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FACULTY OF ELECTRICAL ENGINEERING
DEPARTMENT OF CYBERNETICS



BACHELOR THESIS

RRT-path method used for cooperative surveillance by
group of helicopters

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Abstrakt V předložené práci studujeme... Uvede se abstrakt v rozsahu 80 až 200 slov. Lorem ipsum dolor sit amet, consectetur adipiscing elit. Ut sit amet sem. Mauris nec turpis ac sem mollis pretium. Suspendisse neque massa, suscipit id, dictum in, porta at, quam. Nunc suscipit, pede vel elementum pretium, nisl urna sodales velit, sit amet auctor elit quam id tellus. Nullam sollicitudin.

Klíčová slova: klíčová slova (3 až 5)

Title: RRT-path method used for cooperative surveillance by group of helicopters

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Abstract In the present work we study ... Uvede se anglický abstrakt v rozsahu 80 až 200 slov. Lorem ipsum dolor sit amet, consectetur adipiscing elit. Ut sit amet sem. Mauris nec turpis ac sem mollis pretium. Suspendisse neque massa, suscipit id, dictum in, porta at, quam. Nunc suscipit, pede vel elementum pretium, nisl urna sodales velit, sit amet auctor elit quam id tellus. Nullam sollicitudin. Donec hendrerit. Aliquam ac nibh. Vivamus mi. Sed felis. Proin pretium elit in neque. Pellentesque at turpis. Maecenas convallis. Vestibulum id lectus.

Keywords: klíčová slova (3 až 5) v angličtině

Prohlašuji, že jsem svou bakalářskou práci napsal(a) samostatně a výhradně s použitím citovaných pramenů. Souhlasím se zapůjčováním práce a jejím zveřejňováním.

V Praze dne 24th April 2016

Jméno Příjmení + podpis

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CHAPTER

ONE

MOTIVATION

ALGORITHM

The basis of the whole algorithm is shown in 2.1 in the pseudocode.

The configuration variable is instance of the Configuration class, which holds all configuration data, including a selected map. The map holds all Areas of Interest (AoI) and obstacles. All obstacles and AoIs are represented as rectangles now.

The purpose of the path finding is to find the shortest feasible paths, but real UAVs need to have some minimal distance to obstacles due to weather conditions, sensor errors and other aspects. To solve this issue, every obstacle is amplified before the whole path finding algorithm on line 2. This minimal distance to obstacles allows UAVs to follow their trajectories safely.

The 3rd line represents the discretization of the map to the graph. The discretization divides the map to squares with size set in the configuration and each square is represented by a graph node. In this graph, there are 4 types of nodes: Free, Obstacle, UAV and Goal. If the whole square or its part is covered by an obstacle, the corresponding node has the type Obstacle. If the whole square or its part is covered by an AoI, then the corresponding node has type Goal. If the square contains an UAV, the corresponding node has type UAV and rest of squares have corresponding nodes with type Free.

Edges in this graph are only between nodes of neighbouring squares, so each node has maximally 8 edges. Obstacle nodes do not have any edges.

After converting the map to nodes, the optional grouping of goals for guiding path can be

Algorithm 2.1 The basis of whole algorithm

```
1: map := configuration.getMap();
2: map := amplifyObstacles(map);
3: nodes := mapToNodes(map);
4: paths := createGuidingPaths(nodes);
5: rrtPath := rrtPath(paths, map, nodes);
6: lastState := getBestFitness(rrtPath, map);
7: path := getPath(lastState);
8: path = straightenCrossingTrajectories(path);
9: path := resamplePath(path, map);
10: path := optimizePathByDubins(path, map);
11: savePath(path);
```

turned on. I will cover the grouping in chapter 3.

The 4th line represents the calculation of the guiding paths for RRT-Path algorithm using the A* algorithm with modified cost function. The modification will be covered in section 4.2.

On the 5th line the RRT-Path algorithm takes place. This function returns a structure with a tree with a root at the starting position of UAVs and with an array containing leaves of this tree, where all UAVs are in Areas of Interest.

