

# Machine Learning - Assignment II

## Linear regression

Souhaib BEN TAIEB

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Note: It is strongly recommended to read Sections 3.1 to 3.4 in ISLR. Also, please provide justifications for every step you take in your derivations.

### Question 1

Do Exercise 7 in Chapter 3.7 in ISLR.

### Question 2

Read Section 3.6.2 in ISLR.

Do Exercise 8 in Chapter 3.7 in ISLR. For 8(c), look only at the plot which gives the residuals vs fitted values.

### Question 3

Do Exercise 9 (a), (b), (c), (e) and (f) in Chapter 3.7 in ISLR.

### Question 4

Read Section 3.5 in ISLR.

Let us assume we observe a dataset  $\mathcal{D} = \{(x_i, y_i)\}_{i=1}^n$  where the  $x_i$  are fixed (not random) and  $y_i = f(x_i) + \varepsilon_i$  with  $E[\varepsilon_i] = 0$  and  $E[\varepsilon_i^2] = \sigma^2$ .

If we let the  $k$ th nearest neighbor of  $x_0$  be  $x_k$  for  $k = 1, 2, \dots, K$  and  $K \geq 1$ , the prediction of the KNN regression algorithm for a point  $x_0$  can be written as

$$\hat{f}(x_0) = \frac{1}{K} \sum_{i=1}^K y_i.$$

- (a) What is the squared bias?
- (b) What is the variance?
- (c) What is the mean squared error?

## TURN IN

- Your .Rmd file (which should knit without errors and without assuming any packages have been pre-loaded)
- Your pdf file that results from knitting the Rmd.
- DUE: April 19, 11:55pm (late submissions not allowed), loaded into Moodle