

Import biblioteki **TensorFlow** (<https://www.tensorflow.org/>) z której będziemy korzystali w **uczeniu maszynowym**:

```
import tensorflow as tf
import matplotlib.pyplot as plt
import numpy as np

import keras
from keras.models import Sequential
from keras.layers import Dense
```

## Dwa gangi

Zbiór danych:

```
[0]*10+[1]*10

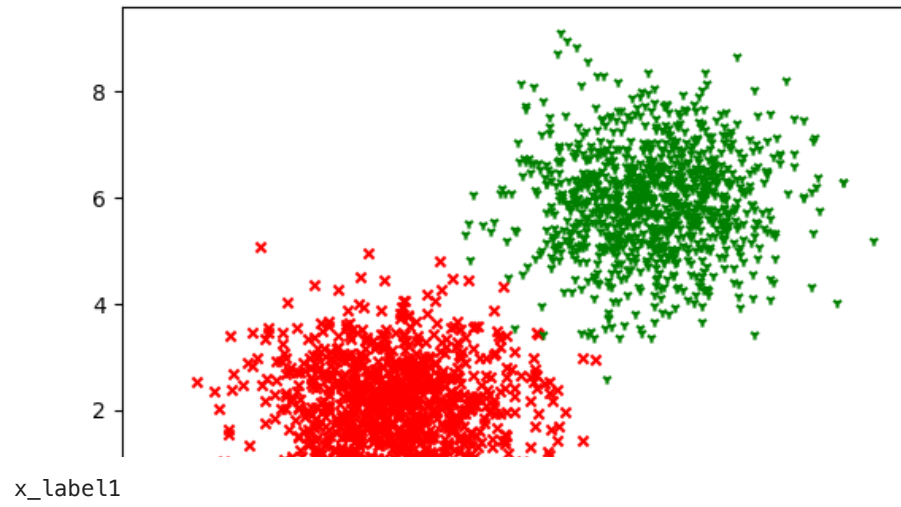
[0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 1, 1, 1, 1, 1, 1, 1, 1, 1, 1]

x_label1 = np.random.normal(3, 1, 1000)
y_label1 = np.random.normal(2, 1, 1000)
x_label2 = np.random.normal(7, 1, 1000)
y_label2 = np.random.normal(6, 1, 1000)

xs = np.append(x_label1, x_label2)
ys = np.append(y_label1, y_label2)
labels = np.asarray([0.]*len(x_label1)+[1.]*len(x_label2))
labels

array([0., 0., 0., ..., 1., 1., 1.])

plt.scatter(x_label1, y_label1, c='r', marker='x', s=20)
plt.scatter(x_label2, y_label2, c='g', marker='1', s=20)
plt.show()
```



```

4.07015015, 2.70147121, 3.40922723, 3.52302214, 2.00100470,
4.01621889, 4.12100604, 2.72752771, 2.75719359, 4.02926479,
3.28814498, 2.54441411, 3.49969971, 1.84603106, 3.01861976,
3.33037865, 4.63877474, 3.22667965, 3.42150617, 2.99610977,
3.92730886, 2.93353636, 3.54677324, 2.18964223, 2.14112941,
2.3725276 , 3.63421524, 4.3018087 , 1.12315323, 0.79435992,
3.72061328, 3.65506081, 3.78239993, 3.7291989 , 2.59910655,
4.04697558, 4.04816327, 2.69502771, 4.34208597, 3.55934781,
4.28531443, 1.87753953, 2.79867148, 2.72406779, 2.58175449,
2.71320505, 4.0847115 , 3.02323071, 2.31744951, 2.60453008,
2.90800369, 2.14776034, 4.21060945, 1.77524038, 2.6312135 ,
3.6106395 , 5.23375638, 4.82731622, 3.27098369, 2.94126894,
3.38526073, 4.3067985 , 2.86913682, 3.22277753, 3.12253827,
3.60975487, 2.27899681, 3.52791693, 1.61311302, 2.32490014,
2.18145502, 2.30392162, 1.77847212, 3.19189672, 2.58963709,
3.99746712, 3.6677791 , 2.53024815, 3.54696023, 4.18354706,
1.29657966, 2.45625325, 3.30326258, 4.56749604, 3.1815515 ,
3.74255693, 3.16999129, 2.73032971, 2.9479818 , 3.05047653,
3.025813 , 3.94078173, 2.46439622, 3.37261736, 4.46956822,
1.7741385 , 3.22896292, 1.84104922, 2.45036858, 3.61103535,
4.03725328, 1.23050797, 3.48538395, 4.73910316, 3.4573818 ,
2.30814498, 5.21912853, 3.56975434, 3.93582052, 4.0883278 ,
1.76238825, 2.3287282 , 2.53005539, 5.4803398 , 5.41313985,
5.21649602, 1.70691479, 3.07901139, 5.59423695, 3.78434683,
3.41518979, 3.01700775, 1.12320482, 2.4850929 , 4.31186964,
2.44639538, 3.44416348, 2.74779462, 3.31551388, 3.15156282])

```

Definiujemy model:

```
model = Sequential()
```

Dodajemy **jedną warstwę** (Dense) z **jednym neuronem** (units=1) z **biasem** (use\_bias=True) i **liniową funkcją aktywacji** (activation="linear"):

```
model.add(Dense(units = 1, use_bias=True, input_dim=2, activation = "softmax"))
```

Definiujemy **optimalizator** i **błąd** (entropia krzyżowa). **Współczynnik uczenia = 0.1**

```
#opt = tf.keras.optimizers.Adam(learning_rate=0.1)
opt = tf.keras.optimizers.SGD(learning_rate=0.1)
```

```
model.compile(loss='binary_crossentropy', optimizer=opt)
```

Informacja o modelu:

```
model.summary()
```

```
Model: "sequential_1"
```

Layer (type)	Output Shape	Param #
dense_1 (Dense)	(None, 1)	3
Total params: 3 (12.00 Byte)		
Trainable params: 3 (12.00 Byte)		
Non-trainable params: 0 (0.00 Byte)		

Przygotowanie danych:

```
xs=xs.reshape(-1,1)
ys=ys.reshape(-1,1)
data_points=np.concatenate([xs,ys],axis=1)
data_points

array([[4.59911355, 0.97664184],
       [5.12942909, 1.3036076 ],
       [2.86082513, 3.42102928],
       ...,
       [6.95434383, 6.18464347],
       [6.07670661, 6.40313423],
       [8.22009436, 6.28592032]])
```

Proces **uczenia**:

```
epochs = 100
h = model.fit(data_points,labels, verbose=1, epochs=epochs,validation_split=0.2)
```

```
Epoch 78/100
50/50 [=====] - 0s 3ms/step - loss: 0.0359 - val_loss: 0.0348
Epoch 79/100
50/50 [=====] - 0s 2ms/step - loss: 0.0355 - val_loss: 0.0331
Epoch 80/100
50/50 [=====] - 0s 2ms/step - loss: 0.0354 - val_loss: 0.0348
Epoch 81/100
50/50 [=====] - 0s 3ms/step - loss: 0.0351 - val_loss: 0.0336
Epoch 82/100
50/50 [=====] - 0s 2ms/step - loss: 0.0348 - val_loss: 0.0383
Epoch 83/100
50/50 [=====] - 0s 2ms/step - loss: 0.0346 - val_loss: 0.0350
Epoch 84/100
50/50 [=====] - 0s 2ms/step - loss: 0.0344 - val_loss: 0.0346
Epoch 85/100
50/50 [=====] - 0s 3ms/step - loss: 0.0341 - val_loss: 0.0347
Epoch 86/100
50/50 [=====] - 0s 3ms/step - loss: 0.0338 - val_loss: 0.0327
Epoch 87/100
50/50 [=====] - 0s 2ms/step - loss: 0.0336 - val_loss: 0.0322
Epoch 88/100
50/50 [=====] - 0s 3ms/step - loss: 0.0334 - val_loss: 0.0363
Epoch 89/100
50/50 [=====] - 0s 3ms/step - loss: 0.0332 - val_loss: 0.0371
Epoch 90/100
50/50 [=====] - 0s 3ms/step - loss: 0.0328 - val_loss: 0.0392
Epoch 91/100
50/50 [=====] - 0s 3ms/step - loss: 0.0328 - val_loss: 0.0364
Epoch 92/100
50/50 [=====] - 0s 4ms/step - loss: 0.0325 - val_loss: 0.0366
Epoch 93/100
50/50 [=====] - 0s 2ms/step - loss: 0.0323 - val_loss: 0.0320
Epoch 94/100
50/50 [=====] - 0s 2ms/step - loss: 0.0318 - val_loss: 0.0286
Epoch 95/100
50/50 [=====] - 0s 2ms/step - loss: 0.0317 - val_loss: 0.0364
Epoch 96/100
50/50 [=====] - 0s 2ms/step - loss: 0.0316 - val_loss: 0.0353
Epoch 97/100
50/50 [=====] - 0s 3ms/step - loss: 0.0315 - val_loss: 0.0353
Epoch 98/100
50/50 [=====] - 0s 3ms/step - loss: 0.0313 - val_loss: 0.0290
Epoch 99/100
50/50 [=====] - 0s 3ms/step - loss: 0.0308 - val_loss: 0.0422
Epoch 100/100
50/50 [=====] - 0s 3ms/step - loss: 0.0309 - val_loss: 0.0349
```

```
Loss = h.history['loss']
Loss
```

```
0.05073777213692665,  
0.05022202432155609,  
0.04928869754076004,  
0.048732005059719086,  
0.04790578782558441,  
0.04718722403049469,  
0.046520642936229706,  
0.04612436890602112,  
0.04560814052820206,
```

```
0.03140437053422323,
0.03125711530447006,
0.030768103897571564,
0.03090226836502552]
```

