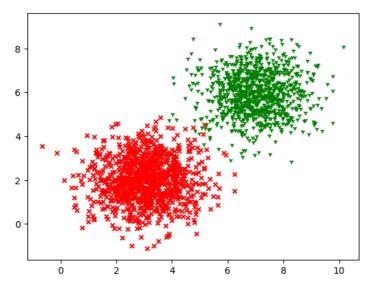
```
import tensorflow as tf
import matplotlib.pyplot as plt
import numpy as np
import keras
from keras.models import Sequential
from keras.layers import Dense
Zbiór danych:
x_{label1} = np.random.normal(3, 1, 1000)
y_label1 = np.random.normal(2, 1, 1000)
x_{label2} = np.random.normal(7, 1, 1000)
y_label2 = np.random.normal(6, 1, 1000)
xs = np.append(x_label1, x_label2)
ys = np.append(y_label1, y_label2)
labels = np.asarray([0.]*len(x_label1)+[1.]*len(x_label2))
plt.scatter(x_label1, y_label1, c='r', marker='x', s=20)
plt.scatter(x_label2, y_label2, c='g', marker='1', s=20)
plt.show()
```



Funkcja błędu (entropia krzyżowa):

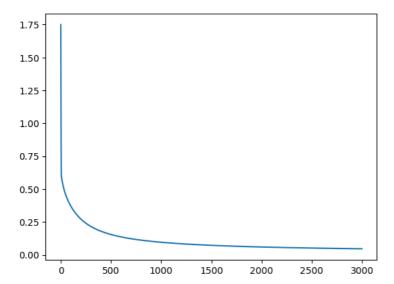
```
def loss_fn(label, label_model):
    return tf.reduce_mean(-label*tf.math.log(label_model)-(1-label)*tf.math.log(1-label_model))
```

Początkowe wartości parametrów i pętla ucząca:

```
import random
a = tf.Variable(random.random())
b = tf.Variable(random.random())
c = tf.Variable(random.random())
Loss = []
epochs = 3000
lr = 0.1
for _ in range(epochs):
 with tf.GradientTape() as tape:
    #predykcja modelu
    pred_y = tf.sigmoid(a * xs + b * ys + c)
    #policzenie błędu
    loss = loss_fn(labels, pred_y)
    #zapisanie aktualnej wartości błędu
    Loss.append(loss.numpy())
  dloss_da, dloss_db, dloss_dc = tape.gradient(loss,(a, b,c))
  a.assign_sub(lr*dloss_da) #a = a - alpha*dloss_da
  b.assign_sub(lr*dloss_db) #b = b - alpha*dloss_db
  c.assign_sub(lr*dloss_dc)
```

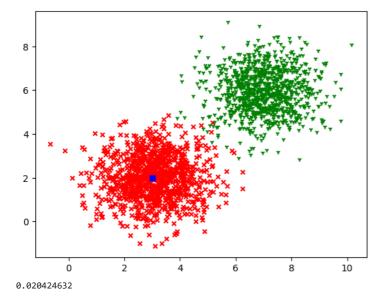
plt.show()

```
אפאטאכפט.ט
plt.plot(Loss)
```



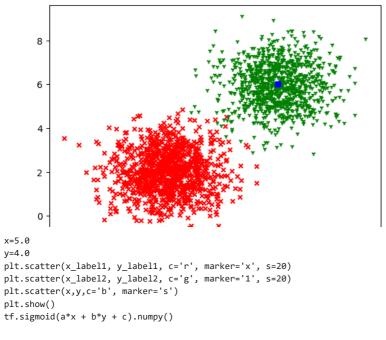
Sprawdzamy dla pewnego punktu:

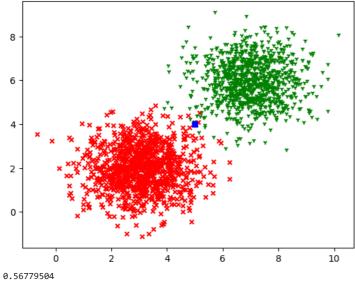
```
x=3.0
y=2.0
plt.scatter(x_label1, y_label1, c='r', marker='x', s=20)
plt.scatter(x_label2, y_label2, c='g', marker='1', s=20)
plt.scatter([x],[y],c='b', marker='s')
plt.show()
#print(a,b,c)
tf.sigmoid(a*x + b*y + c).numpy()
```



```
{\sf tf.sigmoid(a*x + b*y + c).numpy()}
```

```
x=7.0
y=6.0
plt.scatter(x_label1, y_label1, c='r', marker='x', s=20)
plt.scatter(x_label2, y_label2, c='g', marker='1', s=20)
plt.scatter(x,y,c='b', marker='s')
plt.show()
tf.sigmoid(a*x + b*y + c).numpy()
```



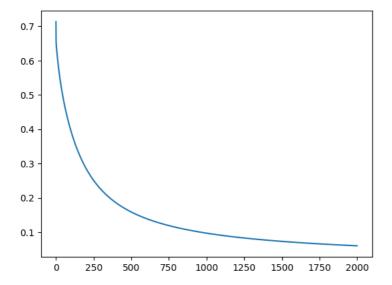


▼ Ilość epok 2000

```
import random
a = tf.Variable(random.random())
b = tf.Variable(random.random())
c = tf.Variable(random.random())
Loss = []
epochs = 2000
lr = 0.1
for _ in range(epochs):
 with tf.GradientTape() as tape:
    #predykcja modelu
    pred_y = tf.sigmoid(a * xs + b * ys + c)
    #policzenie błędu
    loss = loss_fn(labels, pred_y)
    #zapisanie aktualnej wartości błędu
    Loss.append(loss.numpy())
  dloss_da, dloss_db, dloss_dc = tape.gradient(loss,(a, b,c))
  a.assign_sub(lr*dloss_da) #a = a - alpha*dloss_da
  b.assign_sub(lr*dloss_db) #b = b - alpha*dloss_db
  c.assign_sub(lr*dloss_dc)
```

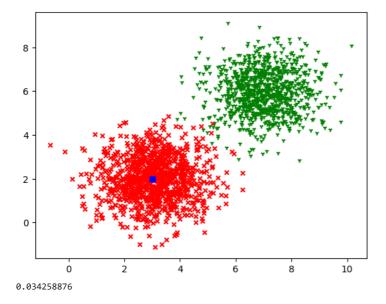
```
, סנסטעסעט.ט
. . . 1
```

```
plt.plot(Loss)
plt.show()
```



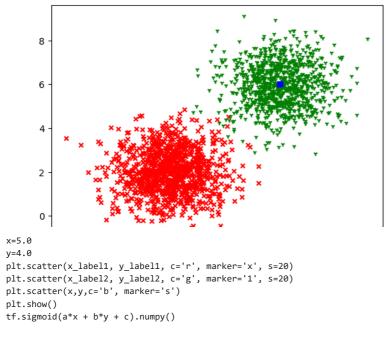
Sprawdzamy dla pewnego punktu:

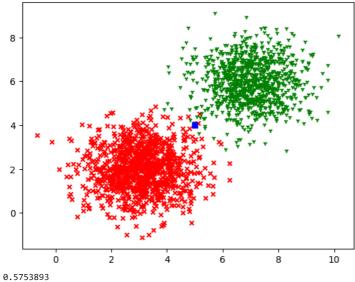
```
x=3.0
y=2.0
plt.scatter(x_label1, y_label1, c='r', marker='x', s=20)
plt.scatter(x_label2, y_label2, c='g', marker='1', s=20)
plt.scatter([x],[y],c='b', marker='s')
plt.show()
#print(a,b,c)
tf.sigmoid(a*x + b*y + c).numpy()
```



```
{\sf tf.sigmoid(a*x + b*y + c).numpy()}
```

```
x=7.0
y=6.0
plt.scatter(x_label1, y_label1, c='r', marker='x', s=20)
plt.scatter(x_label2, y_label2, c='g', marker='1', s=20)
plt.scatter(x,y,c='b', marker='s')
plt.show()
tf.sigmoid(a*x + b*y + c).numpy()
```



