```
import tensorflow as tf
import matplotlib.pyplot as plt
import numpy as np

import keras
from keras.models import Sequential
from keras.layers import Dense
```

→ Regresja softmax

```
s = [0.2, 0.1, 0.6, 0.1]
exps = [np.exp(i) for i in s]
sum_of_exps = sum(exps)
softmax = [j/sum of exps for j in exps]
```

→ 3 gangi

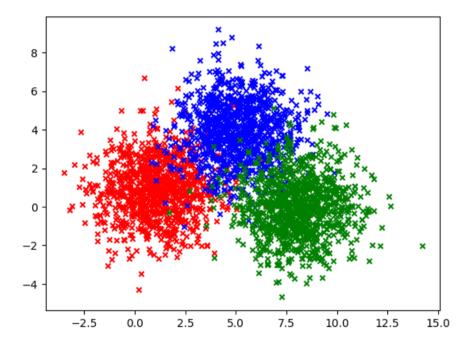
Zbiór danych:

```
x_label0 = np.random.normal(1, 1.5, (1000, 1))
y_label0 = np.random.normal(1, 1.5, (1000, 1))
x_label1 = np.random.normal(5, 1.5, (1000, 1))
y_label1 = np.random.normal(4, 1.5, (1000, 1))
y_label2 = np.random.normal(8, 1.5, (1000, 1))
y_label2 = np.random.normal(8, 1.5, (1000, 1))
y_label2 = np.random.normal(0, 1.5, (1000, 1))

data_label0 = np.concatenate([x_label0, y_label0],axis=1)
data_label1 = np.concatenate([x_label1, y_label1],axis=1)
data_label2 = np.concatenate([x_label2, y_label2],axis=1)
points = np.concatenate([data_label0, data_label1, data_label2],axis=0)

Kodowanie one-hot

labels = np.array([[1., 0., 0.]] * len(data_label0) + [[0., 1., 0.]] * len(data_label1) + [[0., 0., 1.]] * len(data_label2))
```



```
model = Sequential()

model.add(Dense(units = 3, use_bias=True, input_dim=2, activation = "softmax"))

#opt = tf.keras.optimizers.Adam(learning_rate=0.1)
opt = tf.keras.optimizers.Adam()
#opt = tf.keras.optimizers.SGD(learning_rate=0.1)

model.compile(loss='binary_crossentropy',optimizer=opt)

model.summary()
```

Model: "sequential"

Layer	(type)	Output	Shape	Param #
dense	(Dense)	(None,	3)	9

Total params: 9 (36.00 Byte)
Trainable params: 9 (36.00 Byte)
Non-trainable params: 0 (0.00 Byte)

epochs = 1000

#h = model.fit(data_points, labels, verbose=1, epochs=epochs, validation_split=0.2)
h = model.fit(points, labels, verbose=1, epochs=epochs, batch_size= 70, validation_split=0.2)

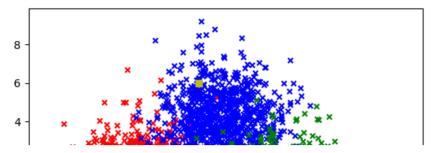
Loss = h.history['loss']