Sprawdźmy jakie są **wartości wag**:

```
weights = model.get_weights()
```

```
print(weights[0])
```

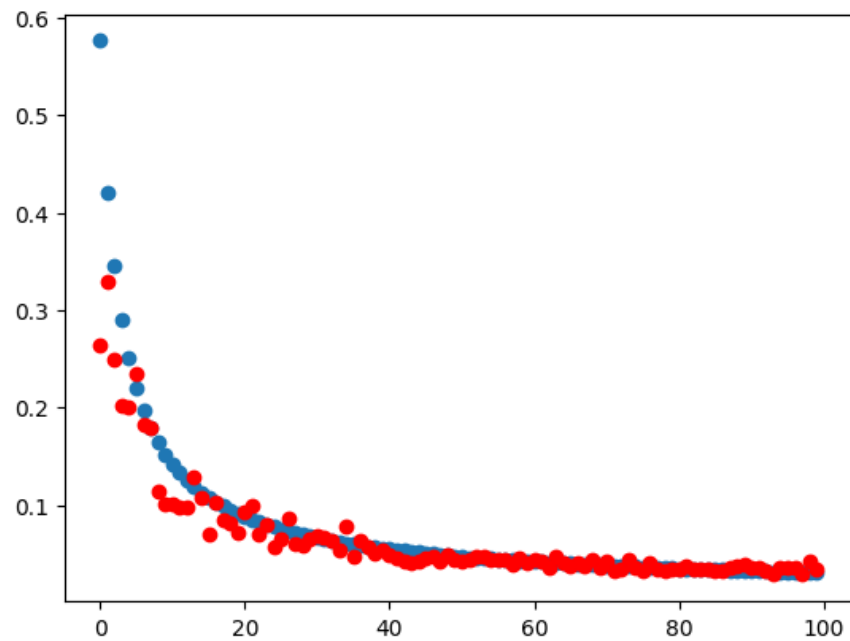
```
print(weights[1])    #bias
```

```
[[0.976188 ]
 [1.4137076]]
[-10.545252]
```

```
plt.scatter(np.arange(epochs),h.history['loss'])
```

```
plt.scatter(np.arange(epochs),h.history['val_loss'],c='r')
```

```
plt.show()
```

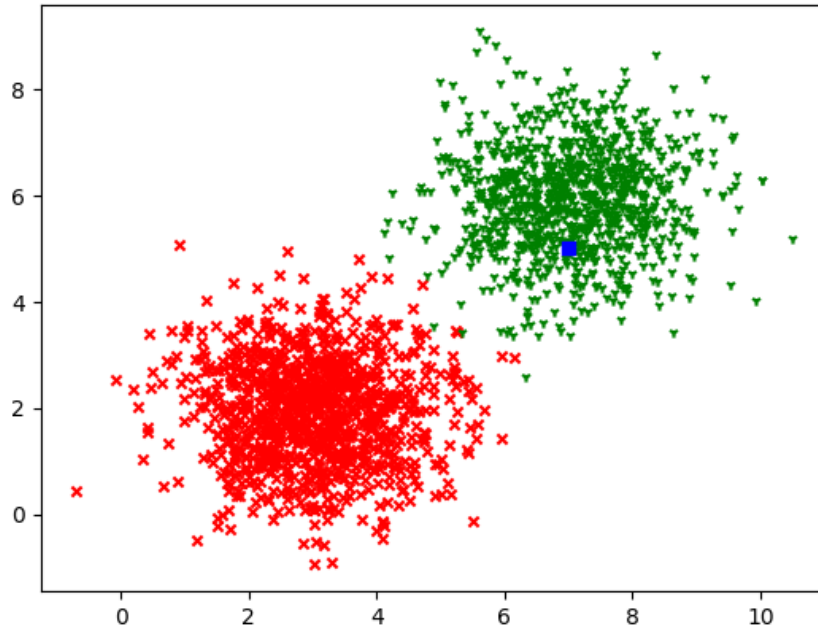


Sprawdzamy działanie modelu dla punktu o współrzędnych **x** i **y**:

```

x=7.0
y=5.0
plt.scatter(x_label1, y_label1, c='r', marker='x', s=20)
plt.scatter(x_label2, y_label2, c='g', marker='1', s=20)
plt.scatter(x,y,c='b', marker='s')
plt.show()

```



```
model.predict([[x,y]])
```

```

1/1 [=====] - 0s 60ms/step
array([[1.]], dtype=float32)

```

Learning rate 0.01

Definiujemy model:

```
model = Sequential()
```



Dodajemy **jedną warstwę** (Dense) z **jednym neuronem** (units=1) z **biasem** (use\_bias=True) i **liniową funkcją aktywacji** (activation="linear"):

```
model.add(Dense(units = 1, use_bias=True, input_dim=2, activation = "softmax"))
```

Definiujemy **optymalizator** i **błąd** (entropia krzyżowa). **Współczynnik uczenia = 0.1**

```
#opt = tf.keras.optimizers.Adam(learning_rate=0.1)
opt = tf.keras.optimizers.SGD(learning_rate=0.01)
```

```
model.compile(loss='binary_crossentropy', optimizer=opt)
```

Informacja o modelu:

```
model.summary()
```

Model: "sequential\_2"

Layer (type)	Output Shape	Param #
dense_2 (Dense)	(None, 1)	3
Total params: 3 (12.00 Byte)		
Trainable params: 3 (12.00 Byte)		
Non-trainable params: 0 (0.00 Byte)		

Przygotowanie danych:

```
xs=xs.reshape(-1,1)
ys=ys.reshape(-1,1)
data_points=np.concatenate([xs,ys],axis=1)
data_points
```

```
array([[4.59911355, 0.97664184],
       [5.12942909, 1.3036076 ],
       [2.86082513, 3.42102928],
       ...,
       [6.95434383, 6.18464347],
       [6.07670661, 6.40313423],
       [8.22009436, 6.28592032]])
```

Proces **uczenia**:

```
epochs = 100  
h = model.fit(data_points, labels, verbose=1, epochs=epochs, validation_split=0.2)
```

```
50/50 [=====] - 0s 2ms/step - loss: 0.1537 - val_loss: 0.1520
Epoch 95/100
50/50 [=====] - 0s 2ms/step - loss: 0.1545 - val_loss: 0.1389
Epoch 96/100
50/50 [=====] - 0s 3ms/step - loss: 0.1535 - val_loss: 0.1307
Epoch 97/100
50/50 [=====] - 0s 3ms/step - loss: 0.1522 - val_loss: 0.1314
Epoch 98/100
50/50 [=====] - 0s 2ms/step - loss: 0.1511 - val_loss: 0.1250
Epoch 99/100
50/50 [=====] - 0s 2ms/step - loss: 0.1501 - val_loss: 0.1223
Epoch 100/100
50/50 [=====] - 0s 3ms/step - loss: 0.1490 - val_loss: 0.1268
```

```
Loss = h.history['loss']
Loss
```

```
0.17914507259292005,
0.17762134969234467,
0.1760701686143875,
0.1745370328426361,
0.17292411625385284,
0.17147022485733032,
0.17005662620067596,
0.16858820617198944,
0.16722595691680908,
0.165882408618927,
0.16447201371192932,
0.16315360367298126,
0.16186299920082092,
0.16056708991527557,
0.1593204140663147,
0.1581363081932068,
0.15687452256679535,
0.15574510395526886,
0.15445458889007568,
0.15347152948379517,
0.15224675834178925,
0.151114821434021,
0.15006545186042786,
0.14902494847774506]
```

Sprawdźmy jakie są **wartości wag**:

```
weights = model.get_weights()
```

```
print(weights[0])
print(weights[1])    #bias
```