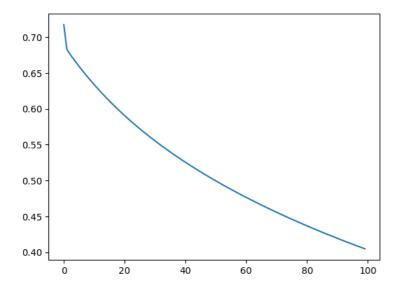


▼ Ilosc epok 100

```
import random
a = tf.Variable(random.random())
b = tf.Variable(random.random())
c = tf.Variable(random.random())
Loss = []
epochs = 100
lr = 0.1
for _ in range(epochs):
  with tf.GradientTape() as tape:
    #predykcja modelu
    pred_y = tf.sigmoid(a * xs + b * ys + c)
    #policzenie błędu
    loss = loss_fn(labels, pred_y)
    #zapisanie aktualnej wartości błędu
    Loss.append(loss.numpy())
  dloss_da, dloss_db, dloss_dc = tape.gradient(loss,(a, b,c))
  a.assign_sub(lr*dloss_da) #a = a - alpha*dloss_da
  b.assign_sub(lr*dloss_db) #b = b - alpha*dloss_db
  c.assign_sub(lr*dloss_dc)
Loss
      0.51997524,
      0.51729715,
      0.5146541,
      0.512045,
      0.5094691,
      0.5069253.
      0.50441265,
      0.5019304,
      0.4994777,
      0.49705383,
      0.4946579,
      0.4922893,
      0.48994732,
      0.4876313,
```

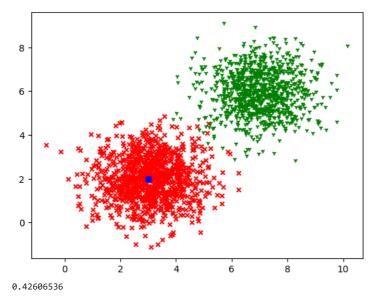
```
0.400291,
0.404724721
```

```
plt.plot(Loss)
plt.show()
```



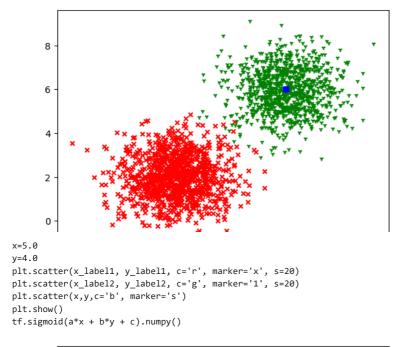
Sprawdzamy dla pewnego punktu:

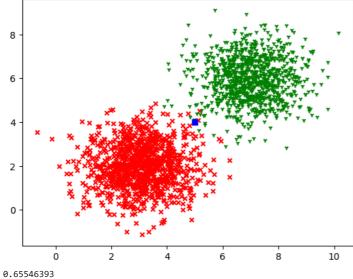
```
x=3.0
y=2.0
plt.scatter(x_label1, y_label1, c='r', marker='x', s=20)
plt.scatter(x_label2, y_label2, c='g', marker='1', s=20)
plt.scatter([x],[y],c='b', marker='s')
plt.show()
#print(a,b,c)
tf.sigmoid(a*x + b*y + c).numpy()
```



```
tf.sigmoid(a*x + b*y + c).numpy()
      0.42606536

x=7.0
y=6.0
plt.scatter(x_label1, y_label1, c='r', marker='x', s=20)
plt.scatter(x_label2, y_label2, c='g', marker='1', s=20)
plt.scatter(x,y,c='b', marker='s')
plt.show()
tf.sigmoid(a*x + b*y + c).numpy()
```



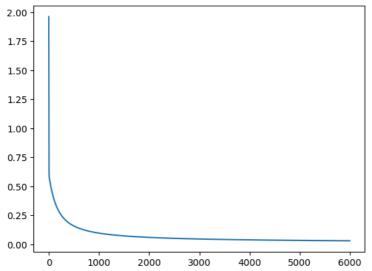


▼ Ilosc epok - 6000

```
import random
a = tf.Variable(random.random())
b = tf.Variable(random.random())
c = tf.Variable(random.random())
Loss = []
epochs = 6000
lr = 0.1
for _ in range(epochs):
 with tf.GradientTape() as tape:
    #predykcja modelu
    pred_y = tf.sigmoid(a * xs + b * ys + c)
    #policzenie błędu
    loss = loss_fn(labels, pred_y)
    #zapisanie aktualnej wartości błędu
    Loss.append(loss.numpy())
  dloss_da, dloss_db, dloss_dc = tape.gradient(loss,(a, b,c))
  a.assign_sub(lr*dloss_da) #a = a - alpha*dloss_da
  b.assign_sub(lr*dloss_db) #b = b - alpha*dloss_db
  c.assign_sub(lr*dloss_dc)
```

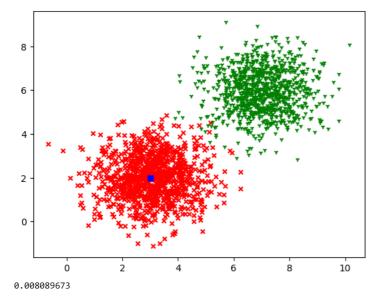
```
...l
```

plt.plot(Loss)
plt.show()



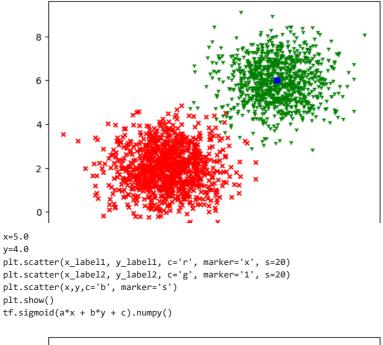
Sprawdzamy dla pewnego punktu:

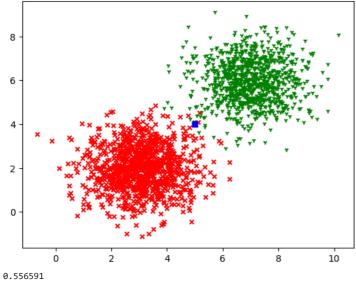
```
x=3.0
y=2.0
plt.scatter(x_label1, y_label1, c='r', marker='x', s=20)
plt.scatter(x_label2, y_label2, c='g', marker='1', s=20)
plt.scatter([x],[y],c='b', marker='s')
plt.show()
#print(a,b,c)
tf.sigmoid(a*x + b*y + c).numpy()
```



```
{\sf tf.sigmoid(a*x + b*y + c).numpy()}
```

```
x=7.0
y=6.0
plt.scatter(x_label1, y_label1, c='r', marker='x', s=20)
plt.scatter(x_label2, y_label2, c='g', marker='1', s=20)
plt.scatter(x,y,c='b', marker='s')
plt.show()
tf.sigmoid(a*x + b*y + c).numpy()
```



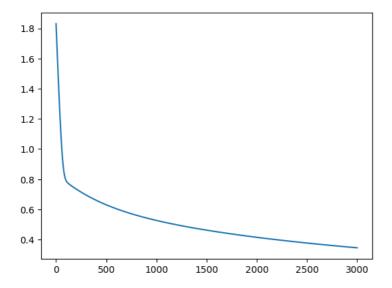


▼ Learning rate - 0.005

```
import random
a = tf.Variable(random.random())
b = tf.Variable(random.random())
c = tf.Variable(random.random())
Loss = []
epochs = 3000
1r = 0.005
for _ in range(epochs):
 with tf.GradientTape() as tape:
    #predykcja modelu
    pred_y = tf.sigmoid(a * xs + b * ys + c)
    #policzenie błędu
    loss = loss_fn(labels, pred_y)
    #zapisanie aktualnej wartości błędu
    Loss.append(loss.numpy())
  dloss_da, dloss_db, dloss_dc = tape.gradient(loss,(a, b,c))
  a.assign_sub(lr*dloss_da) #a = a - alpha*dloss_da
  b.assign_sub(lr*dloss_db) #b = b - alpha*dloss_db
  c.assign_sub(lr*dloss_dc)
```

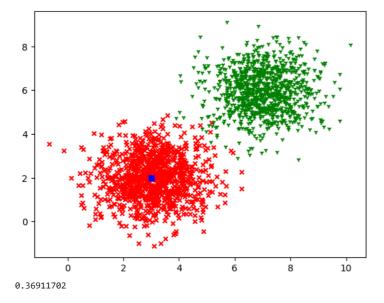
```
0.52/1250,
...1
```

plt.plot(Loss)
plt.show()



