

# Undo and Redo Support for Replicated Registers

A Guided Research Project with Martin Kleppmann

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Leo Stewen

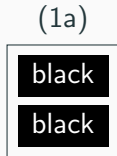
October, 2023

1. Semantics of Undo and Redo with Multiple Users
2. Algorithm
3. Evaluation
4. Future Work

# Semantics of Undo and Redo with Multiple Users

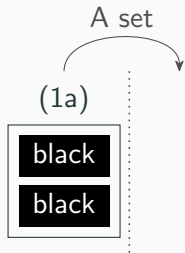
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# Two Registers



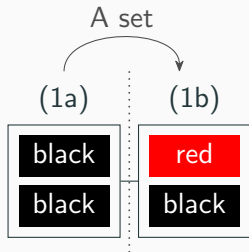
**Figure 1:** Canvas with two Replicated Registers.

## Two Registers



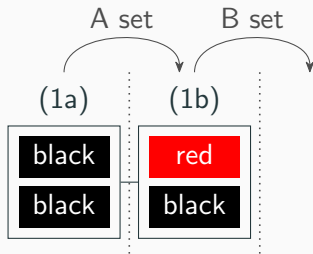
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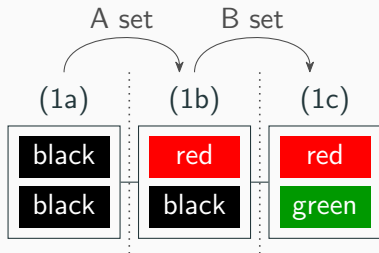
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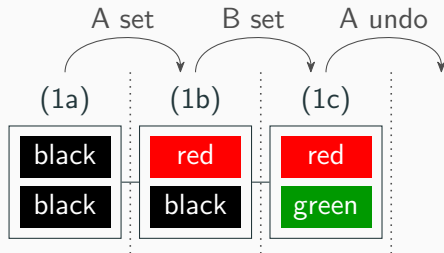
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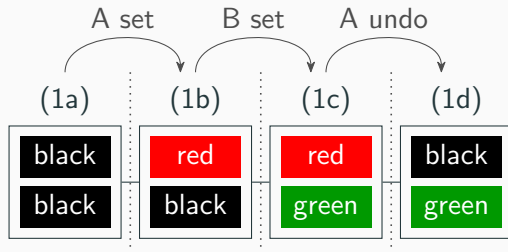


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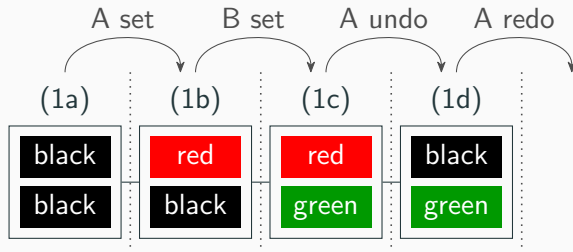
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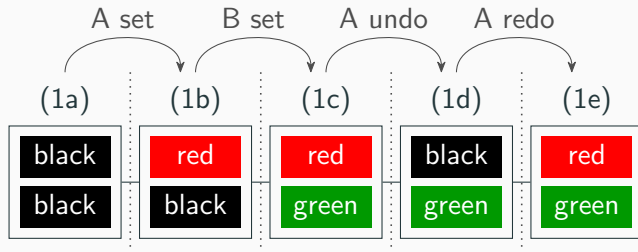
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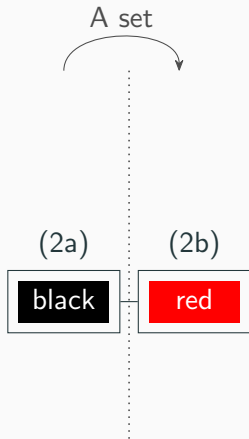
**Figure 2:** Canvas with one Replicated Register.