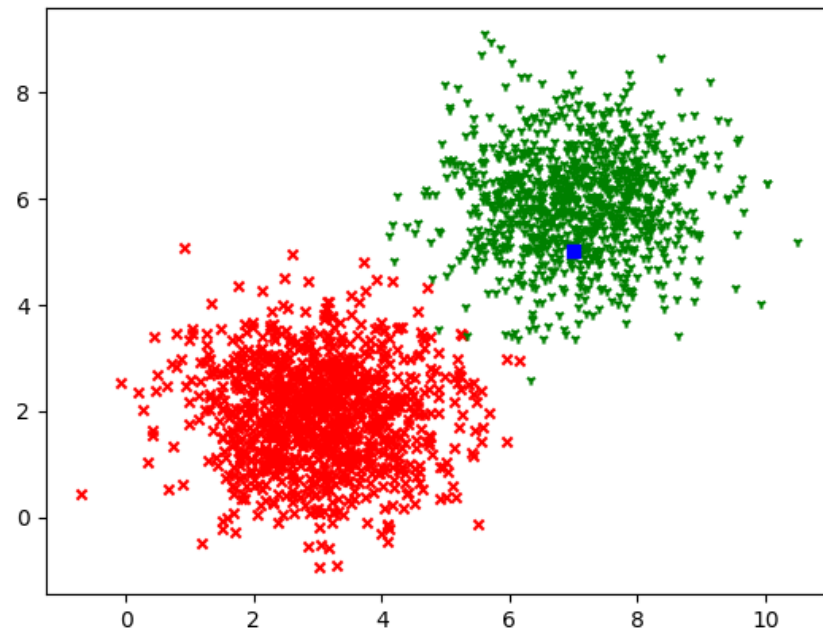
```
[[0.27534017]
 [0.8080815 ]]
[-4.4306183]
```

```
plt.scatter(np.arange(epochs),h.history['loss'])
plt.scatter(np.arange(epochs),h.history['val_loss'],c='r')
plt.show()
```



Sprawdzamy działanie modelu dla punktu o współrzędnych  $x$  i  $y$ :

```
x=7.0
y=5.0
plt.scatter(x_label1, y_label1, c='r', marker='x', s=20)
plt.scatter(x_label2, y_label2, c='g', marker='1', s=20)
plt.scatter(x,y,c='b', marker='s')
plt.show()
```



```
model.predict([[x,y]])
```

```
1/1 [=====] - 0s 74ms/step
array([[1.]], dtype=float32)
```

Learning rate 0.1 optimizer ADAM

Definiujemy model:

```
model = Sequential()
```

Dodajemy **jedną warstwę** (Dense) z **jednym neuronem** (units=1) z **biasem** (use\_bias=True) i **liniową funkcją aktywacji** (activation="linear"):

```
model.add(Dense(units = 1, use_bias=True, input_dim=2, activation = "softmax"))
```

Definiujemy **optymalizator i błąd** (entropia krzyżowa). **Współczynnik uczenia = 0.1**

```
opt = tf.keras.optimizers.Adam(learning_rate=0.1)
#opt = tf.keras.optimizers.SGD(learning_rate=0.1)
```

```
model.compile(loss='binary_crossentropy', optimizer=opt)
```

Informacja o modelu:

```
model.summary()
```

Model: "sequential\_3"

Layer (type)	Output Shape	Param #
dense_3 (Dense)	(None, 1)	3

```
=====
Total params: 3 (12.00 Byte)
Trainable params: 3 (12.00 Byte)
Non-trainable params: 0 (0.00 Byte)
```

Przygotowanie danych:

```
xs=xs.reshape(-1,1)
ys=ys.reshape(-1,1)
data_points=np.concatenate([xs,ys],axis=1)
data_points
```

```
array([[4.59911355, 0.97664184],
       [5.12942909, 1.3036076 ],
       [2.86082513, 3.42102928],
       ...,
       [6.95434383, 6.18464347],
       [6.07670661, 6.40313423],
       [8.22009436, 6.28592032]])
```

Proces **uczenia**:

```
epochs = 100
h = model.fit(data_points,labels, verbose=1, epochs=epochs,validation_split=0.2)
```

```
50/50 [=====] - 0s 2ms/step - loss: 0.0070 - val_loss: 0.0054
Epoch 86/100
50/50 [=====] - 0s 2ms/step - loss: 0.0071 - val_loss: 0.0083
Epoch 87/100
50/50 [=====] - 0s 3ms/step - loss: 0.0071 - val_loss: 0.0232
Epoch 88/100
50/50 [=====] - 0s 2ms/step - loss: 0.0072 - val_loss: 0.0101
Epoch 89/100
50/50 [=====] - 0s 2ms/step - loss: 0.0111 - val_loss: 0.0289
Epoch 90/100
50/50 [=====] - 0s 2ms/step - loss: 0.0096 - val_loss: 0.0129
Epoch 91/100
50/50 [=====] - 0s 2ms/step - loss: 0.0067 - val_loss: 0.0089
Epoch 92/100
50/50 [=====] - 0s 4ms/step - loss: 0.0092 - val_loss: 0.0329
Epoch 93/100
50/50 [=====] - 0s 4ms/step - loss: 0.0067 - val_loss: 0.0145
Epoch 94/100
50/50 [=====] - 0s 3ms/step - loss: 0.0073 - val_loss: 0.0139
Epoch 95/100
50/50 [=====] - 0s 4ms/step - loss: 0.0068 - val_loss: 0.0186
Epoch 96/100
50/50 [=====] - 0s 4ms/step - loss: 0.0076 - val_loss: 0.0175
Epoch 97/100
50/50 [=====] - 0s 5ms/step - loss: 0.0067 - val_loss: 0.0123
Epoch 98/100
50/50 [=====] - 0s 4ms/step - loss: 0.0077 - val_loss: 0.0172
Epoch 99/100
50/50 [=====] - 0s 3ms/step - loss: 0.0070 - val_loss: 0.0070
Epoch 100/100
50/50 [=====] - 0s 4ms/step - loss: 0.0080 - val_loss: 0.0278
```

```
Loss = h.history['loss']
```

```
Loss
```



```

0.0128000493795394097,
0.011629335582256317,
0.007521096616983414,
0.009643647819757462,
0.010077561251819134,
0.00716122193261981,
0.00870305672287941,
0.009027077816426754,
0.007176931947469711,
0.008700431324541569,
0.007629499305039644,
0.007525546010583639,
0.007324058562517166,
0.007840651087462902,
0.006922069936990738,
0.008075136691331863,
0.0075485240668058395,
0.008625146001577377,
0.008245621807873249,
0.006644793786108494,
0.007209888193756342,
0.0069216229021549225,
0.006888733711093664,
0.00666001858189702,
0.006527409423142672,
0.0070349290035665035,
0.007070205174386501,
0.007125018630176783,
0.00721875112503767,
0.011109217070043087,
0.009618628770112991,
0.006656251382082701,
0.00920072291046381,
0.00670555280521512,
0.007280466612428427,
0.006781424395740032,
0.007577568292617798,
0.006670651491731405,
0.007742272689938545,
0.0070458813570439816,
0.007955965586006641]

```

Sprawdźmy jakie są **wartości wag**:

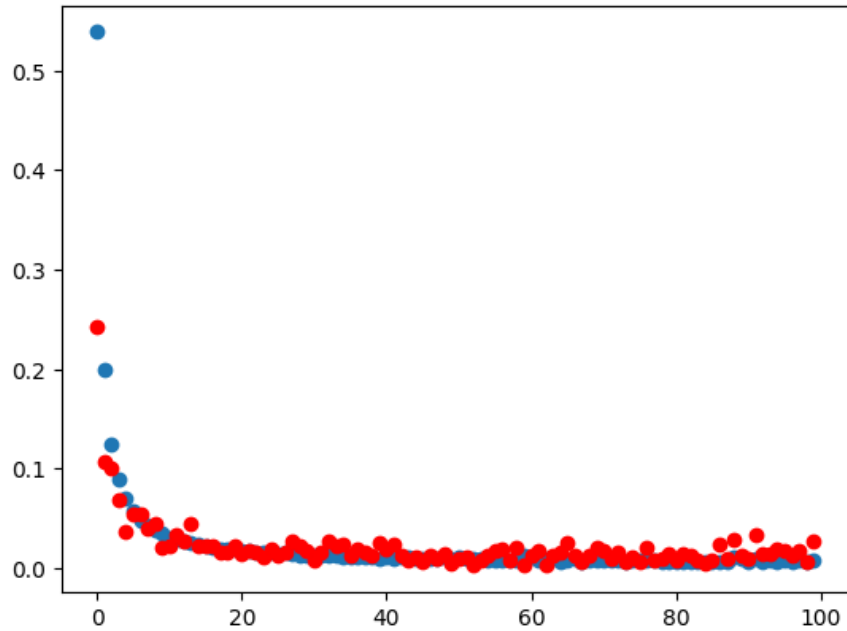
```
weights = model.get_weights()
```

```
print(weights[0])
```

```
print(weights[1])    #bias
```

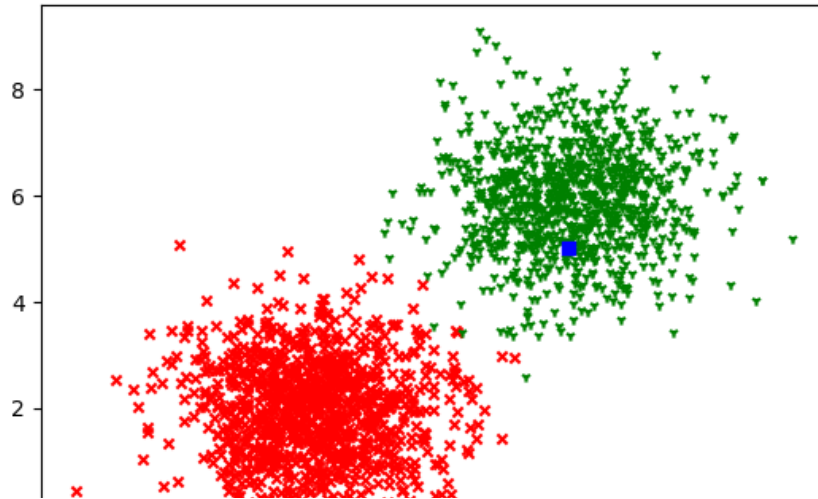
```
[[2.8030927]
 [3.1745062]]
[-28.42742]
```

```
plt.scatter(np.arange(epochs),h.history['loss'])
plt.scatter(np.arange(epochs),h.history['val_loss'],c='r')
plt.show()
```