The leaf, where UAVs have the best coverage of AoI, is chosen on line 6. The quality of the coverage is determined by the cost function, which will be mentioned later.

On the 6th line the path is built from the last state.

On the 8th line there is an optional preparation before the optimization using Dubins curves. In the preparation, all crossings of paths of individual UAVs are straightened, so UAVs do not cross other trajectories during the whole path. During the implementation of this method some complications appeared, which are covered in the chapter 5, and thus the row was removed from the final version of the algorithm.

On the 9th line, the re-sampling of the path is made, mainly due to requirements of real UAVs, which are mentioned in chapter 8.

On the 10th line there is the optimization by Dubins curves. The optimization is covered in chapter 7.

The last line represents persisting of the path to a file for usage of path by different programs. Path is persisted to JSON, due to convenience of the JSON format. JSON is smaller than XML and can be easily parsed by all widely used programming languages. Path is also persisted to CSV format, so it can be loaded to MATLAB and then loaded into real UAVs.

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GROUPING OF GOALS FOR THE GUIDING PATH

During this processing of the map (method `MapProcessor::getEndNodes` in codebase) all AoIs are grouped to one big AoI, which is the smallest rectangle covering all AoIs.

If this modification is turned on, then instead of one goal for every AoI (node in the middle of AoI rectangle is considered as a goal node), only one goal is used for all AoIs. This prevents swarm to split because the whole swarm has only one guiding path. The relative localization is the main reason to have only one big swarm instead of more smaller swarms is that a smaller swarms (or individual UAVs in case of the same count of AoI and UAVs). Advantages of relative localization are more significant when we have only one swarm.

Maps with goals and obstacles are shown in figures 3.1 and 3.2. Goals are coloured green colour and obstacles grey.

This approach has the following advantage: when individual AoIs are near to a global goal of the whole group, as seen in 3.2, then the whole swarm follows one guiding path without any splitting, which makes the RRT-Path run faster and also the advantage of relative localization is included.

The disadvantage of this method is that when individual AoIs have a bigger distance from each other than can be covered by UAVs then this approach totally fails, because RRT-Path, which is much faster than RRT, has goal very distant from AoIs, as can be seen in 3.1.