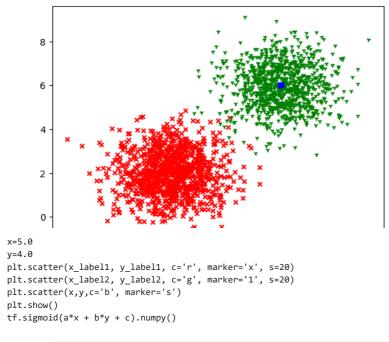
Sprawdzamy dla pewnego punktu:

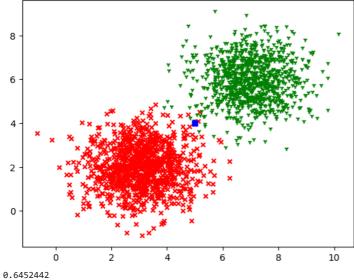
```
x=3.0
y=2.0
plt.scatter(x_label1, y_label1, c='r', marker='x', s=20)
plt.scatter(x_label2, y_label2, c='g', marker='1', s=20)
plt.scatter([x],[y],c='b', marker='s')
plt.show()
#print(a,b,c)
tf.sigmoid(a*x + b*y + c).numpy()
```



```
{\sf tf.sigmoid}({\sf a*x} \, + \, {\sf b*y} \, + \, {\sf c).numpy}()
```

```
x=7.0
y=6.0
plt.scatter(x_label1, y_label1, c='r', marker='x', s=20)
plt.scatter(x_label2, y_label2, c='g', marker='1', s=20)
plt.scatter(x,y,c='b', marker='s')
plt.show()
tf.sigmoid(a*x + b*y + c).numpy()
```





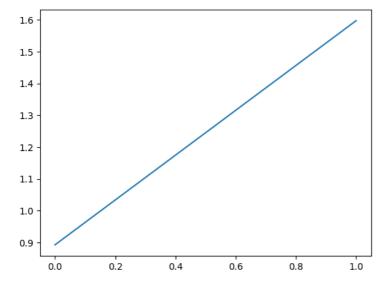
▼ Learning rate - 0.5

```
import random
a = tf.Variable(random.random())
b = tf.Variable(random.random())
c = tf.Variable(random.random())
Loss = []
epochs = 3000
1r = 0.5
for _ in range(epochs):
 with tf.GradientTape() as tape:
    #predykcja modelu
    pred_y = tf.sigmoid(a * xs + b * ys + c)
    #policzenie błędu
    loss = loss_fn(labels, pred_y)
    #zapisanie aktualnej wartości błędu
    Loss.append(loss.numpy())
  dloss_da, dloss_db, dloss_dc = tape.gradient(loss,(a, b,c))
  a.assign_sub(lr*dloss_da) #a = a - alpha*dloss_da
  b.assign_sub(lr*dloss_db) #b = b - alpha*dloss_db
  c.assign_sub(lr*dloss_dc)
```

```
20.11.2023, 22:01
```

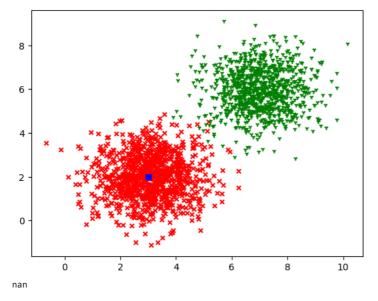
```
nan,
```

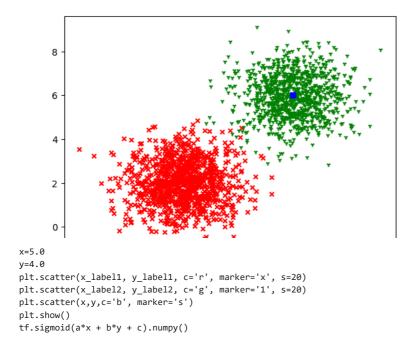
```
plt.plot(Loss)
plt.show()
```

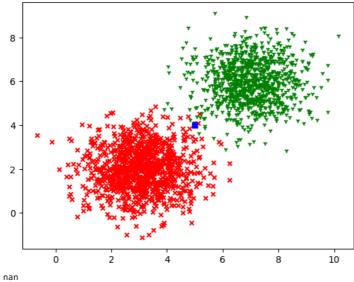


Sprawdzamy dla pewnego punktu:

```
x=3.0
y=2.0
plt.scatter(x_label1, y_label1, c='r', marker='x', s=20)
plt.scatter(x_label2, y_label2, c='g', marker='1', s=20)
plt.scatter([x],[y],c='b', marker='s')
plt.show()
#print(a,b,c)
tf.sigmoid(a*x + b*y + c).numpy()
```





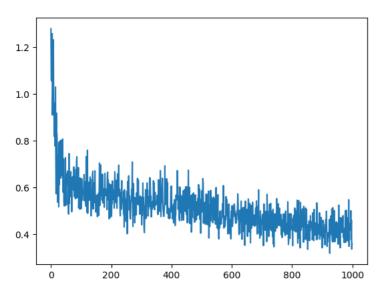


→ Mini batch

```
def subset_dataset_2(x_dataset, y_dataset,label,subset_size):
    arr = np.arange(len(x_dataset))
    np.random.shuffle(arr)
    x_train = x_dataset[arr[0:subset_size]]
    y_train = y_dataset[arr[0:subset_size]]
    label_train = label[arr[0:subset_size]]
    return x_train,y_train,label_train
```

```
Loss = []
epochs = 1000
learning_rate = 0.01
batch_size = 50
a = tf.Variable(random.random())
b = tf.Variable(random.random())
c = tf.Variable(random.random())
for _ in range(epochs):
  xs_batch,ys_batch,labels_batch = subset_dataset_2(xs,ys,labels,batch_size)
 with tf.GradientTape() as tape:
    pred_1 = tf.sigmoid(a * xs_batch + b * ys_batch + c)
    #print(label_batch.shape)
    loss = loss_fn(labels_batch, pred_1)
   Loss.append(loss.numpy())
  dloss_da, dloss_db, dloss_dc = tape.gradient(loss,(a, b,c))
  a.assign sub(learning rate*dloss da) #a = a - alpha*dloss da
  b.assign_sub(learning_rate*dloss_db) #b = b - alpha*dloss_db
  c.assign_sub(learning_rate*dloss_dc)
plt.plot(Loss)
```

plt.show()



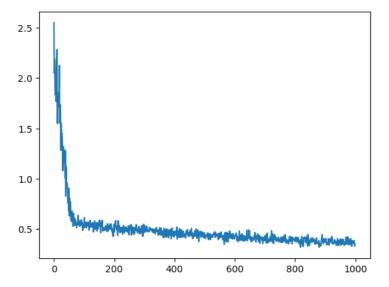
Mini batch - 100

```
Loss = []
epochs = 1000
learning_rate = 0.01
batch_size = 100
a = tf.Variable(random.random())
b = tf.Variable(random.random())
c = tf.Variable(random.random())
for _ in range(epochs):
 xs_batch,ys_batch,labels_batch = subset_dataset_2(xs,ys,labels,batch_size)
 with tf.GradientTape() as tape:
   pred_1 = tf.sigmoid(a * xs_batch + b * ys_batch + c)
    #print(label_batch.shape)
   loss = loss_fn(labels_batch, pred_1)
   Loss.append(loss.numpy())
  dloss_da, dloss_db, dloss_dc = tape.gradient(loss,(a, b,c))
  a.assign_sub(learning_rate*dloss_da) #a = a - alpha*dloss_da
 b.assign_sub(learning_rate*dloss_db) #b = b - alpha*dloss_db
 c.assign_sub(learning_rate*dloss_dc)
```

0.36449/1, 0.37677056, 0.40191123, 0.33797646, 0.3897355, 0.35163426, 0.3958945, 0.37098607, 0.34868005, 0.35818943, 0.39597285, 0.39708325, 0.37527192, 0.37174198, 0.3377356, 0.37106168, 0.36297703, 0.36801812, 0.34583023, 0.36251992, 0.41900155, 0.3534843, 0.38461724, 0.36105064. 0.35310227, 0.37648743, 0.4224778, 0.3782796, 0.3440729, 0.37112737, 0.39931995, 0.38058147, 0.35486615, 0.3744294, 0.34375858, 0.34783754, 0.40513542, 0.36039096, 0.3704394, 0.3281107, 0.35834983, 0.38524735, 0.377896, 0.36143267, 0.35872993, 0.37753052, 0.36032027, 0.3860634, 0.36042136, 0.33057758,