Sprawdzamy działanie modelu dla punktu o współrzędnych **x** i **y**:

```
x=7.0
y=5.0
plt.scatter(x_label1, y_label1, c='r', marker='x', s=20)
plt.scatter(x_label2, y_label2, c='g', marker='1', s=20)
plt.scatter(x,y,c='b', marker='s')
plt.show()
```



```
model.predict([[x,y]])
```

```
1/1 [=====] - 0s 88ms/step  
array([[1.]], dtype=float32)
```

Learning rate 0.01 Optimizer Adam

Definiujemy model:

```
model = Sequential()
```

Dodajemy **jedną warstwę** (Dense) z **jednym neuronem** (units=1) z **biasem** (use\_bias=True) i **liniową funkcją aktywacji** (activation="linear"):

```
model.add(Dense(units = 1, use_bias=True, input_dim=2, activation = "softmax"))
```

Definiujemy **optymalizator** i **błąd** (entropia krzyżowa). **Współczynnik uczenia = 0.1**

```
opt = tf.keras.optimizers.Adam(learning_rate=0.01)  
#opt = tf.keras.optimizers.SGD(learning_rate=0.1)
```

```
model.compile(loss='binary_crossentropy',optimizer=opt)
```

Informacja o modelu:

```
model.summary()
```

Model: "sequential\_4"

Layer (type)	Output Shape	Param #
dense_4 (Dense)	(None, 1)	3
Total params: 3 (12.00 Byte)		
Trainable params: 3 (12.00 Byte)		
Non-trainable params: 0 (0.00 Byte)		

Przygotowanie danych:

```
xs=xs.reshape(-1,1)
ys=ys.reshape(-1,1)
data_points=np.concatenate([xs,ys],axis=1)
data_points
```

```
array([[4.59911355, 0.97664184],
       [5.12942909, 1.3036076 ],
       [2.86082513, 3.42102928],
       ...,
       [6.95434383, 6.18464347],
       [6.07670661, 6.40313423],
       [8.22009436, 6.28592032]])
```

Proces **uczenia**:

```
epochs = 100
h = model.fit(data_points,labels, verbose=1, epochs=epochs,validation_split=0.2)
```

```
Epoch 76/100 [=====] - 0s 2ms/step - loss: 0.0291 - val_loss: 0.0336
Epoch 77/100 [=====] - 0s 2ms/step - loss: 0.0287 - val_loss: 0.0318
Epoch 78/100 [=====] - 0s 2ms/step - loss: 0.0281 - val_loss: 0.0305
Epoch 79/100 [=====] - 0s 5ms/step - loss: 0.0278 - val_loss: 0.0266
Epoch 80/100 [=====] - 0s 5ms/step - loss: 0.0272 - val_loss: 0.0306
Epoch 81/100 [=====] - 0s 4ms/step - loss: 0.0267 - val_loss: 0.0280
Epoch 82/100 [=====] - 0s 4ms/step - loss: 0.0266 - val_loss: 0.0285
Epoch 83/100 [=====] - 0s 4ms/step - loss: 0.0259 - val_loss: 0.0307
Epoch 84/100 [=====] - 0s 4ms/step - loss: 0.0255 - val_loss: 0.0256
Epoch 85/100 [=====] - 0s 4ms/step - loss: 0.0251 - val_loss: 0.0266
Epoch 86/100 [=====] - 0s 4ms/step - loss: 0.0247 - val_loss: 0.0271
Epoch 87/100 [=====] - 0s 5ms/step - loss: 0.0243 - val_loss: 0.0253
Epoch 88/100 [=====] - 0s 4ms/step - loss: 0.0240 - val_loss: 0.0244
Epoch 89/100 [=====] - 0s 4ms/step - loss: 0.0236 - val_loss: 0.0228
Epoch 90/100 [=====] - 0s 5ms/step - loss: 0.0235 - val_loss: 0.0231
Epoch 91/100 [=====] - 0s 4ms/step - loss: 0.0229 - val_loss: 0.0243
Epoch 92/100 [=====] - 0s 3ms/step - loss: 0.0227 - val_loss: 0.0230
Epoch 93/100 [=====] - 0s 4ms/step - loss: 0.0223 - val_loss: 0.0223
Epoch 94/100 [=====] - 0s 4ms/step - loss: 0.0221 - val_loss: 0.0222
Epoch 95/100 [=====] - 0s 4ms/step - loss: 0.0217 - val_loss: 0.0257
Epoch 96/100 [=====] - 0s 3ms/step - loss: 0.0214 - val_loss: 0.0236
Epoch 97/100 [=====] - 0s 4ms/step - loss: 0.0211 - val_loss: 0.0250
Epoch 98/100 [=====] - 0s 4ms/step - loss: 0.0208 - val_loss: 0.0237
Epoch 99/100 [=====] - 0s 3ms/step - loss: 0.0205 - val_loss: 0.0205
Epoch 100/100 [=====] - 0s 2ms/step - loss: 0.0203 - val_loss: 0.0225
Epoch 100/100 [=====] - 0s 2ms/step - loss: 0.0200 - val_loss: 0.0212
```

```
Loss = h.history['loss']
```

```
Loss
```

```
0.058860503137111664,  
0.0572054386138916,  
0.05562101677060127,  
0.05422927439212799,  
0.05283689498901367,  
0.051276255398988724,
```

```
0.0222060750110705094,
0.022267919033765793,
0.0221176128834486,
0.021740354597568512,
0.021388988941907883,
0.02106151357293129,
0.020833753049373627,
0.02054629847407341,
0.020297998562455177,
0.0199813228100538251
```

Sprawdźmy jakie są **wartości wag**:

```
weights = model.get_weights()
```

```
print(weights[0])
```

```
print(weights[1])    #bias
```

```
[[1.2608098]
 [1.6906005]]
[-12.958403]
```

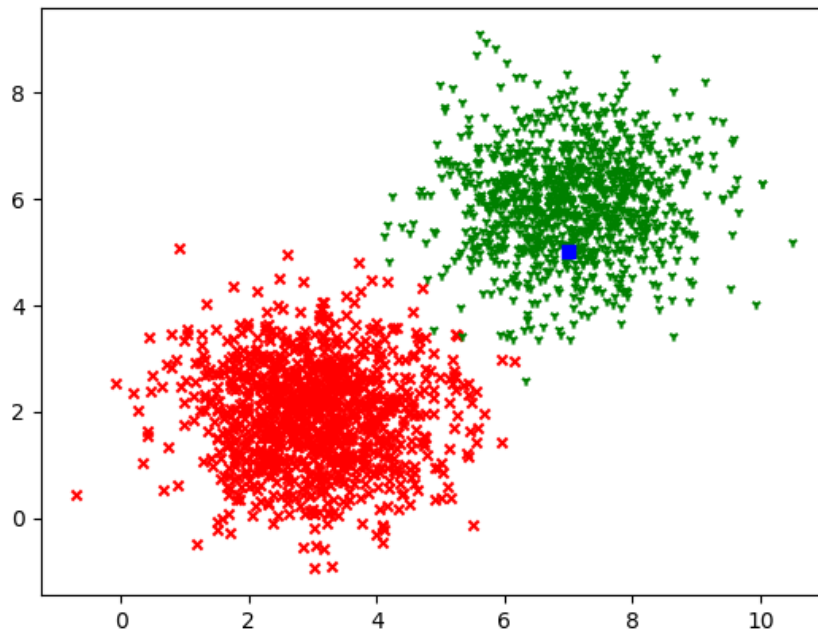
```
plt.scatter(np.arange(epochs),h.history['loss'])
```

```
plt.scatter(np.arange(epochs),h.history['val_loss'],c='r')
```

```
plt.show()
```

Sprawdzamy działanie modelu dla punktu o współrzędnych  $x$  i  $y$ :

```
x=7.0
y=5.0
plt.scatter(x_label1, y_label1, c='r', marker='x', s=20)
plt.scatter(x_label2, y_label2, c='g', marker='v', s=20)
plt.scatter(x,y,c='b', marker='s')
plt.show()
```



```
model.predict([[x,y]])
```

```
WARNING:tensorflow:5 out of the last 5 calls to <function Model.make_predict_function.<locals>.predict_function at 0x7d1f18db2050> triggered tf.function
1/1 [=====] - 0s 61ms/step
array([[1.]], dtype=float32)
```

▼ Number of epochs - 200



Definiujemy model:

```
model = Sequential()
```

Dodajemy **jedną warstwę** (Dense) z **jednym neuronem** (units=1) z **biasem** (use\_bias=True) i **liniową funkcją aktywacji** (activation="linear"):

```
model.add(Dense(units = 1, use_bias=True, input_dim=2, activation = "softmax"))
```

