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FACULTY OF ELECTRICAL ENGINEERING
DEPARTMENT OF CYBERNETICS



BACHELOR THESIS

RRT-path method used for cooperative surveillance by
group of helicopters

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Název práce: Aplikace algoritmu RRT-path v úloze autonomního dohledu skupinou helikoptér

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Abstrakt V předložené práci studujeme... Uvede se abstrakt v rozsahu 80 až 200 slov. Lorem ipsum dolor sit amet, consectetur adipiscing elit. Ut sit amet sem. Mauris nec turpis ac sem mollis pretium. Suspendisse neque massa, suscipit id, dictum in, porta at, quam. Nunc suscipit, pede vel elementum pretium, nisl urna sodales velit, sit amet auctor elit quam id tellus. Nullam sollicitudin.

Klíčová slova: klíčová slova (3 až 5)

Title: RRT-path method used for cooperative surveillance by group of helicopters

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Abstract In the present work we study ... Uvede se anglický abstrakt v rozsahu 80 až 200 slov. Lorem ipsum dolor sit amet, consectetur adipiscing elit. Ut sit amet sem. Mauris nec turpis ac sem mollis pretium. Suspendisse neque massa, suscipit id, dictum in, porta at, quam. Nunc suscipit, pede vel elementum pretium, nisl urna sodales velit, sit amet auctor elit quam id tellus. Nullam sollicitudin. Donec hendrerit. Aliquam ac nibh. Vivamus mi. Sed felis. Proin pretium elit in neque. Pellentesque at turpis. Maecenas convallis. Vestibulum id lectus.

Keywords: klíčová slova (3 až 5) v angličtině

Prohlašuji, že jsem svou bakalářskou práci napsal(a) samostatně a výhradně s použitím citovaných pramenů. Souhlasím se zapůjčováním práce a jejím zveřejňováním.

V Praze dne 20th April 2016

Jméno Příjmení + podpis

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CHAPTER

ONE

MOTIVATION

ALGORITHM

The basis of whole algorithm is shown in 2.1 in the pseudocode.

The configuration variable is instance of Configuration class, which holds all configuration data, including selected map. Map holds all Areas of Interest (AoI) and obstacles. All obstacles and AoIs are represented as rectangles now.

The purpose of the path finding is to find the shortest feasible paths, but real UAVs need to have some minimal distance to obstacles due to weather conditions, sensor errors and other aspects. To solve this issue, every obstacle is amplified before the whole path finding algorithm on line 2. This minimal distance to obstacles allows UAVs to follow their trajectories safely.

Line 3 represents the discretization of map to the graph. Discretization divides the map to squares with size set in configuration and each square is represented by node. In this graph, there are 4 types of nodes: Free, Obstacle, UAV and Goal. If a part of square of whole square is covered by an obstacle, the corresponding node has the type Obstacle. If a part of square or whole square is covered by AoI, corresponding node has type Goal. If a square contains an UAV, the corresponding node has type UAV and rest of squares have corresponding nodes with type Free.

Edges in this graph are only between nodes of neighbouring squares, so each node has maximally 8 edges. Obstacle nodes do not have any edges.

After converting the map to nodes, the optional grouping of goals for guiding path can be

Algorithm 2.1 The basis of whole algorithm

```
1: map := configuration.getMap();
2: map := amplifyObstacles(map);
3: nodes := mapToNodes(map);
4: paths := createGuidingPaths(nodes);
5: rrtPath := rrtPath(paths, map, nodes);
6: lastState := getBestFitness(rrtPath, map);
7: path := getPath(lastState);
8: path = straightenCrossingTrajectories(path);
9: path := resamplePath(path, map);
10: path := optimizePathByDubins(path, map);
11: savePath(path);
```

turned on. I will cover the grouping in chapter 3.

Line 4 represents calculation of the guiding paths for RRT-Path algorithm using the A* algorithm. Algorithm has a modified cost function and in addition to a cost function of the A* algorithm, the cost of current node is added during the calculation. Nodes neighbouring with obstacles have a bigger cost than nodes which do not have obstacles as neighbours. Thanks to this modification, guiding path avoids obstacles and has bigger distance to obstacles.

On line 5 the RRT path algorithm takes place. This function returns a structure with a tree with a root at the starting position of UAVs and with an array containing leaves of this tree, where all UAVs are in Areas of Interest.

On line 6 the leaf, where UAVs have the best coverage of AoI is chosen. Quality of the coverage is determined by cost function, which will be mentioned later.

On line 7 the path is built from the last state.

On line 8 there is an optional preparation before the optimization using Dubins curves. In the preparation, all crossings of paths of individual UAVs are straightened, so UAVs do not cross other UAVs trajectories during the whole path. During the implementation of this method were complications, which are covered in the chapter 4, and thus the row was removed from the final version of the algorithm.

On line 9, the re-sampling of the path is made, mainly due to requirements of real UAVs, which are mentioned in chapter 7.

On line 10 there is the optimization by Dubins curves. The optimization is covered in chapter 6.

The last line represents persisting of the path to a file for usage of result of the whole algorithm by different programs. Path is persisted to JSON, due to convenience of the JSON format. JSON is smaller than XML and can be easily parsed by all widely used programming languages. Path is also persisted to CSV format, so it can be loaded to MATLAB and then loaded to real UAVs.

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GROUPING OF GOALS FOR GUIDING PATH

During this processing of map (method `MapProcessor::getEndNodes` in codebase) all AoIs are grouped to one big AoI, which is the smallest rectangle covering all AoIs.