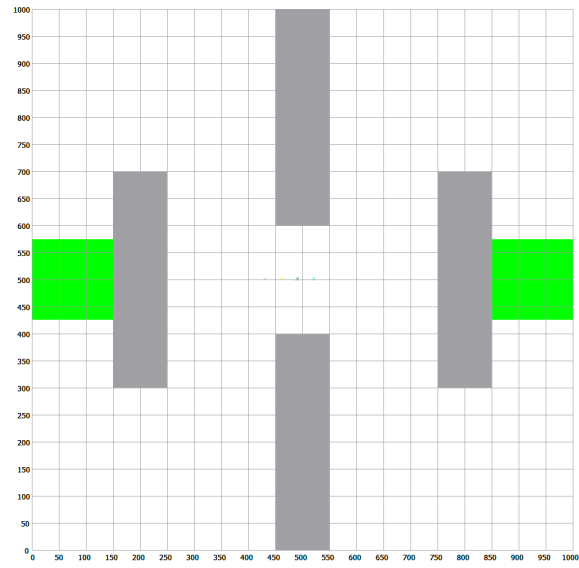


Figure 3.1: Map with goals unsuitable for grouping

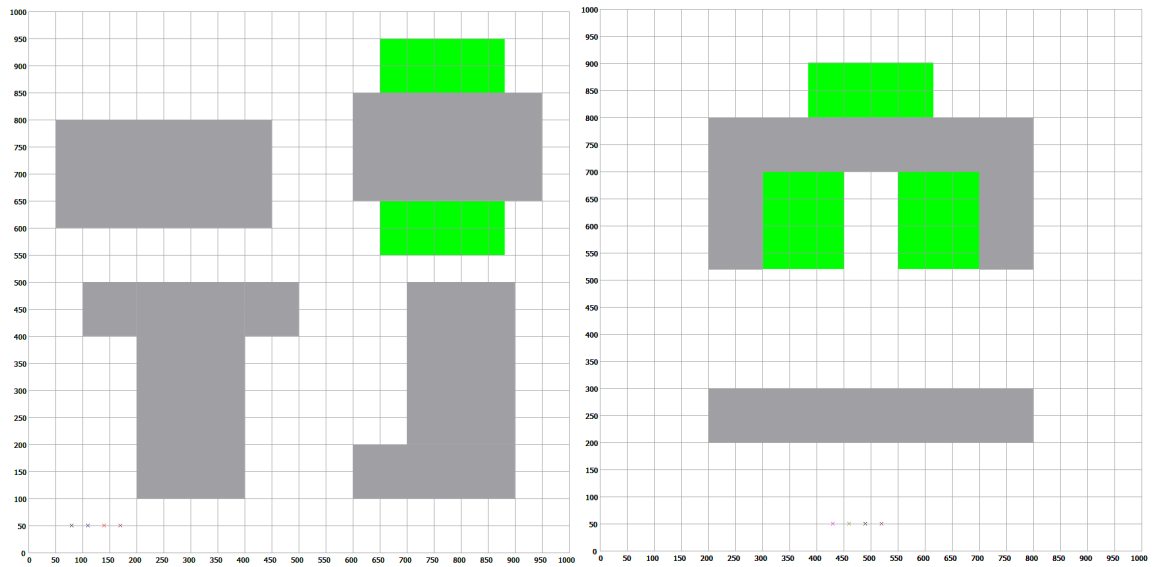


Figure 3.2: Maps with goals suitable for grouping

RRT-PATH

This chapter will cover brief introduction of RRT-Path algorithm. But before that, we need to define RRT algorithm which RRT-Path is based on.

4.1 Rapidly Exploring Random Tree

Rapidly Exploring Random Tree, also abbreviated as RRT, was introduced by LaValle[2] in 1998, is non-deterministic algorithm for motion planning, used to search non-convex spaces by randomly building space-filling tree. The RRT method builds a tree T rooted at q_{start} . The basic RRT algorithm works as follows. In each iteration, a random sample q_{rand} is chosen from C and the nearest node q_{near} in the tree to q_{rand} is found. The node q_{near} is expanded using a local planner to obtain a set of new configurations reachable from q_{near} . The nearest configuration towards q is selected from this set and added to the tree. The edge from q_{near} to the newly added configuration contains control inputs used by the local planner to reach the new configuration. The algorithm terminates if the distance between a node in the tree and q_{goal} is less than d_{goal} or after I_{max} of planning iterations. [5] The basis of RRT is listed in algorithm 4.1.

4.2 Guiding path

This algorithm has a modified cost function and in addition to a cost function of the A* algorithm, the cost of current node is added during the calculation. Nodes neighbouring with obstacles have a bigger cost than nodes which do not have obstacles as neighbours. Thanks to this modification, guiding path avoids obstacles and has bigger distance to obstacles.

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modifikaci cost
function

Algorithm 4.1 RRT algorithm

Input: Configurations q_{alert} and q_{goal} , maximum number of iterations I_{max} , maximum distance to goal d_{goal}

Output: Trajectory P or failure

```
1:  $T.add(q_{start})$  ; // create new tree and add initial conguration q in it
2: for iteration:=1:I do
3:  $q_{rand} :=$  random conguration in C using uniform distribution;
4:  $q_{near} :=$  nearest node in tree  $T$  to q ;
5:  $expandTree(q_{rand}, q_{near})$ ;
6:  $d =$  distance from tree  $T$  to  $q_{goal}$  ;
7: if  $d < d_{goal}$  then
8:  $P =$  extract trajectory from  $q_{start}$  to  $q_{rand}$ ;
9: return  $P$ ;
10: end
11: end
12: return failure; // no solution was found within K iterations start
```