# One Register



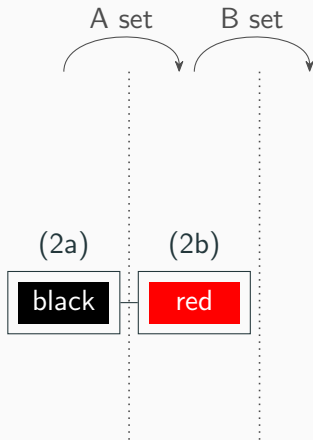
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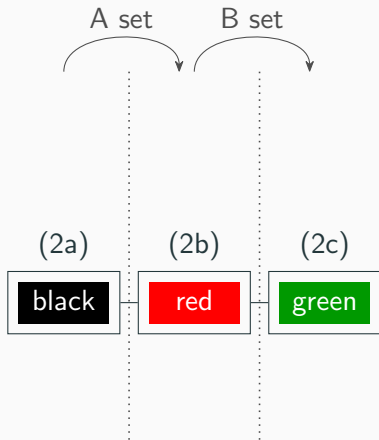
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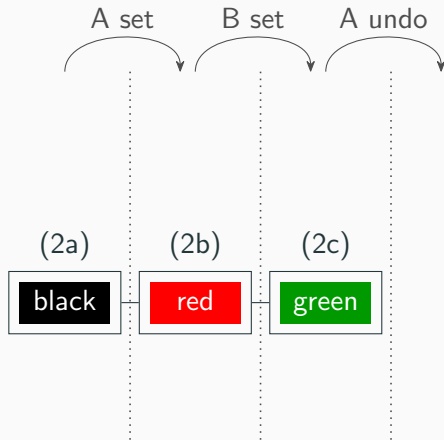


# One Register



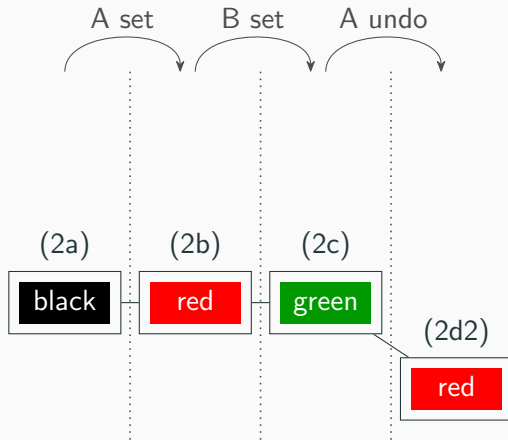
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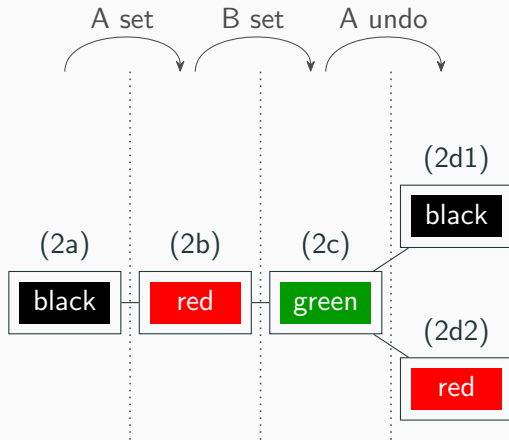
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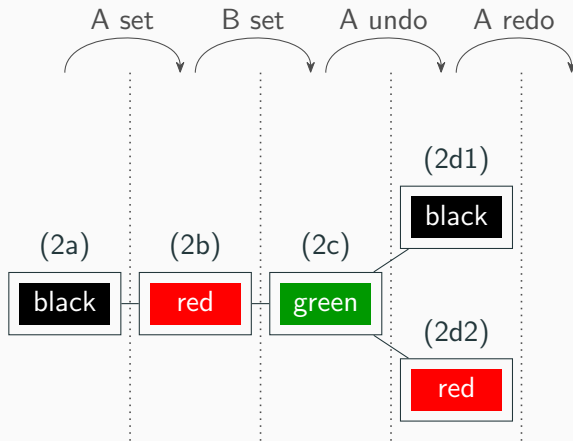
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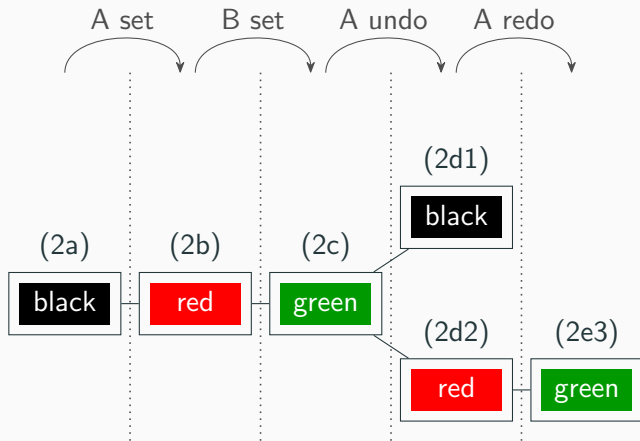
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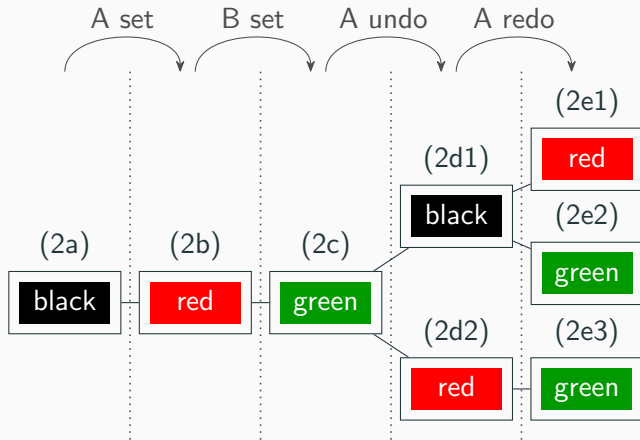
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# A Taxonomy of Undo Behavior