If this modification is turned on, instead of one goal for every AoI (node in middle of AoI rectangle is considered as goal node), only one goal is used for all AoIs. This prevents swarm to split and whole swarm has only one guiding path. The main reason to have one big swarm instead of more smaller swarms is that smaller swarms (or individual UAVs in case of same count of AoI and UAVs) is relative localization, which can be used better when having only one swarm.

Below are images of maps with goals and obstacles. Goals have green colour and obstacles have grey colour.

This approach has advantage, when individual AoIs are near to global goal of whole group, as seen in 3.2.

Disadvantage of this method is, when individual AoIs have big distance from each other than can be covered by UAVs, this approach totally fails, because RRT-Path, which is much faster than RRT, has goal very distant from AoIs, as can be seen in 3.1.

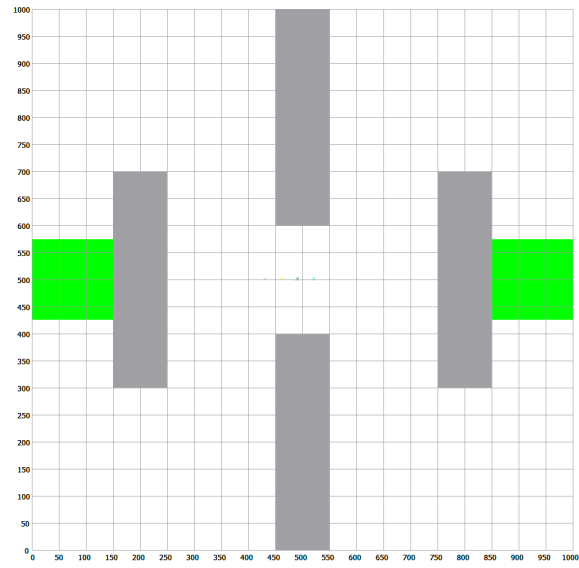


Figure 3.1: Map with goals unsuitable for grouping

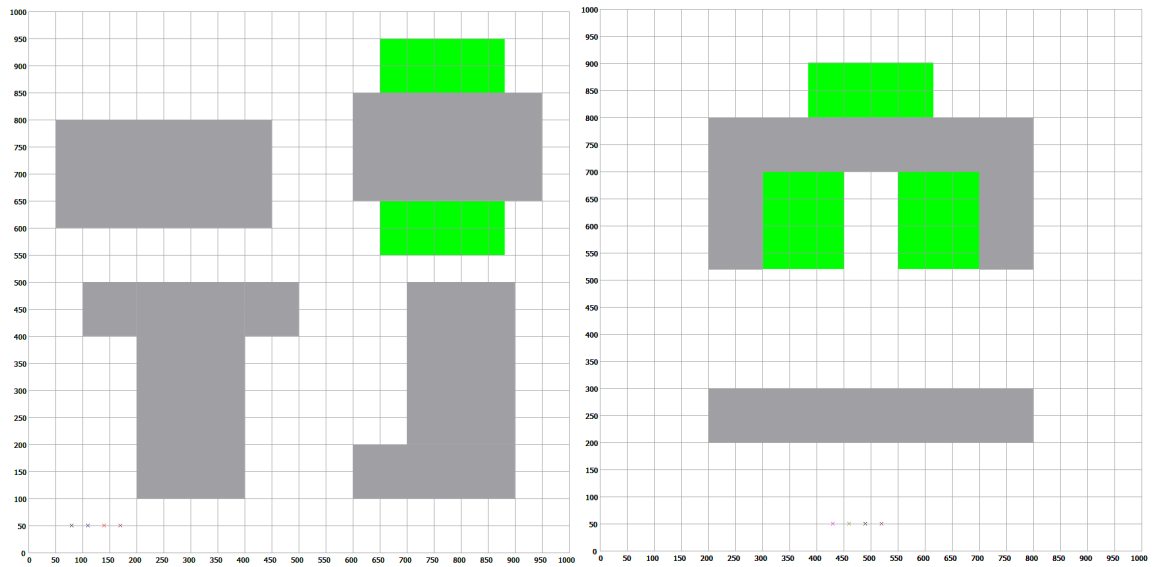


Figure 3.2: Maps with goals suitable for grouping

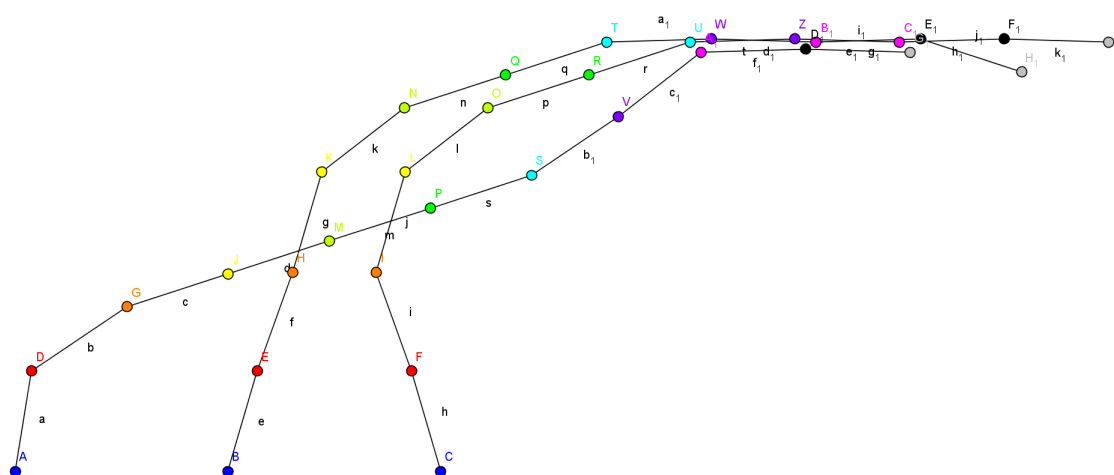
PATHS STRAIGHTENING

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RRT-Path algorithm checks crossing paths between neighbouring states, so between n th state and $n+1$ -th state no trajectories are crossing each other. But between states trajectories are still crossing. In this image 4.1 is shown path found by RRT-Path. Every colour marks one state in RRT-Path. As we can see, check in algorithm prevents from crossing path between neighbouring states, but crossing of paths in different times can not be easily prevented. We can see in image, that paths cross between points J (yellow), M (light green) and H (orange), K (yellow), so there is no easy approach to prevent path collisions between $n-2$ -th state and n th state. Optimization by Dubins curves shortens trajectory of UAVs, so UAVs could be in these trajectories in different time, so there could be collisions after optimization. Another complication occurs, when time difference between two states is too low, then UAVs could collide, because in reality UAV can not follow path precisely, but only with some errors.

I tried to straighten crossing trajectories, but all attempts failed. Straightening was done by switching parts of crossing paths from the earliest crossing state to end. But then paths had different lengths, which was unsuitable for path planning for swarm. This can be done by adding “waiting” points, points in different state but with same position in different time. But then is really hard to straighten longer path with many crossings (this path is really short, paths in other maps are much longer and more complicated). For motion model with inertia is also really hard to deal with waiting states, which complicates following of straightened trajectories. Due to all complications mentioned above, this part was removed from algorithm. But it is possible to add it, when better approach will be found.

Figure 4.1: Crossing paths



MOTION MODEL

The RRT-Path algorithm is universal and works without motion model, which is fine for holonomic robot, but usage of motion model allows us to find path more feasible for swarm of UAVs than without using of holonomic robot. For this purpose, car like model was chosen. Differential equations of motion model in 3D from [3] are