Loss

```
בטטכוו אסא/ דמממ
Epoch 990/1000
35/35 [============== ] - 0s 2ms/step - loss: 0.1567 - val loss: 0.2451
Epoch 991/1000
35/35 [================== ] - 0s 3ms/step - loss: 0.1567 - val loss: 0.2431
Epoch 992/1000
35/35 [============== ] - 0s 3ms/step - loss: 0.1567 - val loss: 0.2419
Epoch 993/1000
35/35 [================== ] - 0s 3ms/step - loss: 0.1567 - val loss: 0.2430
Epoch 994/1000
35/35 [========================= ] - 0s 3ms/step - loss: 0.1567 - val loss: 0.2433
Epoch 995/1000
Epoch 996/1000
35/35 [==============] - 0s 4ms/step - loss: 0.1567 - val loss: 0.2428
Epoch 997/1000
35/35 [============== ] - 0s 3ms/step - loss: 0.1567 - val loss: 0.2434
Epoch 998/1000
Epoch 999/1000
35/35 [================== ] - 0s 3ms/step - loss: 0.1567 - val loss: 0.2450
Epoch 1000/1000
```

```
U.100/43U/94239U442,
     0.15672850608825684,
     0.15678222477436066.
     0.15671847760677338,
     0.15672115981578827,
     0.15673989057540894,
     0.15675140917301178,
     0.15671634674072266,
     0.15681302547454834,
     0.15670068562030792,
     0.1567232459783554,
     0.15674148499965668,
     0.15671007335186005,
     0.15672567486763,
     0.15671215951442719.
     0.15676255524158478,
     0.15670548379421234,
     0.15671847760677338.
     0.15670041739940643,
     0.1567092388868332,
     0.15673935413360596,
     0.15671317279338837,
     0.15672899782657623,
     0.15669238567352295,
     0.15672625601291656,
     0.15672796964645386,
     0.15671248733997345,
     0.1567256599664688,
     0.15672150254249573,
     0.15669448673725128,
     0.15669465065002441,
     0.1567067801952362,
     0.1567171961069107,
     0.15676064789295197]
weights = model.get weights()
print(weights[0])
print(weights[1])
                     #bias
     [[-1.8542533
                    0.37775218 1.5208719 ]
     [-0.9898408 1.4547888 -1.4014187]]
     [ 7.970148 -5.1614227 -8.469914 ]
plt.scatter(np.arange(epochs),h.history['loss'])
plt.scatter(np.arange(epochs),h.history['val_loss'],c='r')
plt.show()
```

```
2.5
     2.0
     1.5
     1.0
     0.5
model.predict([[4,6]])
    1/1 [=======] - 0s 65ms/step
    array([[2.8538452e-05, 9.9997139e-01, 1.2773766e-07]], dtype=float32)
x=4.0
y=6.0
plt.scatter(x_label0, y_label0, c='r', marker='x', s=20)
plt.scatter(x_label1, y_label1, c='b', marker='x', s=20)
plt.scatter(x_label2, y_label2, c='g', marker='x', s=20)
plt.scatter(x,y,c='y', marker='s')
plt.show()
```



→ Number of epochs 100

```
在大大型的企业中的企业的企业,并不是一个企业的企业。
      -4 7
model = Sequential()
model.add(Dense(units = 3, use_bias=True, input_dim=2, activation = "softmax"))
#opt = tf.keras.optimizers.Adam(learning_rate=0.1)
opt = tf.keras.optimizers.Adam()
#opt = tf.keras.optimizers.SGD(learning_rate=0.1)
model.compile(loss='binary_crossentropy',optimizer=opt)
model.summary()
    Model: "sequential 1"
```

Layer (type)	Output	Shape	Param #
dense_1 (Dense)	(None,	3)	9
Total params: 9 (36.00 Byte) Trainable params: 9 (36.00 Byte)		=======	

Non-trainable params: 0 (0.00 Byte)

```
epochs = 100
#h = model.fit(data_points, labels, verbose=1, epochs=epochs, validation_split=0.2)
h = model.fit(points, labels, verbose=1, epochs=epochs, batch size= 70, validation split=0.2)
```

```
U.Z09U339334U19103,
     0.26736921072006226,
     0.265764057636261.
     0.2641422152519226,
     0.26258763670921326,
     0.2610386908054352,
     0.25954481959342957,
     0.2580412030220032,
     0.2566033601760864,
     0.25513237714767456,
     0.25371623039245605,
     0.2523210048675537,
     0.25096815824508667,
     0.24962598085403442,
     0.24828501045703888,
     0.24699103832244873,
     0.2457052618265152]
weights = model.get_weights()
print(weights[0])
print(weights[1])
                     #bias
     [[-0.6192839
                   0.12776168 0.46283087]
     [-0.25504512 0.8719286 -0.91608995]]
     [ 1.8876922 -2.4891806 -2.2122905]
plt.scatter(np.arange(epochs),h.history['loss'])
plt.scatter(np.arange(epochs),h.history['val_loss'],c='r')
plt.show()
```

