

IMAGE FILTERING

Szeliski, Chapter 3.1-3.2, 4.2

内 容

- 滤波的基本思想
- 均值（Box），高斯（Gaussian），中值（Median），双边（Bilateral）滤波处理图像后的效果
- Sobel边缘检测的基本原理
- OpenCV 实现

QUESTION: 去除噪音

- How?



IMAGE FILTERING (图像滤波)

- Modify the pixels in an image based on some function of a local neighborhood of each pixel
- Linear Filtering (线性滤波)
 - Replace each pixel by a linear combination (a weighted sum) of its neighbors
- The prescription for the linear combination is called the “kernel” (核) (or “mask”, “filter”)

10	5	3
4	6	1
1	1	8

Local image data

0	0	0
0	0.5	0
0	1	0.5

kernel

	8	

Modified image data

MEAN FILTER (均值滤波)

1	1	1
1	1	1
1	1	1



H

0	0	0	0	0	0	0	0	0	0
0	0	0	0	0	0	0	0	0	0
0	0	0	90	90	90	90	90	0	0
0	0	0	90	90	90	90	90	0	0
0	0	0	90	90	90	90	90	0	0
0	0	0	90	0	90	90	90	0	0
0	0	0	90	90	90	90	90	0	0
0	0	0	0	0	0	0	0	0	0
0	0	0	0	0	0	0	0	0	0
0	0	0	0	0	0	0	0	0	0

F

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	0	10	20	30	30	30	20	10	
	0	20	40	60	60	60	40	20	
	0	30	60	90	90	90	60	30	
	0	30	50	80	80	90	60	30	
	0	30	50	80	80	90	60	30	
	0	20	30	50	50	60	40	20	
10	20	30	30	30	30	30	20	10	
10	10	10	0	0	0	0	0	0	

G



Original

0	0	0
0	1	0
0	0	0



Filtered
(no change)



Original

0	0	0
0	0	1
0	0	0

?



Original

0	0	0
0	0	1
0	0	0



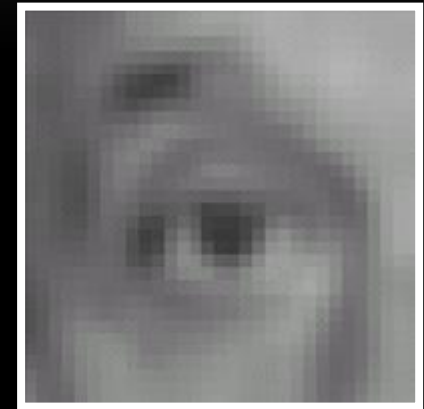
Shifted left
By 1 pixel

EXAMPLE, 模糊



Original

1	1	1
1	1	1
1	1	1



Blur (with a box filter)

EXAMPLE, 锐化



Original



0	0	0
0	2	0
0	0	0

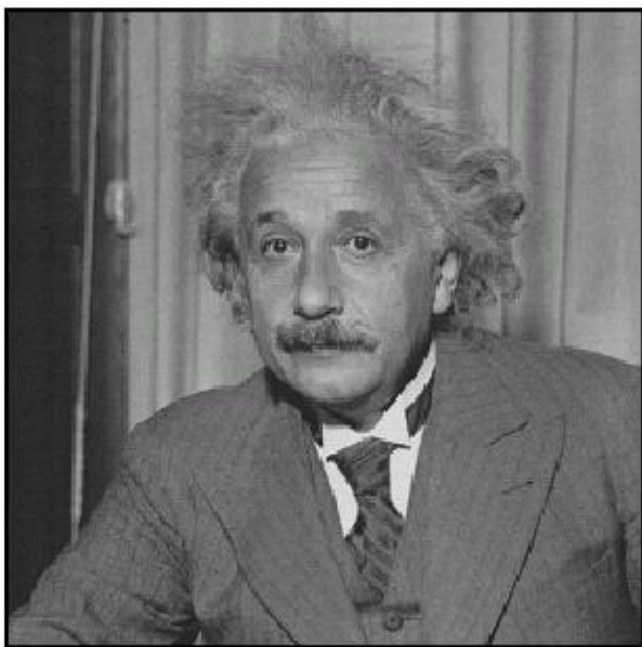


1	1	1
1	1	1
1	1	1

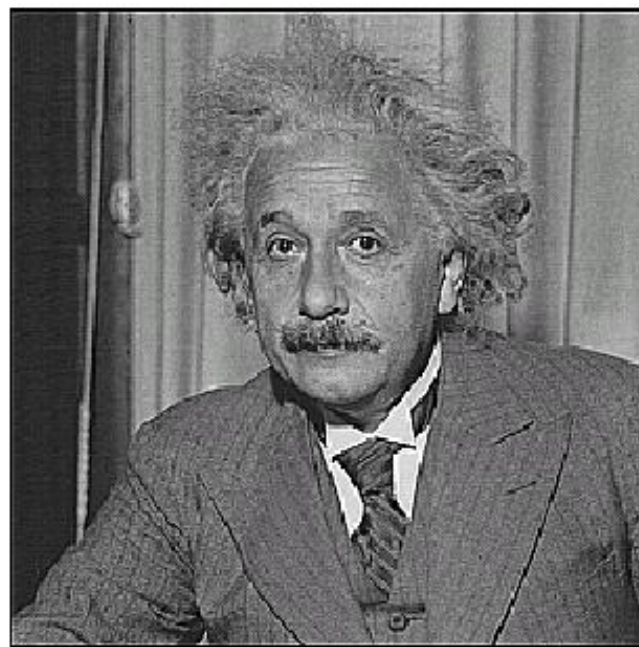


Sharpening filter
(accentuates edges)