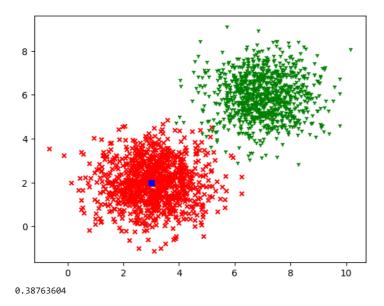
plt.plot(Loss)
plt.show()

0.34787476]



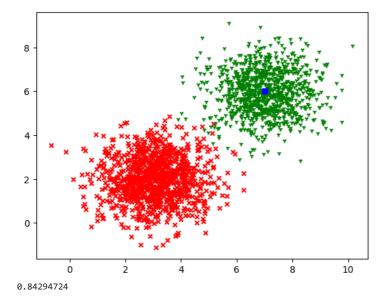
Sprawdzamy dla pewnego punktu:

```
x=3.0
y=2.0
plt.scatter(x_label1, y_label1, c='r', marker='x', s=20)
plt.scatter(x_label2, y_label2, c='g', marker='1', s=20)
plt.scatter([x],[y],c='b', marker='s')
plt.show()
#print(a,b,c)
tf.sigmoid(a*x + b*y + c).numpy()
```

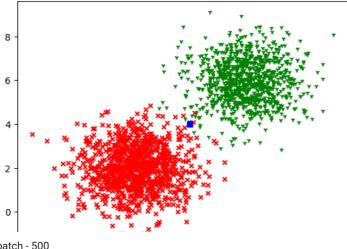


```
tf.sigmoid(a*x + b*y + c).numpy()
```

```
x=7.0
y=6.0
plt.scatter(x_label1, y_label1, c='r', marker='x', s=20)
plt.scatter(x_label2, y_label2, c='g', marker='1', s=20)
plt.scatter(x,y,c='b', marker='s')
plt.show()
tf.sigmoid(a*x + b*y + c).numpy()
```



```
x=5.0
y=4.0
plt.scatter(x_label1, y_label1, c='r', marker='x', s=20)
plt.scatter(x_label2, y_label2, c='g', marker='1', s=20)
plt.scatter(x,y,c='b', marker='s')
plt.show()
tf.sigmoid(a*x + b*y + c).numpy()
```



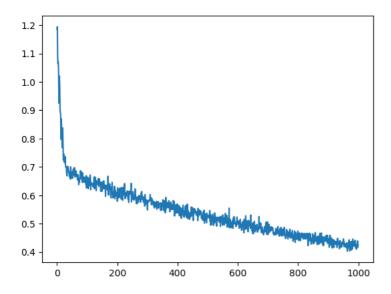
Mini batch - 500

```
Loss = []
epochs = 1000
learning_rate = 0.01
batch_size = 500
a = tf.Variable(random.random())
b = tf.Variable(random.random())
c = tf.Variable(random.random())
for _ in range(epochs):
 xs_batch,ys_batch,labels_batch = subset_dataset_2(xs,ys,labels,batch_size)
 with tf.GradientTape() as tape:
   pred_1 = tf.sigmoid(a * xs_batch + b * ys_batch + c)
   #print(label_batch.shape)
   loss = loss_fn(labels_batch, pred_1)
   Loss.append(loss.numpy())
  dloss_da, dloss_db, dloss_dc = tape.gradient(loss,(a, b,c))
  a.assign_sub(learning_rate*dloss_da) #a = a - alpha*dloss_da
 b.assign_sub(learning_rate*dloss_db) #b = b - alpha*dloss_db
 c.assign_sub(learning_rate*dloss_dc)
```

```
20.11.2023, 22:01
```

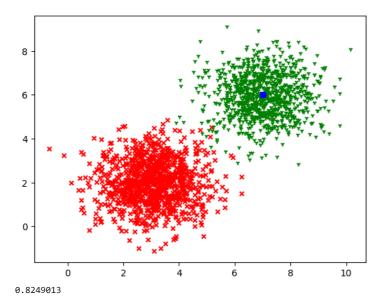
```
0.40089993,
0.42887357,
0.43719596,
0.41100392,
0.44590193,
0.4268462,
0.42680717,
0.42477906,
0.4204055,
0.4367998,
0.42420018,
0.42430976,
0.4413236,
0.4198156,
0.41376477,
0.41646552,
0.41556278,
0.40958786,
0.42824462,
0.4206603,
0.43897077,
0.41698593,
0.42591131
```

plt.plot(Loss)
plt.show()

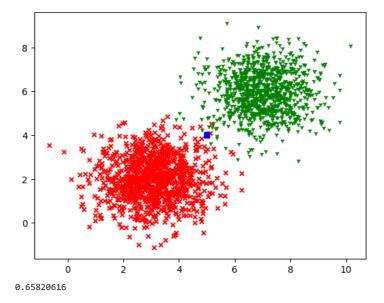


Sprawdzamy dla pewnego punktu:

```
x=3.0
y=2.0
plt.scatter(x_label1, y_label1, c='r', marker='x', s=20)
plt.scatter(x_label2, y_label2, c='g', marker='1', s=20)
plt.scatter([x],[y],c='b', marker='s')
plt.show()
#print(a,b,c)
tf.sigmoid(a*x + b*y + c).numpy()
```

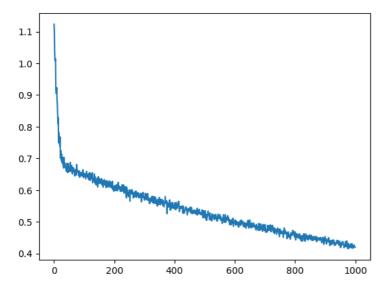


```
x=5.0
y=4.0
plt.scatter(x_label1, y_label1, c='r', marker='x', s=20)
plt.scatter(x_label2, y_label2, c='g', marker='1', s=20)
plt.scatter(x,y,c='b', marker='s')
plt.show()
tf.sigmoid(a*x + b*y + c).numpy()
```



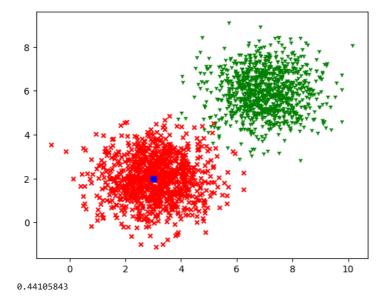
Mini batch - 1000

```
Loss = []
epochs = 1000
learning_rate = 0.01
batch_size = 1000
a = tf.Variable(random.random())
b = tf.Variable(random.random())
c = tf.Variable(random.random())
for _ in range(epochs):
  xs_batch,ys_batch,labels_batch = subset_dataset_2(xs,ys,labels,batch_size)
  with tf.GradientTape() as tape:
    pred_l = tf.sigmoid(a * xs_batch + b * ys_batch + c)
    #print(label_batch.shape)
    loss = loss_fn(labels_batch, pred_1)
    Loss.append(loss.numpy())
  dloss_da, dloss_db, dloss_dc = tape.gradient(loss,(a, b,c))
  a.assign_sub(learning_rate*dloss_da) #a = a - alpha*dloss_da
  b.assign_sub(learning_rate*dloss_db) #b = b - alpha*dloss_db
  c.assign_sub(learning_rate*dloss_dc)
Loss
      0.43631133,
      0.43139648.
      0.43902272,
      0.42618427,
      0.4274808,
      0.43696985,
      0.43860143,
      0.4247756,
      0.42685205.
      0.418484.
      0.43226263.
      0.42838618,
      0.42495143,
      0.43426418,
      0.42888036,
      0.43734533,
      0.43795973,
      0.43478754,
      0.4306711.
      0.42837787.
      0.41828576.
      0.41924506,
      0.42841205,
      0.4285863,
      0.4230459,
      0.43790144,
      0.43286514,
      0.42135784,
      0.4322172.
      0.43681633
      0.43948743.
      0.423264,
      0.43120423
      0.41498664,
      0.4316234,
      0.4172738,
      0.42627335,
      0.41716278,
      0.42090997,
      0.42581177,
      0.4202376.
      0.42909986.
      0.41938856,
      0.42330298,
      0.43055415
      0.42001525,
      0.41751075,
      0.4305068,
      0.42094296,
      0.42247534,
      0.4162971,
      0.42424417.
      0.42452207,
      0.42579523,
      0.4265987,
      0.42000666,
      0.4201903,
      0.41956922]
plt.plot(Loss)
plt.show()
```



