

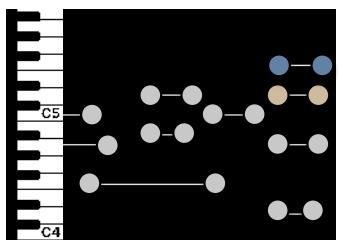




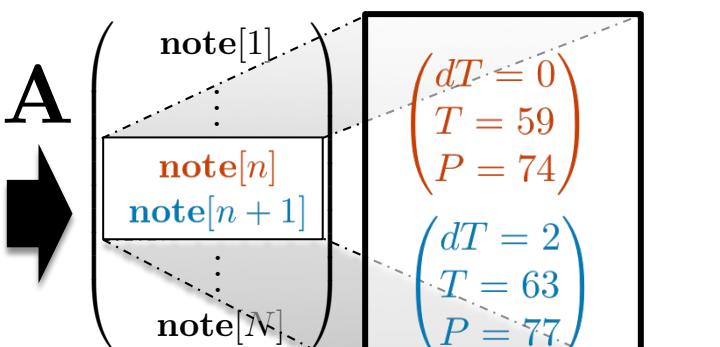
# Normalization | MIDI to note sequence



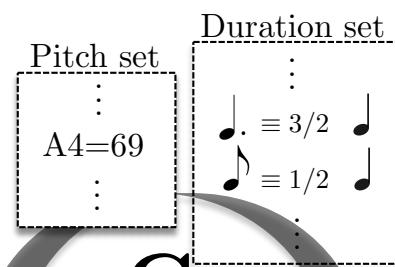
**mifi**



$[dT_{\text{MIDI}} = 0, P = 74]$  Note ON  
 $[dT_{\text{MIDI}} = 2, P = 77]$  Note ON  
 $[dT_{\text{MIDI}} = 0, P = 74]$  Note OFF  
 $[dT_{\text{MIDI}} = 3, P = 77]$  Note OFF

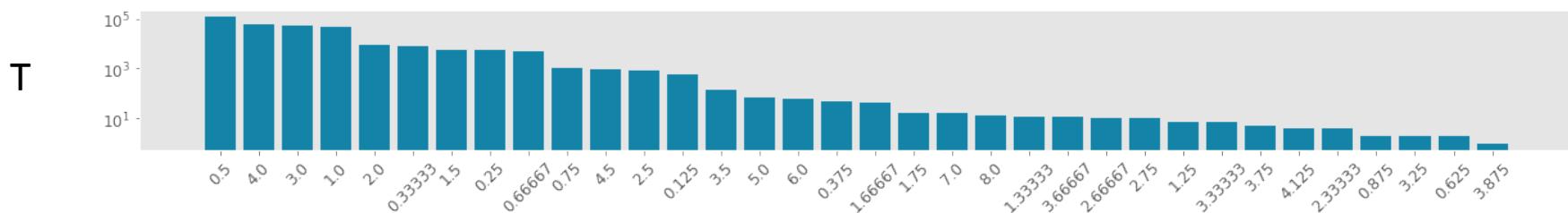
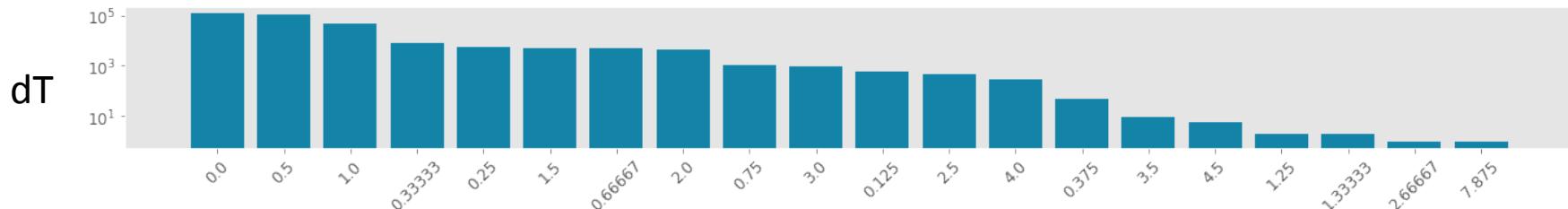


B





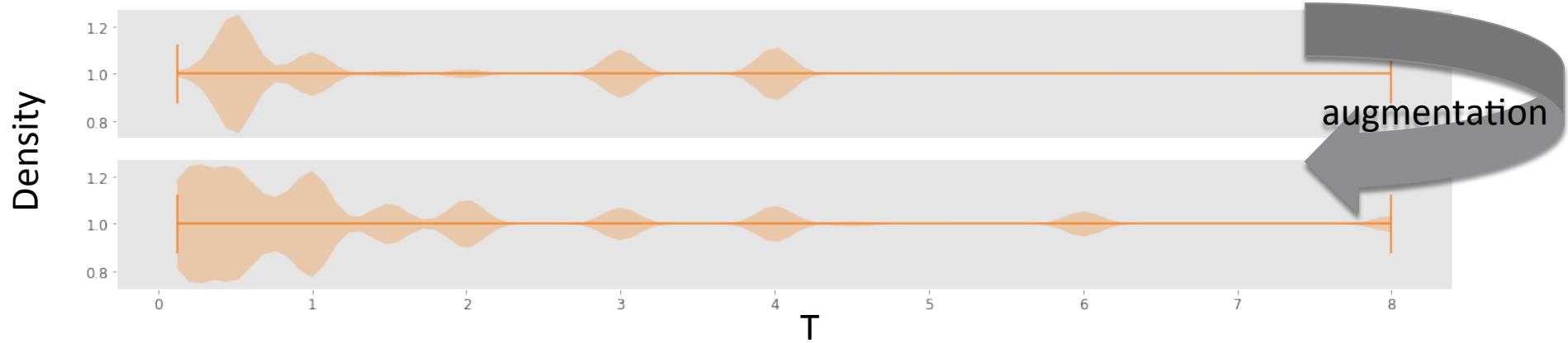
# Feature dictionaries | Distributions





# Data Augmentation | Rhythm

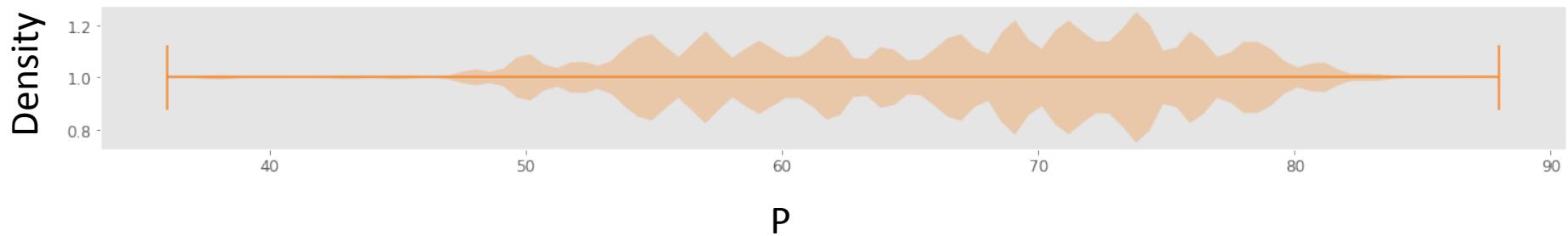
- Dilate and contract durations
  - Factors: [1/4, 1/3, 1/2, 2/3,  $\frac{3}{4}$ , 1.5/4, 3/2, 2, 3, 4]
  - Constrain on the set of possible durations
- Nottingham dataset
  - 1037 songs → 3334 songs

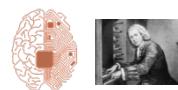




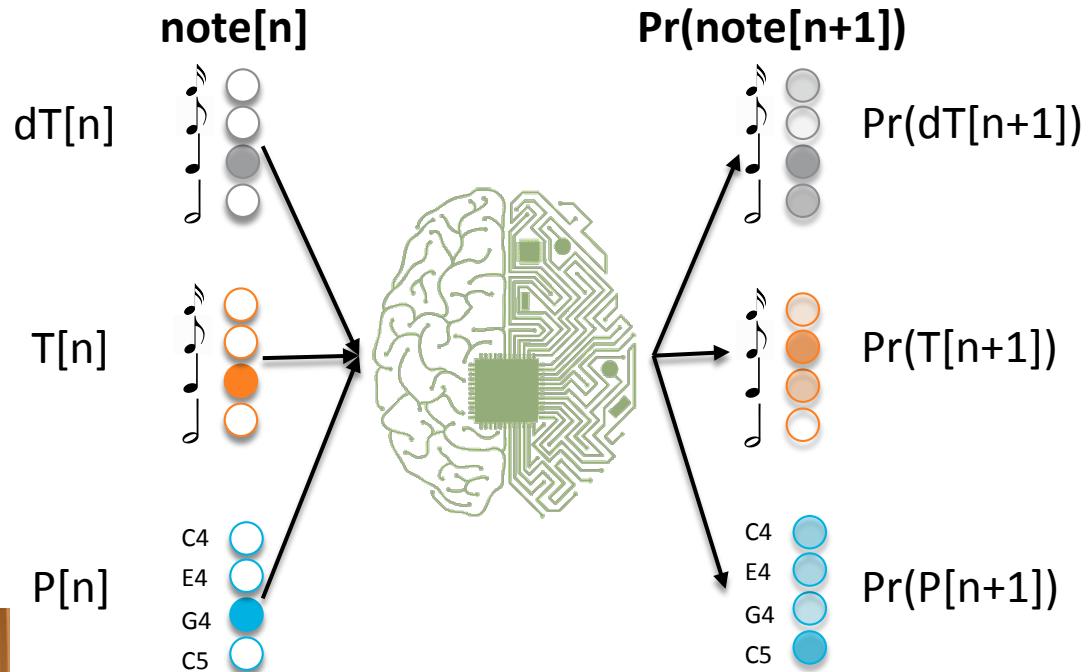
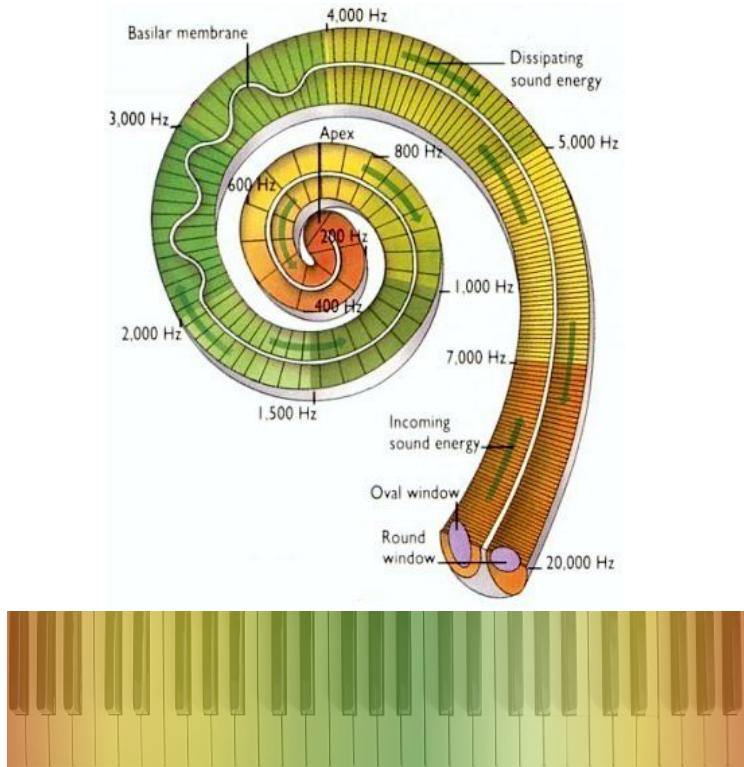
# Data Augmentation | Pitch

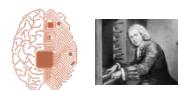
- Music is transposition invariant
  - Transpose in every possible keys greatly increase the number of training samples