Definiujemy **optymalizator** i **błąd** (entropia krzyżowa). **Współczynnik uczenia = 0.1**

```
#opt = tf.keras.optimizers.Adam(learning_rate=0.1)
opt = tf.keras.optimizers.SGD(learning_rate=0.1)
```

```
model.compile(loss='binary_crossentropy', optimizer=opt)
```

Informacja o modelu:

```
model.summary()
```

Model: "sequential\_5"

Layer (type)	Output Shape	Param #
dense_5 (Dense)	(None, 1)	3
Total params: 3 (12.00 Byte)		
Trainable params: 3 (12.00 Byte)		
Non-trainable params: 0 (0.00 Byte)		

Przygotowanie danych:

```
xs=xs.reshape(-1,1)
ys=ys.reshape(-1,1)
data_points=np.concatenate([xs,ys],axis=1)
data_points
```

```
array([[4.59911355, 0.97664184],
       [5.12942909, 1.3036076 ]],
```

```
[2.86082513, 3.42102928],  
...,  
[6.95434383, 6.18464347],  
[6.07670661, 6.40313423],  
[8.22009436, 6.28592032]])
```

Proces **uczenia**:

```
epochs = 200  
h = model.fit(data_points, labels, verbose=1, epochs=epochs, validation_split=0.2)
```

```

Epoch 191/200
50/50 [=====] - 0s 2ms/step - loss: 0.0213 - val_loss: 0.0217
Epoch 192/200
50/50 [=====] - 0s 2ms/step - loss: 0.0212 - val_loss: 0.0240
Epoch 193/200
50/50 [=====] - 0s 3ms/step - loss: 0.0211 - val_loss: 0.0214
Epoch 194/200
50/50 [=====] - 0s 2ms/step - loss: 0.0211 - val_loss: 0.0253
Epoch 195/200
50/50 [=====] - 0s 2ms/step - loss: 0.0210 - val_loss: 0.0233
Epoch 196/200
50/50 [=====] - 0s 2ms/step - loss: 0.0210 - val_loss: 0.0229
Epoch 197/200
50/50 [=====] - 0s 2ms/step - loss: 0.0208 - val_loss: 0.0239
Epoch 198/200
50/50 [=====] - 0s 2ms/step - loss: 0.0208 - val_loss: 0.0234
Epoch 199/200
50/50 [=====] - 0s 2ms/step - loss: 0.0208 - val_loss: 0.0223
Epoch 200/200
50/50 [=====] - 0s 2ms/step - loss: 0.0208 - val_loss: 0.0220

```

```

Loss = h.history['loss']
Loss

```

```
0.022259901550491249,
0.022498061880469322,
0.022502753883600235,
0.02228054776787758,
0.022296320647001266,
0.02225557528436184,
0.0222723837941885,
0.022042419761419296,
0.02201276831328869,
0.02203170210123062,
0.02192268893122673,
0.02181338332593441,
0.02175765298306942,
0.02170962281525135,
0.02156413532793522,
0.02156808227300644,
0.02149846777319908,
0.021432815119624138,
0.021359015256166458,
0.02141267992556095,
0.02129703015089035,
0.021153021603822708,
0.021115155890583992,
0.02106969989836216,
0.02104480005800724,
0.02095261961221695,
0.020845530554652214,
0.02084415592253208,
0.020754141733050346,
0.020753316581249237]
```

Sprawdźmy jakie są **wartości wag**:

```
weights = model.get_weights()
```

```
print(weights[0])
```

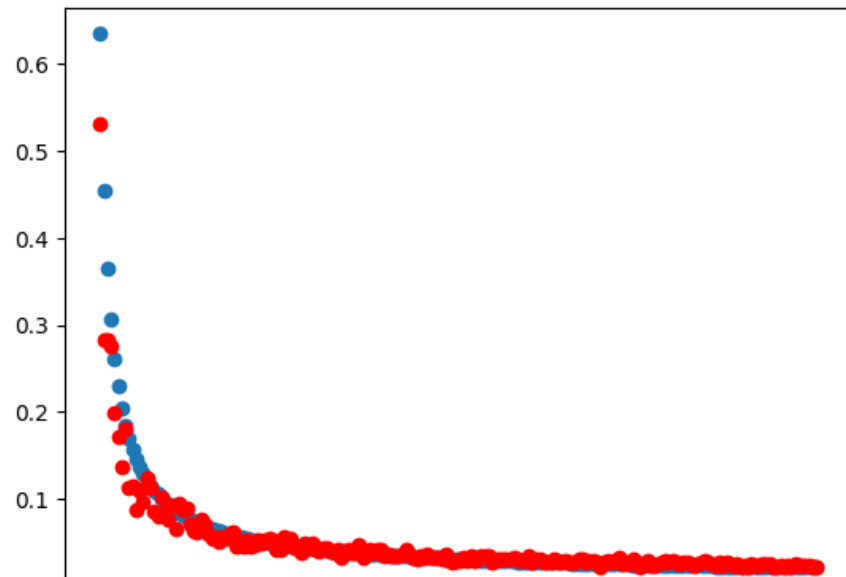
```
print(weights[1])    #bias
```

```
[[1.2378157]
 [1.6589917]]
[-12.722816]
```

```
plt.scatter(np.arange(epochs),h.history['loss'])
```

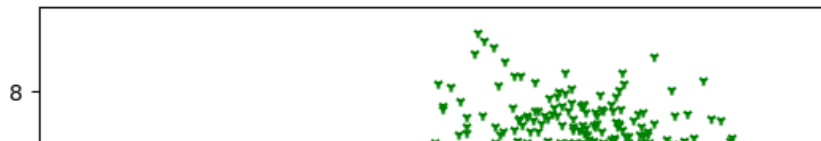
```
plt.scatter(np.arange(epochs),h.history['val_loss'],c='r')
```

```
plt.show()
```



Sprawdzamy działanie modelu dla punktu o współrzędnych  $x$  i  $y$ :

```
x=7.0  
y=5.0  
plt.scatter(x_label1, y_label1, c='r', marker='x', s=20)  
plt.scatter(x_label2, y_label2, c='g', marker='1', s=20)  
plt.scatter(x,y,c='b', marker='s')  
plt.show()
```



```
model.predict([[x,y]])
```

```
WARNING:tensorflow:6 out of the last 6 calls to <function Model.make_predict_function.<locals>.predict_function at 0x7d1f18b09cf0> triggered tf.funct
1/1 [=====] - 0s 67ms/step
array([[1.]], dtype=float32)
```



## ▼ Number of epochs - 10



Definiujemy model:

```
0 2 4 6 8 10
```

```
model = Sequential()
```

Dodajemy **jedną warstwę** (Dense) z **jednym neuronem** (units=1) z **biasem** (use\_bias=True) i **liniową funkcją aktywacji** (activation="linear"):

```
model.add(Dense(units = 1, use_bias=True, input_dim=2, activation = "softmax"))
```

Definiujemy **optimalizator** i **błąd** (entropia krzyżowa). **Współczynnik uczenia = 0.1**

```
#opt = tf.keras.optimizers.Adam(learning_rate=0.1)
opt = tf.keras.optimizers.SGD(learning_rate=0.1)
```

```
model.compile(loss='binary_crossentropy', optimizer=opt)
```

Informacja o modelu:

```
model.summary()
```

```
Model: "sequential_6"
```

Layer (type)	Output Shape	Param #
--------------	--------------	---------

```
=====
dense_6 (Dense)                (None, 1)                3
=====
Total params: 3 (12.00 Byte)
Trainable params: 3 (12.00 Byte)
Non-trainable params: 0 (0.00 Byte)
=====
```

Przygotowanie danych:

```
xs=xs.reshape(-1,1)
ys=ys.reshape(-1,1)
data_points=np.concatenate([xs,ys],axis=1)
data_points
```

```
array([[4.59911355, 0.97664184],
       [5.12942909, 1.3036076 ],
       [2.86082513, 3.42102928],
       ...,
       [6.95434383, 6.18464347],
       [6.07670661, 6.40313423],
       [8.22009436, 6.28592032]])
```

Proces **uczenia**:

```
epochs = 10
h = model.fit(data_points,labels, verbose=1, epochs=epochs,validation_split=0.2)

Epoch 1/10
50/50 [=====] - 0s 5ms/step - loss: 0.7866 - val_loss: 0.3952
Epoch 2/10
50/50 [=====] - 0s 2ms/step - loss: 0.4571 - val_loss: 0.2438
Epoch 3/10
50/50 [=====] - 0s 3ms/step - loss: 0.3674 - val_loss: 0.2025
Epoch 4/10
50/50 [=====] - 0s 2ms/step - loss: 0.3076 - val_loss: 0.2083
Epoch 5/10
50/50 [=====] - 0s 3ms/step - loss: 0.2644 - val_loss: 0.2335
Epoch 6/10
50/50 [=====] - 0s 2ms/step - loss: 0.2302 - val_loss: 0.2031
Epoch 7/10
50/50 [=====] - 0s 2ms/step - loss: 0.2054 - val_loss: 0.1173
Epoch 8/10
50/50 [=====] - 0s 3ms/step - loss: 0.1858 - val_loss: 0.1901
Epoch 9/10
50/50 [=====] - 0s 2ms/step - loss: 0.1700 - val_loss: 0.1430
```