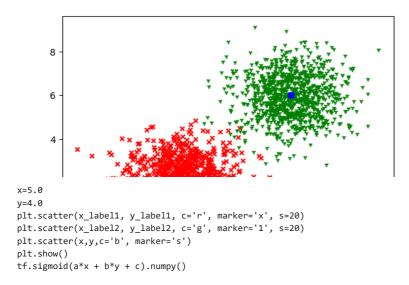
Sprawdzamy dla pewnego punktu:

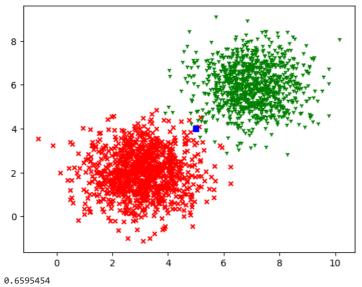
```
x=3.0
y=2.0
plt.scatter(x_label1, y_label1, c='r', marker='x', s=20)
plt.scatter(x_label2, y_label2, c='g', marker='1', s=20)
plt.scatter([x],[y],c='b', marker='s')
plt.show()
#print(a,b,c)
tf.sigmoid(a*x + b*y + c).numpy()
```



```
tf.sigmoid(a*x + b*y + c).numpy()
      0.44105843

x=7.0
y=6.0
plt.scatter(x_label1, y_label1, c='r', marker='x', s=20)
plt.scatter(x_label2, y_label2, c='g', marker='1', s=20)
plt.scatter(x,y,c='b', marker='s')
plt.show()
tf.sigmoid(a*x + b*y + c).numpy()
```





Na uczenie modelu ma najwiekszy wpływ użycie batcha (bez batcha jest podawany cały zbiór uczący), dzięki temu wprowadza, że pewną losowość w procesie uczenia, pomoga to uniknąć utknięcia w minimach lokalnych. Model uczony z minibatchem osiąga lepsze rezultaty jeżeli chodzi o wyniki uczenia(szybszy spadek funkcji błędu oraz mniejszy błąd). Model lepiej i szybciej się uczy gdy mini-batch jest większy niż gdy jest on mniejszy.

Ponadto na proces uczenia modelu ma wpływ ilość epok. Za mała ilość epok skutkuje niedouczeniem modelu (model nie nauczył się wystarczająco dobrze dostosowywać się do danych treningowych). Ostatnim sprawdzonym przeze mnie parametrem jest współczynnik uczenia. Po przestawieniu na współczynnik Adam model uczy się lepiej Jego zbyt duża wartość rowadzi do skakania wokół minimum globalnego przy czym model go nie osiągnie. W przypadku zastosowania zbyt małej wartości współczynnika uczenia proces uczenia jest bardzo wolny na przełomie epok, a model "utyka" w minimach lokalnych.

▼ Zad 3

```
def val_train_split(x_dataset, y_dataset, label, subset_size):
    arr = np.arange(len(x_dataset))
    l=len(x_dataset)
    split = int(len(x_dataset)*(1-subset_size))
    #print(split)
    np.random.shuffle(arr)
    x_train = x_dataset[arr[0:split]]
    y_train = y_dataset[arr[0:split]]
    label_train = label[arr[0:split]]
    x_val = x_dataset[arr[split:]]
    y_val = y_dataset[arr[split:]]
    label_val = label[arr[split:]]
    return x_train,y_train,label_train,x_val,y_val,label_val
```

```
x_train,y_train,label_train,x_val,y_val,label_val = val_train_split(xs,ys,labels,0.3)
x train
      array([6.91062517, 1.86620459, 7.16670689, ..., 6.66336346, 2.97810775,
               8.58583595])
y_train
      array([5.2058503, 1.63066471, 6.03677807, ..., 8.04114962, 1.99420774,
               6.11005225])
label train
      array([1., 0., 1., ..., 1., 0., 1.])
x_val
                4.23694609, 2.91191872, 6.0912127, 5.70518108, 8.86489112,
                5.94411632, 4.51912111, 5.37275078, 2.8167457, 8.44842017, 4.81990471, 3.02350407, 6.91427337, 4.69000927, 2.101145,
                6.75936073, 3.08415557, 3.29051266, 1.84098755, 7.1696774, 2.66655593, 7.35838444, 4.71377893, 3.63550263, 2.37783577,
                8.63173557, 2.78508198, 7.18862536, 1.10872565, 2.52166115, 3.15585692, 7.4851557, 6.3676335, 4.82641085, 7.97824238,
                2.44365795, \quad 7.82831203, \quad 6.28704851, \quad 5.14974123, \quad 5.74784951,
                7.93088747, 1.85632838, 6.4829709, 6.78583236, 7.19470486,
                3.97958991, 9.08200539, 8.17546581, 8.5047958 , 7.44453121,
                5.87826447,
                               5.59702182, 7.16837046, 2.12006002, 6.63933388
                2.67798459, 8.12685975, 6.70738643, 2.86143356, 5.06511404,
                9.02763323, 3.63368754, 6.87508214, 7.60547582, 5.8100315
                3.44737307, \quad 2.81111461, \quad 4.91056081, \quad 1.94986937, \quad 7.00444617,
                3.74224051, 5.06804891, 6.80014827, 3.13913316, 3.6203136,
                2.9540079 \;\; , \quad 4.01082403 , \quad 5.07502731 , \quad 7.45838013 , \quad 6.69834813 ,
                2.76201795, 8.44685572, 6.61285688, 2.46594098, 2.86484903, 6.16700905, 2.90397817, 4.22771483, 1.70952092, 7.82374281,
                6.80197321, \quad 6.8117379 \ , \quad 7.83189026, \quad 6.42669079, \quad 3.87656615,
                3.34273807, 2.79649021, 6.01848158, 3.19896792, 7.44614514,
                3.45647553, 2.3289811 , 4.24423223, 3.9094234 , 7.74150088
                8.61332315, 5.5964156, 1.49499143, 6.98556966, 6.92131532,
                3.5712222 , 2.73321808, 7.14313807, 3.52723391, 7.51479919, 6.28598755, 7.01427886, 6.65558955, 7.76756807, 1.59913118,
                4.92994678, 8.35095865, 7.20508928, 3.37596598, 5.82691756, 5.08021014, 6.55038007, 7.83112397, 3.22928966, 3.66980601,
                4.90141626, 6.72304854, 3.02026616, 3.93241336, 6.33215033,
                2.88320561, 3.27251291, 7.02718079, 1.49940707, 3.35819982, 1.85314964, 7.69470293, 7.55502122, 2.98064708, 7.20510279,
                1.10518237, 4.09480348, 2.72496657, 8.57422408, 4.15638057,
                7.36366368, 4.80117851, 5.64832464, 5.81387501, 4.8453065
                4.03726593, 2.49845719, 3.32018095, 5.62988135, 5.24235881,
                8.03289982, 1.6834958, 7.79806985, 3.79015445, 6.25049221,
                3.62594723, 4.42028074, 2.5224419, 6.31636402, 6.21600662,
                6.65977894, 3.75226202, 3.20682518, 3.27439361, 5.96233354,
                0.78392538, 7.3375129, 3.57786424, 3.13436021, 7.03321665, 5.658583, 4.04731204, 2.92029948, 7.00567891, 3.16264786, 7.93808692, 5.63447072, 6.24337001, 2.50803228, 1.7623002,
                7.2043096 , 6.35729188, 2.20558531, 3.00741247, 6.79068139, 4.39269078, 2.21406522, 3.68392228, 3.15671941, 6.77538828,
                7.39704329, 6.91858995, 7.14708798, 1.74233449, 2.49664437, 2.27444626, -0.14026429, 7.20499643, 6.47223703, 2.91237916,
                4.35705282, 3.09189768, 6.48034276, 5.83099128, 3.18776237,
                4.84198757, 2.04315866, 8.3608385, 2.67063246, 2.09726167,
                7.15818386, 2.04700681, 5.67658673, 7.35533256, 6.33601599, 7.94557774, 4.05935818, 3.50225365, 8.58454067, 5.35655785,
                3.45079445, 3.70303089, 3.88225816, 2.53114841, 3.80024565,
                4.07030286, 7.82737085, 1.01532056, 3.45480824, 4.3632894, 7.69797158, 4.60807321, 6.54354876, 2.22801172, 2.36381613,
                7.53953759, 6.34351408, 6.48938576, 3.78289686, 1.83558853,
                3.20395532, 6.79032428, 8.49446895, 8.51148023, 4.20950751,
                7.3371662 , 7.33051474, 5.64669623, 3.64537087, 6.66108337,
                3.00428296, 2.84711054, 3.61282705, 7.72362696, 3.36517355,
                2.41048018, 6.99421566, 1.21861423, 6.12147182, 7.7357632,
                3.46873568,
                               8.13685489, 1.97649507, 6.24991713, 7.02707294,
                3.66144264, 7.81397427, 3.3238234, 4.84576016, 6.43853202,
                6.82956582, 9.76113332, 6.3393887,
                                                               7.69642098, 6.52329306
                4.03716165, 2.80238311, 2.15842014, 2.84545068, 3.20545672])
y_val
```