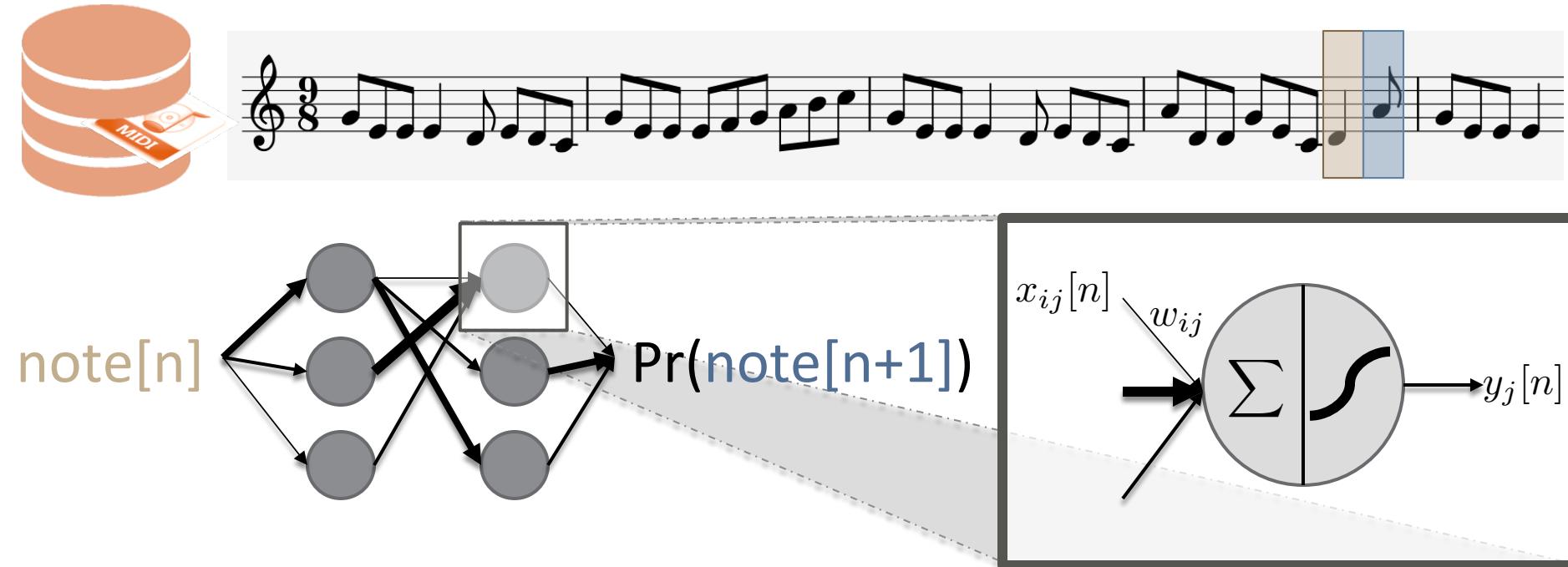


# Data Representation | I/O



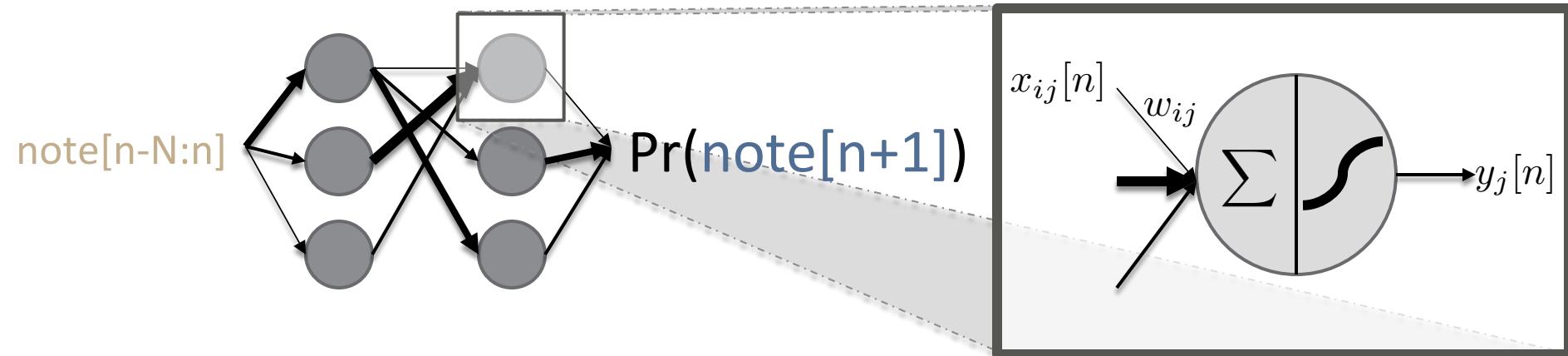


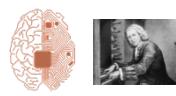
# Model | Feedforward



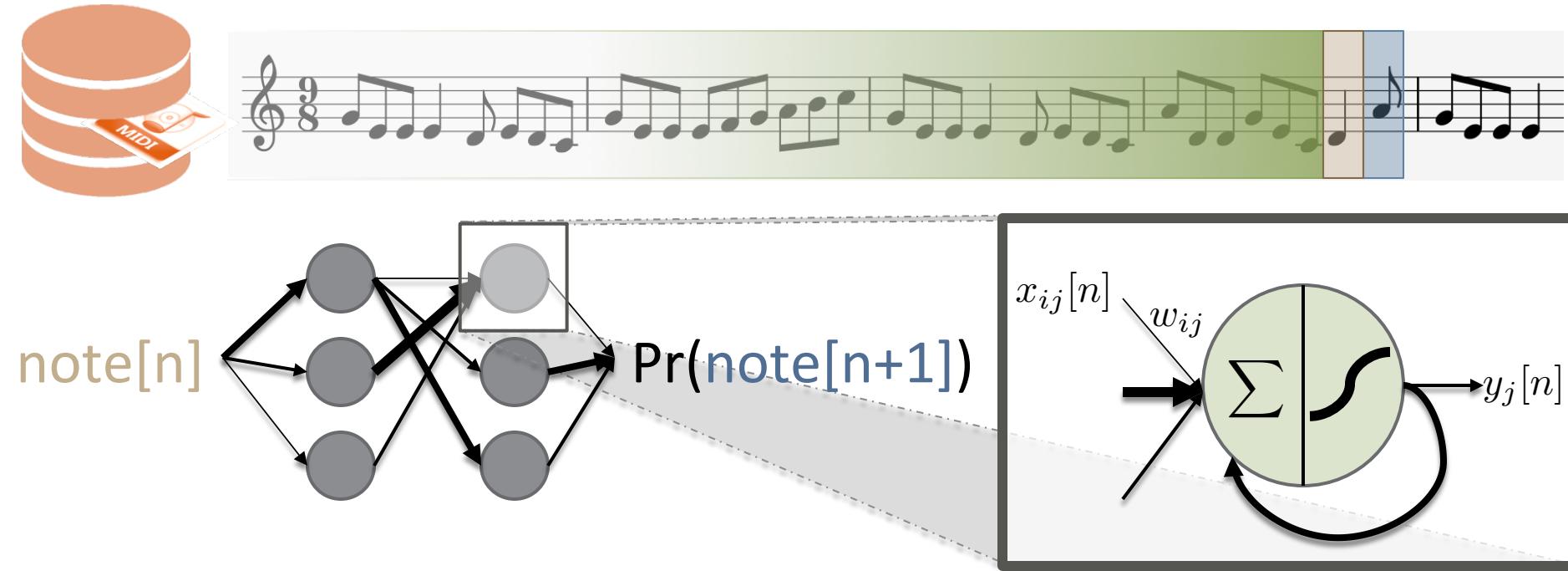


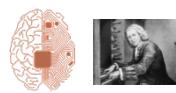
# Model | Feedforward



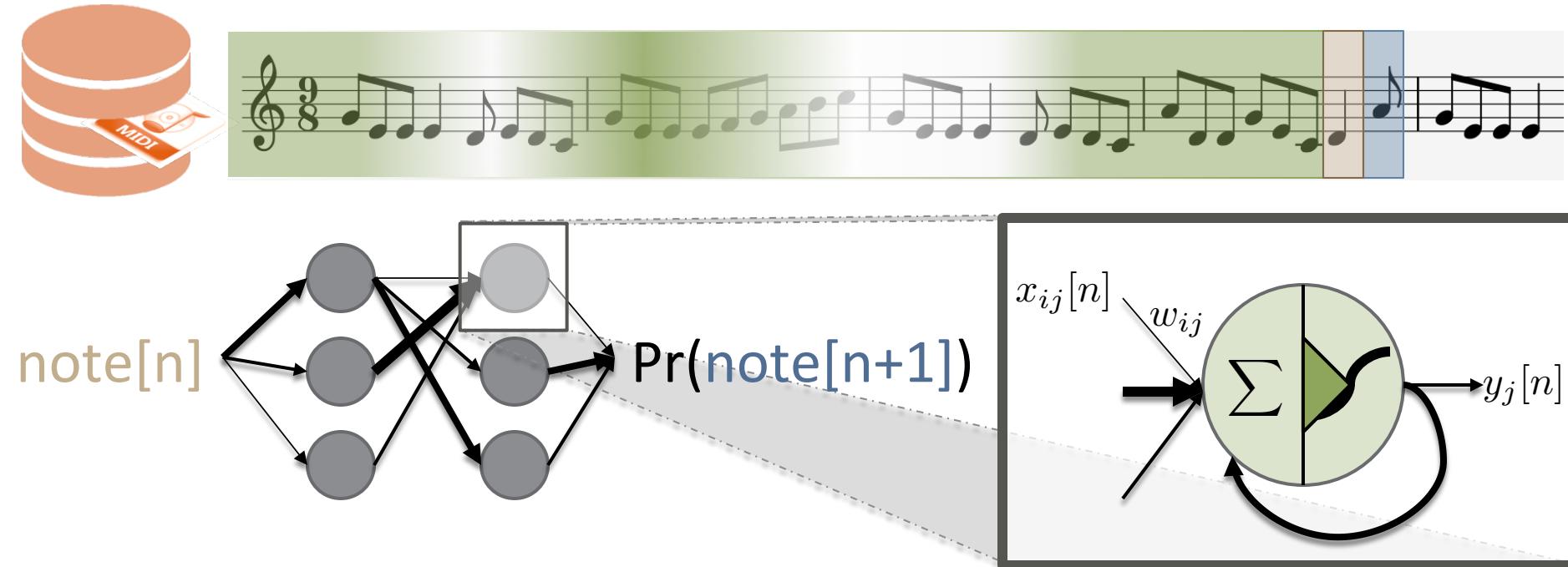


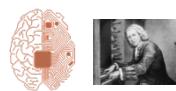
# Model | Recurrent



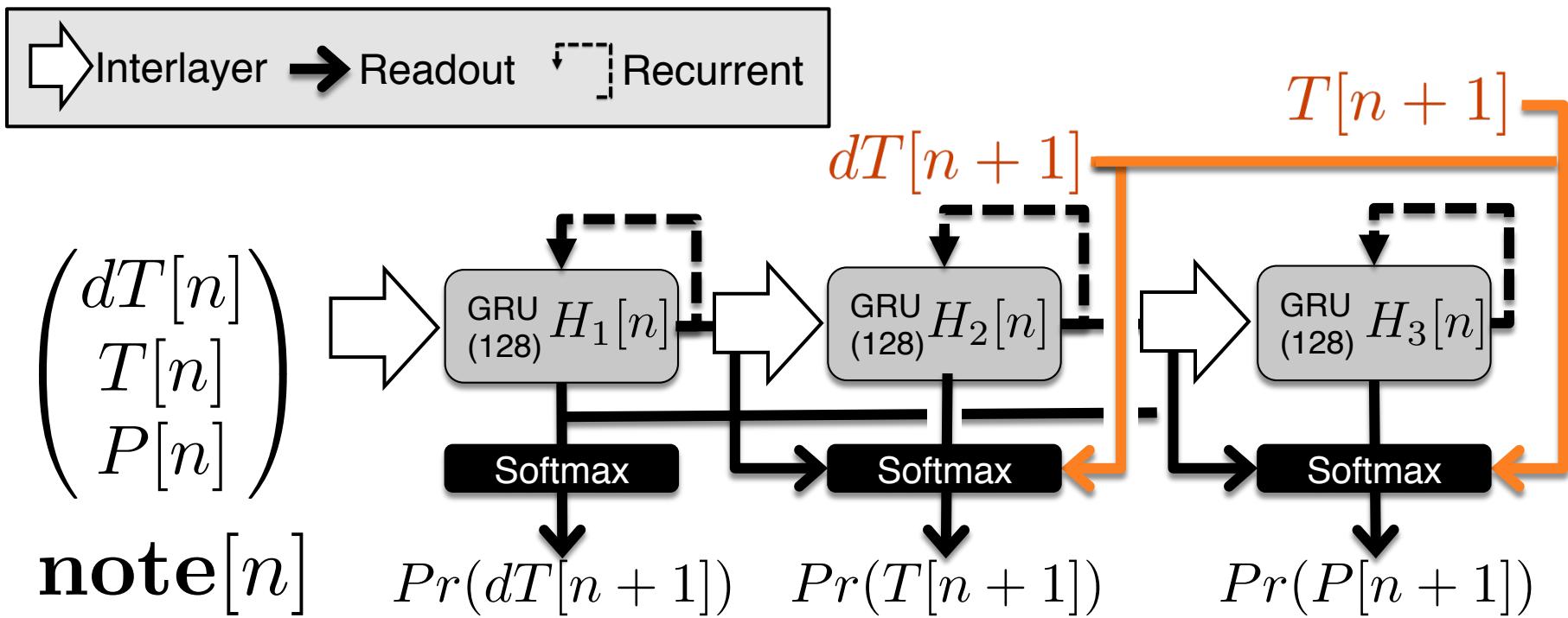


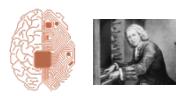
# Model | LSTM (GRU)





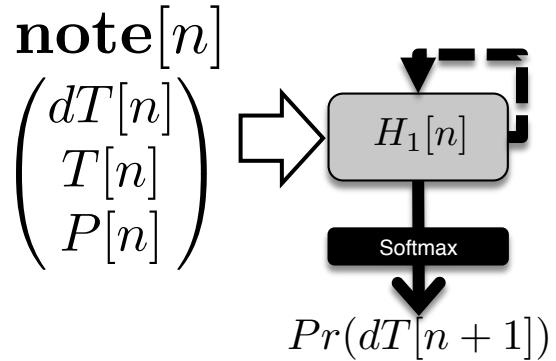
# Neural Network Architecture





# Probabilistic interpretation

$$Pr(\mathbf{note}[1 : N]) = Pr(\mathbf{note}[1]) \prod_{n=1}^{N-1} Pr(\mathbf{note}[n + 1] | \mathbf{note}[1 : n])$$



$$Pr(\mathbf{note}[n + 1] | \mathbf{note}[1 : n]) =$$

$$Pr(dT[n + 1] | \mathbf{note}[1 : n]) \times$$

$$Pr(T[n + 1] | \mathbf{note}[1 : n], dT[n + 1]) \times$$

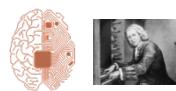
$$Pr(P[n + 1] | \mathbf{note}[1 : n], dT[n + 1], T[n + 1])$$



$$\approx Pr(dT[n + 1] | H_{dT}[n])$$

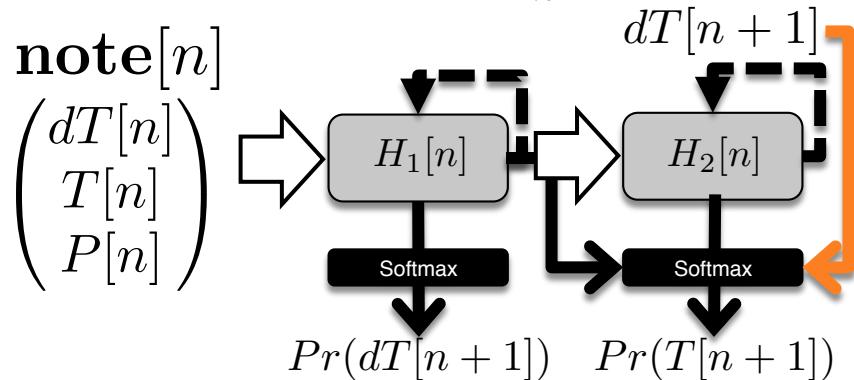
$$\approx Pr(T[n + 1] | H_T[n], dT[n + 1])$$

$$\approx Pr(P[n + 1] | H_P[n], dT[n + 1], T[n + 1])$$



# Probabilistic interpretation

$$Pr(\mathbf{note}[1 : N]) = Pr(\mathbf{note}[1]) \prod_{n=1}^{N-1} Pr(\mathbf{note}[n + 1] | \mathbf{note}[1 : n])$$

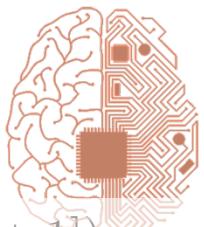


$$Pr(\mathbf{note}[n + 1] | \mathbf{note}[1 : n]) =$$

$$Pr(dT[n + 1] | \mathbf{note}[1 : n]) \times$$

$$Pr(T[n + 1] | \mathbf{note}[1 : n], dT[n + 1]) \times$$

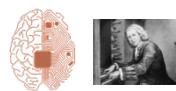
$$Pr(P[n + 1] | \mathbf{note}[1 : n], dT[n + 1], T[n + 1])$$



$$\approx Pr(dT[n + 1] | H_{dT}[n])$$

$$\approx Pr(T[n + 1] | H_T[n], \mathbf{dT}[n + 1])$$

$$\approx Pr(P[n + 1] | H_P[n], dT[n + 1], T[n + 1])$$



# Probabilistic interpretation

$$Pr(\mathbf{note}[1 : N]) = Pr(\mathbf{note}[1]) \prod_{n=1}^{N-1} Pr(\mathbf{note}[n + 1] | \mathbf{note}[1 : n])$$