Epoch 10/10

50/50 [=====] - 0s 2ms/step - loss: 0.1575 - val\_loss: 0.1046

```
Loss = h.history['loss']
```

```
Loss
```

```
[0.7865601181983948,  
0.45706140995025635,  
0.3674454987049103,  
0.3076130747795105,  
0.26441678404808044,  
0.23018169403076172,  
0.20535224676132202,  
0.18581746518611908,  
0.16995273530483246,  
0.15750856697559357]
```

Sprawdźmy jakie są **wartości wag**:

```
weights = model.get_weights()
```

```
print(weights[0])
```

```
print(weights[1])    #bias
```

```
[[0.29183912]  
 [0.81965226]]  
[-4.3890634]
```

```
plt.scatter(np.arange(epochs),h.history['loss'])
```

```
plt.scatter(np.arange(epochs),h.history['val_loss'],c='r')
```

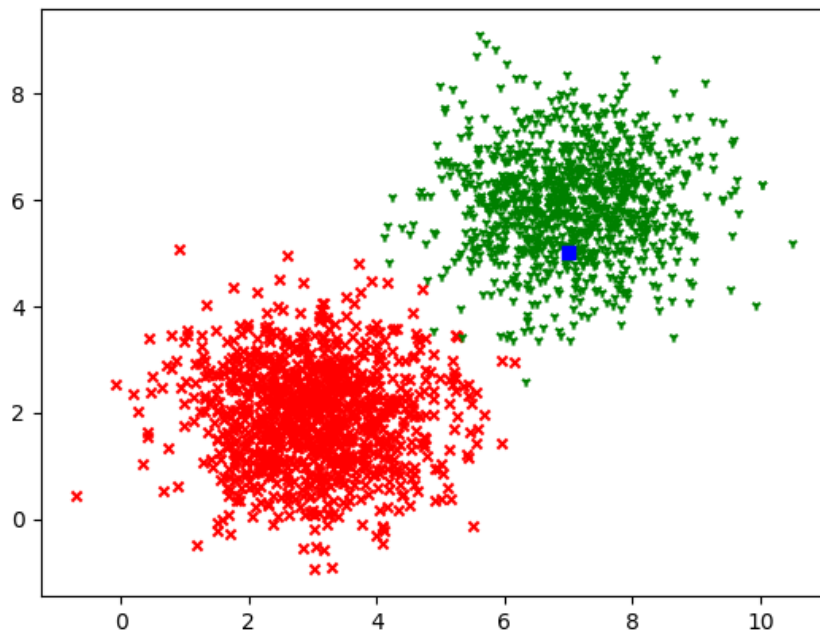
```
plt.show()
```





Sprawdzamy działanie modelu dla punktu o współrzędnych  $x$  i  $y$ :

```
x=7.0
y=5.0
plt.scatter(x_label1, y_label1, c='r', marker='x', s=20)
plt.scatter(x_label2, y_label2, c='g', marker='1', s=20)
plt.scatter(x,y,c='b', marker='s')
plt.show()
```



```
model.predict([[x,y]])
```

```
1/1 [=====] - 0s 68ms/step
array([[1.]], dtype=float32)
```

## ▼ Batch size - 10

Definiujemy model:

```
model = Sequential()
```

Dodajemy **jedną warstwę** (Dense) z **jednym neuronem** (units=1) z **biasem** (use\_bias=True) i **liniową funkcją aktywacji** (activation="linear"):

```
model.add(Dense(units = 1, use_bias=True, input_dim=2, activation = "softmax"))
```

Definiujemy **optymalizator i błąd** (entropia krzyżowa). **Współczynnik uczenia = 0.1**

```
#opt = tf.keras.optimizers.Adam(learning_rate=0.1)
opt = tf.keras.optimizers.SGD(learning_rate=0.1)
```

```
model.compile(loss='binary_crossentropy', optimizer=opt)
```

Informacja o modelu:

```
model.summary()
```

Model: "sequential\_7"

Layer (type)	Output Shape	Param #
dense_7 (Dense)	(None, 1)	3

```
=====
Total params: 3 (12.00 Byte)
Trainable params: 3 (12.00 Byte)
Non-trainable params: 0 (0.00 Byte)
=====
```

Przygotowanie danych:

```
xs=xs.reshape(-1,1)
ys=ys.reshape(-1,1)
data_points=np.concatenate([xs,ys],axis=1)
data_points
```

```
array([[4.59911355, 0.97664184],
       [5.12942909, 1.3036076 ],
       [2.86082513, 3.42102928],
       ...,
       [6.95434383, 6.18464347],
       [6.07670661, 6.40313423],
       [8.22009436, 6.28592032]])
```

Proces **uczenia**:

```
epochs = 100
h = model.fit(data_points,labels, verbose=1, epochs=epochs,validation_split=0.2, batch_size=10)
```

```
100/100 [=====] - 0s 2ms/step - loss: 0.0174 - val_loss: 0.0159
Epoch 88/100
160/160 [=====] - 0s 2ms/step - loss: 0.0175 - val_loss: 0.0231
Epoch 89/100
160/160 [=====] - 0s 2ms/step - loss: 0.0175 - val_loss: 0.0184
Epoch 90/100
160/160 [=====] - 0s 2ms/step - loss: 0.0173 - val_loss: 0.0262
Epoch 91/100
160/160 [=====] - 0s 2ms/step - loss: 0.0168 - val_loss: 0.0132
Epoch 92/100
160/160 [=====] - 0s 3ms/step - loss: 0.0171 - val_loss: 0.0185
Epoch 93/100
160/160 [=====] - 1s 3ms/step - loss: 0.0170 - val_loss: 0.0206
Epoch 94/100
160/160 [=====] - 0s 3ms/step - loss: 0.0166 - val_loss: 0.0281
Epoch 95/100
160/160 [=====] - 1s 3ms/step - loss: 0.0169 - val_loss: 0.0195
Epoch 96/100
160/160 [=====] - 1s 3ms/step - loss: 0.0168 - val_loss: 0.0186
Epoch 97/100
160/160 [=====] - 1s 3ms/step - loss: 0.0167 - val_loss: 0.0236
Epoch 98/100
160/160 [=====] - 1s 3ms/step - loss: 0.0165 - val_loss: 0.0227
Epoch 99/100
160/160 [=====] - 1s 3ms/step - loss: 0.0164 - val_loss: 0.0162
Epoch 100/100
160/160 [=====] - 0s 2ms/step - loss: 0.0165 - val_loss: 0.0178
```

```
Loss = h.history['loss']
```

```
Loss
```



```

0.02000032107100900037,
0.020555077120661736,
0.020151283591985703,
0.02014980837702751,
0.02003246359527111,
0.019833596423268318,
0.019581222906708717,
0.019504787400364876,
0.019469643011689186,
0.01912849023938179,
0.01909606158733368,
0.018833132460713387,
0.018953680992126465,
0.018806057050824165,
0.018672440201044083,
0.018537817522883415,
0.01850062981247902,
0.01818443089723587,
0.018275076523423195,
0.017901865765452385,
0.01781781017780304,
0.017891157418489456,
0.01760541833937168,
0.0173624437302351,
0.01749018393456936,
0.01753355748951435,
0.017299102619290352,
0.016815299168229103,
0.017127567902207375,
0.01703708805143833,
0.016594650223851204,
0.01686752215027809,
0.016810324043035507,
0.016653338447213173,
0.01652146875858307,
0.016429556533694267,
0.016491206362843513]

```

Sprawdźmy jakie są **wartości wag**:

```
weights = model.get_weights()
```

```
print(weights[0])
```