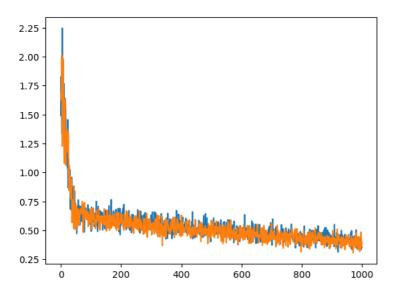
```
4.0958338ZE+00, Z.0010800ZE+00, 1.550/015/E+00, 4./90Z4344E+00,
5.14177868e-01, 6.35847706e-01, 1.67786402e+00, 7.25749170e+00,
5.62376841e+00,
                7.32547782e+00,
                                  7.58707903e+00,
                                                   7.09544461e+00.
-5.21137703e-01,
                 1.65410461e+00,
                                  3.99467882e+00,
                                                   5.18873694e+00.
1.28603565e+00,
                 5.17399510e+00,
                                  2.10768938e+00,
                                                   1.80904199e+00.
                 1.38306085e+00,
                                  4.63415280e+00,
3.51095658e-01,
                                                   5.24120884e+00
6.49862817e+00,
                 6.78239858e-01,
                                  5.83215975e+00, 5.75405946e+00,
1.14032911e+00,
                 2.27319357e+00,
                                  7.03774862e+00,
                                                   2.23984355e+00,
3.18865412e+00,
                 5.43353592e+00,
                                  6.30411269e+00,
                                                   5.79333176e+00,
5.90989796e+00.
                 2.62467807e+00.
                                  7.02653561e+00.
                                                   7.89089572e+00.
7.57967702e+00.
                 2.79258118e+00,
                                  6.22351909e+00, 1.82936025e+00,
3.37888185e+00,
                 6.13260128e+00,
                                  1.57118241e+00,
                                                   2.38137832e+00,
                                  1.65950070e+00, 1.51783372e+00,
1.48486280e+00,
                 4.90651764e+00,
7.43386080e+00.
                 2.23129562e+00.
                                  2.70311074e+00.
                                                   4.54939613e+00.
1.98005170e+00.
                 3.22862015e+00.
                                  1.62907263e+00,
                                                   7.17246962e+00.
                 1.05556550e+00,
5.95908800e+00,
                                  6.29638886e+00,
                                                   8.50338789e-01.
2.33564656e+00,
                 1.72746606e+00,
                                  6.06434089e+00,
                                                   1.75270649e+00,
4.82567608e+00,
                 8.71320162e-02,
                                  1.23955250e+00,
                                                   7.07502001e+00.
                 2.92364236e+00,
                                  2.05120282e+00,
4.34448057e-01.
                                                   2.41700127e+00.
4.60219501e+00,
                 4.55315007e+00,
                                  5.93196809e+00,
                                                   1.81220693e+00,
5.06423146e+00,
                 2.07346970e+00,
                                  6.50964240e+00,
                                                   1.86300278e+00,
                 2.78909918e+00,
                                  7.61113595e+00,
2.50318270e+00,
                                                   6.45338418e+00,
                                  2.05781992e+00,
5.95519509e+00.
                 2.28649949e+00.
                                                   2.66506987e+00.
6.94127531e+00.
                 2.87076846e+00.
                                  4.48837486e+00.
                                                   1.06742733e+00.
                 7.22293978e+00,
                                  5.63657543e+00,
                                                   2.63860025e+00.
4.12038891e+00.
2.25734972e+00,
                 7.51472156e+00,
                                  2.14991896e+00,
                                                   5.37399947e+00.
                                  1.37516722e-01,
5.23085486e+00,
                 5.31539456e+00,
                                                   2.26303062e+00.
5.30451521e+00.
                 6.89387085e+00, -6.23922190e-01,
                                                   2.03792432e+00
                 3.61149968e-01,
                                  1.30497531e+00,
                                                   1.03407953e+00
8.29309505e+00.
2.93409456e-01,
                 5.90386230e+00,
                                  7.54874256e+00,
                                                   5.75196236e+00,
6.24965685e+00,
                 2.70146968e+00,
                                  1.57697034e+00, 3.01408259e+00,
3.23248300e+00.
                 7.28369052e+00.
                                  4.69427033e+00.
                                                   1.18365785e+00.
1.86687794e+00.
                 3.79955820e+00.
                                  7.51107687e+00.
                                                   6.38283801e+00.
1.06622008e+00.
                 5.28949605e+00.
                                  1.99625106e+00.
                                                   6.20507002e+00.
2.69560360e+00,
                 2.88760367e+00,
                                  7.03096805e+00,
                                                   1.94884661e+00,
6.44190181e+00,
                 4.45431892e+00,
                                  6.60657263e+00,
                                                   6.92444337e+00.
                 2.25564722e+00,
                                  6.78415732e+00,
2.22537405e+00,
                                                   3.97424022e+00.
                                  1.08233401e+00,
2.93374217e+00.
                 3.19360015e+00.
                                                   2.93422995e+00.
                                  5.18649550e+00,
                 3.89079325e+00,
                                                   5.87310870e-01
7.52529729e-01,
1.32198227e+00,
                 1.77839653e+00,
                                  6.37079104e+00,
                                                   2.39623031e+00,
                 1.40481533e+00,
                                  2.01982939e+00,
5.40857970e+00,
                                                   6.82496979e+00,
5.06765712e+00.
                 7.47075397e+00.
                                  3.41261940e+00, 2.21730097e+00,
1.14327894e+00.
                 6.98943376e+00.
                                  6.90996821e+00.
                                                   7.19881115e+00.
                 5.33989743e+00,
1.13514595e+00.
                                  5.23668805e+00, 6.74665698e+00,
                 4.29129580e+00,
                                  1.40545277e+00,
                                                   1.85960265e+00,
9.49592949e-01,
2.10899633e+00.
                 5.04394842e+00.
                                  3.38686292e+00, 1.35942285e+00,
                                  4.25571356e+00,
6.86905636e+00,
                 2.73380973e+00,
                                                   6.96747522e+00.
                                  5.50342675e-01,
1.88126941e+00.
                 5.91671958e+00.
                                                   2.28110512e+00.
7.59724760e+00,
                 2.80363205e+00,
                                  5.50737696e+00,
                                                   1.31309762e+00,
2.61362848e+00,
                 5.55329887e+00,
                                  7.38661289e+00,
                                                   6.08458955e+00,
5.42463473e+00,
                 7.96990411e+00,
                                  3.05453946e+00,
                                                   6.67023727e+00
1.05707159e+00.
                 1.18291146e+00,
                                  3.94751234e+00,
                                                   2.17371789e+00])
```