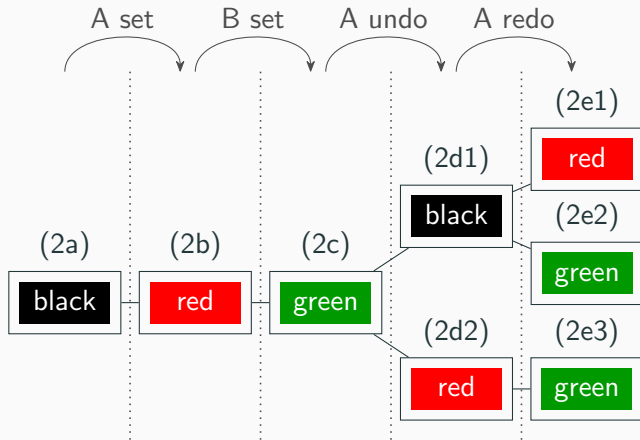
	Generating Replica	Any Replica
Reverse Chronological	local undo	global undo
Selective	revert <sup>1</sup>	

<sup>1</sup>often called *selective undo* in the literature



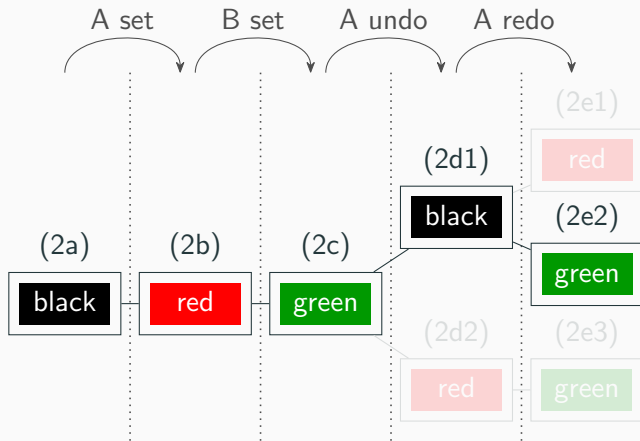
## Local Undo and Global Redo

# One Register



**Figure 3:** Canvas with one Replicated Register.

# One Register



**Figure 3:** Canvas with one Replicated Register.

# Algorithm

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# Exemplary Operation History

Register: [1]



**Figure 4:** An operation history with undo and redo. Internally, both undo and redo operations are *RestoreOps*. Their respective anchor operations are indicated by blue dashed arrows.