SHAPENING 锐化

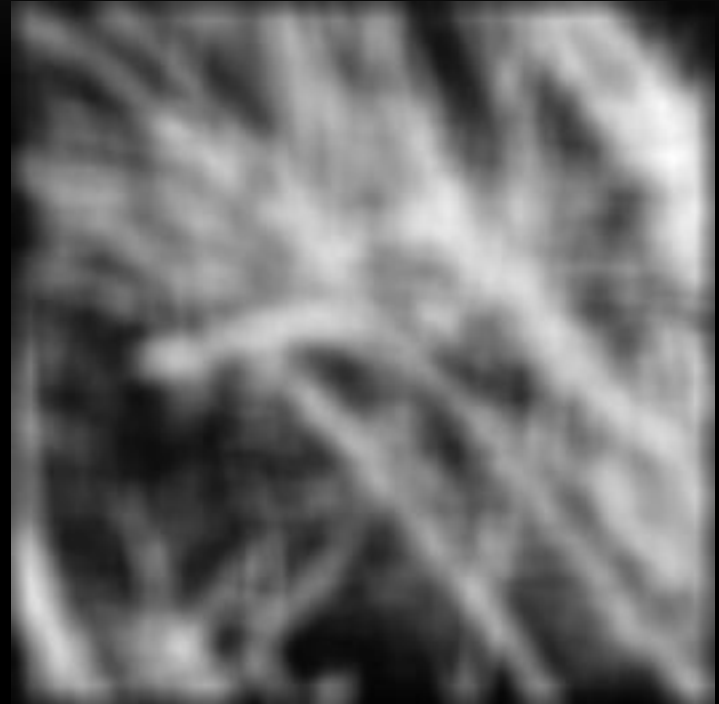
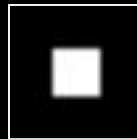


before

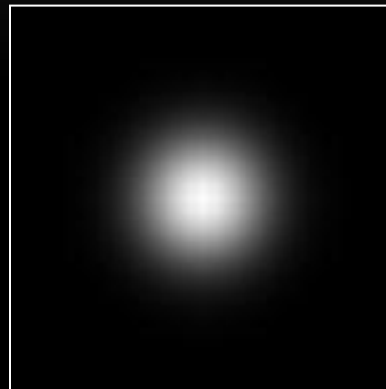
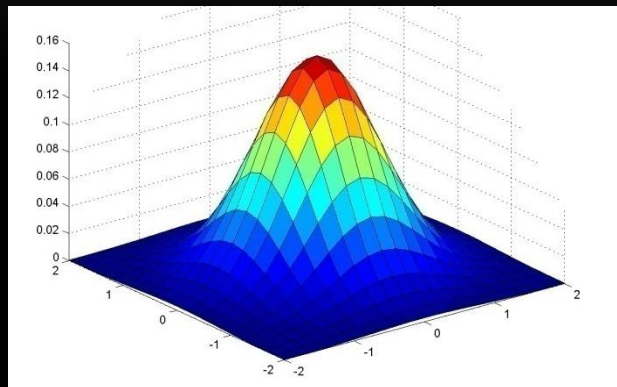


after

BOX FILTER



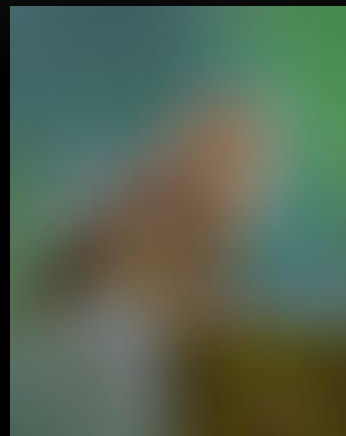
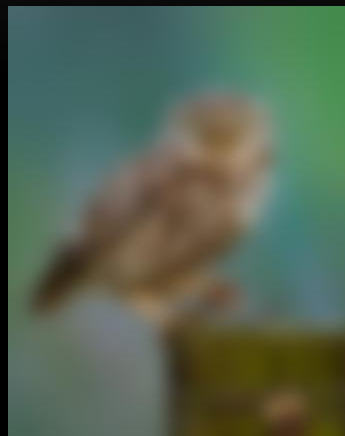
GAUSSIAN FILTER (高斯滤波)





$$G_{\sigma} = \frac{1}{2\pi\sigma^2} e^{-\frac{(x^2+y^2)}{2\sigma^2}}$$

0.003	0.013	0.022	0.013	0.003
0.013	0.059	0.097	0.059	0.013
0.022	0.097	0.159	0.097	0.022
0.013	0.059	0.097	0.059	0.013
0.003	0.013	0.022	0.013	0.003

5 x 5, $\sigma = 1$



 = 1 pixel

 = 5 pixels

 = 10 pixels

 = 30 pixels



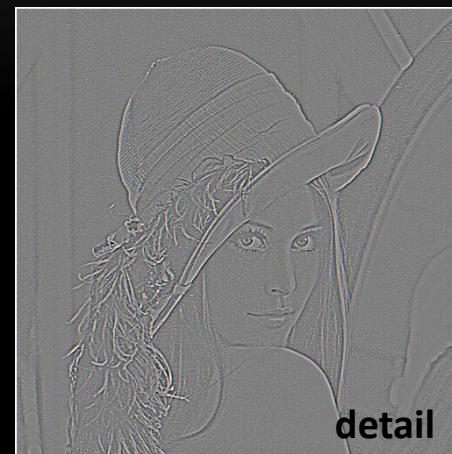
APPLICATIONS 应用



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Let's add it back:



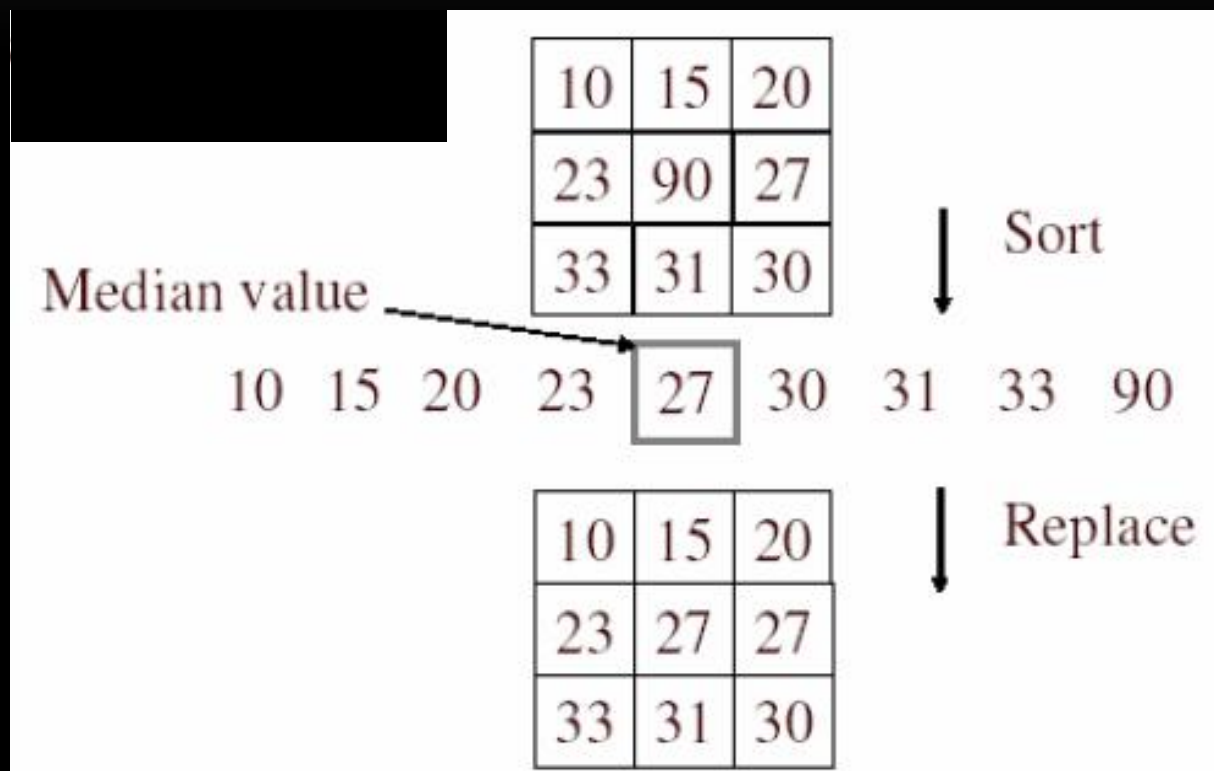
+ α



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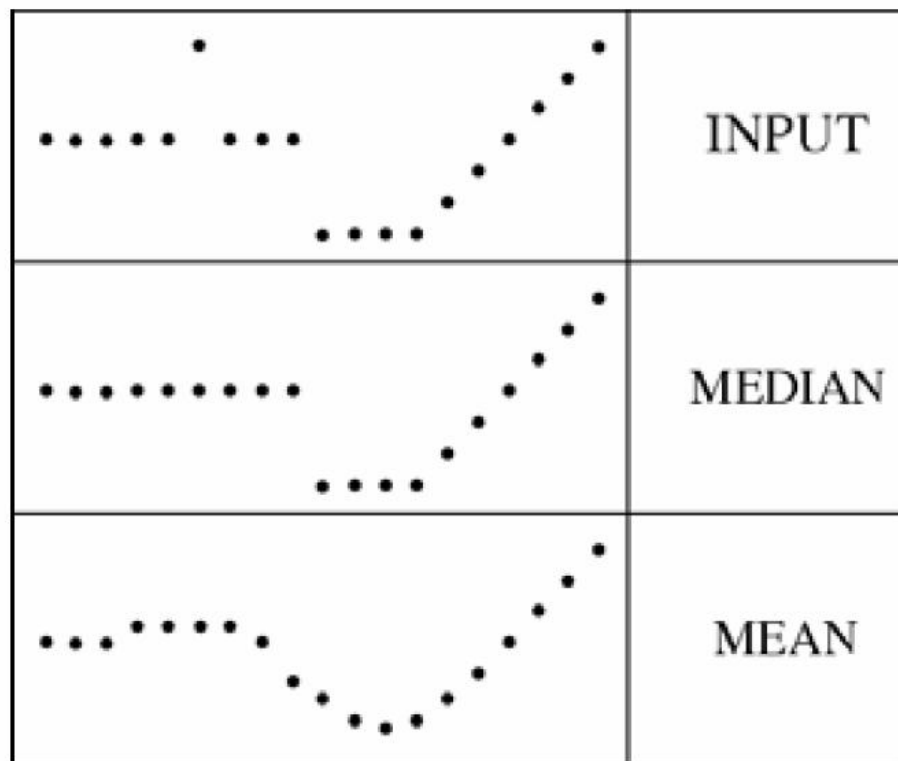
MEDIAN FILTER 中值滤波



• 是否线性滤波？

抗 噪 音

filters have width 5 :