label_val

```
array([0., 0., 0., 1., 1., 1., 1., 0., 0., 0., 0., 1., 1., 1., 0., 0., 0.,
      0., 1., 1., 0., 1., 0., 0., 0., 0., 1., 0., 0., 1., 0., 1., 1., 1.,
      1., 1., 0., 0., 1., 1., 1., 0., 0., 0., 1., 1., 1., 0., 0., 1., 1.,
      0.,\;0.,\;1.,\;1.,\;1.,\;1.,\;0.,\;0.,\;1.,\;1.,\;0.,\;0.,\;1.,\;0.,\;0.,\;1.,\;1.,
      0., 0., 0., 1., 0., 1., 0., 0., 1., 0., 0., 0., 1., 0., 1., 1., 1.,
      0.,\; 1.,\; 1.,\; 0.,\; 0.,\; 1.,\; 0.,\; 0.,\; 1.,\; 0.,\; 0.,\; 1.,\; 1.,\; 0.,\; 0.,\; 0.,\; 0.,
      0., 0., 1., 0., 0., 0., 1., 0., 1., 1., 0., 0., 1., 1., 0., 1.,
      1., 1., 0., 1., 0., 1., 1., 0., 1., 0., 1., 1., 0., 0., 0., 0., 1.,
      0., 0., 0., 1., 1., 1., 0., 0., 0., 0., 1., 1., 1., 1., 1., 1.,
      0.,\ 0.,\ 0.,\ 1.,\ 0.,\ 0.,\ 1.,\ 1.,\ 1.,\ 0.,\ 0.,\ 0.,\ 0.,\ 0.,\ 1.,\ 1.,\ 0.,
      0., 0., 1., 0., 1., 1., 0., 0., 1., 0., 0., 1., 0., 0., 0., 1., 1.,
      1., 1., 1., 0., 1., 0., 1., 1., 0., 1., 0., 0., 0., 0., 0., 1., 0.,
      0., 1., 0., 1., 0., 1., 0., 1., 0., 1., 0., 1., 0., 1.,
      0., 0., 1., 0., 1., 0., 1., 0., 1., 0., 0., 0., 1., 1., 1., 0., 1.,
      1., 0., 0., 0., 1., 0., 0., 0., 1., 1., 0., 0., 1., 0., 0., 0.,
      1.,\; 1.,\; 1.,\; 0.,\; 0.,\; 0.,\; 1.,\; 1.,\; 1.,\; 1.,\; 0.,\; 1.,\; 0.,\; 1.,\; 1.,\; 0.,\;
      0., 0., 1., 0., 0., 0., 1., 0., 1., 0., 0., 0., 1., 0., 1., 0.,
      0., 1., 1., 1., 1., 0., 1., 1., 1., 1., 1., 0., 1., 1., 1., 0., 1.,
      1., 1., 1., 1., 1., 0., 1., 0., 1., 1., 0., 1., 1., 0., 1., 1.,
      1., 0., 0., 1., 0., 1., 0., 1., 0., 0., 0., 0., 0., 1., 1., 0.,
      1., 1., 0., 0., 1., 0., 0., 0., 1., 1., 1., 1., 1., 0., 0., 0., 1.,
      0., 1., 0., 0., 0., 0., 1., 1., 1., 0., 1., 1., 0., 0., 1., 0., 1.
      1., 1., 1., 1., 0., 1., 1., 1., 0., 1., 0., 1., 1., 0., 0., 0., 1.,
      0., 0., 1., 0., 0., 1., 0., 0., 1., 1., 0., 1., 0., 0., 0., 1.,
      0.,\;1.,\;0.,\;0.,\;1.,\;0.,\;0.,\;0.,\;0.,\;1.,\;1.,\;1.,\;0.,\;1.,\;0.,\;1.,
      0., 0., 1., 1., 1., 0., 0., 0., 1., 0., 1., 0., 0., 1., 1., 0., 0.,
      1., 0., 1., 1., 1., 0., 0., 1., 1., 0., 0., 1., 0., 0., 0., 0., 1.,
      1., 1., 1., 0., 0., 0., 0., 1., 1., 0., 0., 0., 1., 1., 0., 1., 0.,
          0., 0., 1., 0., 1., 1., 1., 0., 0., 1., 1., 0., 0., 0.,
      0., 0., 1., 0., 0., 0., 1., 0., 1., 0., 1., 1., 1., 0., 0., 0.,
      1., 1., 1., 0., 1., 1., 1., 0., 1., 0., 0., 0., 1., 0., 0., 1., 0.,
```

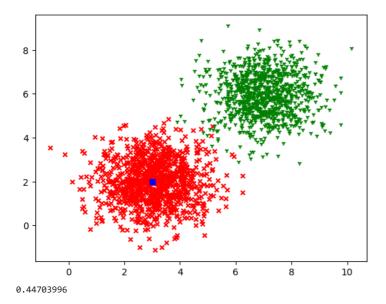
```
1., 1., 0., 1., 0., 0., 1., 0., 1., 0., 0., 1., 1., 1., 1., 1., 1.,
            1., 0., 0., 0., 0.])
def subset_dataset_2(x_dataset, y_dataset,label,subset_size):
    arr = np.arange(len(x_dataset))
    np.random.shuffle(arr)
   x_train = x_dataset[arr[0:subset_size]]
   y_train = y_dataset[arr[0:subset_size]]
    label_train = label[arr[0:subset_size]]
    return x_train,y_train,label_train
Loss = []
Val_loss =[]
epochs = 1000
learning_rate = 0.01
batch_size = 50
val\_split = 0.3
a = tf.Variable(random.random())
b = tf.Variable(random.random())
c = tf.Variable(random.random())
x_tr,y_tr,label_tr,x_val,y_val,label_val = val_train_split(xs,ys,labels,val_split)
for _ in range(epochs):
 xs_batch,ys_batch,labels_batch = subset_dataset_2(x_tr,y_tr,label_tr,batch_size)
  xsv\_batch, ysv\_batch, labelsv\_batch = subset\_dataset\_2(x\_val, y\_val, label\_val, batch\_size)
  with tf.GradientTape() as tape:
   pred_l = tf.sigmoid(a * xs_batch + b * ys_batch + c)
pred_lv = tf.sigmoid(a * xsv_batch + b * ysv_batch + c)
    #print(label_batch.shape)
    loss = loss_fn(labels_batch, pred_1)
    val_loss = loss_fn(labelsv_batch,pred_lv)
   Loss.append(loss.numpy())
   Val_loss.append(val_loss.numpy())
  dloss da, dloss db, dloss dc = tape.gradient(loss,(a, b,c))
  a.assign_sub(learning_rate*dloss_da) #a = a - alpha*dloss_da
  b.assign_sub(learning_rate*dloss_db) #b = b - alpha*dloss_db
  c.assign_sub(learning_rate*dloss_dc)
```

```
plt.plot(Loss)
plt.plot(Val_loss)
plt.show()
```



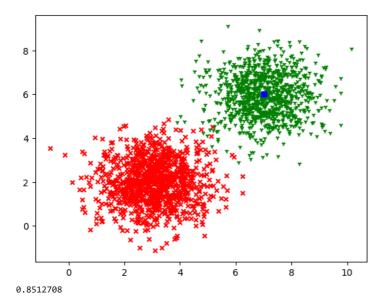
Sprawdzamy dla pewnego punktu:

```
x=3.0
y=2.0
plt.scatter(x_label1, y_label1, c='r', marker='x', s=20)
plt.scatter(x_label2, y_label2, c='g', marker='1', s=20)
plt.scatter([x],[y],c='b', marker='s')
plt.show()
#print(a,b,c)
tf.sigmoid(a*x + b*y + c).numpy()
```

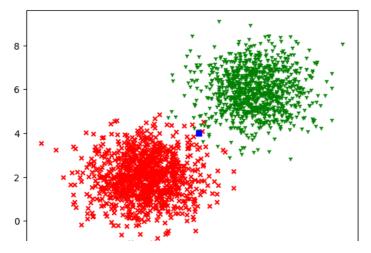


```
tf.sigmoid(a*x + b*y + c).numpy()
```

```
x=7.0
y=6.0
plt.scatter(x_label1, y_label1, c='r', marker='x', s=20)
plt.scatter(x_label2, y_label2, c='g', marker='1', s=20)
plt.scatter(x,y,c='b', marker='s')
plt.show()
tf.sigmoid(a*x + b*y + c).numpy()
```



```
x=5.0
y=4.0
plt.scatter(x_label1, y_label1, c='r', marker='x', s=20)
plt.scatter(x_label2, y_label2, c='g', marker='1', s=20)
plt.scatter(x,y,c='b', marker='s')
plt.show()
tf.sigmoid(a*x + b*y + c).numpy()
```