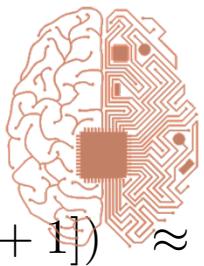
$\mathbf{note}[n]$   
 $\begin{pmatrix} dT[n] \\ T[n] \\ P[n] \end{pmatrix}$   
 $H_1[n]$        $H_2[n]$        $H_3[n]$   
 $Softmax$        $Softmax$        $Softmax$   
 $Pr(dT[n + 1])$        $Pr(T[n + 1])$        $Pr(P[n + 1])$

$$Pr(\mathbf{note}[n + 1] | \mathbf{note}[1 : n]) =$$

$$Pr(dT[n + 1] | \mathbf{note}[1 : n]) \times$$

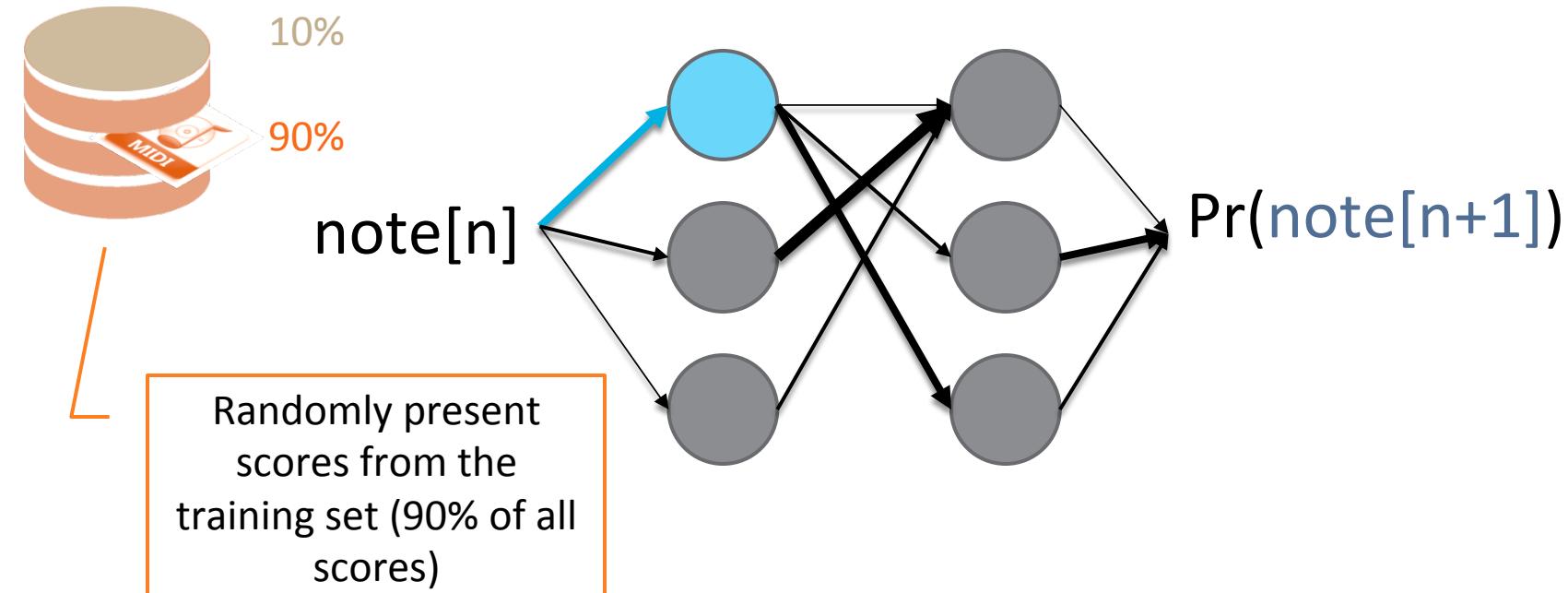
$$Pr(T[n + 1] | \mathbf{note}[1 : n], dT[n + 1]) \times$$

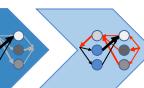
$$Pr(P[n + 1] | \mathbf{note}[1 : n], dT[n + 1], T[n + 1]) \approx Pr(P[n + 1] | H_P[n], dT[n + 1], T[n + 1])$$