$$\begin{aligned}\dot{x}(t) &= v(t) \sin \varphi(t) \\ \dot{y}(t) &= v(t) \cos \varphi(t) \\ \dot{z}(t) &= w(t) \\ \dot{\varphi}(t) &= K(t) v(t)\end{aligned}\tag{5.1}$$

where $x(t)$, $y(t)$, $z(t)$ are coordinates of UAV, $\varphi(t)$ represents heading of UAV, $v(t)$ is forward velocity, $K(t)$ is curvature, $w(t)$ is ascent velocity. $\begin{bmatrix} K(t) & w(t) & v(t) \end{bmatrix}$ represent input vector of motion model. Differential equations are useful for representation in equations, but not useful for computer algorithm. For usage in algorithm are better difference equations instead of differential equations. When inputs are held constant in each time interval between two time steps, difference equations are

$$\begin{aligned}x(k+1) &= \begin{cases} \text{if } K(k+1) \neq 0 \\ x(k) + \frac{1}{K(k+1)} (\sin(\varphi(k) + K(k+1)v(k+1)\Delta t(k+1)) - \sin(\varphi(k))) \\ \text{if } K(k+1) = 0 \\ x(k) + v(k+1) \cos(\varphi(k)) \Delta t(k+1) \end{cases} \\ y(k+1) &= \begin{cases} \text{if } K(k+1) \neq 0 \\ y(k) - \frac{1}{K(k+1)} (\cos(\varphi(k) + K(k+1)v(k+1)\Delta t(k+1)) - \cos(\varphi(k))) \\ \text{if } K(k+1) = 0 \\ y(k) + v(k+1) \sin(\varphi(k)) \Delta t(k+1) \end{cases} \\ z(k+1) &= z(k) + w(k+1) \Delta t(k+1) \\ \varphi(k+1) &= \varphi(k) + K(k+1)v(k+1)\Delta t(k+1)\end{aligned}\tag{5.2}$$

DUBINS CURVES

Dubins curves, also called Dubins manoeuvres or Dubins path were published by Lester Eli Dubins in 1957 [1]. Dubins path is optimal path for car like motion model. Path is optimal, when car moves at constant forward speed. The other important constraint is the maximum steering angle ϕ_{max} , which results in a minimum turning radius ρ_{min} . As the car travels, consider the length of the curve in $\mathcal{W} = \mathbb{R}^2$ traced out by a pencil attached to the centre of the car. The task is to minimize the length of this curve as the car travels between any q_I and q_G . Due to ρ_{min} , this can be considered as a bounded-curvature shortest-path problem. If $\rho_{min} = 0$, then there is no curvature bound, and the shortest path follows a straight line in \mathbb{R}^2 . In terms of a cost function, the criterion to optimize is

$$L(\tilde{q}, \tilde{u}) = \int_0^{t_F} \sqrt{\dot{x}(t)^2 + \dot{y}(t)^2} dt \quad (6.1)$$

, where t_F is the time at which q_G is reached, and a configuration is denoted as $q = (x, y, \theta)$, \tilde{x}_t denotes the function $\tilde{x}_t : [0, t] \rightarrow X$, which is called the state trajectory (or state history). This is a continuous-time version of the state history, which was defined previously for problems that have discrete stages. Similarly, \tilde{u}_t denotes the action trajectory (or action history),. If q_G is not reached, then it is assumed that $L(\tilde{q}, \tilde{u}) = \infty$. [2]

When considering constraints of inputs (actions) for motion model, the system can be simplified to

$$\begin{aligned} \dot{x} &= \cos \theta \\ \dot{y} &= \sin \theta \\ \dot{\theta} &= u \end{aligned} \quad (6.2)$$

in which u is chosen from the interval $U = \{-\tan \phi_{max}, 0, \tan \phi_{max}\}$. For simplicity, assume that $\tan \phi = 1$. The following results also hold for any $\phi_{max} \in (0, \pi/2)$.