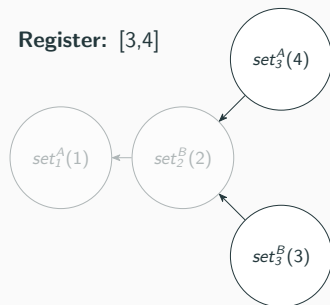
# Exemplary Operation History

Register: [2]



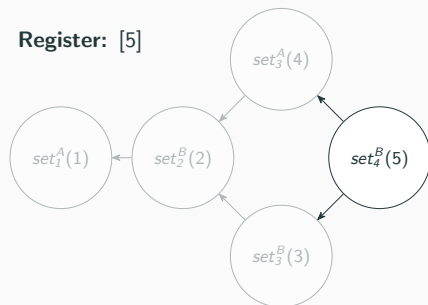
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# Exemplary Operation History



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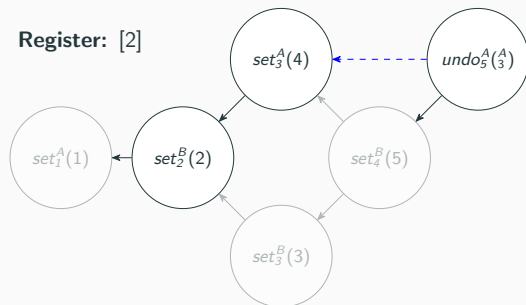
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**Figure 4:** An operation history with undo and redo. Internally, both undo and redo operations are *RestoreOps*. Their respective anchor operations are indicated by blue dashed arrows.