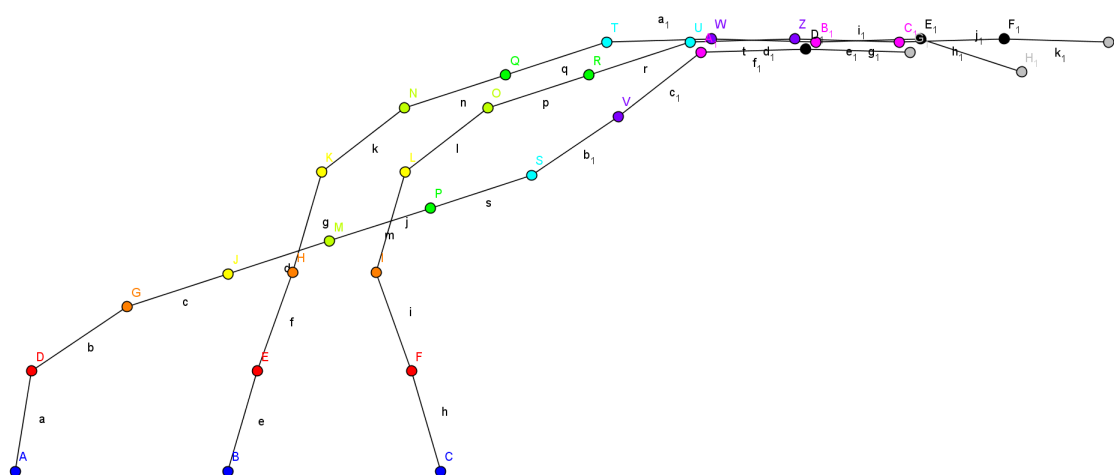
PATHS STRAIGHTENING

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RRT-Path algorithm checks crossing paths between neighbouring states, so between n th state and $n+1$ -th state no trajectories are crossing each other. But between states trajectories are still crossing. In this image 5.1 is shown path found by RRT-Path. Every colour marks one state in RRT-Path. As we can see, check in algorithm prevents from crossing path between neighbouring states, but crossing of paths in different times can not be easily prevented. We can see in image, that paths cross between points J (yellow), M (light green) and H (orange), K (yellow), so there is no easy approach to prevent path collisions between $n-2$ -th state and n th state. Optimization by Dubins curves shortens trajectory of UAVs, so UAVs could be in these trajectories in different time, so there could be collisions after optimization. Another complication occurs, when time difference between two states is too low, then UAVs could collide, because in reality UAV can not follow path precisely, but only with some errors.

I tried to straighten crossing trajectories, but all attempts failed. Straightening was done by switching parts of crossing paths from the earliest crossing state to end. But then paths had different lengths, which was unsuitable for path planning for swarm. This can be done by adding “waiting” points, points in different state but with same position in different time. But then is really hard to straighten longer path with many crossings (this path is really short, paths in other maps are much longer and more complicated). For motion model with inertia is also really hard to deal with waiting states, which complicates following of straightened trajectories. Due to all complications mentioned above, this part was removed from algorithm. But it is possible to add it, when better approach will be found.

Figure 5.1: Crossing paths



MOTION MODEL

The RRT-Path algorithm is universal and works without motion model, which is fine for holonomic robot, but usage of motion model allows us to find path more feasible for swarm of UAVs than without using of holonomic robot. For this purpose, car like model was chosen. Differential equations of motion model in 3D from [?] are

$$\begin{aligned}\dot{x}(t) &= v(t) \sin \varphi(t) \\ \dot{y}(t) &= v(t) \cos \varphi(t) \\ \dot{z}(t) &= w(t) \\ \dot{\varphi}(t) &= K(t) v(t)\end{aligned}\tag{6.1}$$