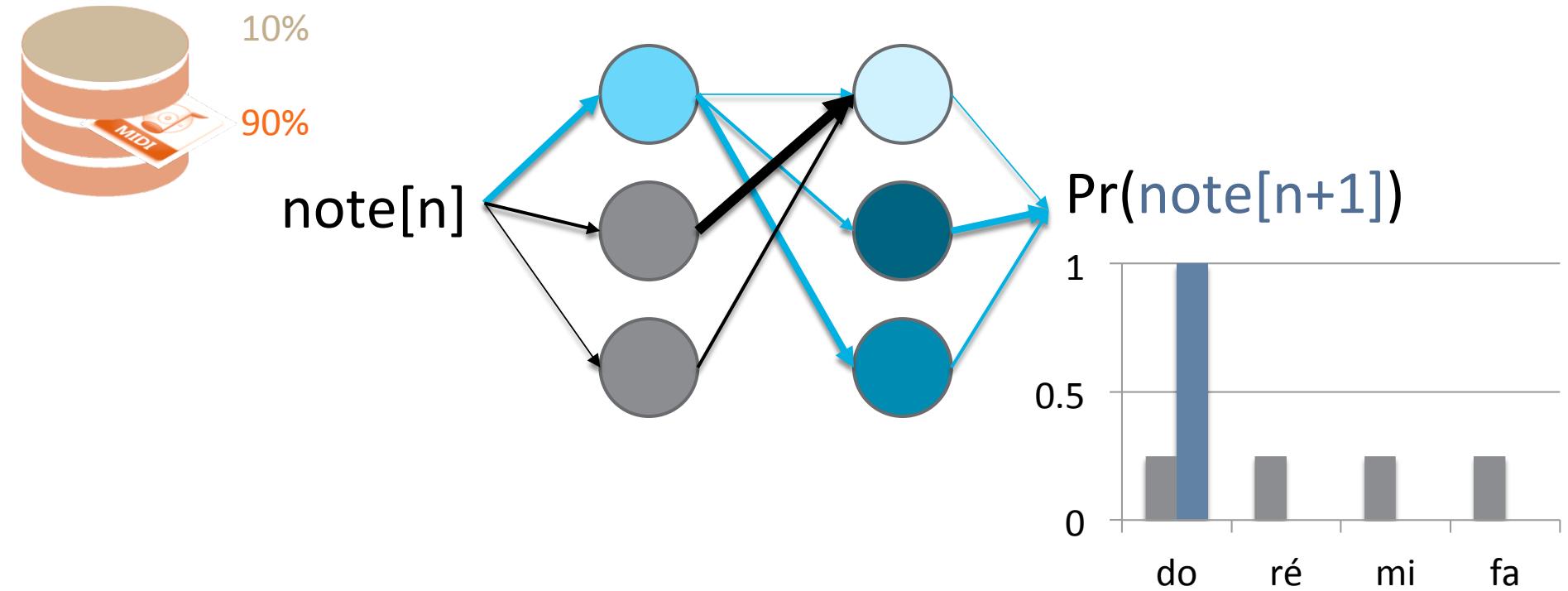


# Training | Forward pass



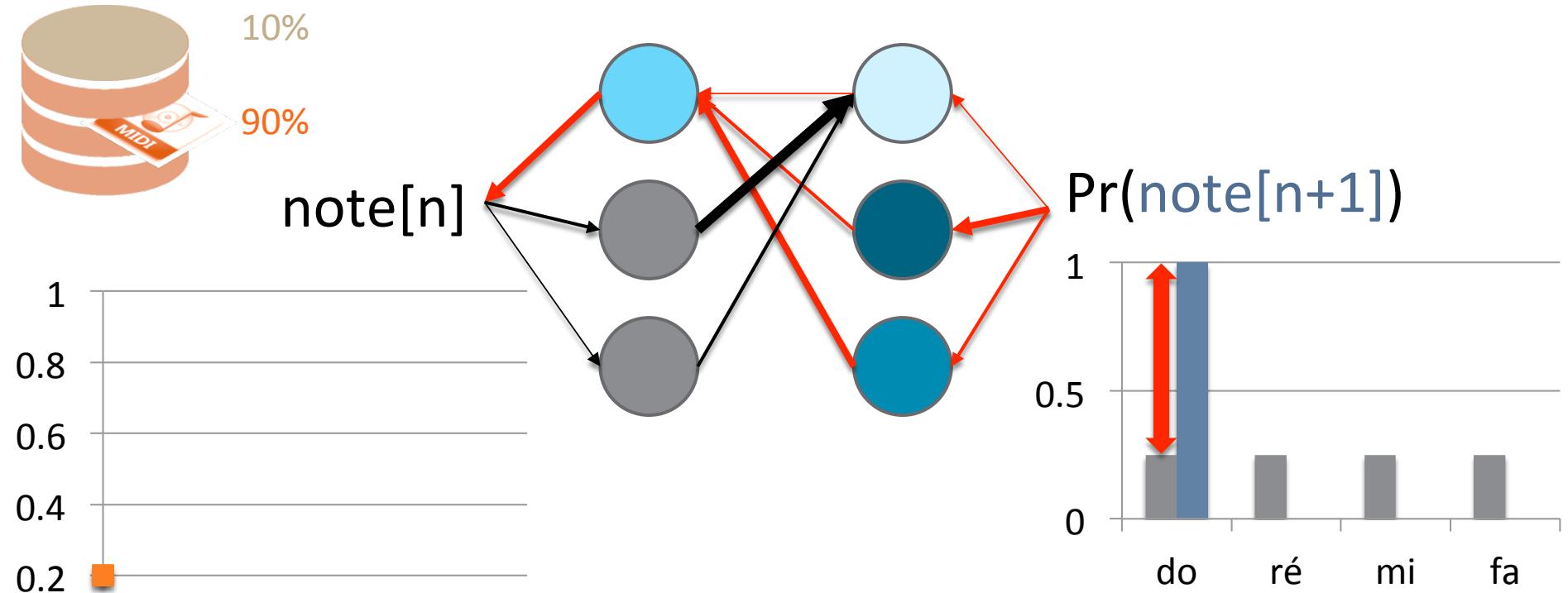


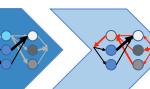
# Training | Forward pass



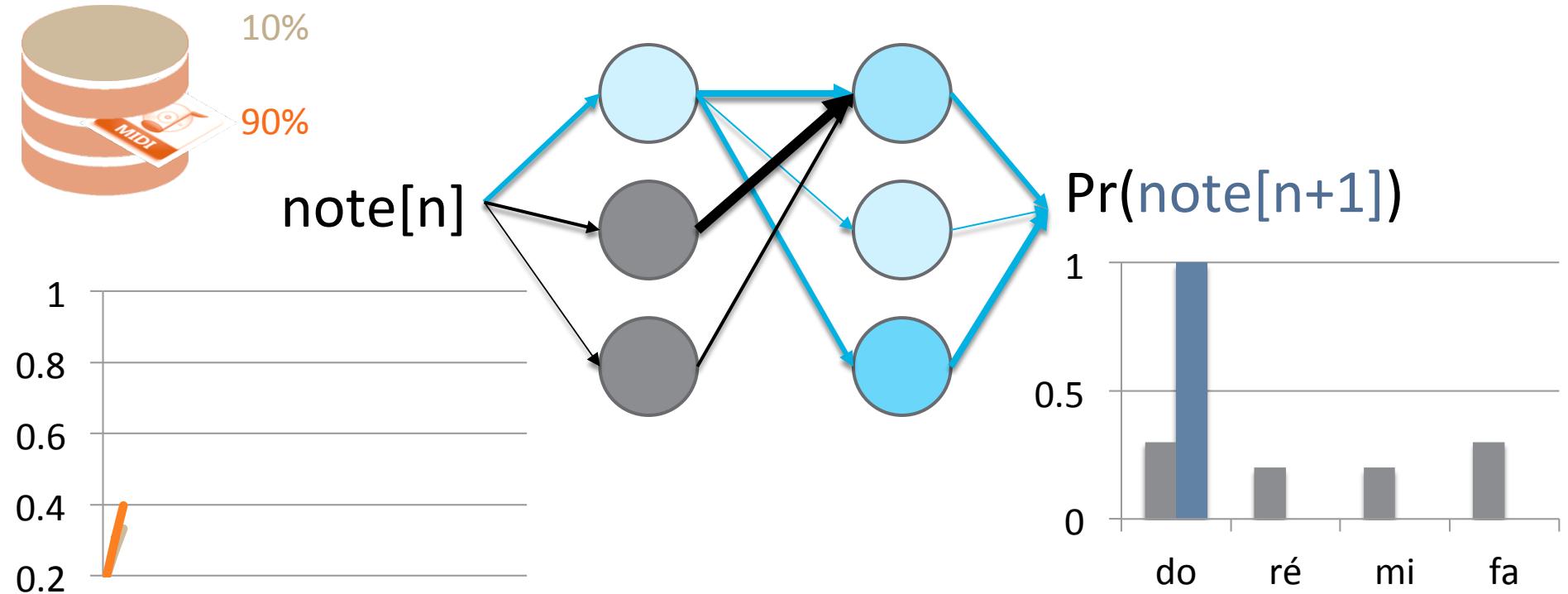


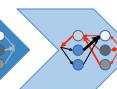
# Training | BackProp through time



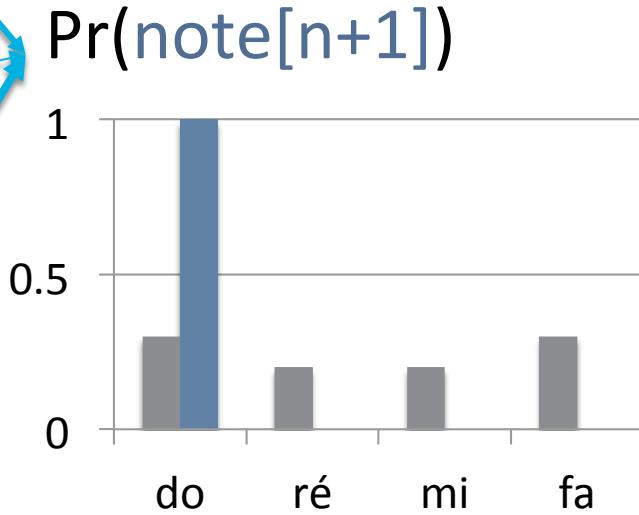
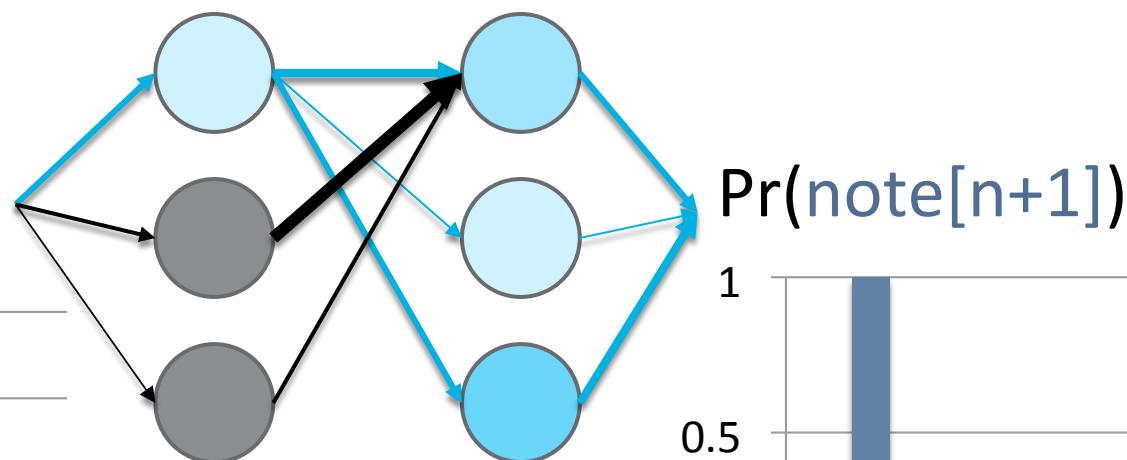
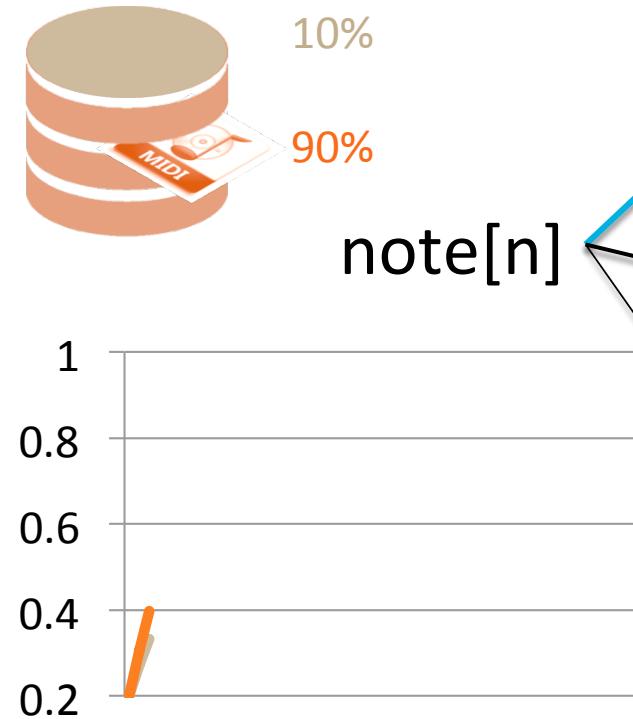


# Training | Update parameters



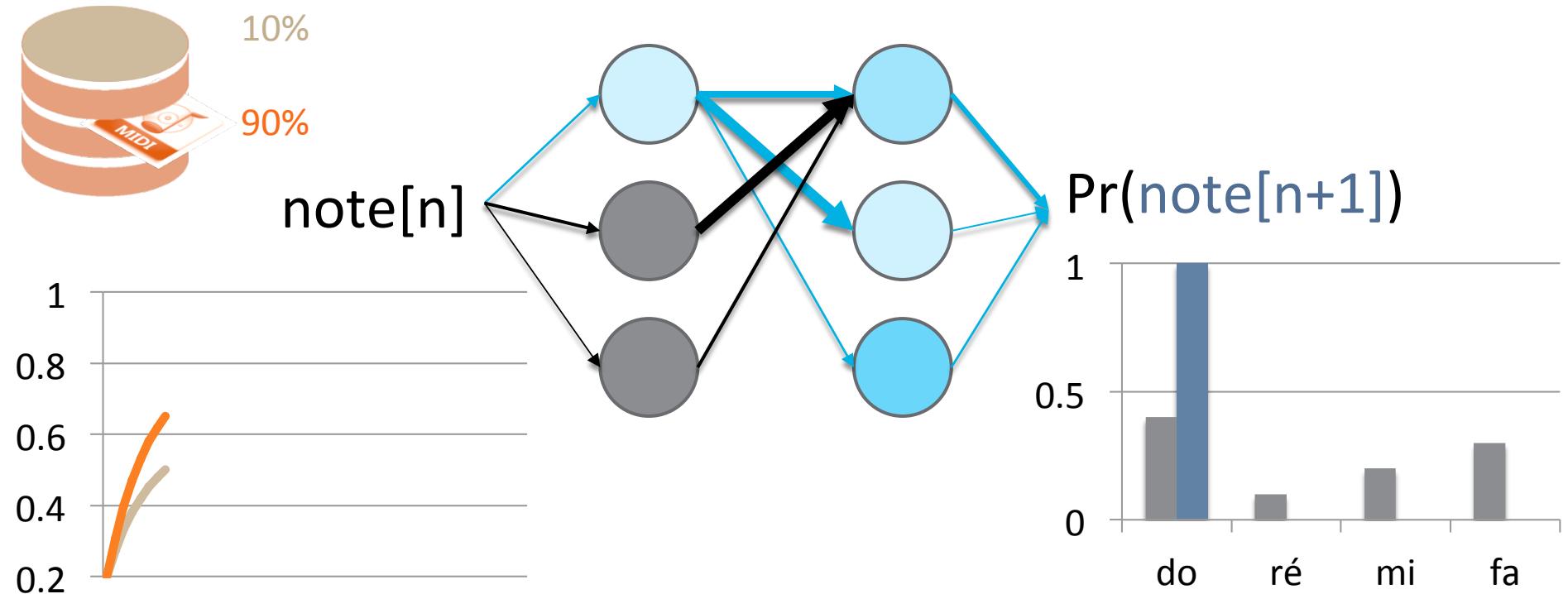


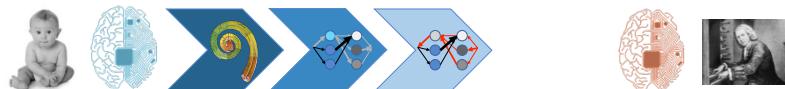
# Training | Update parameters



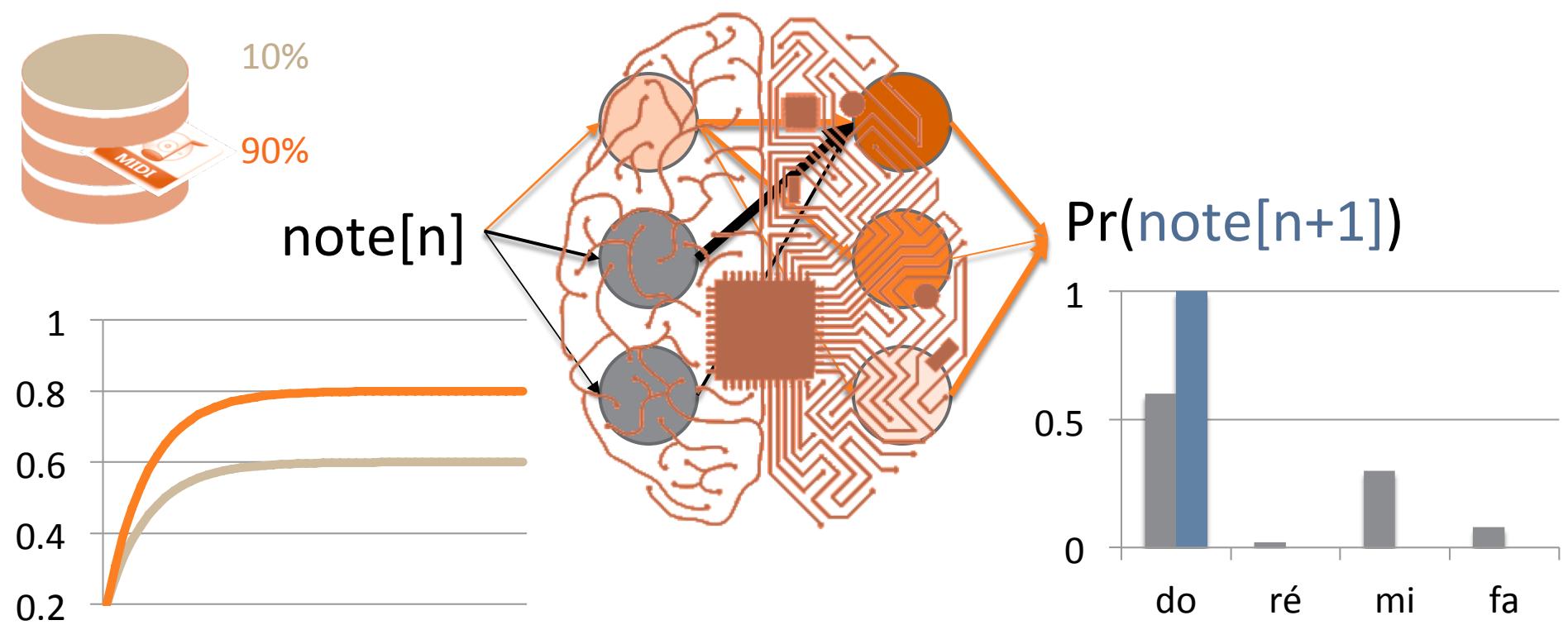


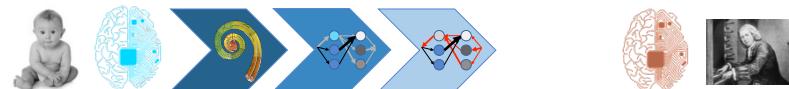
# Training | Update parameters



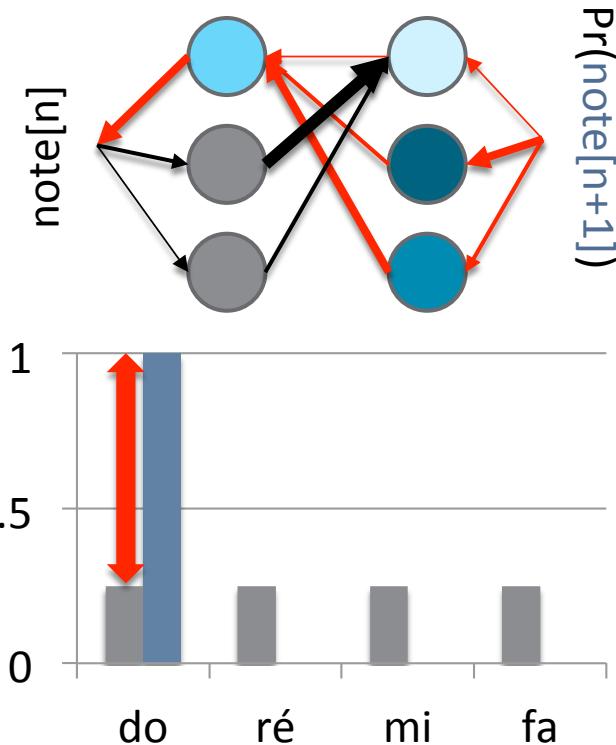


# Training | End

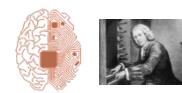




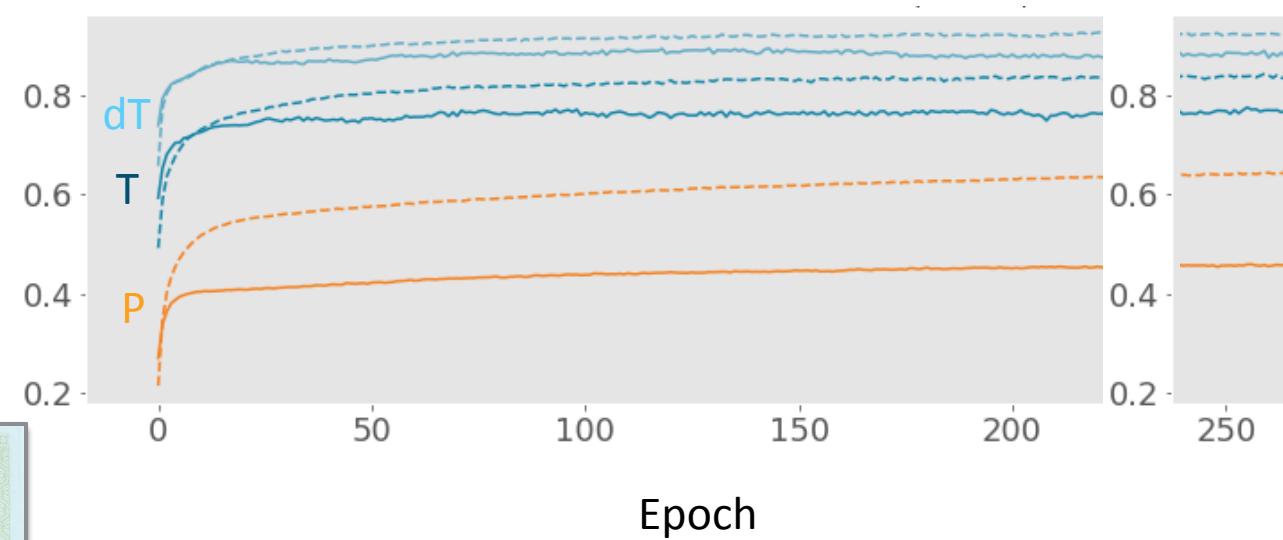
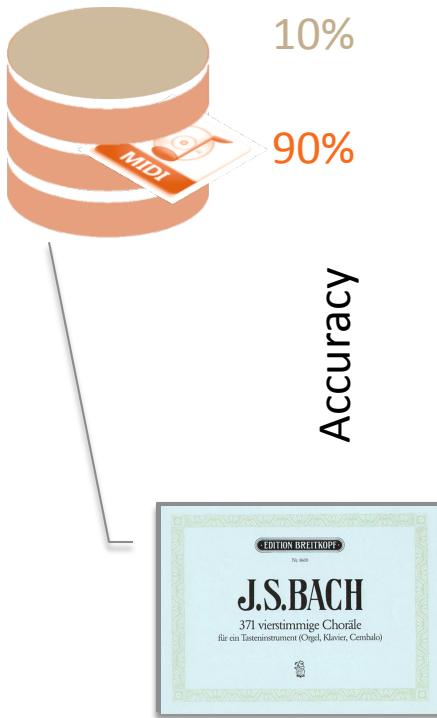
# Training