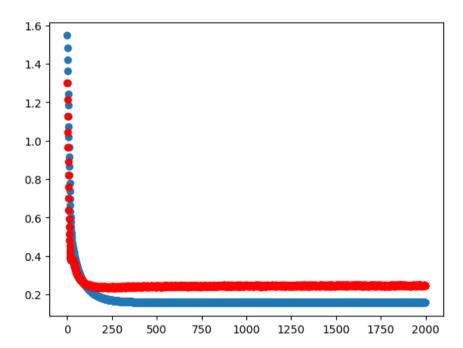
```
3.0
     2.5 -
model.predict([[4,6]])
    1/1 [======] - 0s 59ms/step
    array([[4.6175518e-03, 9.9527246e-01, 1.0992816e-04]], dtype=float32)
x=4.0
y=6.0
plt.scatter(x_label0, y_label0, c='r', marker='x', s=20)
plt.scatter(x_label1, y_label1, c='b', marker='x', s=20)
plt.scatter(x_label2, y_label2, c='g', marker='x', s=20)
plt.scatter(x,y,c='y', marker='s')
plt.show()
     -2
            -2.5
                    0.0
                            2.5
                                          7.5
                                                 10.0
                                                        12.5
                                   5.0
                                                                15.0
```

→ Number of epochs 2000

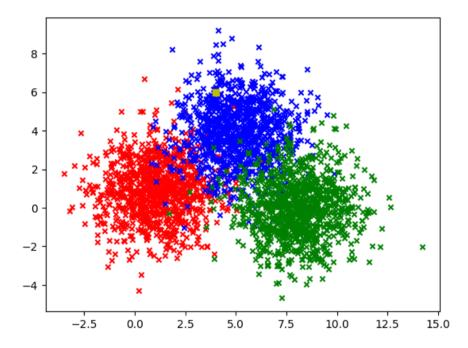
```
model = Sequential()
model.add(Dense(units = 3, use_bias=True, input_dim=2, activation = "softmax"))
#opt = tf.keras.optimizers.Adam(learning_rate=0.1)
opt = tf.keras.optimizers.Adam()
#opt = tf.keras.optimizers.SGD(learning rate=0.1)
model.compile(loss='binary_crossentropy',optimizer=opt)
model.summary()
    Model: "sequential 2"
     Layer (type)
                               Output Shape
                                                       Param #
     dense 2 (Dense)
                               (None, 3)
    ______
    Total params: 9 (36.00 Byte)
    Trainable params: 9 (36.00 Byte)
    Non-trainable params: 0 (0.00 Byte)
epochs = 2000
#h = model.fit(data_points, labels, verbose=1, epochs=epochs, validation_split=0.2)
h = model.fit(points, labels, verbose=1, epochs=epochs, batch_size= 70, validation_split=0.2)
```

```
EDOCII 1900/2000
Epoch 1981/2000
35/35 [============= ] - 0s 3ms/step - loss: 0.1566 - val loss: 0.2444
Epoch 1982/2000
35/35 [============== ] - 0s 3ms/step - loss: 0.1566 - val loss: 0.2419
Epoch 1983/2000
Epoch 1984/2000
Epoch 1985/2000
Epoch 1986/2000
Epoch 1987/2000
35/35 [============= ] - 0s 3ms/step - loss: 0.1566 - val loss: 0.2445
Epoch 1988/2000
35/35 [============== ] - 0s 2ms/step - loss: 0.1566 - val loss: 0.2450
Epoch 1989/2000
Epoch 1990/2000
35/35 [=================== ] - 0s 3ms/step - loss: 0.1566 - val loss: 0.2470
Epoch 1991/2000
Epoch 1992/2000
35/35 [============== ] - 0s 2ms/step - loss: 0.1566 - val loss: 0.2466
Epoch 1993/2000
Epoch 1994/2000
Epoch 1995/2000
Epoch 1996/2000
35/35 [========================= ] - 0s 2ms/step - loss: 0.1566 - val loss: 0.2469
Epoch 1997/2000
35/35 [========================= ] - 0s 2ms/step - loss: 0.1566 - val loss: 0.2461
Epoch 1998/2000
Epoch 1999/2000
Epoch 2000/2000
```

```
Loss = h.history['loss']
Loss
```



```
x=4.0
y=6.0
plt.scatter(x_label0, y_label0, c='r', marker='x', s=20)
plt.scatter(x_label1, y_label1, c='b', marker='x', s=20)
plt.scatter(x_label2, y_label2, c='g', marker='x', s=20)
plt.scatter(x,y,c='y', marker='s')
plt.show()
```