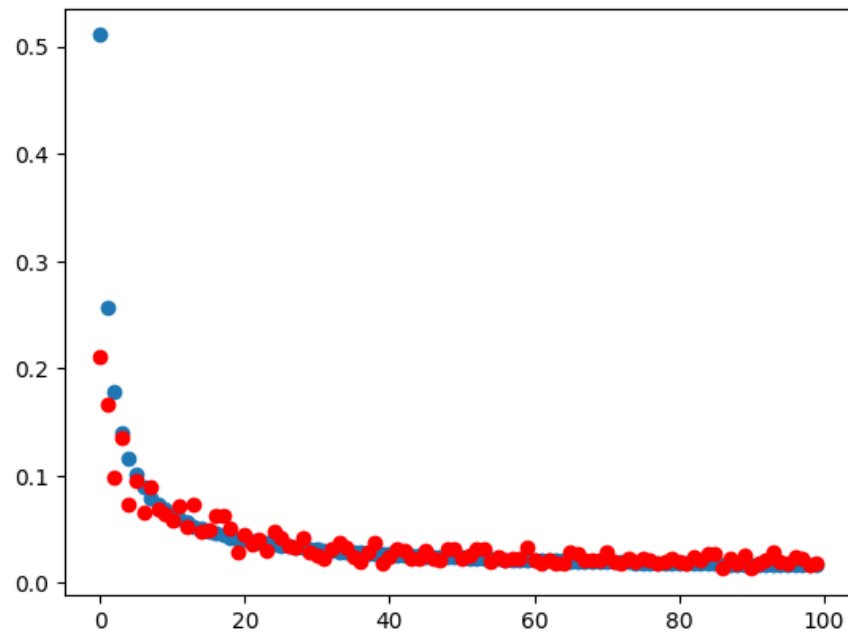
```
print(weights[1])    #bias
```

```

[[1.418916 ]
 [1.8477014]]
[-14.371391]

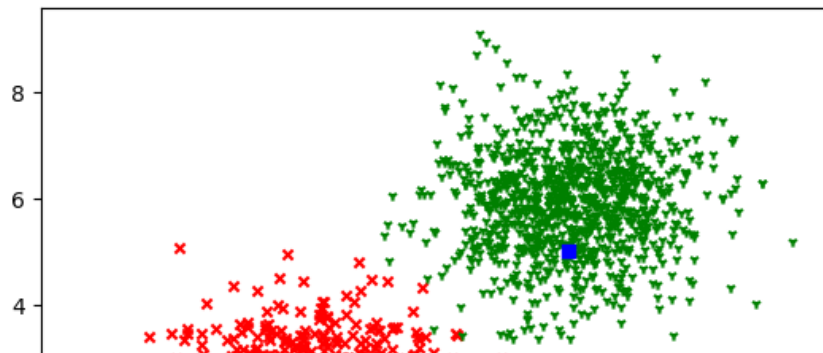
```

```
plt.scatter(np.arange(epochs),h.history['loss'])
plt.scatter(np.arange(epochs),h.history['val_loss'],c='r')
plt.show()
```



Sprawdzamy działanie modelu dla punktu o współrzędnych  $x$  i  $y$ :

```
x=7.0
y=5.0
plt.scatter(x_label1, y_label1, c='r', marker='x', s=20)
plt.scatter(x_label2, y_label2, c='g', marker='1', s=20)
plt.scatter(x,y,c='b', marker='s')
plt.show()
```



```
model.predict([[x,y]])
```

```
1/1 [=====] - 0s 63ms/step
```

```
array([[1.]], dtype=float32)
```

```
0.1
```

▼ Batch size - 20

Definiujemy model:

```
model = Sequential()
```

Dodajemy **jedną warstwę** (Dense) z **jednym neuronem** (units=1) z **biasem** (use\_bias=True) i **liniową funkcją aktywacji** (activation="linear"):

```
model.add(Dense(units = 1, use_bias=True, input_dim=2, activation = "softmax"))
```

Definiujemy **optimalizator** i **błąd** (entropia krzyżowa). **Współczynnik uczenia = 0.1**

```
#opt = tf.keras.optimizers.Adam(learning_rate=0.1)
```

```
opt = tf.keras.optimizers.SGD(learning_rate=0.1)
```

```
model.compile(loss='binary_crossentropy', optimizer=opt)
```

Informacja o modelu:

```
model.summary()
```

```
Model: "sequential_8"
```

Layer (type)	Output Shape	Param #
dense_8 (Dense)	(None, 1)	3
Total params: 3 (12.00 Byte)		
Trainable params: 3 (12.00 Byte)		
Non-trainable params: 0 (0.00 Byte)		

Przygotowanie danych:

```
xs=xs.reshape(-1,1)
ys=ys.reshape(-1,1)
data_points=np.concatenate([xs,ys],axis=1)
data_points
```

```
array([[4.59911355, 0.97664184],
       [5.12942909, 1.3036076 ],
       [2.86082513, 3.42102928],
       ...,
       [6.95434383, 6.18464347],
       [6.07670661, 6.40313423],
       [8.22009436, 6.28592032]])
```

Proces **uczenia**:

```
epochs = 100
h = model.fit(data_points,labels, verbose=1, epochs=epochs,validation_split=0.2,batch_size=20)
```



```

Epoch 78/100
80/80 [=====] - 0s 3ms/step - loss: 0.0272 - val_loss: 0.0314
Epoch 79/100
80/80 [=====] - 0s 2ms/step - loss: 0.0267 - val_loss: 0.0299
Epoch 80/100
80/80 [=====] - 0s 3ms/step - loss: 0.0266 - val_loss: 0.0245
Epoch 81/100
80/80 [=====] - 0s 2ms/step - loss: 0.0265 - val_loss: 0.0315
Epoch 82/100
80/80 [=====] - 0s 3ms/step - loss: 0.0263 - val_loss: 0.0258
Epoch 83/100
80/80 [=====] - 0s 2ms/step - loss: 0.0261 - val_loss: 0.0285
Epoch 84/100
80/80 [=====] - 0s 3ms/step - loss: 0.0260 - val_loss: 0.0246
Epoch 85/100
80/80 [=====] - 0s 3ms/step - loss: 0.0258 - val_loss: 0.0244
Epoch 86/100
80/80 [=====] - 0s 3ms/step - loss: 0.0258 - val_loss: 0.0284
Epoch 87/100
80/80 [=====] - 0s 2ms/step - loss: 0.0254 - val_loss: 0.0292
Epoch 88/100
80/80 [=====] - 0s 3ms/step - loss: 0.0254 - val_loss: 0.0292
Epoch 89/100
80/80 [=====] - 0s 2ms/step - loss: 0.0249 - val_loss: 0.0383
Epoch 90/100
80/80 [=====] - 0s 2ms/step - loss: 0.0249 - val_loss: 0.0206
Epoch 91/100
80/80 [=====] - 0s 3ms/step - loss: 0.0248 - val_loss: 0.0225
Epoch 92/100
80/80 [=====] - 0s 2ms/step - loss: 0.0246 - val_loss: 0.0256
Epoch 93/100
80/80 [=====] - 0s 2ms/step - loss: 0.0245 - val_loss: 0.0279
Epoch 94/100
80/80 [=====] - 0s 2ms/step - loss: 0.0244 - val_loss: 0.0261
Epoch 95/100
80/80 [=====] - 0s 2ms/step - loss: 0.0241 - val_loss: 0.0265
Epoch 96/100
80/80 [=====] - 0s 2ms/step - loss: 0.0240 - val_loss: 0.0211
Epoch 97/100
80/80 [=====] - 0s 2ms/step - loss: 0.0239 - val_loss: 0.0275
Epoch 98/100
80/80 [=====] - 0s 2ms/step - loss: 0.0239 - val_loss: 0.0235
Epoch 99/100
80/80 [=====] - 0s 3ms/step - loss: 0.0234 - val_loss: 0.0275
Epoch 100/100
80/80 [=====] - 0s 2ms/step - loss: 0.0233 - val_loss: 0.0185

```

```

Loss = h.history['loss']
Loss

```

```
0.03918968141078949,  
0.03852969780564308,  
0.03800367936491966,  
0.03734232485294342,  
0.036846622824668884,  
0.03639788553118706,  
0.036081910133361816,  
0.03542118892073631,  
0.035184700042009354,
```

```
0.024500252110105112,
0.02413579449057579,
0.023975389078259468,
0.023930862545967102,
0.02390175312757492,
0.023398425430059433,
0.023250408470630646]
```

Sprawdźmy jakie są **wartości wag**:

```
weights = model.get_weights()
```

```
print(weights[0])
```

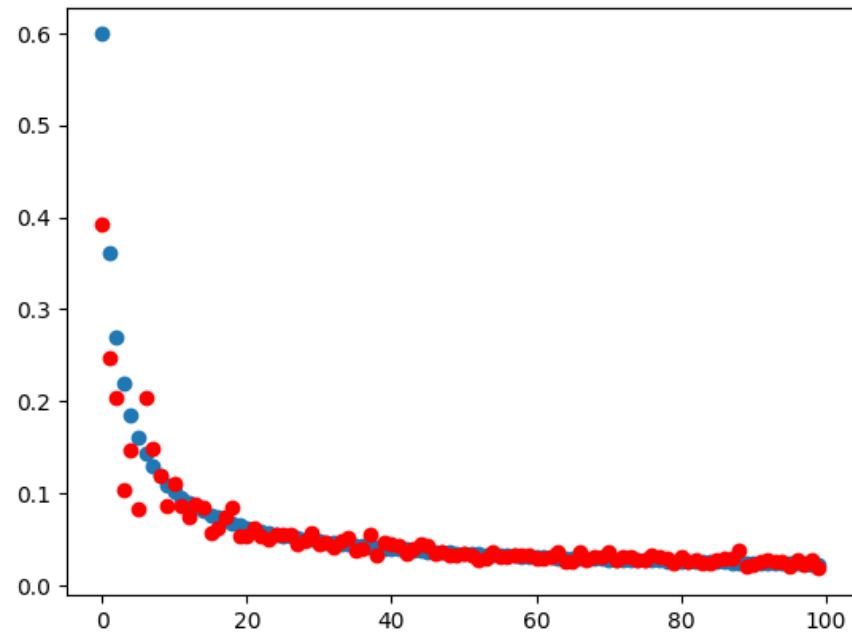
```
print(weights[1])    #bias
```

```
[[1.1901294]
 [1.6065422]]
[-12.003977]
```

```
plt.scatter(np.arange(epochs),h.history['loss'])
```