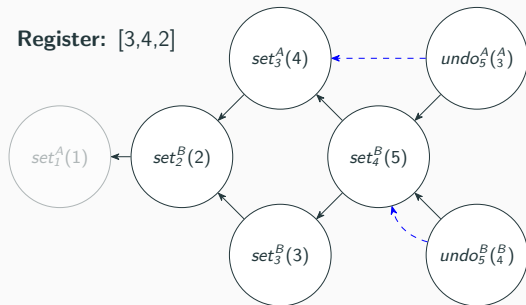


# Exemplary Operation History



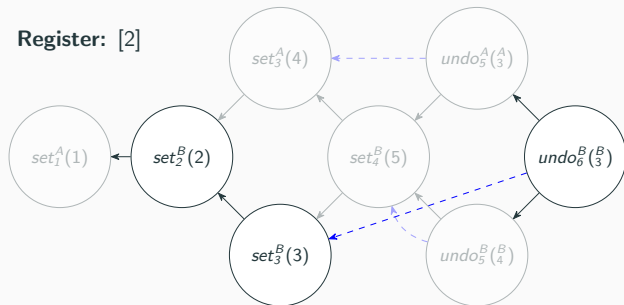
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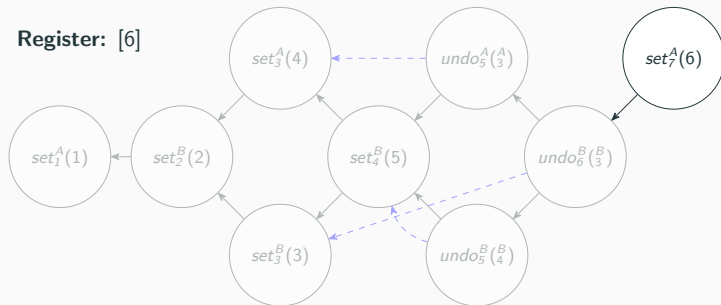
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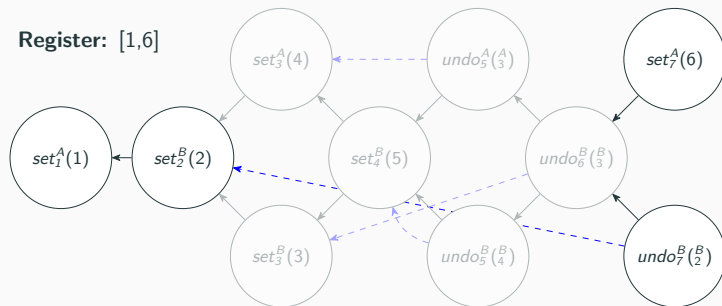
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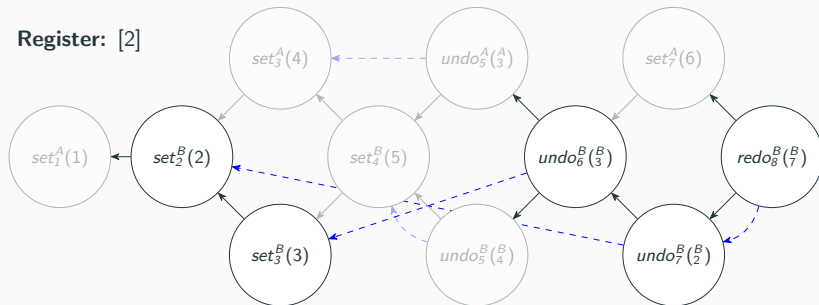
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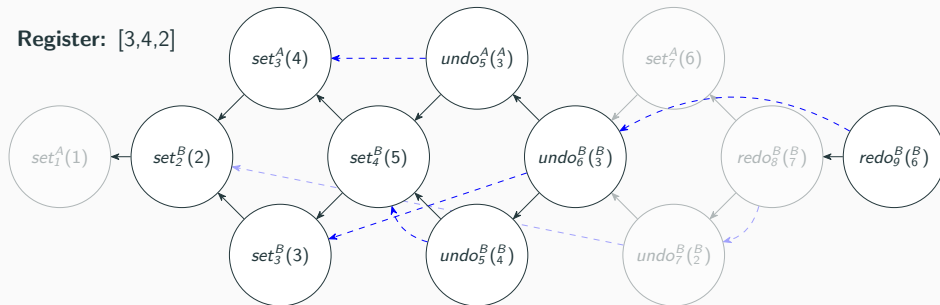
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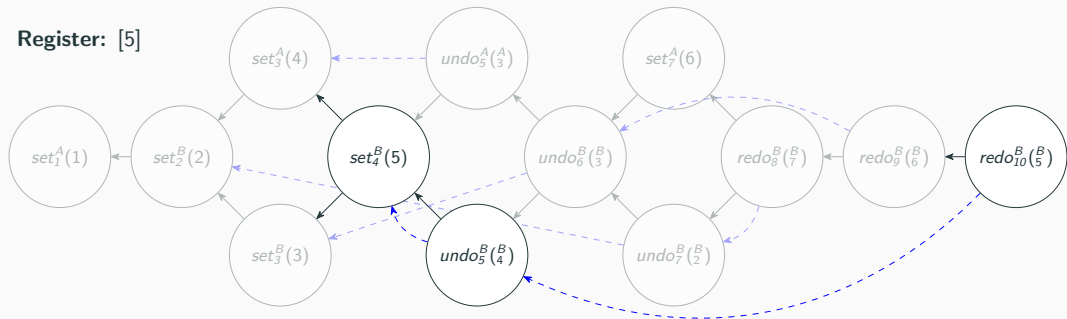
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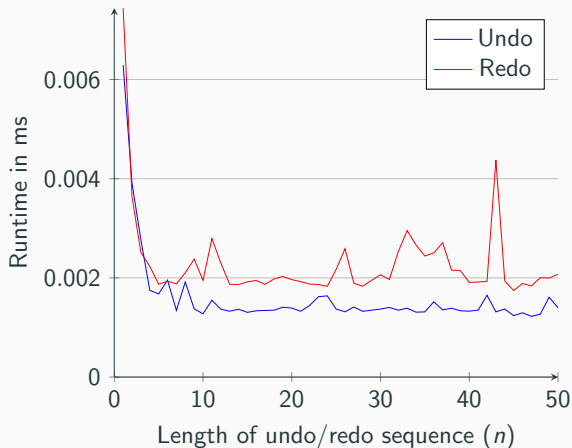
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# Evaluation