3x3

5x5

7x7

Gaussian

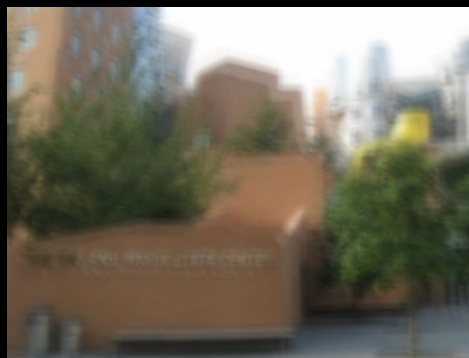


Median



特殊的滤波核

Camera shake



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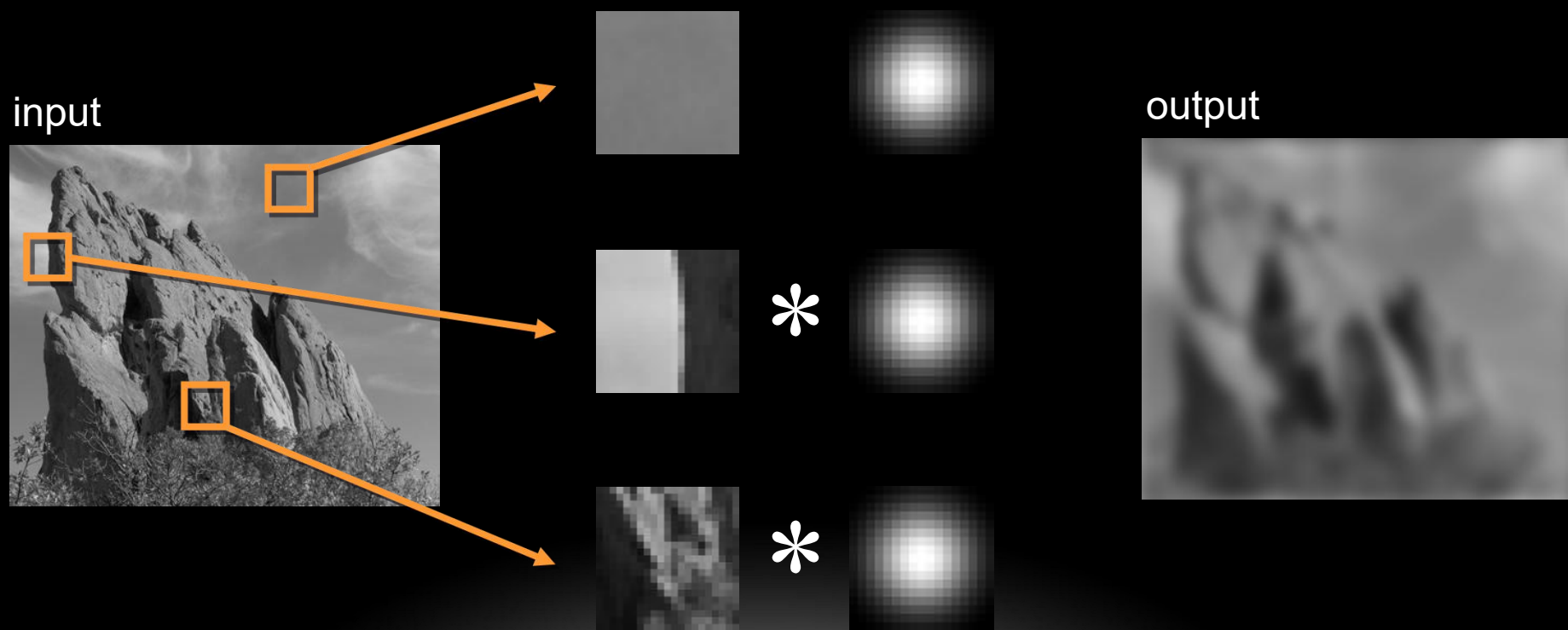


Source: Fergus, *et al.* "Removing Camera Shake from a Single Photograph", SIGGRAPH 2006

EDGE-AWARE FILTER (边缘保持滤波)

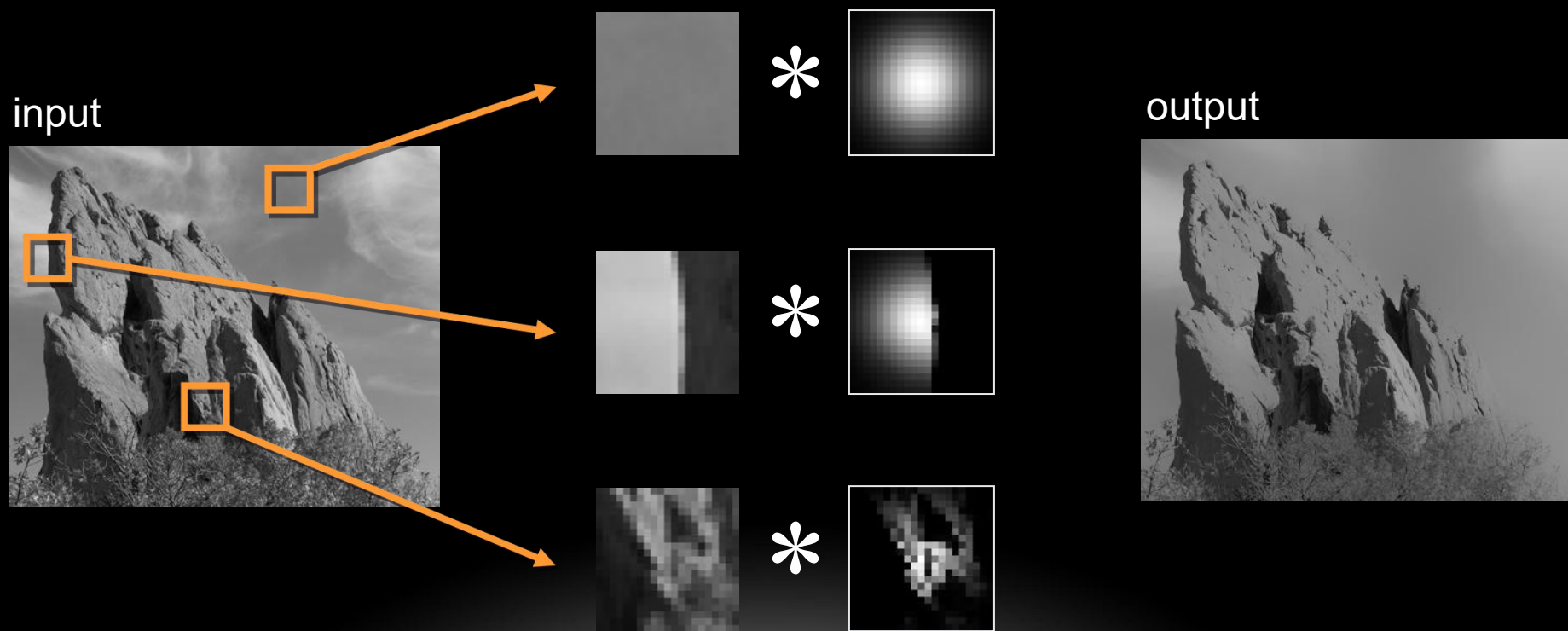
- Bilateral Filter (双边滤波)
- Guided Image Filter (导向图滤波)

高斯滤波



Same Gaussian kernel everywhere.