where $x(t)$, $y(t)$, $z(t)$ are coordinates of UAV, $\varphi(t)$ represents heading of UAV, $v(t)$ is forward velocity, $K(t)$ is curvature, $w(t)$ is ascent velocity. $\begin{bmatrix} K(t) & w(t) & v(t) \end{bmatrix}$ represent input vector of motion model. Differential equations are useful for representation in equations, but not useful for computer algorithm. For usage in algorithm are better difference equations instead of differential equations. When inputs are held constant in each time interval between two time steps, difference equations are

$$\begin{aligned}x(k+1) &= \begin{cases} \text{if } K(k+1) \neq 0 \\ x(k) + \frac{1}{K(k+1)} (\sin(\varphi(k) + K(k+1)v(k+1)\Delta t(k+1)) - \sin(\varphi(k))) \\ \text{if } K(k+1) = 0 \\ x(k) + v(k+1) \cos(\varphi(k)) \Delta t(k+1) \end{cases} \\ y(k+1) &= \begin{cases} \text{if } K(k+1) \neq 0 \\ y(k) - \frac{1}{K(k+1)} (\cos(\varphi(k) + K(k+1)v(k+1)\Delta t(k+1)) - \cos(\varphi(k))) \\ \text{if } K(k+1) = 0 \\ y(k) + v(k+1) \sin(\varphi(k)) \Delta t(k+1) \end{cases} \\ z(k+1) &= z(k) + w(k+1) \Delta t(k+1) \\ \varphi(k+1) &= \varphi(k) + K(k+1)v(k+1)\Delta t(k+1)\end{aligned}\tag{6.2}$$

DUBINS CURVES

Dubins curves, also called Dubins manoeuvres or Dubins path were published by Lester Eli Dubins in 1957 [1]. Dubins path is optimal path for car like motion model. Path is optimal, when car moves at constant forward speed. The other important constraint is the maximum steering angle ϕ_{max} , which results in a minimum turning radius ρ_{min} . As the car travels, consider the length of the curve in $\mathcal{W} = \mathbb{R}^2$ traced out by a pencil attached to the centre of the car. The task is to minimize the length of this curve as the car travels between any q_I and q_G . Due to ρ_{min} , this can be considered as a bounded-curvature shortest-path problem. If $\rho_{min} = 0$, then there is no curvature bound, and the shortest path follows a straight line in \mathbb{R}^2 . In terms of a cost function, the criterion to optimize is

$$L(\tilde{q}, \tilde{u}) = \int_0^{t_F} \sqrt{\dot{x}(t)^2 + \dot{y}(t)^2} dt \quad (7.1)$$

, where t_F is the time at which q_G is reached, and a configuration is denoted as $q = (x, y, \theta)$, \tilde{x}_t denotes the function $\tilde{x}_t : [0, t] \rightarrow X$, which is called the state trajectory (or state history). This is a continuous-time version of the state history, which was defined previously for problems that have discrete stages. Similarly, \tilde{u}_t denotes the action trajectory (or action history),. If q_G is not reached, then it is assumed that $L(\tilde{q}, \tilde{u}) = \infty$. [3]

When considering constraints of inputs (actions) for motion model, the system can be simplified to

$$\begin{aligned} \dot{x} &= \cos \theta \\ \dot{y} &= \sin \theta \\ \dot{\theta} &= u \end{aligned} \quad (7.2)$$

in which u is chosen from the interval $U = \{-\tan \phi_{max}, 0, \tan \phi_{max}\}$. For simplicity, assume that $\tan \phi = 1$. The following results also hold for any $\phi_{max} \in (0, \pi/2)$.

It was shown in [1] that between any two configurations, the shortest path for the Dubins car can always be expressed as a combination of no more than three motion primitives. Each motion primitive applies a constant action over an interval of time. Furthermore, the only actions that are needed to traverse the shortest paths are $u \in \{-1, 0, 1\}$. The primitives and their associated symbols are shown in 7.1. The S primitive drives the car straight ahead. The L and R primitives turn as sharply as possible to the left and right, respectively. Using these symbols, each possible kind of shortest path can be designated as a sequence of three symbols that corresponds to the

Table 7.1: The three motion primitives from which all optimal curves for the Dubins car can be constructed.