It was shown in [1] that between any two configurations, the shortest path for the Dubins car can always be expressed as a combination of no more than three motion primitives. Each motion primitive applies a constant action over an interval of time. Furthermore, the only actions that are needed to traverse the shortest paths are $u \in \{-1, 0, 1\}$. The primitives and their associated symbols are shown in 6.1. The S primitive drives the car straight ahead. The L and R primitives turn as sharply as possible to the left and right, respectively. Using these symbols, each possible kind of shortest path can be designated as a sequence of three symbols that corresponds to the

Table 6.1: The three motion primitives from which all optimal curves for the Dubins car can be constructed.

Symbol	Steering u
L	-1
S	0
R	1

order in which the primitives are applied. Let such a sequence be called a word . There is no need to have two consecutive primitives of the same kind because they can be merged into one. Under this observation, ten possible words of length three are possible. Dubins showed that only these six words are possibly optimal:

$$\{LRL, RLR, LSL, LSR, RSL, RSR\}. \quad (6.3)$$

The shortest path between any two configurations can always be characterized by one of these words. These are called the Dubins curves.

6.1 Optimization using Dubins curves

Because of the fact that Dubins curves provide us optimal trajectory, they can be used to optimize trajectory found with RRT-Path algorithm.

For only one UAV, the situation is quite simple and optimization works as follows.

Two random points of trajectory are chosen and Dubins curves are calculated between them. If calculated curves do not collide with the obstacles, they are used instead of original trajectory between chosen points. This points choosing and trajectory replacing is repeated until the whole trajectory can not be shortened more and thus is optimal.

In real situation, we do not know whether found trajectory is optimal or not, so we need to determine conditions for stopping the optimization. The optimization is stopped if the trajectory is not shortened after many (e. g. 150) iterations or optimization is too slow and path is shortened only by small distances (e. g. shortening by 5% per 1000 iterations).

But in swarm, the situation is complicated because of relative localization and minimal and maximal distances between individual UAVs.

So the algorithm must be modified. Dubins curves must be sampled in same frequency as rest of trajectory (this is frequency of RRT-Path algorithm or higher frequency when path is being re-sampled) and each point has to be validated for feasibility in terms of minimal and maximal distance from another UAVs. So the curves can be used only when all trajectories between minimal and maximal distance of relative localization.

6.1.1 One UAV demonstration

In 6.1 we have trajectory of one UAV found by RRT-Path algorithm in map with one obstacle marked by dark grey rectangle. Obstacle amplification is marked by light grey rectangle. In 6.2 we can see optimal path found using Dubins curves. The resulting path consists of many Dubins curves and it was obtained by algorithm mentioned above. Random points have been replaced by Dubins curves and after many iterations, optimal path was found.

Figure 6.1: One UAV before Dubins curves optimization

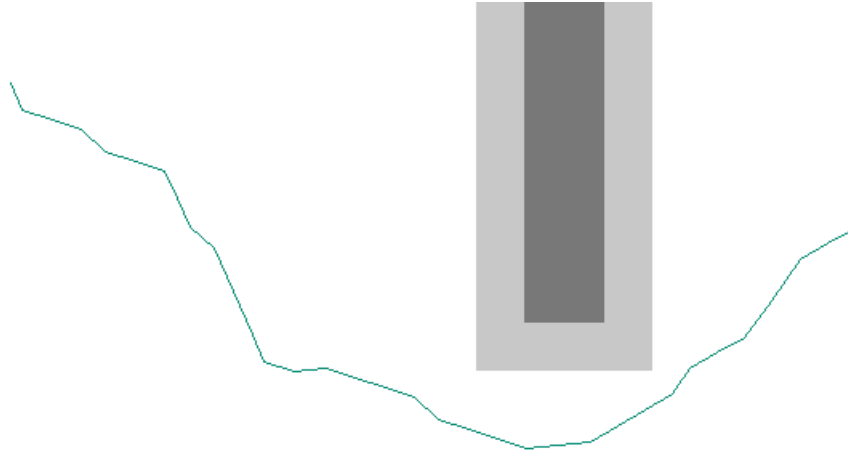
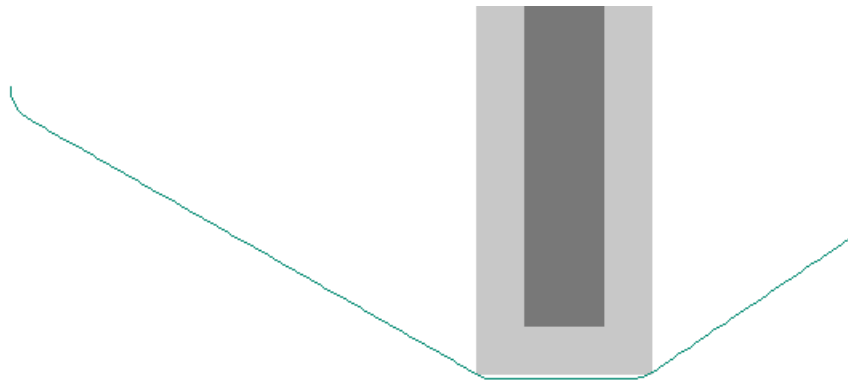


Figure 6.2: One UAV after Dubins curves optimization



PATH RE-SAMPLING

Motion model in RRT-Path algorithm uses constant input in range from 0.5 to 1 second. Smaller interval for constant input causes RRT-Path algorithm to run for too long. When using too short constant input interval, the tree has too many nodes, grows slowly and runs out of memory much faster than longer interval. Interval longer than 1 second makes UAVs unable to manoeuvre between smaller obstacles. Thus range from 0.5 to 1 second was experimentally chosen as best interval. Using x seconds long constant input interval also means $\frac{1}{x}$ Hz frequency of points in resulting trajectory in output of the algorithm. So the range from 0.5 to 1 second implies resulting frequency is in range 1Hz to 2Hz.