双边滤波

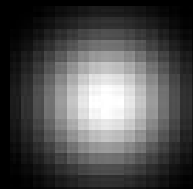


The kernel shape depends on the image content.

Same idea: **weighted average of pixels.**

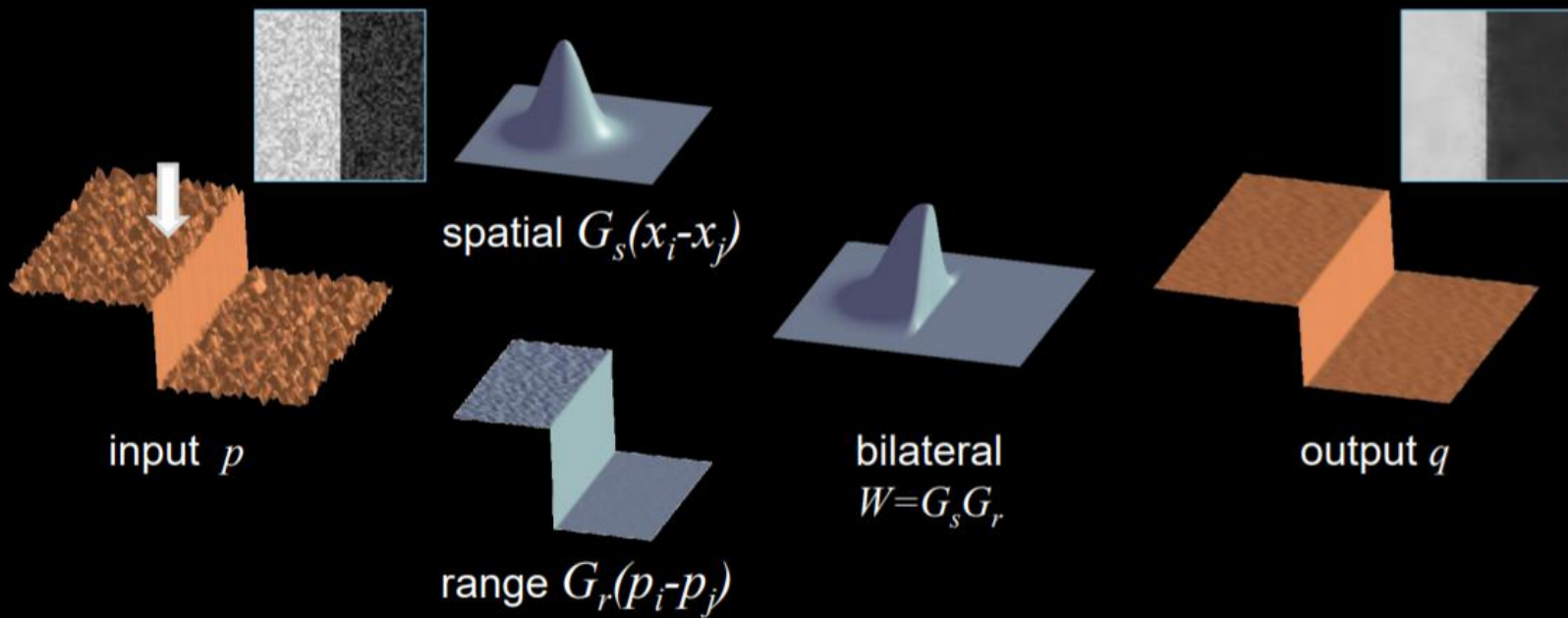
$$BF[I]_p = \overset{\text{new}}{\frac{1}{W_p}} \sum_{q \in S} \overset{\text{not new}}{G_{\sigma_s}(\|p - q\|)} \overset{\text{new}}{G_{\sigma_r}(\|I_p - I_q\|)} I_q$$