→ Learning rate 0.1

```
model = Sequential()

model.add(Dense(units = 3, use_bias=True, input_dim=2, activation = "softmax"))

opt = tf.keras.optimizers.Adam(learning_rate=0.1)
#opt = tf.keras.optimizers.Adam()
#opt = tf.keras.optimizers.SGD(learning_rate=0.1)
```

model.compile(loss='binary crossentropy',optimizer=opt)

model.summary()

Model: "sequential 3"

Layer (type)	Output Shape	Param #
dense_3 (Dense)	(None, 3)	9

Total params: 9 (36.00 Byte)
Trainable params: 9 (36.00 Byte)
Non-trainable params: 0 (0.00 Byte)

```
epochs = 1000
```

#h = model.fit(data_points, labels, verbose=1, epochs=epochs, validation_split=0.2)
h = model.fit(points, labels, verbose=1, epochs=epochs, batch_size= 70, validation_split=0.2)

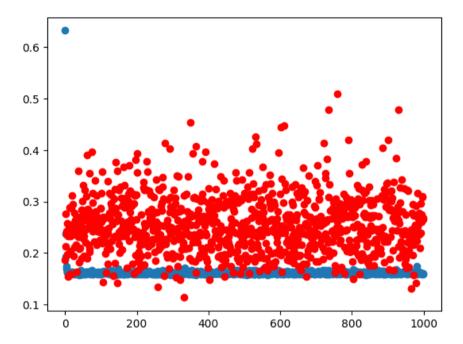
Loss = h.history['loss']