Real UAVs in Multi-Robot Systems group at CTU use frequency 70Hz for providing target points to UAVs and trajectories with lower frequency are linear interpolated to have frequency 70Hz. That means frequency 2Hz is too low for real usage because trajectory generated with this frequency would not be smooth enough.

Change of frequency before the RRT-Path algorithm makes the algorithm unable to run efficiently in bigger maps, so this does not solve the problem.

Another solution is to re-sample the path after Dubins curves. But this method failed because after Dubins optimization, the curves had different length and different constant input durations.

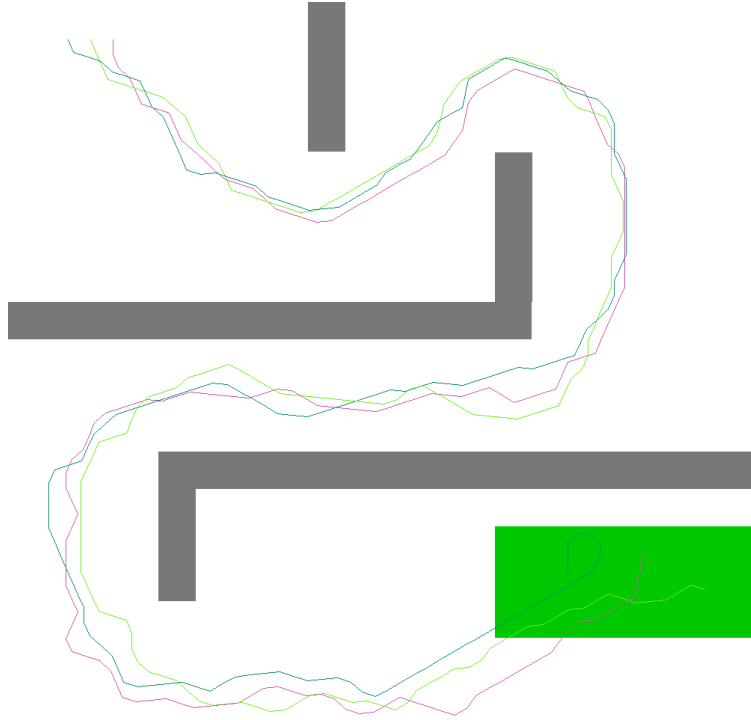
The best solution for this problem is re-sampling of trajectory generated by RRT-Path algorithm before it is optimized by Dubins curves. This solution also has big advantage in Dubins curves optimization because it results to shorter final path as will be shown in following experiment.

7.1 Influence of re-sampling on Dubins curves optimization

To demonstrate the optimization, I created map and let the RRT-Path algorithm find the trajectories for UAVs. The map with trajectories can be seen in 7.1. Obstacles are grey rectangles, AoI is green rectangle and each UAV has trajectory marked with different colour. For measuring of influence of re-sampling of path to Dubins curves optimization, I picked frequencies: 1 Hz (initial frequency used in RRT-Path algorithm), 2 Hz, 4 Hz, 6 Hz, 8 Hz, 10 Hz, 12 Hz, 14 Hz, 16 Hz, 18 Hz, 20 Hz.

The best result of Dubins curves optimization (re-sampling of 20Hz) is shown in 7.2. As we can see, trajectories are much shorter than trajectories before optimization in 7.1. On the beginning of trajectories, in the left upper corner of picture, we can see much smoother curves than

Figure 7.1: Path before Dubins curves optimization



before optimization. This is due to re-sampling to frequency 20Hz, which smooths trajectories.

In real flight, it is undesirable to have trajectories tight to obstacles, so obstacles are amplified before optimization. This can be seen in 7.2 where UAVs keep certain distance from the obstacles.

As stated above, due to time and memory consumption, each optimization is stopped after 150 iterations where optimization did not shorten the path or when speed of path shortening was slower than 5% of original path length per 1000 iterations.

For each frequency, the optimization process was run 100 times to obtain relevant results because of using random numbers during the optimization.

Following table shows average total, minimal and maximal distance of all trajectories from 100 optimizations after the re-sampling and optimization.

The results are also shown in graph 7.3. On the graph we can see that initial frequency 1 Hz has worst results and the frequency 20 Hz has best results. We can also see that in frequency 14 Hz and higher, all 100 iterations had same results, the minimum, maximum and mean value are the same. But the second best frequency in terms of minimal, maximal and mean value is 6 Hz and even the worst optimization in 6 Hz has smaller total distance than 8 to 18 Hz.

Depending on re-sampling frequency, the courses of optimization are also different.

In 7.4, 7.5 and 7.6 we can see mean values and standard deviations for different frequencies, divided into three graphs for better readability. The vertical lines are error bars, they show standard deviation during the optimization. Because the error bars would be too dense if they were shown for each iteration, only every 100th iteration is shown on graphs. For comparison, on each graph is shown also frequency 1 Hz, the initial frequency before re-sampling.