Symbol	Steering u
L	-1
S	0
R	1

order in which the primitives are applied. Let such a sequence be called a word . There is no need to have two consecutive primitives of the same kind because they can be merged into one. Under this observation, ten possible words of length three are possible. Dubins showed that only these six words are possibly optimal:

$$\{LRL, RLR, LSL, LSR, RSL, RSR\}. \quad (7.3)$$

The shortest path between any two configurations can always be characterized by one of these words. These are called the Dubins curves.

7.1 Optimization using Dubins curves

Because of the fact that Dubins curves provide us optimal trajectory, they can be used to optimize trajectory found with RRT-Path algorithm.

For only one UAV, the situation is quite simple and optimization works as follows.

Two random points of trajectory are chosen and Dubins curves are calculated between them. If calculated curves do not collide with the obstacles, they are used instead of original trajectory between chosen points. This points choosing and trajectory replacing is repeated until the whole trajectory can not be shortened more and thus is optimal.

In real situation, we do not know whether found trajectory is optimal or not, so we need to determine conditions for stopping the optimization. The optimization is stopped if the trajectory is not shortened after many (e. g. 150) iterations or optimization is too slow and path is shortened only by small distances (e. g. shortening by 5% per 1000 iterations).

But in swarm, the situation is complicated because of relative localization and minimal and maximal distances between individual UAVs.

So the algorithm must be modified. Dubins curves must be sampled in same frequency as rest of trajectory (this is frequency of RRT-Path algorithm or higher frequency when path is being re-sampled) and each point has to be validated for feasibility in terms of minimal and maximal distance from another UAVs. So the curves can be used only when all trajectories between minimal and maximal distance of relative localization.

7.1.1 One UAV demonstration

In 7.1 we have trajectory of one UAV found by RRT-Path algorithm in map with one obstacle marked by dark grey rectangle. Obstacle amplification is marked by light grey rectangle. In 7.2 we can see optimal path found using Dubins curves. The resulting path consists of many Dubins curves and it was obtained by algorithm mentioned above. Random points have been replaced by Dubins curves and after many iterations, optimal path was found.

Figure 7.1: One UAV before Dubins curves optimization

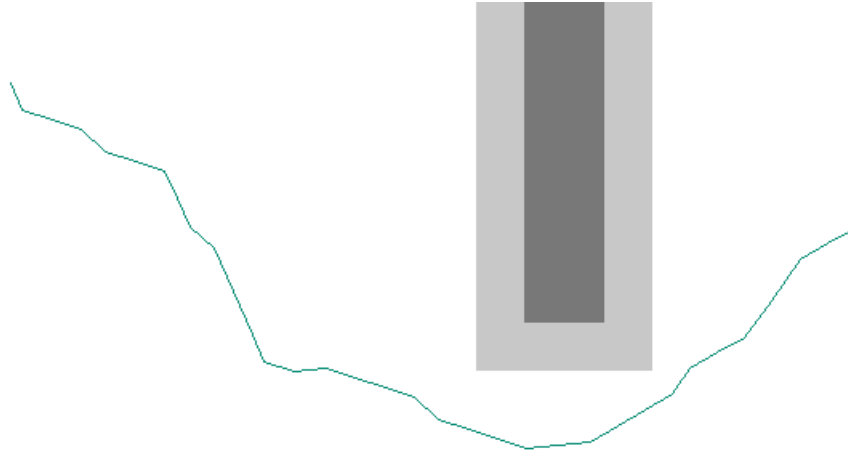
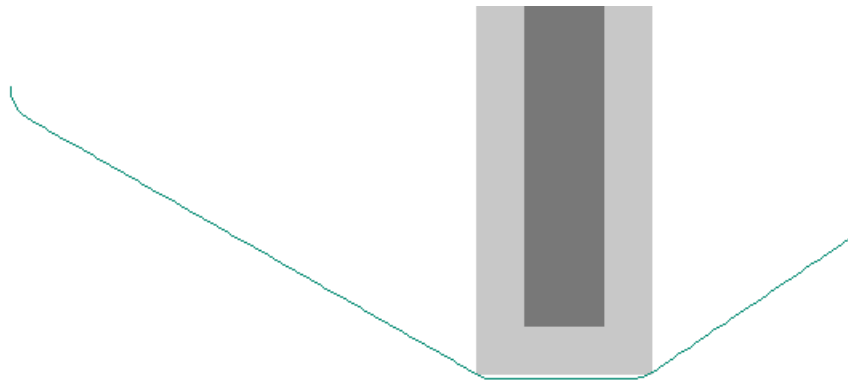


