```
import gym
import numpy as np
import random
env = gym.make("FrozenLake-v0", map_name='4x4', is_slippery=False)
Funkcja generująca politykę deterministyczną:
def create random det policy(env):
    policy = {}
   for key in range(0, env.observation_space.n):
        policy[key] = np.random.randint(4);
    return policy
Testujemy:
policy = create random det policy(env)
policy
     {0: 1,
     1: 3,
      2: 0,
      3: 2,
      4: 2,
      5: 1,
      6: 0,
      7: 1,
      8: 0,
      9: 3,
      10: 3,
      11: 0,
      12: 0,
      13: 1,
```

```
14: 1,
      15: 2}
Wygenerowanie słownika reprezentującego funkcję Q:
def create state action dictionary(env, policy):
    Q = \{\}
    for key in policy.keys():
         Q[key] = {a: 0.0 for a in range(0, env.action space.n)}
    return 0
Q = create state action dictionary(env, policy)
Q
     \{0: \{0: 0.0, 1: 0.0, 2: 0.0, 3: 0.0\},\
      1: {0: 0.0, 1: 0.0, 2: 0.0, 3: 0.0},
      2: {0: 0.0, 1: 0.0, 2: 0.0, 3: 0.0},
      3: {0: 0.0, 1: 0.0, 2: 0.0, 3: 0.0},
      4: {0: 0.0, 1: 0.0, 2: 0.0, 3: 0.0},
      5: {0: 0.0, 1: 0.0, 2: 0.0, 3: 0.0},
      6: {0: 0.0, 1: 0.0, 2: 0.0, 3: 0.0},
      7: {0: 0.0, 1: 0.0, 2: 0.0, 3: 0.0},
      8: {0: 0.0, 1: 0.0, 2: 0.0, 3: 0.0},
      9: {0: 0.0, 1: 0.0, 2: 0.0, 3: 0.0},
      10: {0: 0.0, 1: 0.0, 2: 0.0, 3: 0.0},
      11: {0: 0.0, 1: 0.0, 2: 0.0, 3: 0.0},
      12: {0: 0.0, 1: 0.0, 2: 0.0, 3: 0.0},
      13: {0: 0.0, 1: 0.0, 2: 0.0, 3: 0.0},
      14: {0: 0.0, 1: 0.0, 2: 0.0, 3: 0.0},
      15: {0: 0.0, 1: 0.0, 2: 0.0, 3: 0.0}}
Funkcja generująca epizod:
def generate_episode_det(env, policy):
    env.reset()
```

```
episode = []
    finished = False
    while not finished:
        s = env.s
        #s = np.random.randint(16)
        #print(s)
        timestep = []
        timestep.append(s)
        action = policy[s]
        , reward, finished, = env.step(action)
        timestep.append(action)
        timestep.append(reward)
        episode.append(timestep)
    return episode
Testujemy:
print("LEFT = 0 DOWN = 1 RIGHT = 2 UP = 3")
for i in range(10):
  print("Epizod ",i,": ",generate episode det(env, policy))
     LEFT = 0 DOWN = 1 RIGHT = 2 UP = 3
     Epizod 0: [[0, 3, 0.0], [0, 3, 0.0], [0, 3, 0.0], [0, 3, 0.0], [0, 3, 0.0], [0, 3, 0.0], [0, 3, 0.0], [0, 3, 0.0]
     Epizod 1: [[0, 3, 0.0], [0, 3, 0.0], [0, 3, 0.0], [0, 3, 0.0], [0, 3, 0.0], [0, 3, 0.0], [0, 3, 0.0], [0, 3, 0.0], [0, 3, 0.0]
     Epizod 2: [[0, 3, 0.0], [0, 3, 0.0], [0, 3, 0.0], [0, 3, 0.0], [0, 3, 0.0], [0, 3, 0.0], [0, 3, 0.0], [0, 3, 0.0]