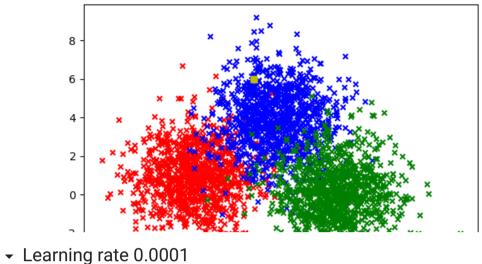
Loss

```
Epoch 987/1000
Epoch 988/1000
Epoch 989/1000
Epoch 990/1000
35/35 [============== ] - 0s 2ms/step - loss: 0.1616 - val loss: 0.2718
Epoch 991/1000
35/35 [============= ] - 0s 2ms/step - loss: 0.1605 - val loss: 0.2094
Epoch 992/1000
Epoch 993/1000
35/35 [============== ] - 0s 2ms/step - loss: 0.1603 - val loss: 0.2967
Epoch 994/1000
35/35 [========================= ] - 0s 2ms/step - loss: 0.1599 - val loss: 0.2399
Epoch 995/1000
35/35 [========================= ] - 0s 2ms/step - loss: 0.1610 - val loss: 0.2613
Epoch 996/1000
35/35 [============== ] - 0s 3ms/step - loss: 0.1598 - val loss: 0.2741
Epoch 997/1000
35/35 [============= ] - 0s 2ms/step - loss: 0.1600 - val loss: 0.3083
Epoch 998/1000
Epoch 999/1000
Epoch 1000/1000
35/35 [================== ] - 0s 2ms/step - loss: 0.1598 - val loss: 0.2681
```

```
U.103/9U1210/403/00,
     0.16042982041835785,
     0.16075921058654785,
     0.16320320963859558,
     0.16297510266304016,
     0.16055388748645782,
     0.1608719378709793,
     0.16025833785533905,
     0.1604868471622467,
     0.1593562811613083,
     0.16037946939468384,
     0.16341416537761688,
     0.15937060117721558,
     0.16094814240932465,
     0.15983568131923676.
     0.1607755869626999,
     0.1638484001159668,
     0.16113193333148956.
     0.16345638036727905,
     0.17447996139526367,
     0.16293780505657196,
     0.16053014993667603,
     0.16081421077251434,
     0.1586494892835617,
     0.16016899049282074,
     0.16359543800354004,
     0.16283239424228668,
     0.16302351653575897,
     0.16162802278995514,
     0.16053351759910583,
     0.16038376092910767,
     0.16029150784015656,
     0.15989957749843597,
     0.1610257625579834,
     0.1598190814256668,
     0.15997277200222015,
     0.1602095067501068,
     0.16083262860774994,
     0.1598118096590042]
weights = model.get_weights()
print(weights[0])
print(weights[1])
                     #bias
     [[-1.9795942 0.4349273 1.706098]
     [-0.8989535 1.4161886 -1.5113696]]
     [ 8.54315 -5.302328 -9.565231]
```

```
plt.scatter(np.arange(epochs),h.history['loss'])
plt.scatter(np.arange(epochs),h.history['val_loss'],c='r')
plt.show()
```





model = Sequential()

model.add(Dense(units = 3, use_bias=True, input_dim=2, activation = "softmax"))

opt = tf.keras.optimizers.Adam(learning_rate=0.0001)

#opt = tf.keras.optimizers.Adam()

#opt = tf.keras.optimizers.SGD(learning_rate=0.1)

model.compile(loss='binary_crossentropy',optimizer=opt)

model.summary()

Model: "sequential_4"

Layer (type)	Output Shape	Param #
dense_4 (Dense)	(None, 3)	9

Total params: 9 (36.00 Byte)
Trainable params: 9 (36.00 Byte)
Non-trainable params: 0 (0.00 Byte)

epochs = 1000
#h = model.fit(data_points, labels, verbose=1, epochs=epochs, validation_split=0.2)
h = model.fit(points, labels, verbose=1, epochs=epochs, batch_size= 70, validation_split=0.2)

```
EDOCII 332/ TAMA
Epoch 994/1000
Epoch 995/1000
35/35 [============== ] - 0s 2ms/step - loss: 0.2104 - val loss: 0.2480
Epoch 996/1000
35/35 [============== ] - 0s 2ms/step - loss: 0.2103 - val loss: 0.2483
Epoch 997/1000
35/35 [============== ] - 0s 2ms/step - loss: 0.2102 - val loss: 0.2483
Epoch 998/1000
35/35 [============== ] - 0s 2ms/step - loss: 0.2101 - val loss: 0.2485
Epoch 999/1000
35/35 [==============] - 0s 2ms/step - loss: 0.2100 - val loss: 0.2483
Epoch 1000/1000
35/35 [=============== ] - 0s 2ms/step - loss: 0.2099 - val loss: 0.2481
```