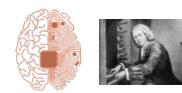


- TBPTT with 128 notes truncation
- Recurrent cells are stateful
  - ▣ Hidden state is kept after truncation
- Adam optimizer
  - ▣ Weighted ( $dT: 0.1$ ,  $T: 0.3$ ,  $P: 0.6$ ) cross-entropy loss functions

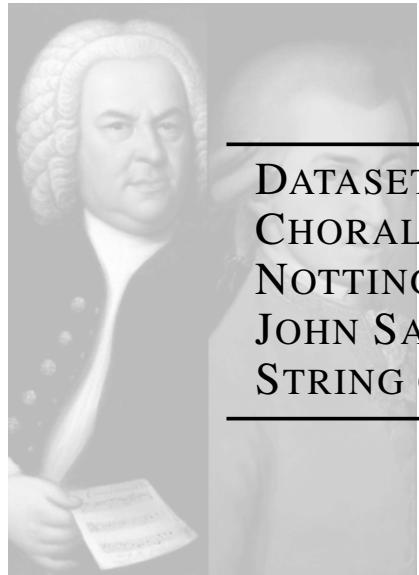


# Training | Learning Curves

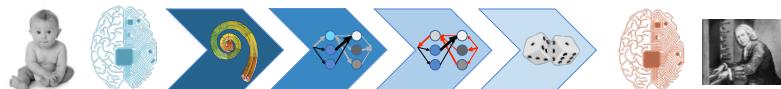




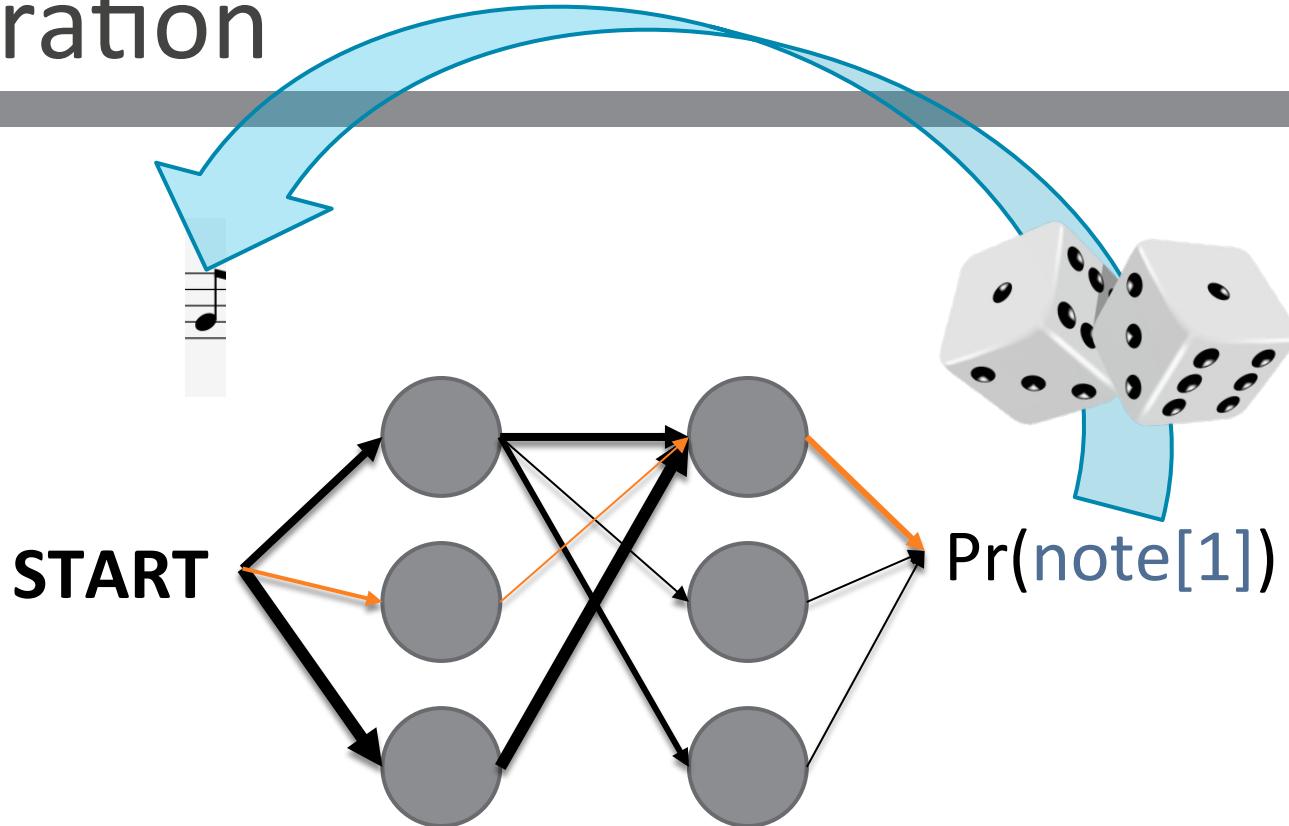
# Training | Other Datasets

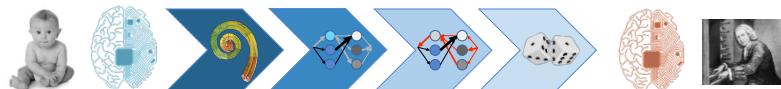


DATASET	NLL	$dT$	$T$	$P$	SIZE [SCORE]	SIZE [NOTE]
CHORALES	0.419	0.97	0.91	0.77	357	95'337
NOTTINGHAM	0.587	0.98	0.89	0.70	1037	313'975
JOHN SANKEY	1.002	0.89	0.77	0.45	135	358'211
STRING QUARTETS	0.936	0.88	0.83	0.49	215	738'739

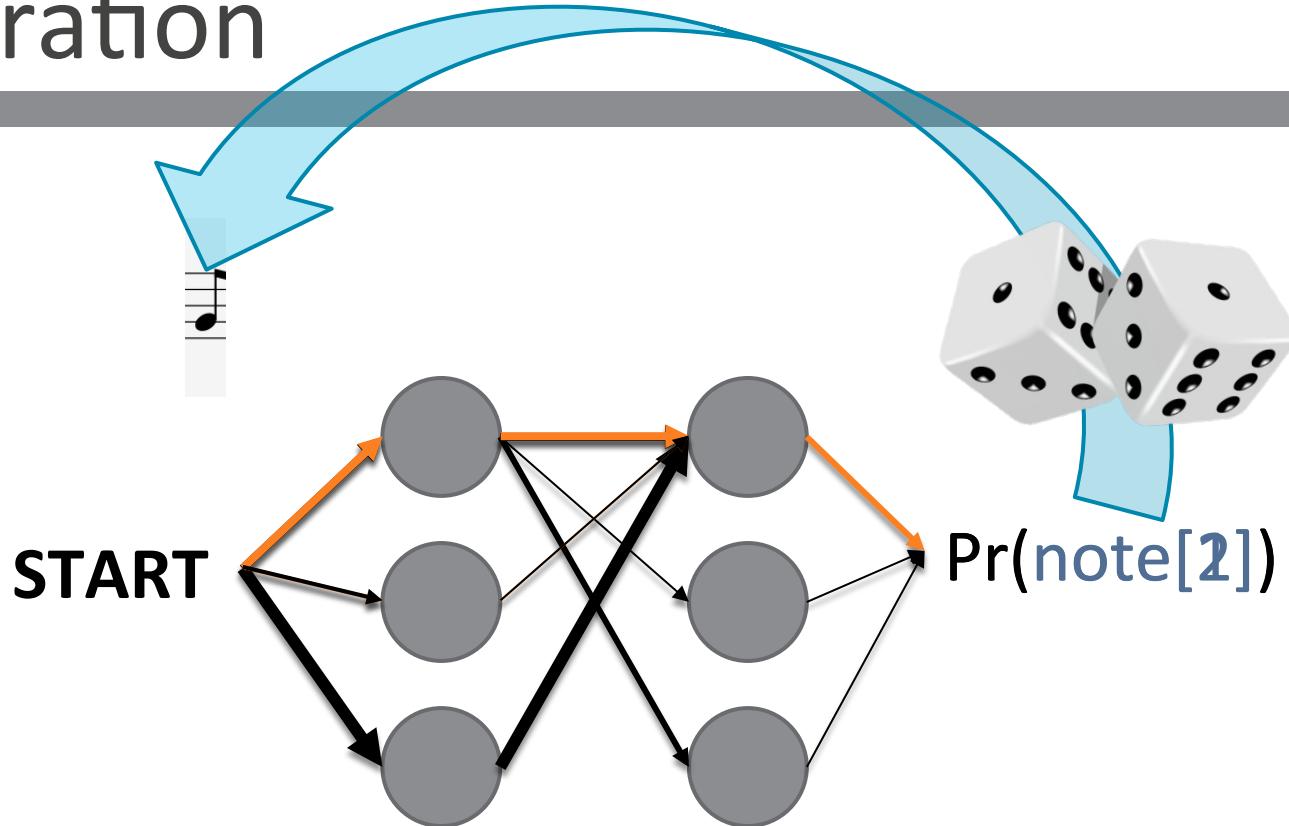


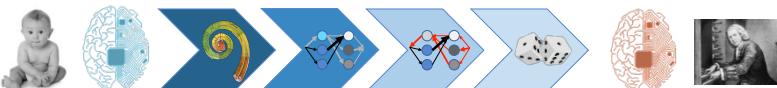
# Generation





# Generation

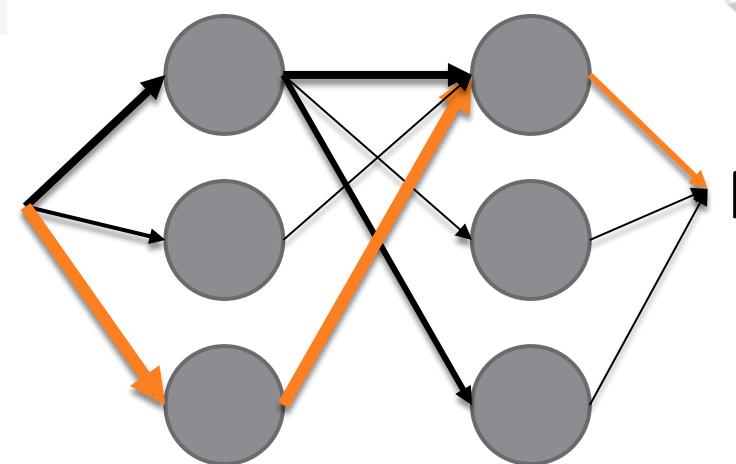




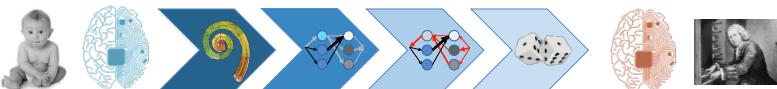
# Generation



$\text{note}[n]$



$\Pr(\text{note}[n+1])$

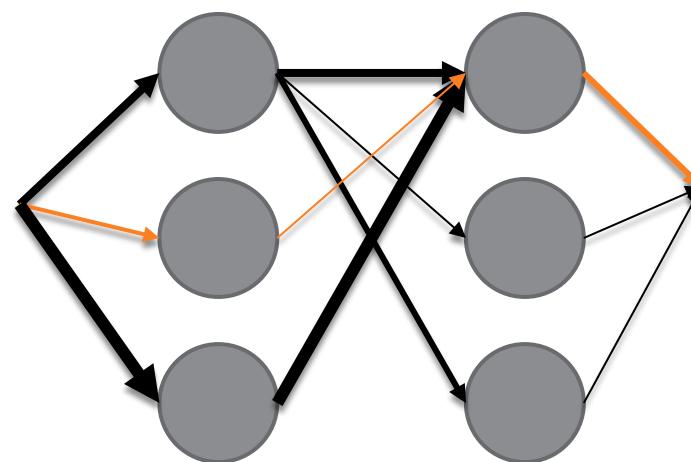


# Generation

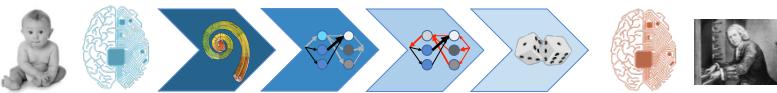


END

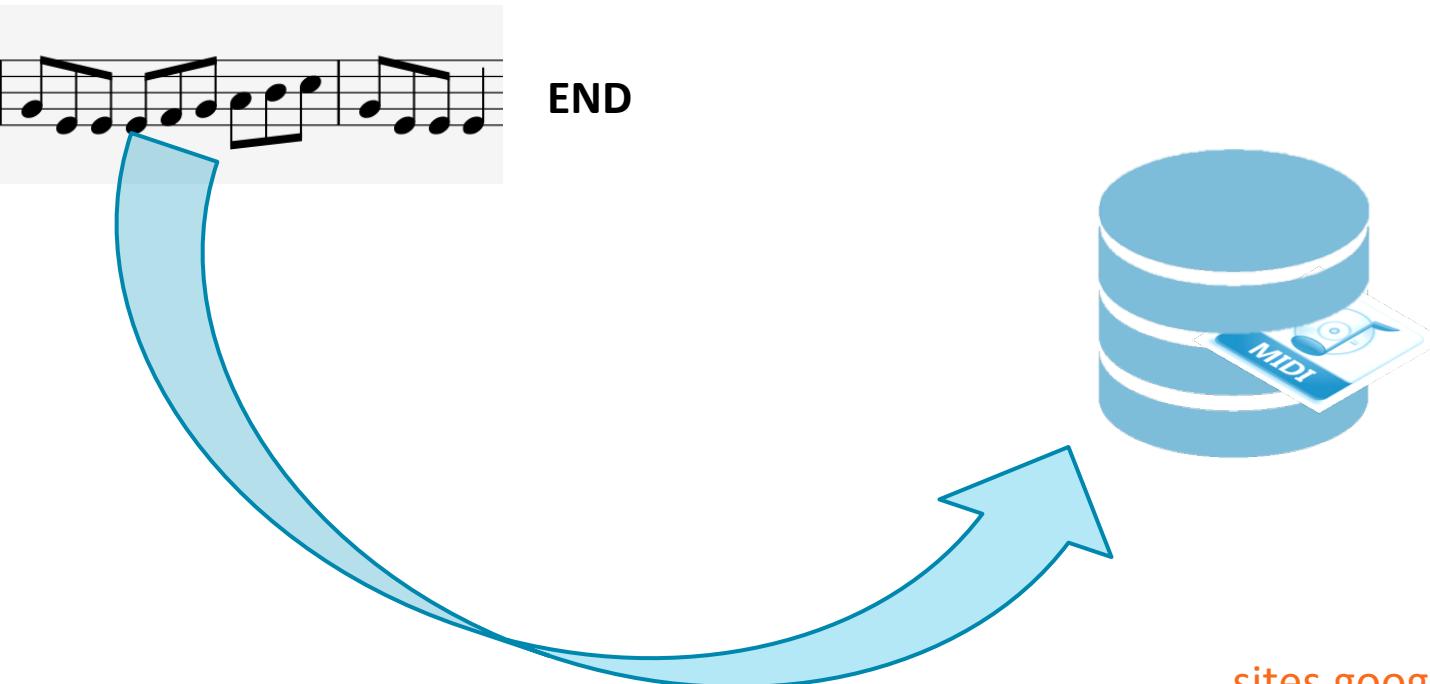
note[n]