     Epizod 3: [[0, 3, 0.0], [0, 3, 0.0], [0, 3, 0.0], [0, 3, 0.0], [0, 3, 0.0], [0, 3, 0.0], [0, 3, 0.0], [0, 3, 0.0], [0, 3, 0.0]
     Epizod 4: [[0, 3, 0.0], [0, 3, 0.0], [0, 3, 0.0], [0, 3, 0.0], [0, 3, 0.0], [0, 3, 0.0], [0, 3, 0.0], [0, 3, 0.0], [0, 3, 0.0]
     Epizod 5: [[0, 3, 0.0], [0, 3, 0.0], [0, 3, 0.0], [0, 3, 0.0], [0, 3, 0.0], [0, 3, 0.0], [0, 3, 0.0], [0, 3, 0.0], [0, 3, 0.0]
     Epizod 6: [[0, 3, 0.0], [0, 3, 0.0], [0, 3, 0.0], [0, 3, 0.0], [0, 3, 0.0], [0, 3, 0.0], [0, 3, 0.0], [0, 3, 0.0], [0, 3, 0.0]
```

```
Epizod 7: [[0, 3, 0.0], [0, 3, 0.0], [0, 3, 0.0], [0, 3, 0.0], [0, 3, 0.0], [0, 3, 0.0], [0, 3, 0.0], [0, 3, 0.0], [0, 3, 0.0], [0, 3, 0.0], [0, 3, 0.0], [0, 3, 0.0], [0, 3, 0.0], [0, 3, 0.0], [0, 3, 0.0], [0, 3, 0.0], [0, 3, 0.0], [0, 3, 0.0], [0, 3, 0.0], [0, 3, 0.0], [0, 3, 0.0], [0, 3, 0.0], [0, 3, 0.0], [0, 3, 0.0], [0, 3, 0.0], [0, 3, 0.0], [0, 3, 0.0], [0, 3, 0.0], [0, 3, 0.0], [0, 3, 0.0], [0, 3, 0.0], [0, 3, 0.0], [0, 3, 0.0], [0, 3, 0.0], [0, 3, 0.0], [0, 3, 0.0], [0, 3, 0.0], [0, 3, 0.0], [0, 3, 0.0], [0, 3, 0.0], [0, 3, 0.0], [0, 3, 0.0], [0, 3, 0.0], [0, 3, 0.0], [0, 3, 0.0], [0, 3, 0.0], [0, 3, 0.0], [0, 3, 0.0], [0, 3, 0.0], [0, 3, 0.0], [0, 3, 0.0], [0, 3, 0.0], [0, 3, 0.0], [0, 3, 0.0], [0, 3, 0.0], [0, 3, 0.0], [0, 3, 0.0], [0, 3, 0.0], [0, 3, 0.0], [0, 3, 0.0], [0, 3, 0.0], [0, 3, 0.0], [0, 3, 0.0], [0, 3, 0.0], [0, 3, 0.0], [0, 3, 0.0], [0, 3, 0.0], [0, 3, 0.0], [0, 3, 0.0], [0, 3, 0.0], [0, 3, 0.0], [0, 3, 0.0], [0, 3, 0.0], [0, 3, 0.0], [0, 3, 0.0], [0, 3, 0.0], [0, 3, 0.0], [0, 3, 0.0], [0, 3, 0.0], [0, 3, 0.0], [0, 3, 0.0], [0, 3, 0.0], [0, 3, 0.0], [0, 3, 0.0], [0, 3, 0.0], [0, 3, 0.0], [0, 3, 0.0], [0, 3, 0.0], [0, 3, 0.0], [0, 3, 0.0], [0, 3, 0.0], [0, 3, 0.0], [0, 3, 0.0], [0, 3, 0.0], [0, 3, 0.0], [0, 3, 0.0], [0, 3, 0.0], [0, 3, 0.0], [0, 3, 0.0], [0, 3, 0.0], [0, 3, 0.0], [0, 3, 0.0], [0, 3, 0.0], [0, 3, 0.0], [0, 3, 0.0], [0, 3, 0.0], [0, 3, 0.0], [0, 3, 0.0], [0, 3, 0.0], [0, 3, 0.0], [0, 3, 0.0], [0, 3, 0.0], [0, 3, 0.0], [0, 3, 0.0], [0, 3, 0.0], [0, 3, 0.0], [0, 3, 0.0], [0, 3, 0.0], [0, 3, 0.0], [0, 3, 0.0], [0, 3, 0.0], [0, 3, 0.0], [0, 3, 0.0], [0, 3, 0.0], [0, 3, 0.0], [0, 3, 0.0], [0, 3, 0.0], [0, 3, 0.0], [0, 3, 0.0], [0, 3, 0.0], [0, 3, 0.0], [0, 3, 0.0], [0, 3, 0.0], [0, 3, 0.0], [0, 3, 0.0], [0, 3, 0.0], [0, 3, 0.0], [0, 3, 0.0], [0, 3, 0.0], [0, 3, 0.0], [0, 3, 0.0], [0, 3, 0.0], [0, 3, 0.0], [0, 3, 0.0], [0, 3, 0.0], [0, 3, 0.0], [0, 3, 0.0], [0, 3, 0.0], [0, 3, 0.0], [0, 3, 0.0], [0, 3, 0.0], [0, 3, 0.0], [0, 3, 0.0], [0, 3, 0.0], [0, 3, 0.0], [0, 3, 0.0], [0, 3,
```

Czy pierwsza wizyta w danym stanie?