Loss = h.history['loss']
Loss

```
U. Z1Z430UZU3/4Z981,
     0.21233676373958588,
     0.21223615109920502,
     0.21213240921497345,
     0.21203115582466125,
     0.21193036437034607,
     0.21183323860168457,
     0.21174253523349762,
     0.21163320541381836,
     0.21153868734836578,
     0.2114371806383133,
     0.21134229004383087,
     0.21124067902565002,
     0.21115081012248993,
     0.21105551719665527.
     0.21095231175422668,
     0.21085263788700104,
     0.21075329184532166,
     0.21066242456436157,
     0.2105596661567688,
     0.21046391129493713,
     0.21037010848522186,
     0.2102724313735962,
     0.21017520129680634,
     0.21008704602718353,
     0.20998099446296692,
     0.209891825914382931
weights = model.get_weights()
print(weights[0])
print(weights[1])
                     #bias
     [[-0.86395454 0.15022355 0.5943968]
     [-0.38220945 0.91327024 -0.95378107]]
     [ 3.0835235 -2.6992445 -2.9725344]
plt.scatter(np.arange(epochs),h.history['loss'])
plt.scatter(np.arange(epochs),h.history['val loss'],c='r')
plt.show()
```

```
2.25
      2.00
      1.75
      1.50
      1.25
      1.00
model.predict([[4,6]])
```

```
WARNING:tensorflow:5 out of the last 5 calls to <function Model.make_predict_function.<locals>.predict_function at 0x788676b92440> triggered tf.funct
1/1 [=======] - 0s 48ms/step
array([[2.3596396e-03, 9.9757916e-01, 6.1202118e-05]], dtype=float32)
```

```
x=4.0
y=6.0
plt.scatter(x_label0, y_label0, c='r', marker='x', s=20)
plt.scatter(x_label1, y_label1, c='b', marker='x', s=20)
plt.scatter(x_label2, y_label2, c='g', marker='x', s=20)
plt.scatter(x,y,c='y', marker='s')
plt.show()
```

Minibatch

▼ Minibatch-20

Model: "sequential_5"

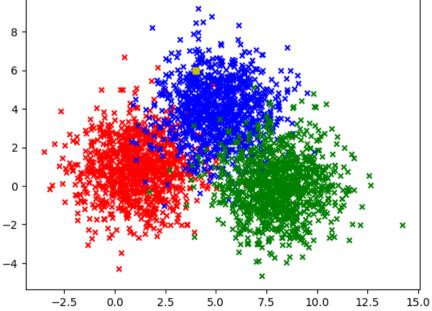
Layer (type)	Output Shape	Param #		
dense_5 (Dense)	(None, 3)	9		
Total params: 9 (36.00 Byte) Trainable params: 9 (36.00 Byte)				

Non-trainable params: 0 (0.00 Byte)

```
epochs = 1000
#h = model.fit(data_points, labels, verbose=1, epochs=epochs, validation_split=0.2)
h = model.fit(points, labels, verbose=1, epochs=epochs, validation_split=0.2, batch_size=20)
```

Loss

```
U.104000191993/1338,
     0.16453391313552856,
     0.1645217388868332,
     0.16450464725494385,
     0.1644873470067978,
     0.16446520388126373,
     0.16444945335388184,
     0.1644359529018402,
     0.1644258201122284,
     0.1644003540277481,
     0.16438671946525574,
     0.16437384486198425,
     0.16434895992279053,
     0.16434694826602936,
     0.16432400047779083.
     0.16430972516536713,
     0.1642874926328659]
weights = model.get_weights()
print(weights[0])
print(weights[1])
                     #bias
     [[-1.376739 0.3119349 1.0393476]
     [-0.7011174 1.2859708 -1.1403483]]
     [ 5.670027 -4.416901 -5.620191]
plt.scatter(np.arange(epochs),h.history['loss'])
plt.scatter(np.arange(epochs),h.history['val_loss'],c='r')
plt.show()
```