Figure 7.2: Path after Dubins curves optimization

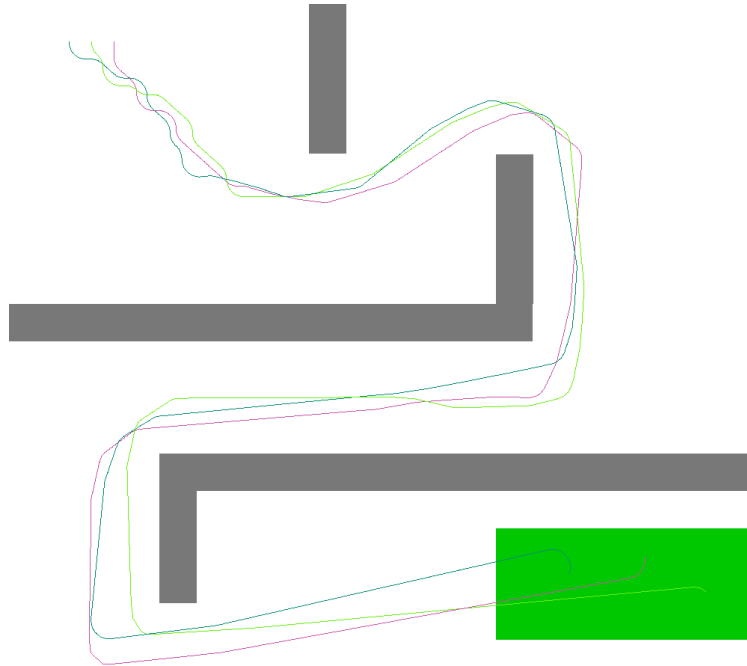


Table 7.1: Re-sampling and optimization results

Frequency [Hz]	Minimal distance [m]	Maximal distance [m]	Average distance [m]
1	8582.18	8849.7	8721.2904
2	8311.65	8548.81	8430.23
4	8366.88	8393.09	8379.985
6	8248.9	8275.7	8262.3
8	8249.88	8378.51	8314.195
10	8286.22	8472.2	8379.21
12	8302.51	8309.2	8307.6613
14	8303.18	8303.18	8303.18
16	8363.92	8363.92	8363.92
18	8510.32	8510.32	8510.32
20	8194.22	8194.22	8194.22