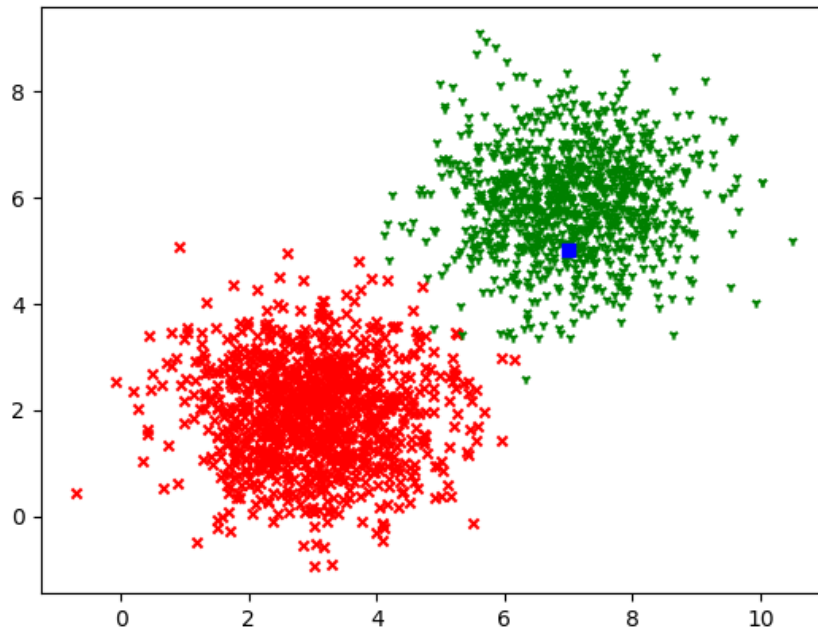
```
plt.scatter(np.arange(epochs),h.history['val_loss'],c='r')
```

```
plt.show()
```



Sprawdzamy działanie modelu dla punktu o współrzędnych  $x$  i  $y$ :

```
x=7.0
y=5.0
plt.scatter(x_label1, y_label1, c='r', marker='x', s=20)
plt.scatter(x_label2, y_label2, c='g', marker='v', s=20)
plt.scatter(x,y,c='b', marker='s')
plt.show()
```



```
model.predict([[x,y]])
```

```
1/1 [=====] - 0s 56ms/step
array([[1.]], dtype=float32)
```

▼ Batch size 50

Definiujemy model:

```
model = Sequential()
```

Dodajemy **jedną warstwę** (Dense) z **jednym neuronem** (units=1) z **biasem** (use\_bias=True) i **liniową funkcją aktywacji** (activation="linear"):

```
model.add(Dense(units = 1, use_bias=True, input_dim=2, activation = "softmax"))
```

Definiujemy **optymalizator** i **błąd** (entropia krzyżowa). **Współczynnik uczenia = 0.1**

```
#opt = tf.keras.optimizers.Adam(learning_rate=0.1)
opt = tf.keras.optimizers.SGD(learning_rate=0.1)
```

```
model.compile(loss='binary_crossentropy', optimizer=opt)
```

Informacja o modelu:

```
model.summary()
```

Model: "sequential\_9"

Layer (type)	Output Shape	Param #
dense_9 (Dense)	(None, 1)	3
Total params: 3 (12.00 Byte)		
Trainable params: 3 (12.00 Byte)		
Non-trainable params: 0 (0.00 Byte)		

Przygotowanie danych:

```
xs=xs.reshape(-1,1)
ys=ys.reshape(-1,1)
data_points=np.concatenate([xs,ys],axis=1)
data_points
```

```
array([[4.59911355, 0.97664184],
       [5.12942909, 1.3036076 ]],
```

```
[2.86082513, 3.42102928],  
...,  
[6.95434383, 6.18464347],  
[6.07670661, 6.40313423],  
[8.22009436, 6.28592032]])
```

Proces **uczenia**:

```
epochs = 100  
h = model.fit(data_points, labels, verbose=1, epochs=epochs, validation_split=0.2, batch_size=50)
```

```

Epoch 91/100
32/32 [=====] - 0s 3ms/step - loss: 0.0431 - val_loss: 0.0368
Epoch 92/100
32/32 [=====] - 0s 4ms/step - loss: 0.0429 - val_loss: 0.0454
Epoch 93/100
32/32 [=====] - 0s 4ms/step - loss: 0.0425 - val_loss: 0.0476
Epoch 94/100
32/32 [=====] - 0s 4ms/step - loss: 0.0423 - val_loss: 0.0460
Epoch 95/100
32/32 [=====] - 0s 4ms/step - loss: 0.0421 - val_loss: 0.0426
Epoch 96/100
32/32 [=====] - 0s 4ms/step - loss: 0.0417 - val_loss: 0.0453
Epoch 97/100
32/32 [=====] - 0s 4ms/step - loss: 0.0413 - val_loss: 0.0402
Epoch 98/100
32/32 [=====] - 0s 4ms/step - loss: 0.0410 - val_loss: 0.0455
Epoch 99/100
32/32 [=====] - 0s 4ms/step - loss: 0.0410 - val_loss: 0.0438
Epoch 100/100
32/32 [=====] - 0s 4ms/step - loss: 0.0406 - val_loss: 0.0423

```

```
Loss = h.history['loss']
```

```
Loss
```

```
0.05102117559050214,
0.050185270607471466,
0.049949631094932556,
0.04948272183537483,
0.04902293533086777,
0.048761483281850815,
0.04820432513952255,
0.04773036018013954,
0.047397080808877945,
0.04695950821042061,
0.04658462479710579,
0.04623636603355408,
0.04589775577187538,
0.04555024951696396,
0.045185331255197525,
0.04477369785308838,
0.04453828185796738,
0.04416794702410698,
0.0438012070953846,
0.04348074272274971,
0.043111030012369156,
0.04287131875753403,
0.0424988716840744,
0.0423225462436676,
0.04207630082964897,
0.04169486090540886,
0.04128500074148178,
0.041049886494874954,
0.04099629074335098,
0.040603771805763245]
```

Sprawdźmy jakie są **wartości wag**:

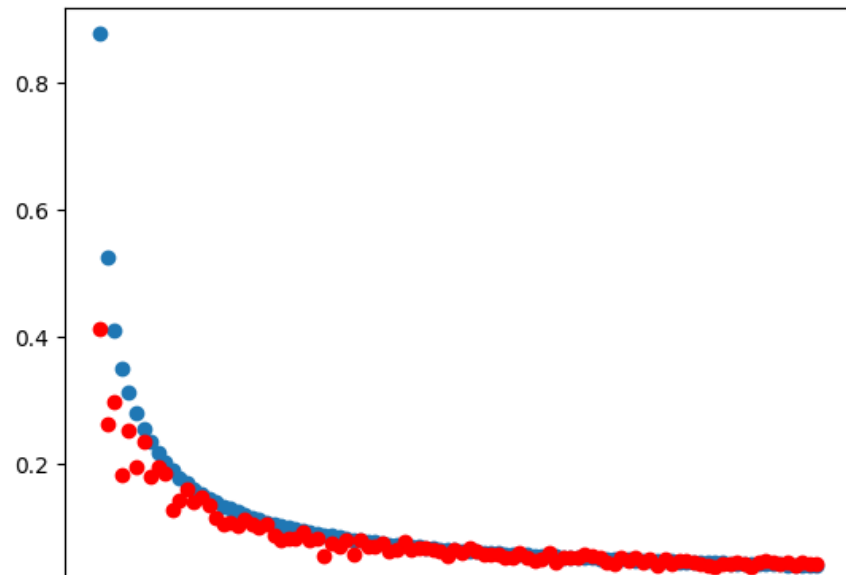
```
weights = model.get_weights()
```

```
print(weights[0])
print(weights[1])    #bias
```

```
[[0.8336686]
 [1.2803266]]
[-9.240546]
```

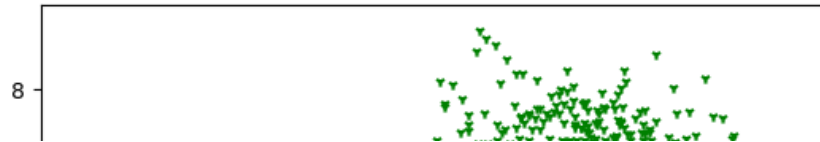
```
plt.scatter(np.arange(epochs),h.history['loss'])
plt.scatter(np.arange(epochs),h.history['val_loss'],c='r')
plt.show()
```





Sprawdzamy działanie modelu dla punktu o współrzędnych  $x$  i  $y$ :

```
x=7.0  
y=5.0  
plt.scatter(x_label1, y_label1, c='r', marker='x', s=20)  
plt.scatter(x_label2, y_label2, c='g', marker='1', s=20)  
plt.scatter(x,y,c='b', marker='s')  
plt.show()
```



```
model.predict([[x,y]])
```

```
1/1 [=====] - 0s 58ms/step
```

```
array([[1.]], dtype=float32)
```



Najlepsze wyniki otrzymałem dla współczynnika uczenia 0.1, liczby epok 3000, batcha równego 20, najgorsze dla współczynnika uczenia 0.001, liczby epok 10, batcha równego 50