normalization factor
space weight
range weight



- Bilateral filter

$$q_i = \sum_{j \in N(i)} W_{ij}(p) p_j$$



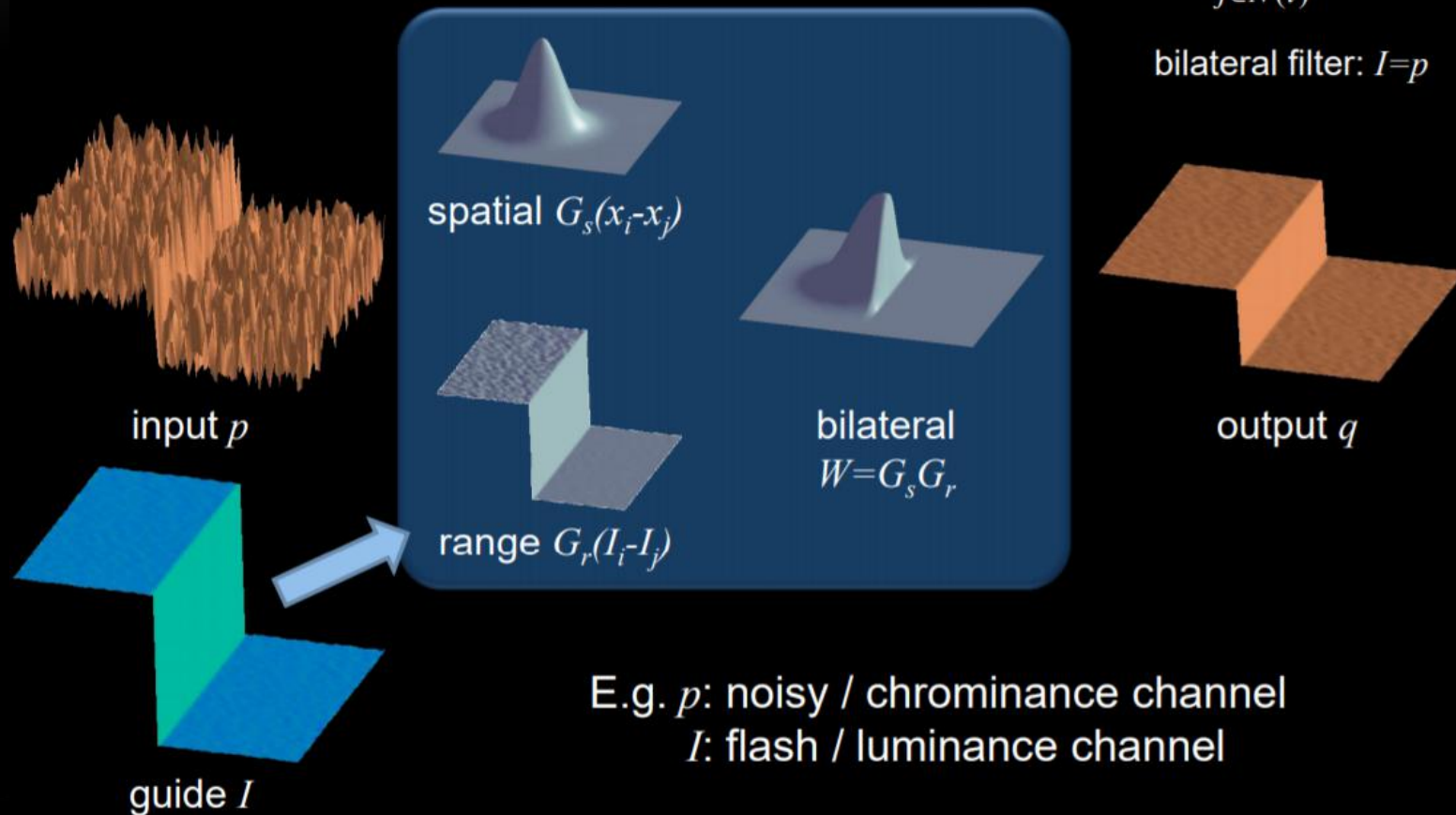
双边滤波的扩展

- 两个滤波核中，空间计算与图像无关，而颜色值计算与图像相关
- 能否利用其他图像的颜色值作为参考，处理双边滤波，会达到什么效果？

- Joint bilateral filter [Petschnigg et al. 2004]

$$q_i = \sum_{j \in N(i)} W_{ij}(I) p_j$$

bilateral filter: $I=p$



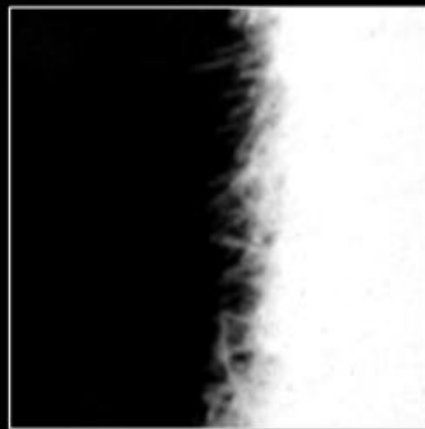
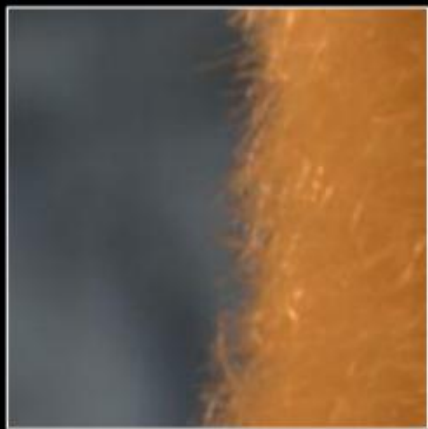
结果



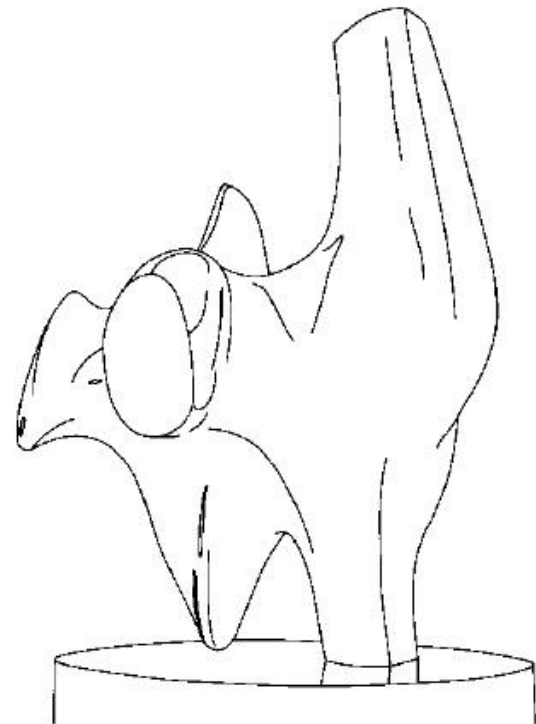
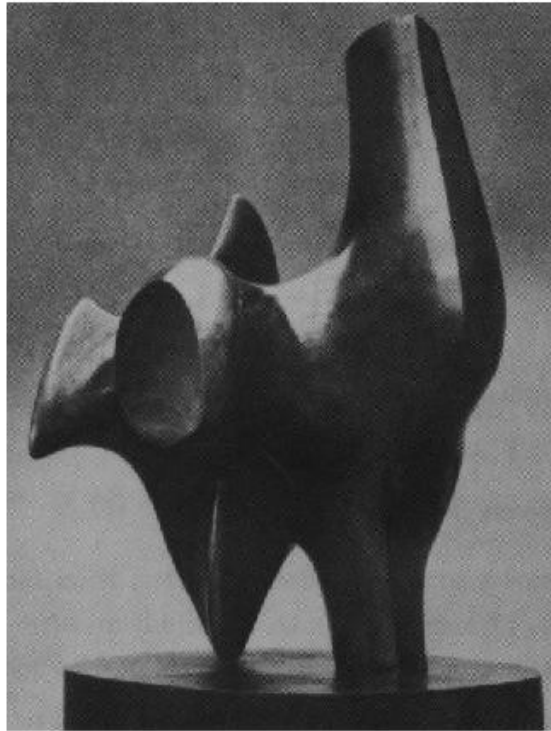
存在的问题