Figure 7.3: Re-sampling and optimization results graph

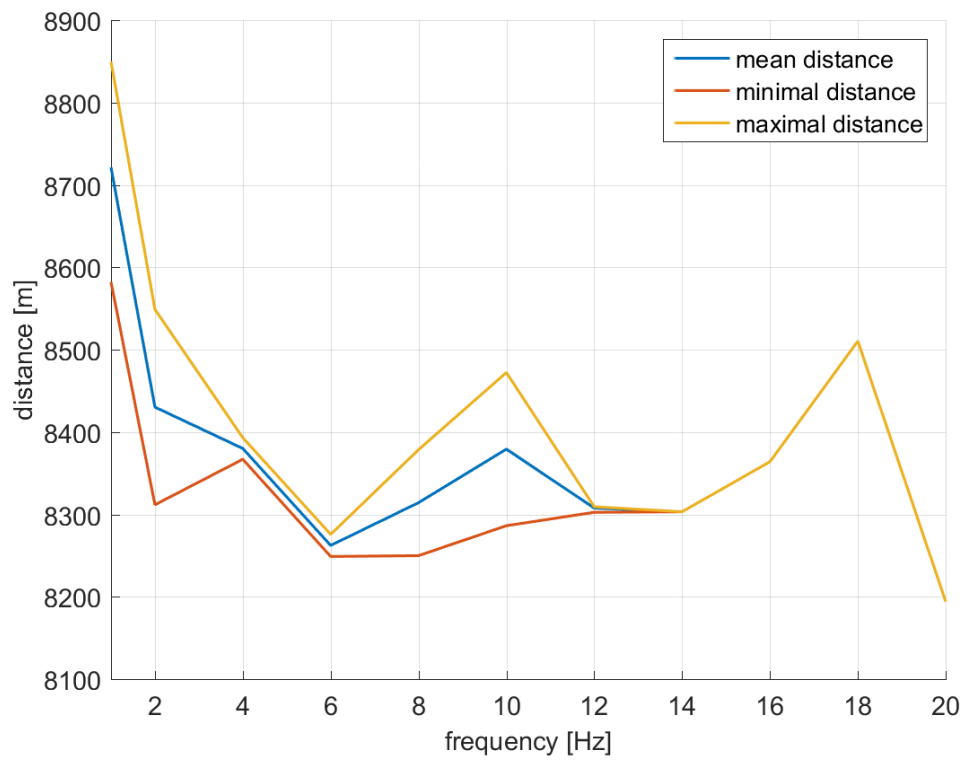


Figure 7.4: Time course of optimization for 2 Hz, 4 Hz, 6 Hz

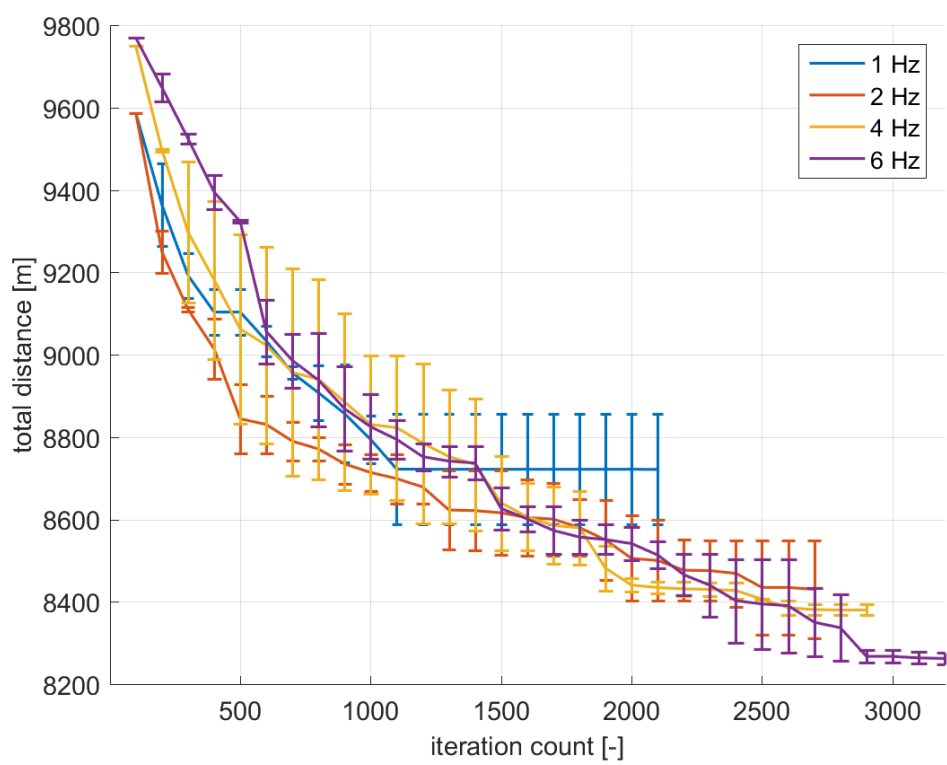


Figure 7.5: Time course of optimization for 8 Hz, 10 Hz, 12 Hz

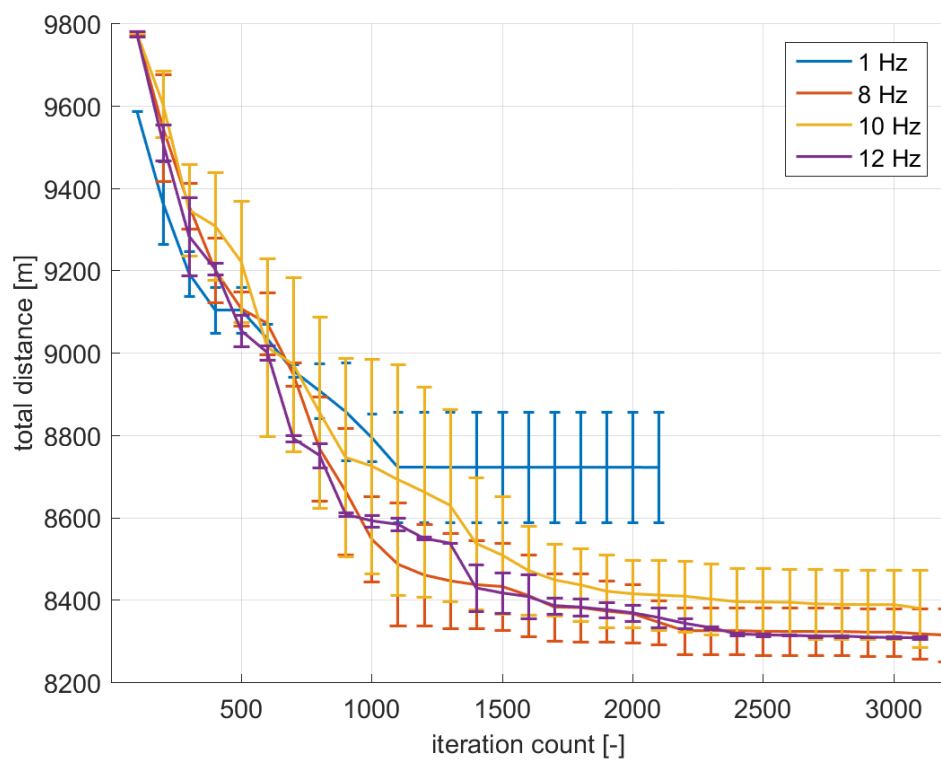
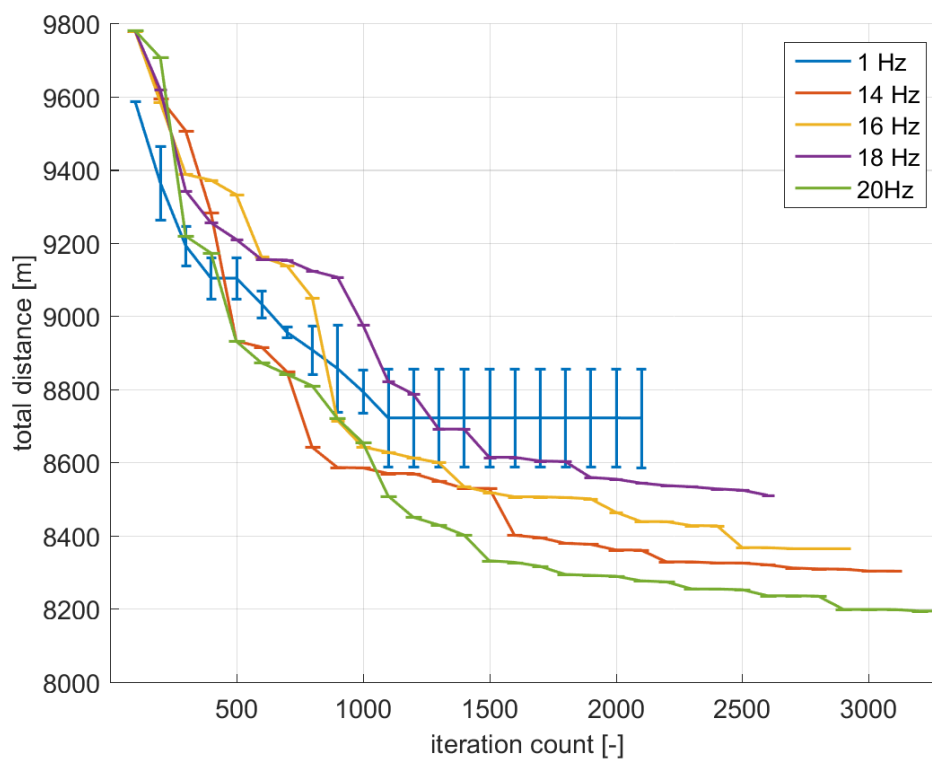