Unless the pair S_t, A_t appears in $S_0, A_0, S_1, A_1, \ldots, S_{t-1}, A_{t-1}$:

```
policy = create_random_det_policy(env)
episode = generate_episode_det(env, policy)
print(episode)

for time_step in reversed(range(0, len(episode))):

    S_t, A_t, R_t = episode[time_step]
    state_action = (S_t, A_t)

if not state_action in [(x[0], x[1]) for x in episode[0:time_step]]:
    print("t=",time_step," pierwsza wizyta w (s,a): ",state_action)

[[0, 2, 0.0], [1, 0, 0.0], [0, 2, 0.0], [1, 0, 0.0], [0, 2, 0.0], [1, 0, 0.0], [0, 2, 0.0], [1, 0, 0.0], [0, 2, 0.0], [1, 0, 0.0], [0, 2, 0.0], [1, 0, 0.0], [0, 2, 0.0], [1, 0, 0.0], [0, 2, 0.0], [1, 0, 0.0], [0, 2, 0.0], [1, 0, 0.0], [0, 2, 0.0], [1, 0, 0.0], [0, 2, 0.0], [1, 0, 0.0], [0, 2, 0.0], [1, 0, 0.0], [0, 2, 0.0], [1, 0, 0.0], [0, 2, 0.0], [1, 0, 0.0], [0, 2, 0.0], [1, 0, 0.0], [0, 2, 0.0], [1, 0, 0.0], [0, 2, 0.0], [1, 0, 0.0], [0, 2, 0.0], [1, 0, 0.0], [0, 2, 0.0], [1, 0, 0.0], [0, 2, 0.0], [1, 0, 0.0], [0, 2, 0.0], [1, 0, 0.0], [0, 2, 0.0], [1, 0, 0.0], [0, 2, 0.0], [1, 0, 0.0], [0, 2, 0.0], [1, 0, 0.0], [0, 2, 0.0], [1, 0, 0.0], [0, 2, 0.0], [1, 0, 0.0], [0, 2, 0.0], [1, 0, 0.0], [0, 2, 0.0], [1, 0, 0.0], [0, 2, 0.0], [1, 0, 0.0], [0, 2, 0.0], [1, 0, 0.0], [0, 2, 0.0], [1, 0, 0.0], [0, 2, 0.0], [1, 0, 0.0], [0, 2, 0.0], [1, 0, 0.0], [0, 2, 0.0], [1, 0, 0.0], [0, 2, 0.0], [1, 0, 0.0], [0, 2, 0.0], [1, 0, 0.0], [0, 2, 0.0], [1, 0, 0.0], [0, 2, 0.0], [1, 0, 0.0], [0, 2, 0.0], [1, 0, 0.0], [0, 2, 0.0], [1, 0, 0.0], [0, 2, 0.0], [1, 0, 0.0], [0, 2, 0.0], [1, 0, 0.0], [0, 2, 0.0], [1, 0, 0.0], [0, 2, 0.0], [1, 0, 0.0], [0, 2, 0.0], [1, 0, 0.0], [0, 2, 0.0], [1, 0, 0.0], [0, 2, 0.0], [1, 0, 0.0], [0, 2, 0.0], [1, 0, 0.0], [1, 0, 0.0], [1, 0, 0.0], [1, 0, 0.0], [1, 0, 0.0], [1, 0, 0.0], [1, 0, 0.0], [1, 0, 0.0], [1, 0, 0.0], [1, 0, 0.0], [1, 0, 0.0], [1, 0, 0.0], [1, 0, 0.0], [1, 0, 0.0], [1, 0, 0.0], [1, 0, 0.0], [1, 0, 0.0], [1, 0, 0.0], [1, 0, 0.0], [1, 0, 0.0], [1, 0, 0.0], [1, 0, 0.0], [1, 0, 0.0], [1, 0, 0.0], [1, 0, 0.0], [1, 0, 0.0], [1, 0, 0.0], [1, 0, 0.0], [1, 0, 0.0], [1, 0, 0.0], [1, 0, 0.0], [1, 0, 0.0], [1, 0, 0.0], [1, 0, 0.0], [1,
```

Słownik, którego kluczami są pary (stan,akcja) tzn. (S,A) a wartościami listy zwrotów G

Append G to $Returns(S_t, A_t)$

```
Returns = \{(3,2):[4,5,-1],(1,1):[2,3,6,7,1],(6,3):[2,-1,3,1]\}
```

```
Returns = {}
Returns[(3,1)]=[3]
print(Returns)
Returns[(3,1)].append(4)
print(Returns)
Returns[(3,1)].append(8)
print(Returns)
     \{(3, 1): [3]\}
     \{(3, 1): [3, 4]\}
     \{(3, 1): [3, 4, 8]\}
Returns[(4,2)]=[7]
print(Returns)
Returns[(4,2)].append(-4)
print(Returns)
Returns[(4,2)].append(2)
print(Returns)
     \{(3, 1): [3, 4, 8], (4, 2): [7]\}