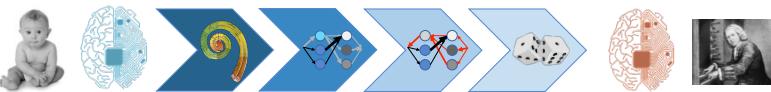


$\Pr(\text{note}[n+1])$



# Generation | Generated corpus





# Generation | Temperature Sampling

- Temperature of sampling can be adapted to the confidence we give to the model predictions
- A model trained with a corpus that exhibits many repetition of patterns, will generate scores with more examples of these repetitions for lower sampling temperatures
  - ▣ Lower temperature will reduce the probability to select an undesired note that is not part of the pattern to be repeated



# Evaluation | Turing Test

---

Quel est votre niveau de musique?  Novice  Intermédiaire  Expert

---

**Extraits musicaux** Ecoutez les extraits et répondez aux deux questions.

1. Quel extrait a été composé par un humain (vs machine)?  1  2  3

(Pour 2 réponses correctes à la suite, vous recevrez une récompense)

2. Quel extrait préferez-vous?  1  2  3  4

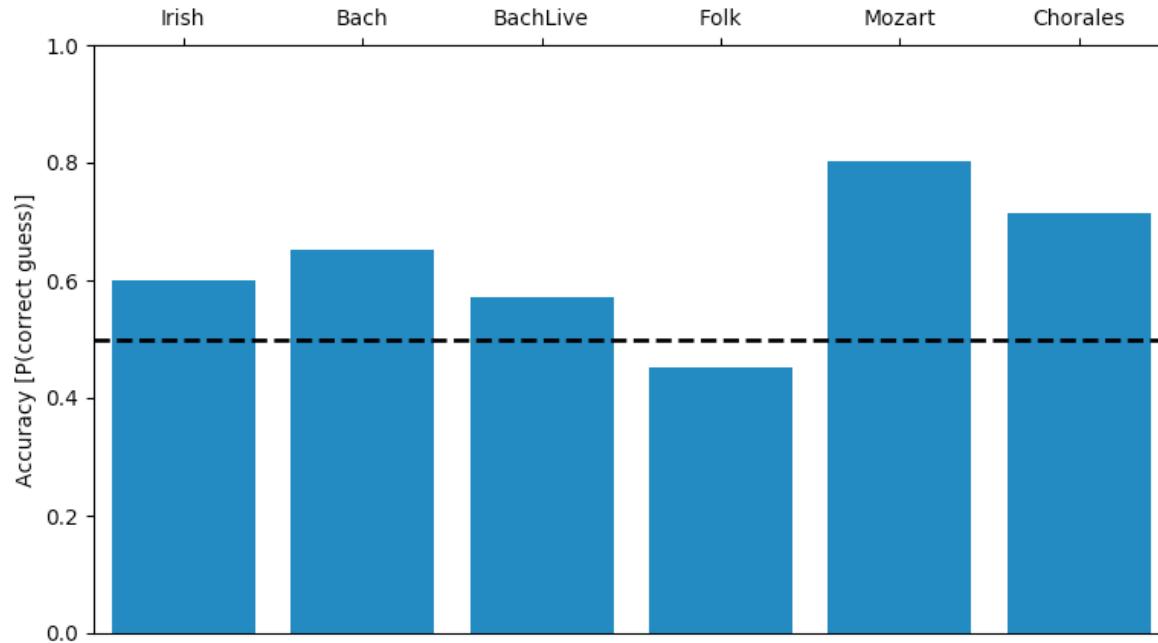
Appuyez sur **Submit** lorsque vous avez répondu aux deux questions.

---

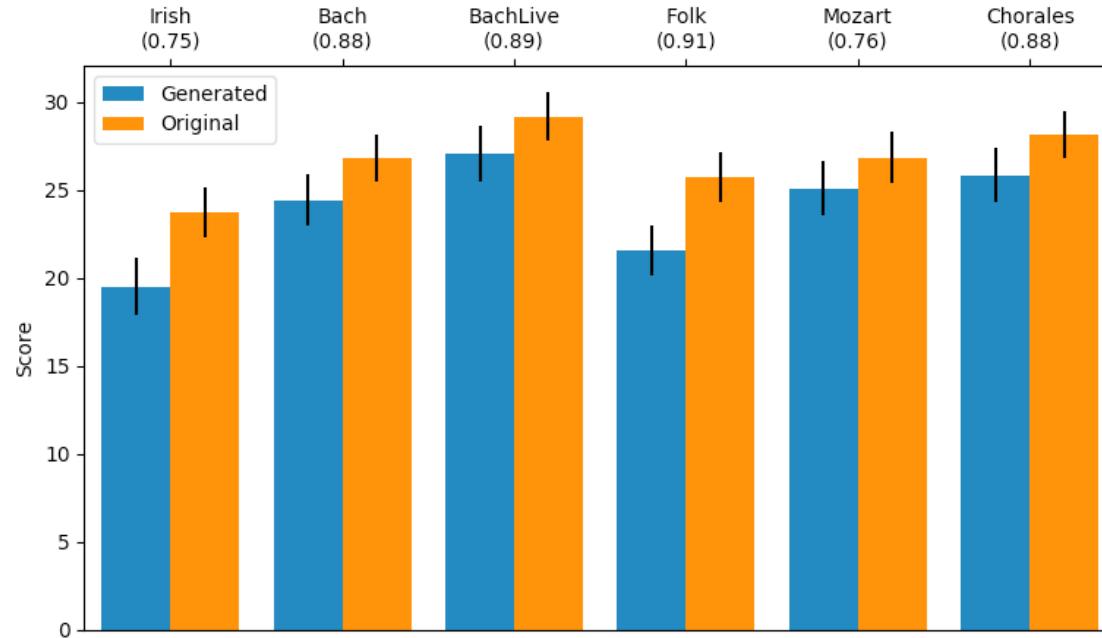
**Résultats** 224 votes



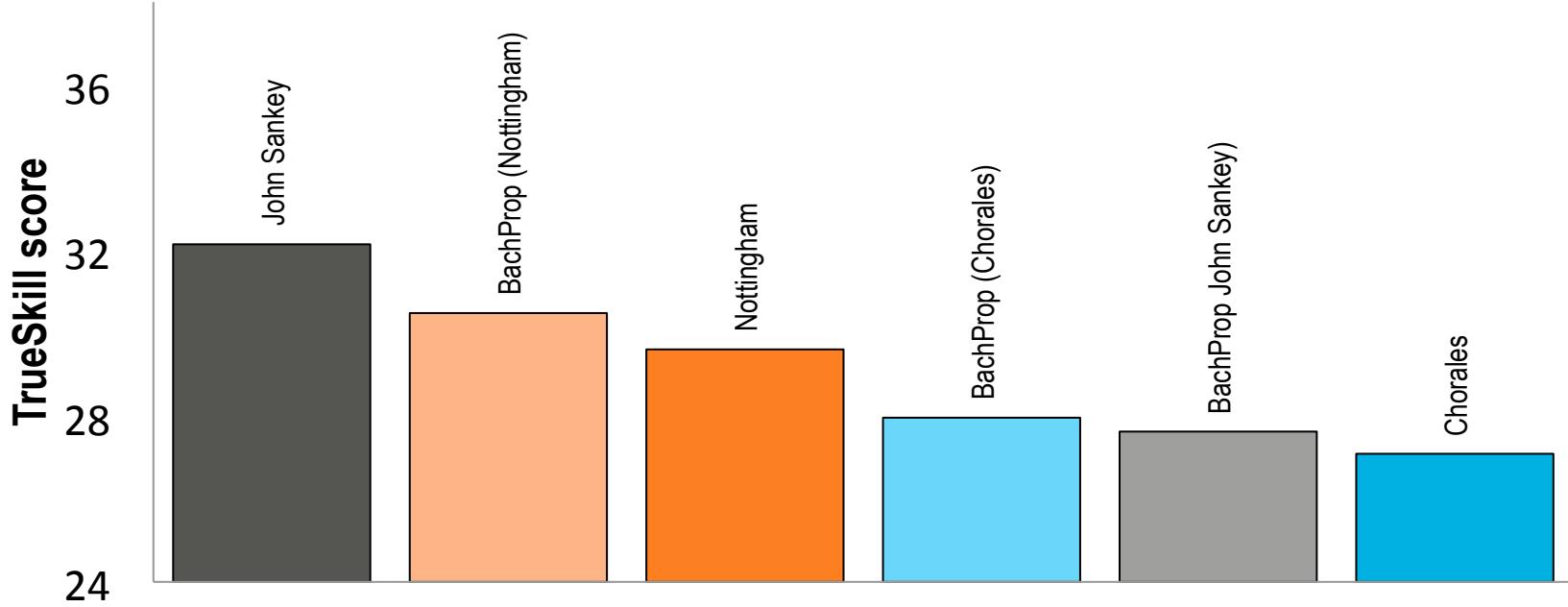
# Evaluation | Turing Test



# Evaluation | Scoring corpora



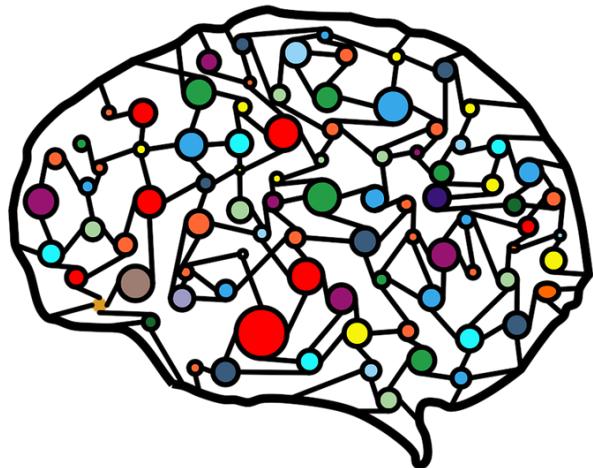
# Evaluation | Subjective



# Other models | Controls

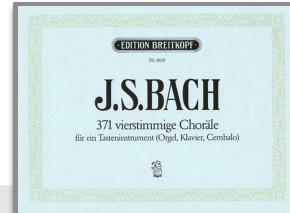
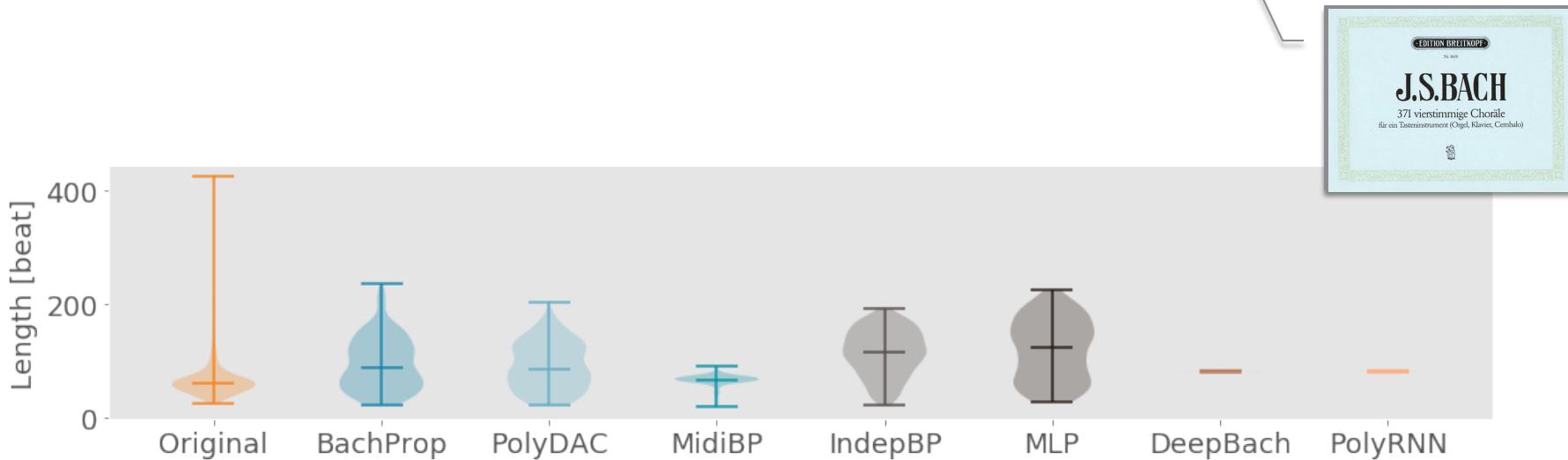
- **MLP**
  - 3 ReLU layers; History of 5 notes
- **PolyDAC**
  - 3 separate networks
- **IndepBP**
  - Independence between note features
- **MidiBP**
  - Uses MIDI data structure
- **DeepBach**
  - Temporal discretization; 4 voices; Designed for the Bach Chorales dataset
- **PolyRNN**
  - Temporal discretization; NEW\_NOTE(PITCH), CONTINUED\_NOTE(PITCH) and STEP\_END events