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## Common Editing Scenario (Constant Runtime)



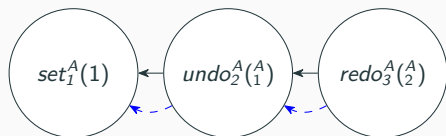
**Figure 5:** Runtime of the last undo/redo operation in a sequence of  $n$  consecutive undo/redo operations.

## Degenerate Editing Scenario



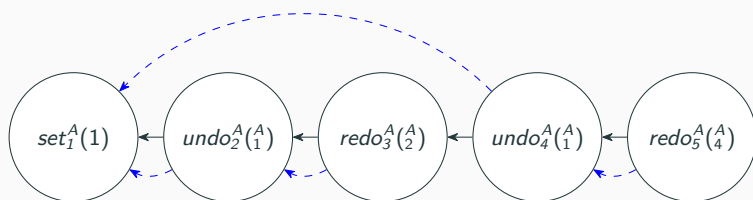
**Figure 6:** Sequence of alternating undo-redo operations.

## Degenerate Editing Scenario



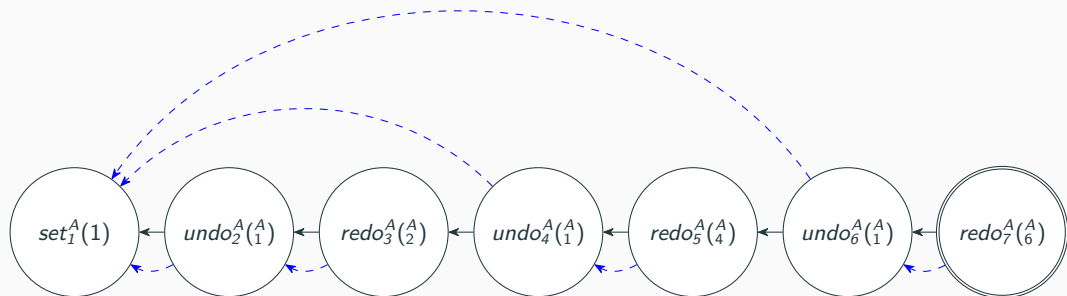
**Figure 6:** Sequence of alternating undo-redo operations of length 1.

## Degenerate Editing Scenario



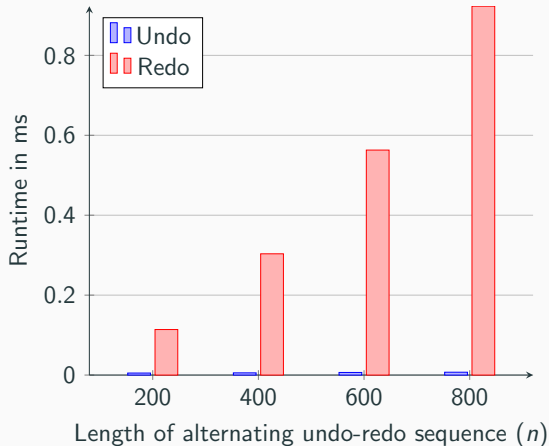
**Figure 6:** Sequence of alternating undo-redo operations of length 2.

## Degenerate Editing Scenario



**Figure 6:** Sequence of alternating undo-redo operations of length 3.

## Degenerate Editing Scenario (Linear Runtime)



**Figure 7:** Runtime of the last undo/redo operation in a sequence of alternating undo-redo operations of length  $n$ .

## Future Work

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- Integration with Automerge (the Counter CRDT...)
- How does undo and redo work with text CRDTs?
- Support other kinds of undo: selective undo, global undo?

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## Questions? Feedback?

Reach me at [lstwn@mailbox.org](mailto:lstwn@mailbox.org)