     \{(3, 1): [3, 4, 8], (4, 2): [7, -4]\}
     \{(3, 1): [3, 4, 8], (4, 2): [7, -4, 2]\}
#Q = np.zeros((env.nS,env.nA))
Pi = np.zeros(env.nS)
Returns = {}
for u in range(10000):
  y=1
  policy = create_random_det_policy(env)
  anicada - gananata anicada dat/any malicyl
```

```
episoue = generace_episoue_uec(env, poiicy)
 #print(episode)
  G=0
  for time step in reversed(range(0, len(episode))):
   S t, A t, R t = episode[time step]
   state action = (S t, A t)
   G = v*G + R t
   if not state action in [(x[0], x[1]) for x in episode[0:time step]]:
       #print("t=",time step," pierwsza wizyta w (s,a): ",state action)
       if not state action in Returns.keys():
       Returns[state action]=[G]
      else :
       Returns[state action].append(G)
       Q[state action] = np.average(Returns[state action])
       # Pi[state action[0]] = np.argmax([state action])
      # Q[S t][A t] = sum(Returns[state action]) / len(Returns[state action]) # Average reward across episodes
           # Finding the action with maximum value.
       Q list = list(map(lambda x: x[1], Q[S t].items()))
       max Q = np.argmax(Q list)
      Pi[S t]=max Q
Q list
     [0.0, 0.0024459845087647777, 0.0003961965134706815, 0.0]
Returns
     array([[0. , 0.0011957 , 0.00197006, 0.
                                                          ],
                      , 0. , 0.00777605, 0.
            [0.
```

Q

```
[0.
         , 0.02840909, 0.
                         , 0.
         , 0. , 0.
[0.
                              , 0.
                                        ],
[0.
         , 0.00505902, 0.
                              , 0.
              , 0.
[0.
         , 0.
                              , 0.
[0.
         , 0.09433962, 0.
                              , 0.
[0.
         , 0.
                  , 0.
                            , 0.
[0.
         , 0.
                  , 0.0234375 , 0.
         , 0.04166667, 0.06451613, 0.
[0.
[0.
         , 0.31818182, 0.
                              , 0.
[0.
         , 0.
                  , 0.
                              , 0.
         , 0.
                  , 0.
                                        ],
[0.
                              , 0.
         , 0.
                  , 0.25
[0.
                              , 0.
         , 0.
[0.
                  , 1.
                             , 0.
                                        ],
         , 0.
                  , 0.
[0.
                            , 0.
                                        ]])
```

Ρi

```
array([1., 2., 1., 0., 1., 0., 1., 0., 2., 2., 1., 0., 0., 2., 2., 0.])
```

```
from plot_utils import plot_values
plot_values(Pi)
```