# Bach Chorales | Comparison of Architectures

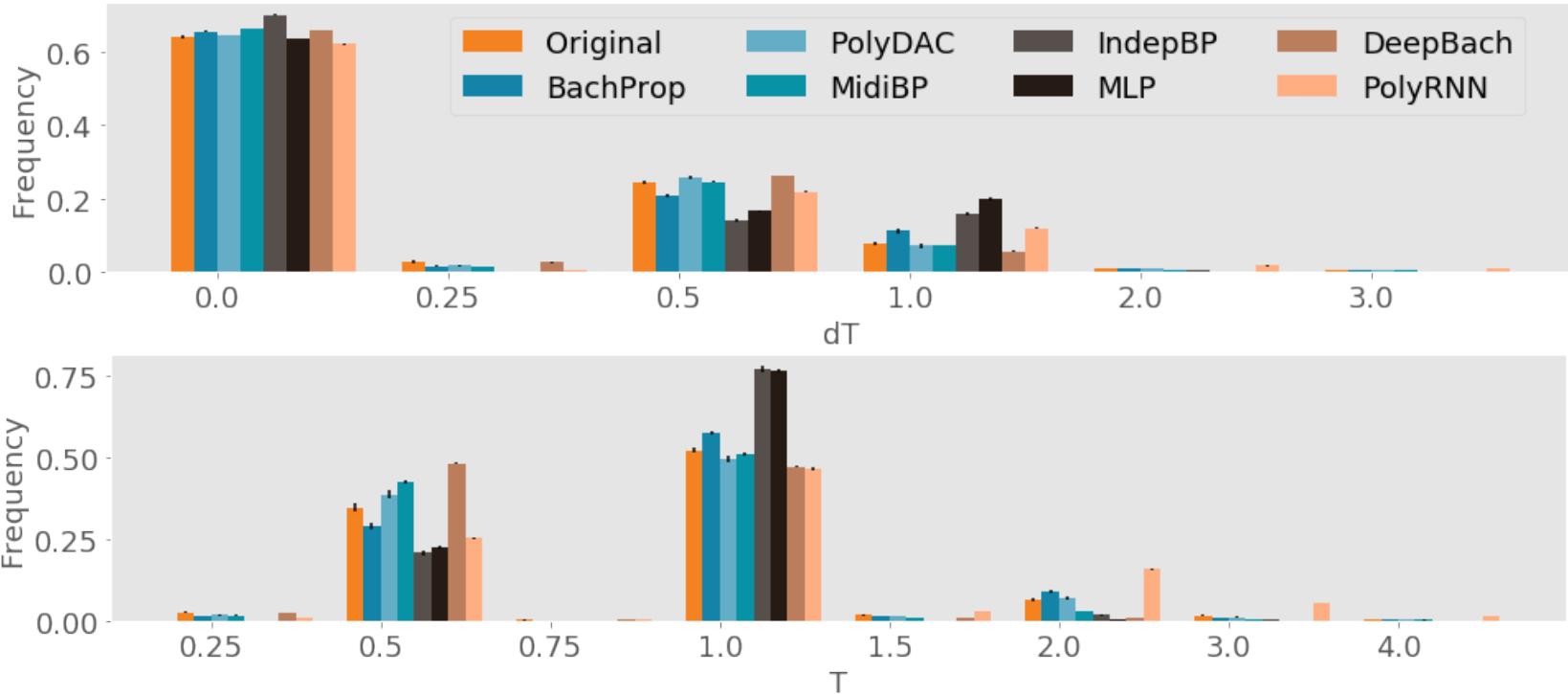


MODEL	NLL	$dT$	$T$	$P$
BACHPROP	0.419	0.97	0.91	0.77
POLYDACP	0.647	0.97	0.94	0.69
INDEPBPP	0.647	0.97	0.75	0.63
MLP	0.796	0.95	0.76	0.49

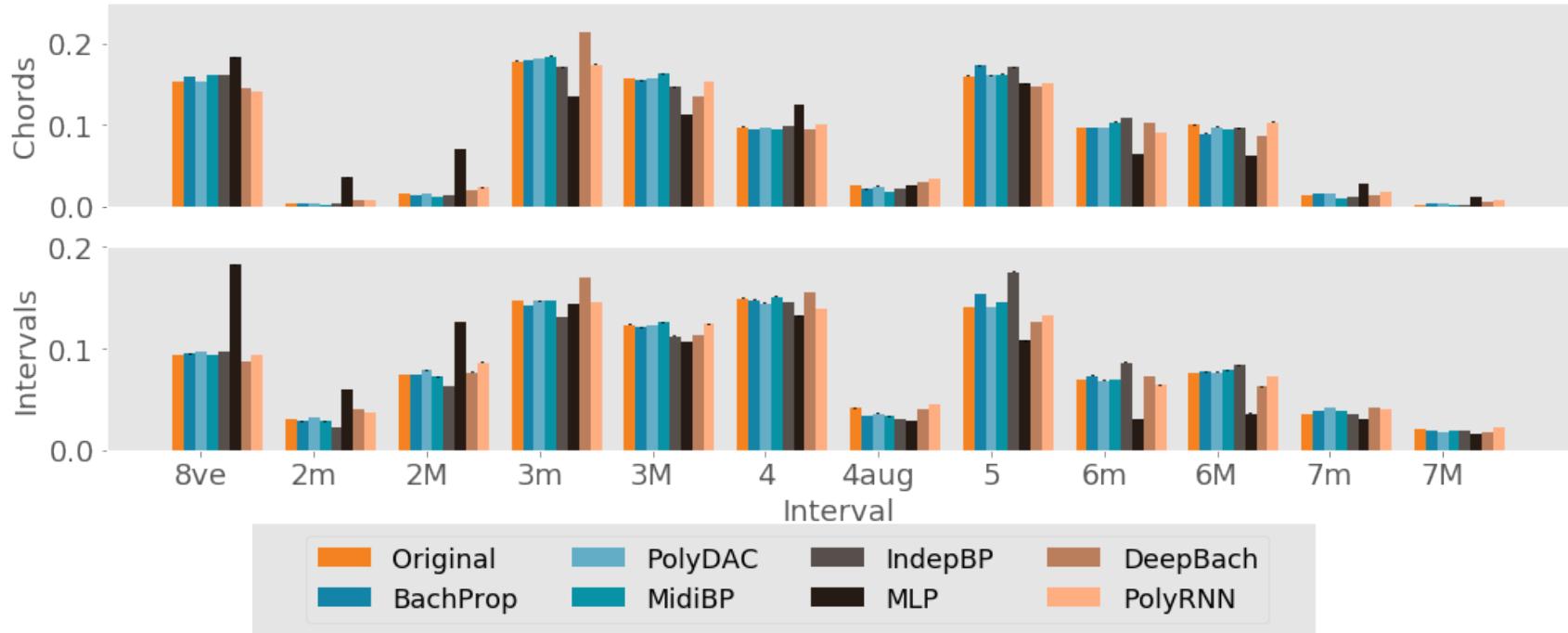
# Evaluation | Lengths



# Evaluation | Rhythms



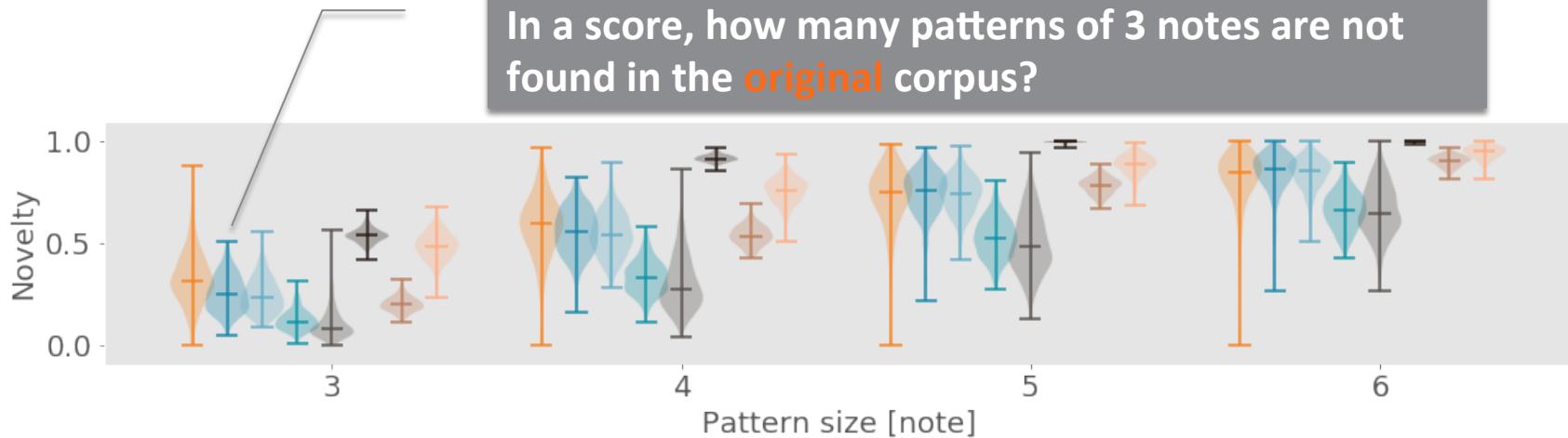
# Evaluation | Intervals





# Evaluation | Originality

In a score, how many patterns of 3 notes are not found in the **original** corpus?

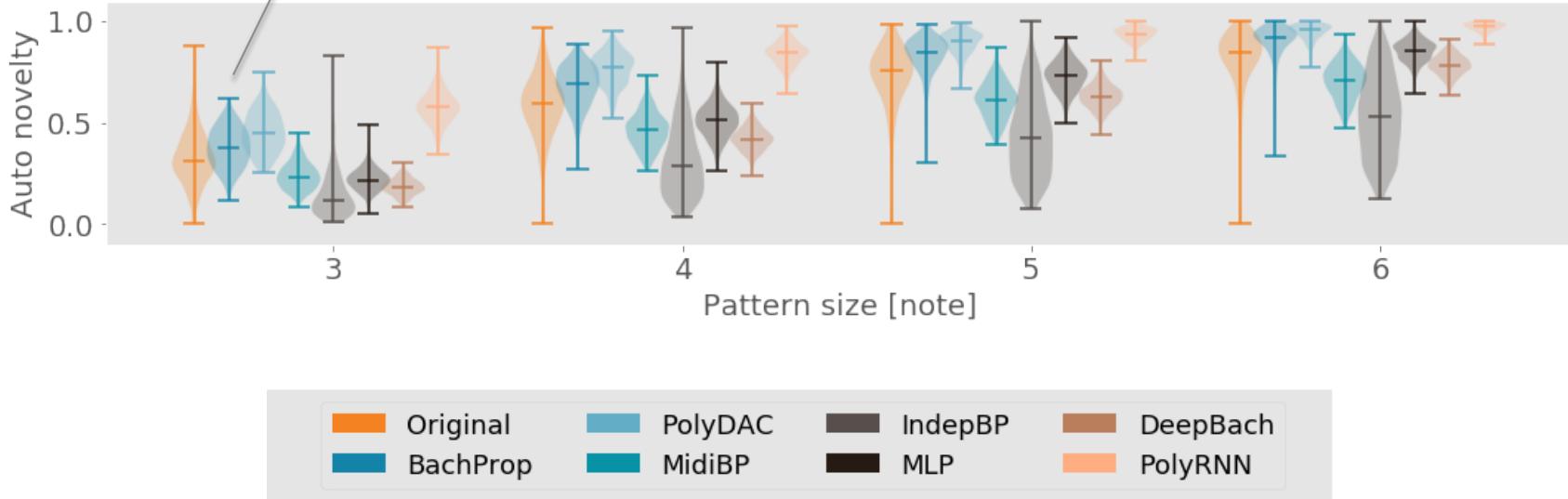


Original	PolyDAC	IndepBP	DeepBach
BachProp	MidiBP	MLP	PolyRNN



# Evaluation | Diversity

In a score, how many patterns of 3 notes are not found in the rest of the corpus?

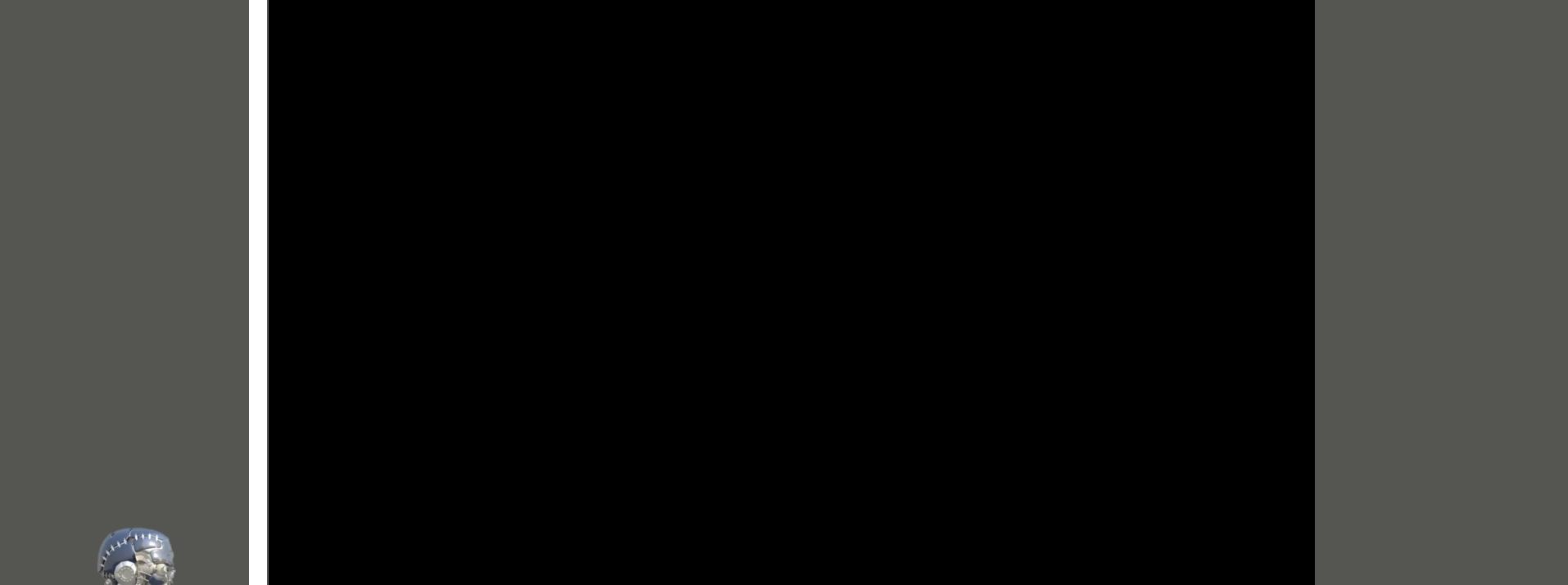


# Evaluation | Take Home Message

- Plagiarism-free music (*creativity*)
  - ▣ Novelty profiles
- Predefined style or mood
  - ▣ Training on a *homogeneous* dataset
  - ▣ Comparative statistics
- Pleasant to listen to
  - ▣ Subjective evaluation
- Diversity in generated pieces
  - ▣ Auto-novelty

# Contributions

1. Note-sequence based representation of music with minimal distortion of the rhythm for training neural network models
2. A network architecture that learns to generate pleasant music in this representation
3. A set of metrics to compare generative models that operate on different representations of music



Live interpretation | Ada String Quartet

[sites.google.com/view/bachprop/](https://sites.google.com/view/bachprop/)