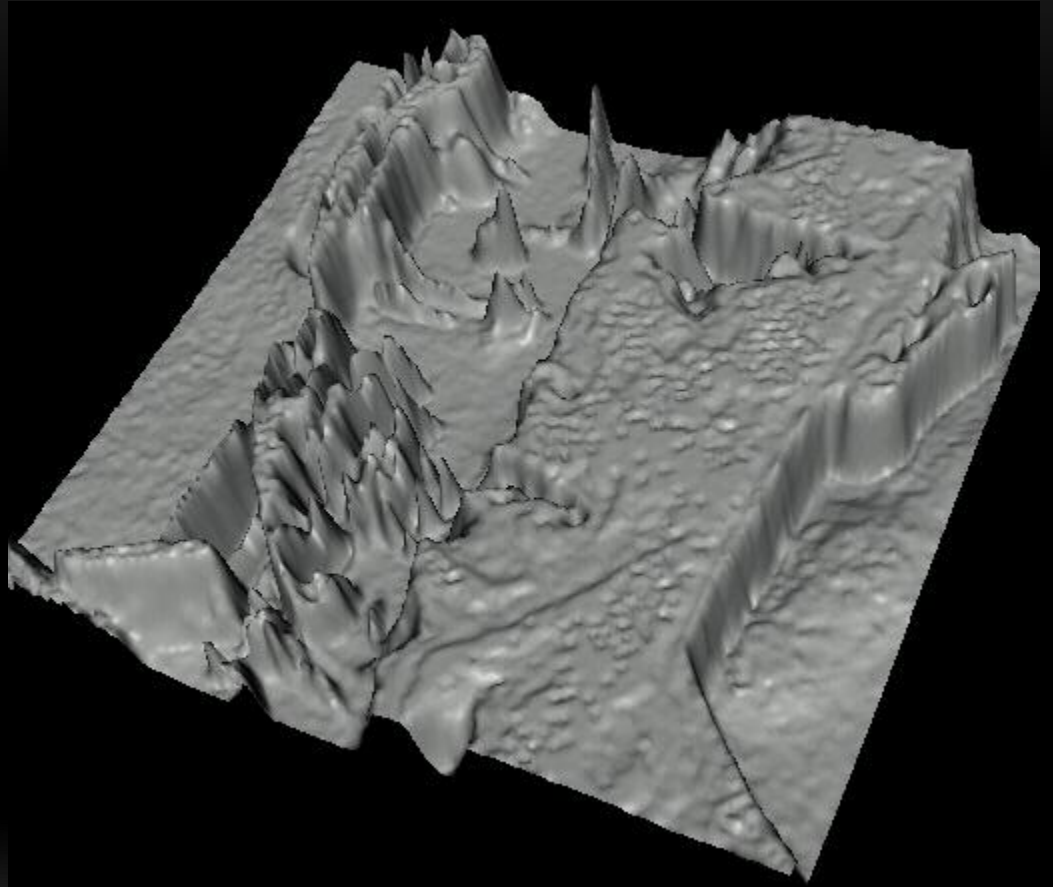
- 计算速度很慢
- 梯度变形

GUIDED IMAGE FILTER (导向图滤波)



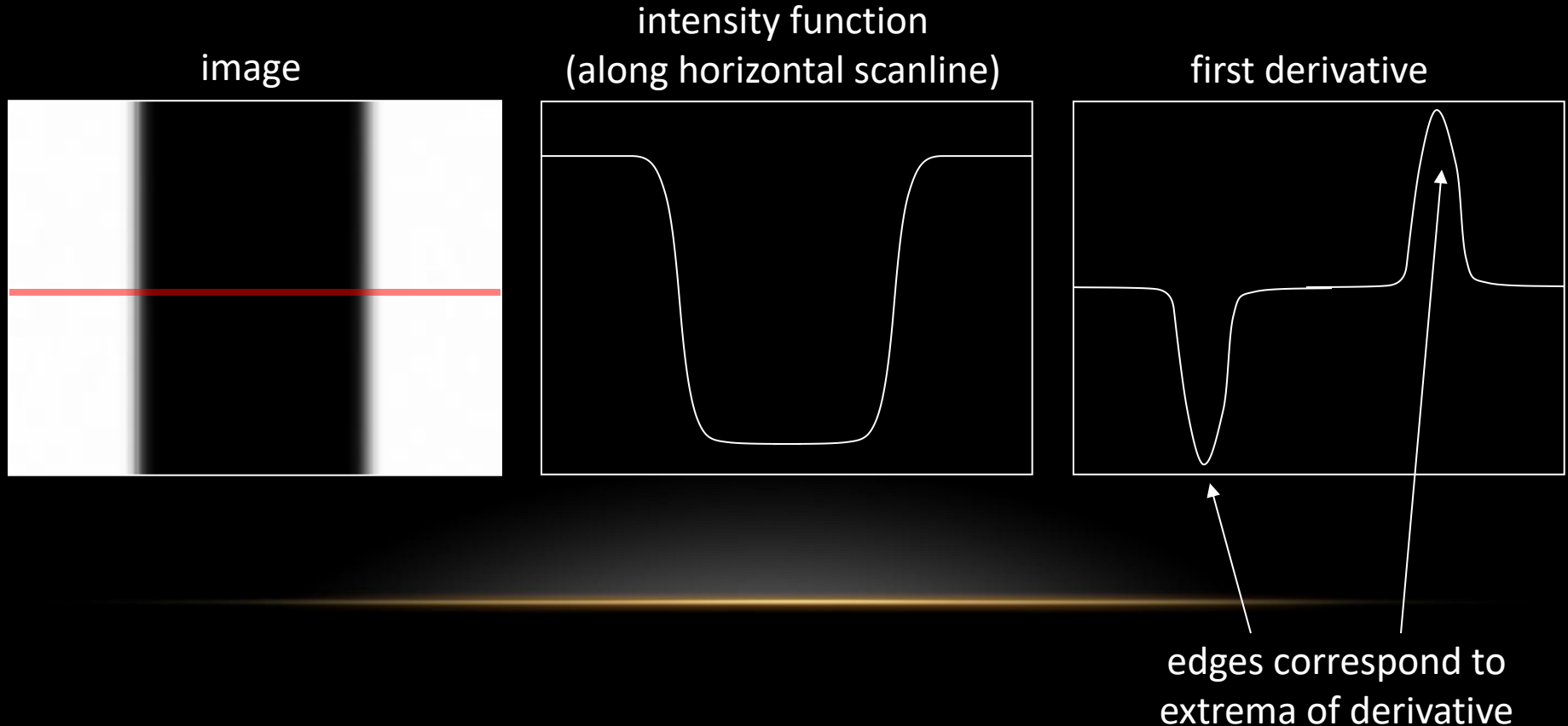
EDGE DETECTOR (边缘检测)