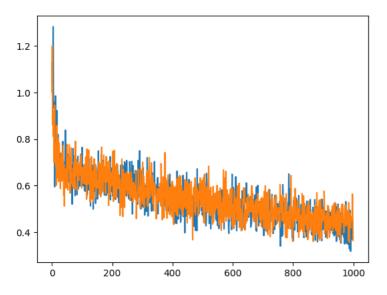


▼ Val_split - 0.4

```
Loss = []
Val_loss =[]
epochs = 1000
learning_rate = 0.01
batch_size = 50
val_split = 0.4
a = tf.Variable(random.random())
b = tf.Variable(random.random())
c = tf.Variable(random.random())
x_tr,y_tr,label_tr,x_val,y_val,label_val = val_train_split(xs,ys,labels,val_split)
for _ in range(epochs):
 xs_batch,ys_batch,labels_batch = subset_dataset_2(x_tr,y_tr,label_tr,batch_size)
  xsv\_batch, ysv\_batch, labelsv\_batch = subset\_dataset\_2(x\_val, y\_val, label\_val, batch\_size)
 with tf.GradientTape() as tape:
   pred_l = tf.sigmoid(a * xs_batch + b * ys_batch + c)
    pred_lv = tf.sigmoid(a * xsv_batch + b * ysv_batch + c)
    #print(label_batch.shape)
   loss = loss_fn(labels_batch, pred_l)
    val_loss = loss_fn(labelsv_batch,pred_lv)
   Loss.append(loss.numpy())
   Val_loss.append(val_loss.numpy())
  dloss_da, dloss_db, dloss_dc = tape.gradient(loss,(a, b,c))
  a.assign_sub(learning_rate*dloss_da) #a = a - alpha*dloss_da
  b.assign_sub(learning_rate*dloss_db) #b = b - alpha*dloss_db
  c.assign_sub(learning_rate*dloss_dc)
```

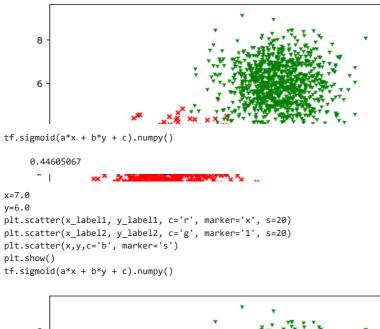
```
0.3883/14/,
0.37817046,
0.45636854,
0.35064736,
0.38606307,
0.3596329,
0.42598155,
0.5318419,
0.42551738,
0.47840893,
0.35215783,
0.43179715,
0.40277427,
0.41627347,
0.3937735,
0.34894252,
0.39706868,
0.48803025,
0.3864722,
0.32954022,
0.40705982,
0.49416503,
0.40349248,
0.31906512.
0.35690677,
0.40477276,
0.46485162,
0.39797634,
0.37145865,
0.45478436,
0.39694333,
0.40097886]
```

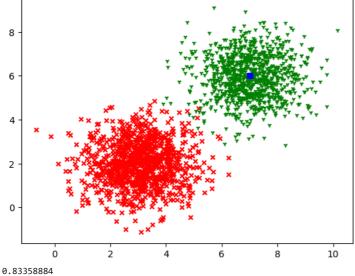
plt.plot(Loss)
plt.plot(Val_loss)
plt.show()



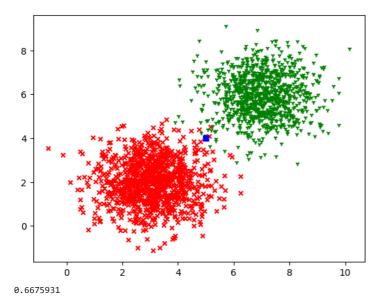
Sprawdzamy dla pewnego punktu:

```
x=3.0
y=2.0
plt.scatter(x_label1, y_label1, c='r', marker='x', s=20)
plt.scatter(x_label2, y_label2, c='g', marker='1', s=20)
plt.scatter([x],[y],c='b', marker='s')
plt.show()
#print(a,b,c)
tf.sigmoid(a*x + b*y + c).numpy()
```





```
x=5.0
y=4.0
plt.scatter(x_label1, y_label1, c='r', marker='x', s=20)
plt.scatter(x_label2, y_label2, c='g', marker='1', s=20)
plt.scatter(x,y,c='b', marker='s')
plt.show()
tf.sigmoid(a*x + b*y + c).numpy()
```



Aby edytować zawartość komórki, kliknij ją dwukrotnie (lub naciśnij klawisz Enter)

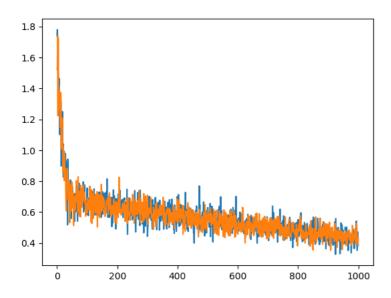
▼ Val_split - 0.1

```
Loss = []
Val_loss =[]
epochs = 1000
learning_rate = 0.01
batch_size = 50
val_split = 0.1
a = tf.Variable(random.random())
b = tf.Variable(random.random())
c = tf.Variable(random.random())
x_tr,y_tr,label_tr,x_val,y_val,label_val = val_train_split(xs,ys,labels,val_split)
for _ in range(epochs):
 xs_batch,ys_batch,labels_batch = subset_dataset_2(x_tr,y_tr,label_tr,batch_size)
  xsv_batch,ysv_batch,labelsv_batch = subset_dataset_2(x_val,y_val,label_val,batch_size)
 with tf.GradientTape() as tape:
   pred_l = tf.sigmoid(a * xs_batch + b * ys_batch + c)
   pred_lv = tf.sigmoid(a * xsv_batch + b * ysv_batch + c)
    #print(label_batch.shape)
   loss = loss_fn(labels_batch, pred_1)
   val_loss = loss_fn(labelsv_batch,pred_lv)
   Loss.append(loss.numpy())
   Val_loss.append(val_loss.numpy())
  dloss_da, dloss_db, dloss_dc = tape.gradient(loss,(a, b,c))
  a.assign_sub(learning_rate*dloss_da) #a = a - alpha*dloss_da
  b.assign_sub(learning_rate*dloss_db) #b = b - alpha*dloss_db
  c.assign_sub(learning_rate*dloss_dc)
```

```
20.11.2023, 22:01
```

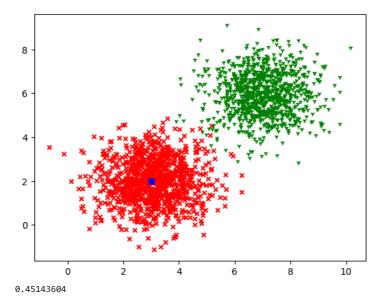
```
0.402/3422,
0.49227914,
0.4793527,
0.4120394,
0.5415535,
0.48539612,
0.3821492,
0.3525137,
0.46637332,
0.47075132,
0.38399902]
```

plt.plot(Loss)
plt.plot(Val_loss)
plt.show()



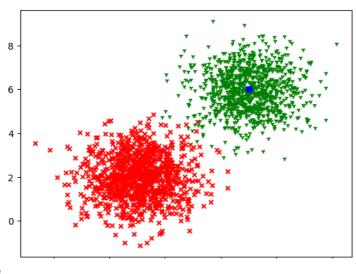
Sprawdzamy dla pewnego punktu:

```
x=3.0
y=2.0
plt.scatter(x_label1, y_label1, c='r', marker='x', s=20)
plt.scatter(x_label2, y_label2, c='g', marker='1', s=20)
plt.scatter([x],[y],c='b', marker='s')
plt.show()
#print(a,b,c)
tf.sigmoid(a*x + b*y + c).numpy()
```



```
tf.sigmoid(a*x + b*y + c).numpy()
```

```
x=7.0
y=6.0
plt.scatter(x_label1, y_label1, c='r', marker='x', s=20)
plt.scatter(x_label2, y_label2, c='g', marker='1', s=20)
plt.scatter(x,y,c='b', marker='s')
plt.show()
tf.sigmoid(a*x + b*y + c).numpy()
```



x=5.0 y=4.0n=1 contains a label of the marken-in marken-in contains x=1