Figure 7.6: Time course of optimization for 14 Hz, 16 Hz, 18 Hz, 20 Hz



IMPLEMENTATION

This part will cover implementation of algorithm, which was used for simulations. Whole code-base can be found at this github repository.

8.1 External libraries

In implementation are used some external libraries. Every used library is mentioned here. Boost libraries is used for smart pointers, libraries for Dubins curves are from Master Thesis by Petr Váňa[4]. Generating of JSON from C++ object is done via Json Spirit library. Another external library is V-Collide from The University of North Carolina at Chapel Hill.

Because V-Collide sources were written in 1997 and because I used C++11 compiler to compile my source codes, I had to rewrite part of this library for compatibility and to make public API easier to use. Modifications can be seen in this github repository.

Last use external library is QT, which was used to create platform independent GUI.

8.2 Code structure and services

Here is shown brief UML scheme demonstrating dependency diagram of codebase. To keep diagram simple, only services are displayed, other classes, which are not services, were left out for lucidity. Diagram was generated using software StarUML

Core class holds core of whole Application and has all other classes as dependencies, as is shown in image 8.1.

As mentioned in 2 chapter Configuration is DTO for all configuration variables, but to keep reasonable amount of classes, Configuration is also service, which delegates all configuration changes from GUI to Core class. Configuration and GuiDrawer implementation LoggerInterface are the only connections between Core and GUI.

State factory creates State classes according to Factory pattern. State class represents state in RRT-Path algorithm. State has coordinates and rotations for all UAVs.

Persister persists found path to JSON using Json Spirit library.

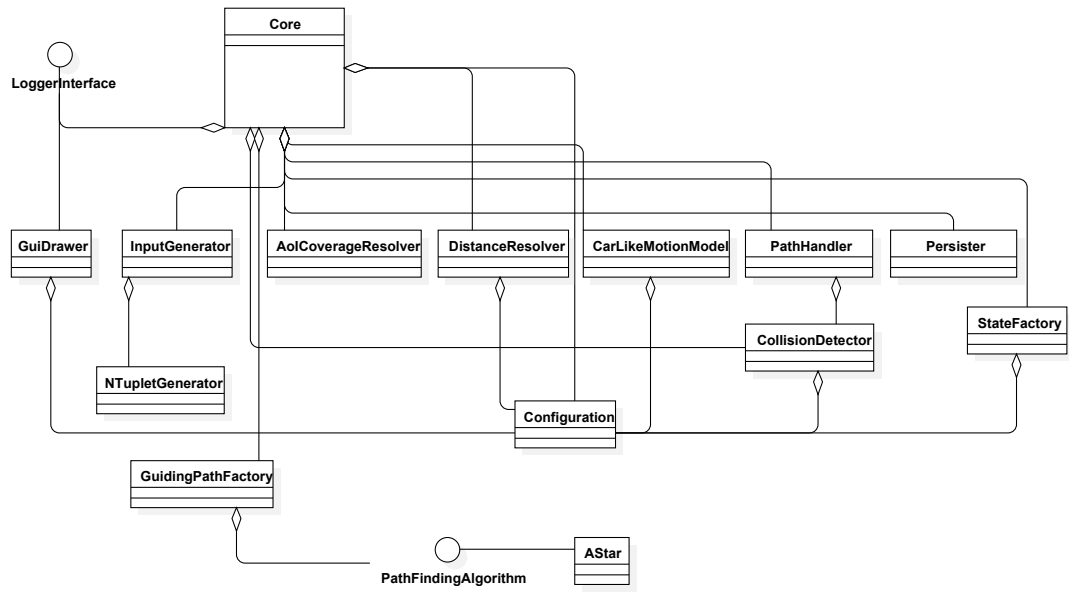
PathHandler serves as utils class for manipulations with path (vector of State classes).

CarLikeMotionModel holds motion model algorithm.

InputGenerator is used to generate inputs to motion model.

NTupletGenerator only generates variation with repeating for given input.

Figure 8.1: Dependency diagram



DistanceResolver counts distances between two states and distance of path.

AoICoverageResolver determines cost function for states, where all UAVs are in AoIs.

GuidingPathFactory is wrapper for PathFindingAlgorithm interface and is used by Core to find guiding path.

Implementation of PathFindingAlgorithm is AStar class.

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