→ mini batch - 50

```
model = Sequential()
model.add(Dense(units = 3, use_bias=True, input_dim=2, activation = "softmax"))
opt = tf.keras.optimizers.Adam(learning_rate=0.0001)
#opt = tf.keras.optimizers.Adam()
#opt = tf.keras.optimizers.SGD(learning rate=0.1)
model.compile(loss='binary_crossentropy',optimizer=opt)
model.summary()
    Model: "sequential 6"
     Layer (type)
                               Output Shape
                                                        Param #
     dense 6 (Dense)
                               (None, 3)
    ______
    Total params: 9 (36.00 Byte)
    Trainable params: 9 (36.00 Byte)
    Non-trainable params: 0 (0.00 Byte)
epochs = 1000
#h = model.fit(data_points, labels, verbose=1, epochs=epochs, validation_split=0.2)
h = model.fit(points, labels, verbose=1, epochs=epochs, batch_size= 50, validation_split=0.2)
```

```
EDOCII AQA\ TAAA
Epoch 981/1000
48/48 [============= ] - 0s 2ms/step - loss: 0.1897 - val loss: 0.2442
Epoch 982/1000
48/48 [==============] - 0s 2ms/step - loss: 0.1896 - val loss: 0.2440
Epoch 983/1000
Epoch 984/1000
Epoch 985/1000
Epoch 986/1000
Epoch 987/1000
Epoch 988/1000
48/48 [============== ] - 0s 2ms/step - loss: 0.1892 - val loss: 0.2437
Epoch 989/1000
48/48 [============== ] - 0s 2ms/step - loss: 0.1892 - val loss: 0.2441
Epoch 990/1000
48/48 [==============] - 0s 2ms/step - loss: 0.1891 - val loss: 0.2439
Epoch 991/1000
Epoch 992/1000
48/48 [============= ] - 0s 2ms/step - loss: 0.1890 - val loss: 0.2435
Epoch 993/1000
Epoch 994/1000
Epoch 995/1000
Epoch 996/1000
48/48 [==============] - 0s 2ms/step - loss: 0.1887 - val loss: 0.2439
Epoch 997/1000
48/48 [==============] - 0s 2ms/step - loss: 0.1886 - val loss: 0.2436
Epoch 998/1000
Epoch 999/1000
Epoch 1000/1000
```

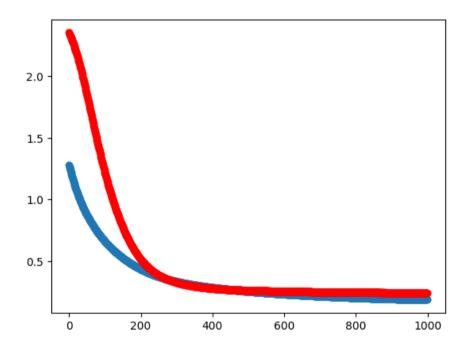
Loss = h.history['loss']
Loss

```
weights = model.get_weights()

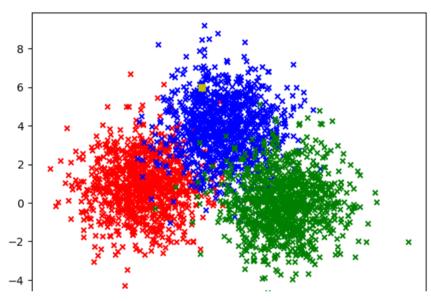
print(weights[0])
print(weights[1])  #bias

[[-0.98609793  0.21861346  0.7294145 ]
       [-0.46031675  1.0607656  -0.997672 ]]
       [ 3.722764  -3.4068813  -3.7914543]

plt.scatter(np.arange(epochs),h.history['loss'])
plt.scatter(np.arange(epochs),h.history['val_loss'],c='r')
plt.show()
```



```
x=4.0
y=6.0
plt.scatter(x_label0, y_label0, c='r', marker='x', s=20)
plt.scatter(x_label1, y_label1, c='b', marker='x', s=20)
plt.scatter(x_label2, y_label2, c='g', marker='x', s=20)
plt.scatter(x,y,c='y', marker='s')
plt.show()
```



Najlepsze wyniki otrzymałem dla współczynnika uczenia 0.1, liczby epok 2000,batcha równego 20, najgorsze dla współczynnika uczenia 0.0001, liczby epok 100, batcha równego 50.