Youtube Florian Colombo

# What's next?

- Repetitions are intrinsic to music
  - ▣ Probabilistic models are by design bad at generating repetitions
    - Structured generation
    - Higher order grammar
    - Attention mechanisms
- Improving the model with future direction information
  - ▣ Condition on harmony progression

# Aims of Grammar-ANNs Interaction

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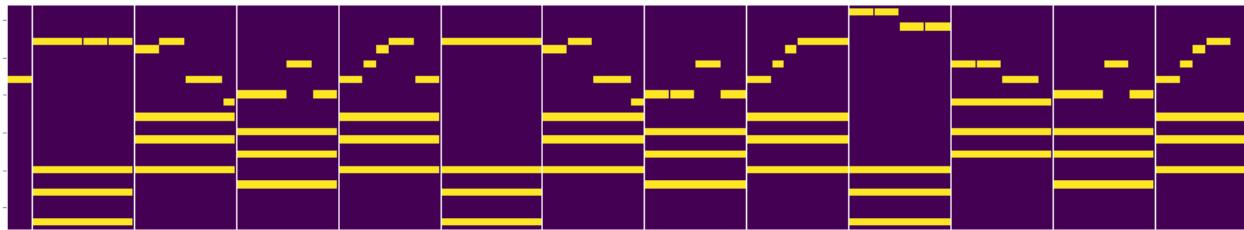
- Improve quality/structure of generated music by constraining the rules of generation
- thereby keeping the activity and dynamics of the networks in *comfortable* states
- And preventing mistakes that could bring the networks in *uncomfortable* states

# Structured Generation | Algorithm

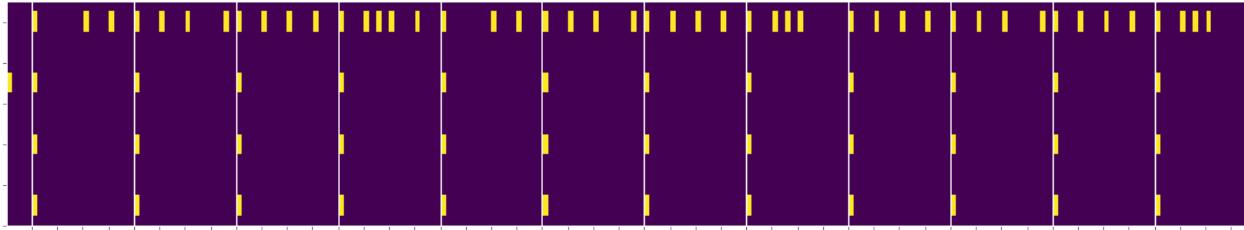
1. Compute reference repetition profiles
2. Impose the reference dT repetition profile to generate a new dT sequence from the dT network
3. Given this new dT sequence, impose the reference T repetition profile to generate a new T sequence from the T network
4. Given these new dT and T sequences, impose the reference P repetition profile to generate a new P sequence from the P network

# Repetition Profile | dT Example

- Automatic upbeat and metric extraction



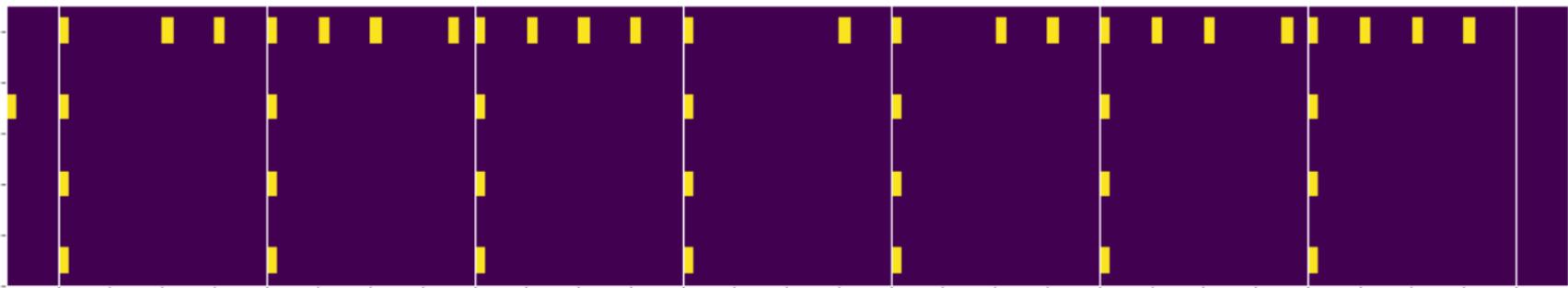
- Repetition profile is extracted by comparing bars



[0    0    0    0    1    2    3    0    3    2    3    8]

# Structured Generation | dT

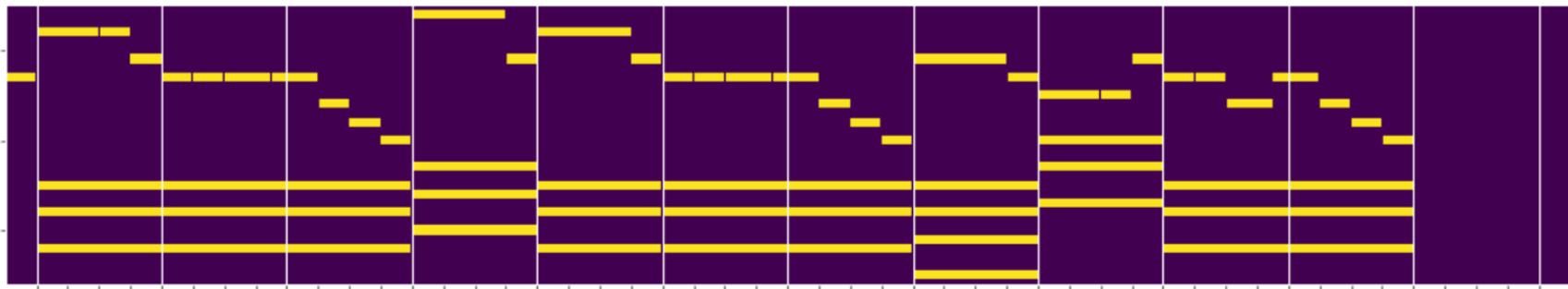
```
[0, 0, 0, 0, 1, 2, 3]  
[0, 3, 2, 3, 8]
```



```
Updating hidden state: 100%|██████████| 46/46 [00:04<00:00, 10.40it/s]  
Generating continuation: 100%|██████████| 64/64 [00:06<00:00, 9.81it/s]
```

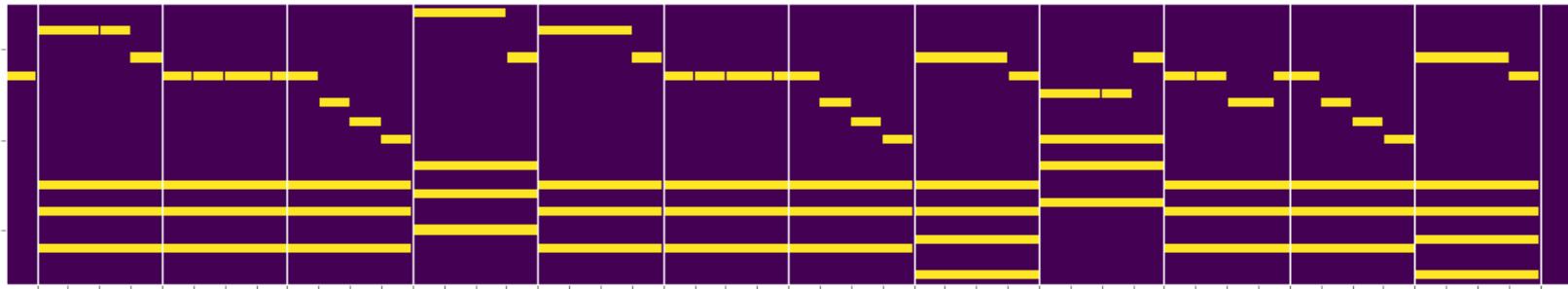
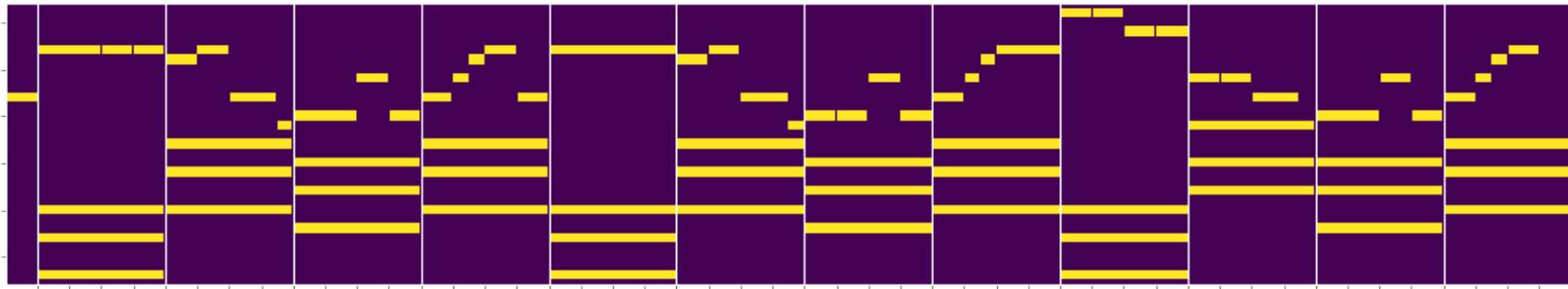
# Structured Generation | P

```
[0, 0, 0, 0, 1, 2, 3, 0, 0, 0, 3]  
[8]
```



Generating a P continuation | dT: 100% | 80/80 [00:14<00:00, 5.44it/s]

# Reference vs Generated



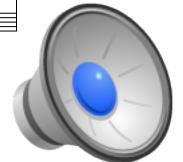
# Structured generation | Examples

Gigue  $\text{♩} = 104$

This musical score consists of four staves: Violin (Vln), Violin (Vln), Alto (Alt.), and Cello/Bassoon (Vlc). The music is in G major (two sharps) and common time. The first section (measures 1-4) features the Vlns playing eighth-note patterns, while the Alt. and Vlc provide harmonic support. The second section (measures 5-8) continues with similar patterns, with the Vlc taking a more prominent role. The third section (measures 9-12) returns to the initial pattern. Measure numbers 5, 9, and 12 are explicitly marked.

Gigue  $\text{♩} = 104$

This musical score is identical to the one above, featuring the same four instruments (Vln, Vln, Alt., Vlc) in G major at  $\text{♩} = 104$ . It consists of three sections of eight measures each, with measure numbers 7 and 14 explicitly marked. The instrumentation and harmonic patterns remain consistent with the first score.



# Structured generation | Examples

Choral  $\text{♩} = 72$

This musical score consists of four staves: Violin (Vln), Violin (Vln), Alto (Alt.), and Bassoon (Vlc.). The key signature is three flats, and the time signature is common time. The tempo is marked as Choral  $\text{♩} = 72$ . The music features eighth-note patterns with grace notes and sustained notes. Measure numbers 6 and 5 are visible at the beginning of each staff respectively.



Choral  $\text{♩} = 72$

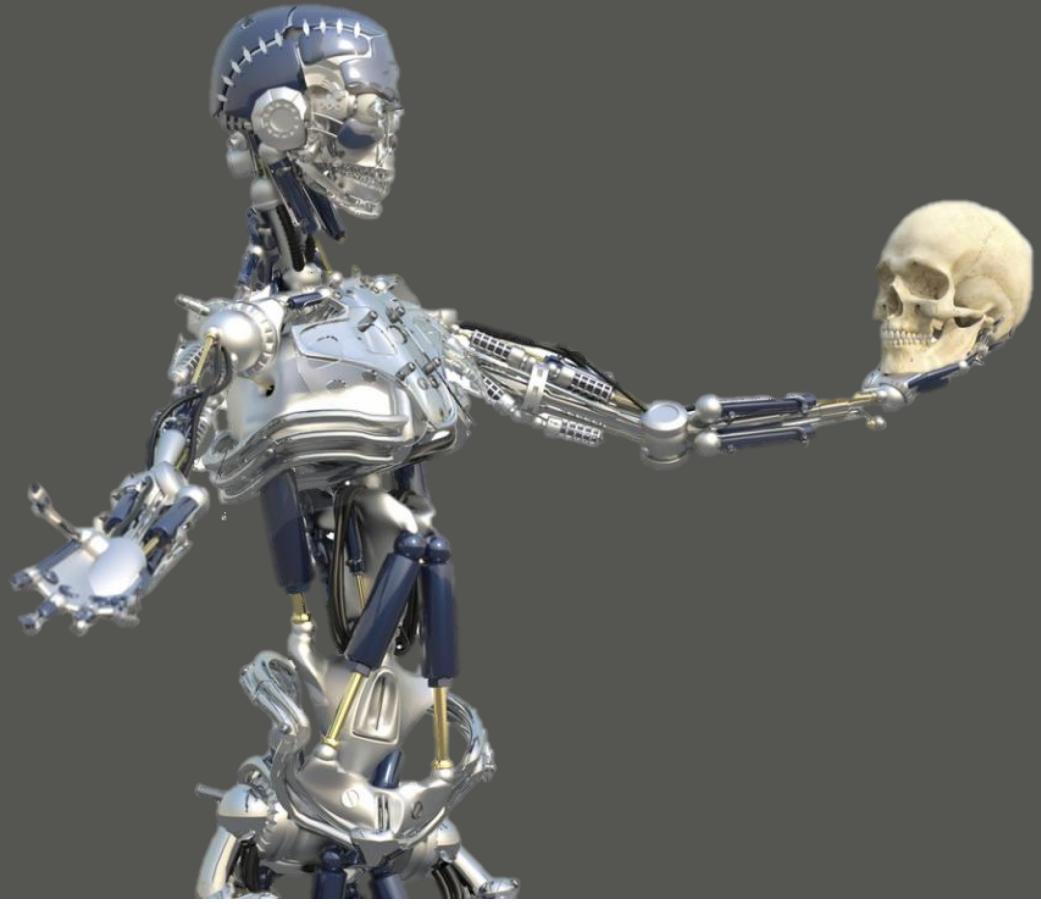
This musical score consists of four staves: Violin (Vln), Violin (Vln), Alto (Alt.), and Bassoon (Vlc.). The key signature is three flats, and the time signature is common time. The tempo is marked as Choral  $\text{♩} = 72$ . The music features eighth-note patterns with grace notes and sustained notes. Measure numbers 5 and 6 are visible at the beginning of each staff respectively.



Thanks for your attention!

Wulfram Gerstner

Johanni Brea  
Samuel P. Muscinelli



QUESTIONS?

# Link to exercises and slides



<https://github.com/FlorianColombo/MagliasoMusic2019>