EDGE

- An edge is a place of *rapid change* in the image intensity function



THE SOBEL OPERATOR

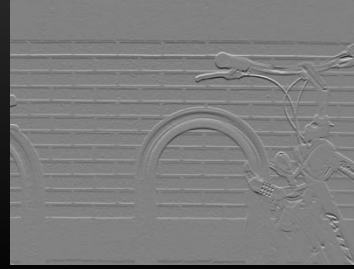
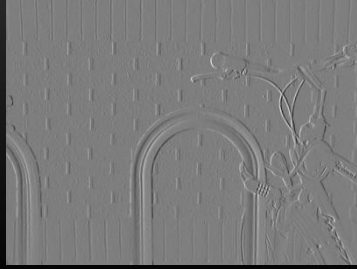
- The standard defn. of the Sobel operator omits the $1/8$ term
 - doesn't make a difference for edge detection
 - the $1/8$ term **is** needed to get the right gradient magnitude

$$\frac{1}{8} \begin{bmatrix} -1 & 0 & 1 \\ -2 & 0 & 2 \\ -1 & 0 & 1 \end{bmatrix}$$

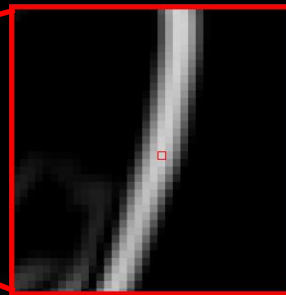
S_x

$$\frac{1}{8} \begin{bmatrix} 1 & 2 & 1 \\ 0 & 0 & 0 \\ -1 & -2 & -1 \end{bmatrix}$$

S_y



Source: Wikipedia



where is the edge?

CANNY EDGE DETECTOR

- Good Detection, Localization
- Single Response (清晰的边界线)

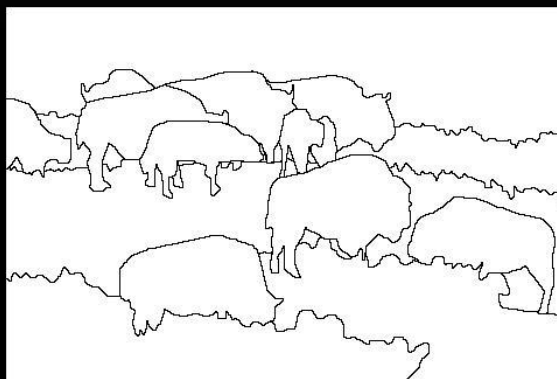


简单的边缘检测远远不够

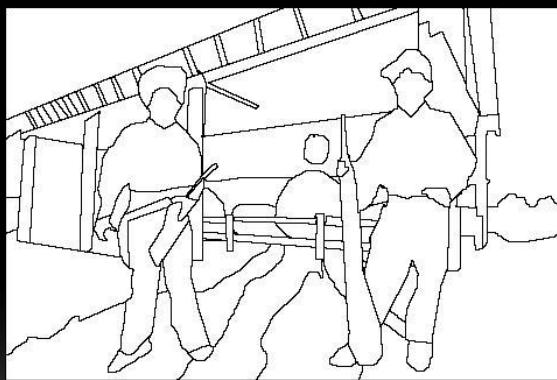
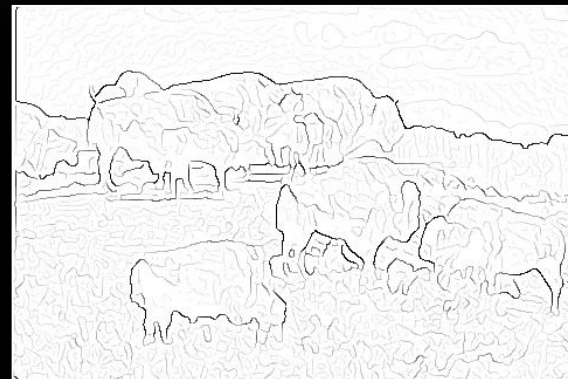
image



human segmentation



gradient magnitude



OPENCV EXAMPLES

- 上述方法均存在对应函数
- 作业
 - 使用OpenCV函数实现各种滤波计算
 - 根据方法思想实现对像素操作，完成上述滤波方法