Figure 7.2: One UAV after Dubins curves optimization



PATH RE-SAMPLING

Motion model in RRT-Path algorithm uses constant input in range from 0.5 to 1 second. Smaller interval for constant input causes RRT-Path algorithm to run for too long. When using too short constant input interval, the tree has too many nodes, grows slowly and runs out of memory much faster than longer interval. Interval longer than 1 second makes UAVs unable to manoeuvre between smaller obstacles. Thus range from 0.5 to 1 second was experimentally chosen as best interval. Using x seconds long constant input interval also means $\frac{1}{x}$ Hz frequency of points in resulting trajectory in output of the algorithm. So the range from 0.5 to 1 second implies resulting frequency is in range 1Hz to 2Hz.

Real UAVs in Multi-Robot Systems group at CTU use frequency 70Hz for providing target points to UAVs and trajectories with lower frequency are linear interpolated to have frequency 70Hz. That means frequency 2Hz is too low for real usage because trajectory generated with this frequency would not be smooth enough.

Change of frequency before the RRT-Path algorithm makes the algorithm unable to run efficiently in bigger maps, so this does not solve the problem.

Another solution is to re-sample the path after Dubins curves. But this method failed because after Dubins optimization, the curves had different length and different constant input durations.

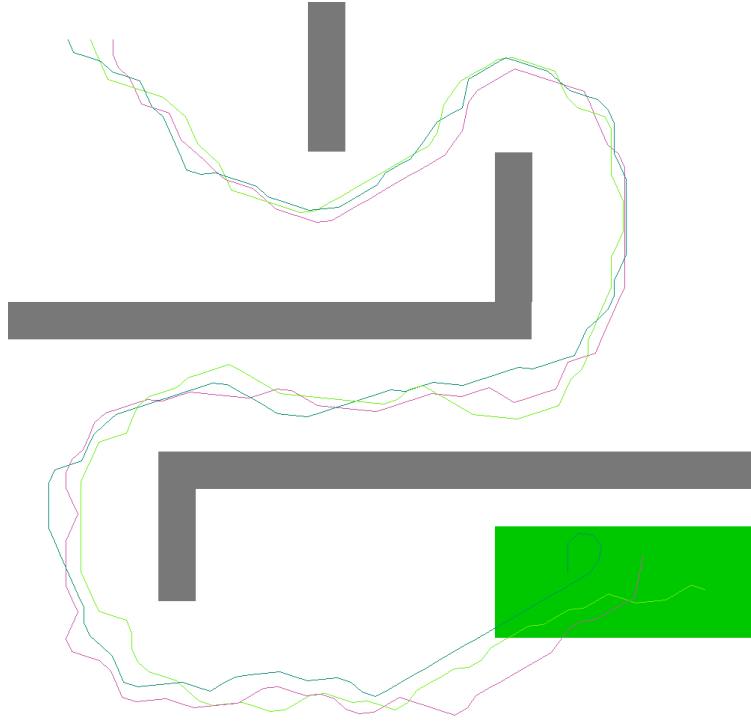
The best solution for this problem is re-sampling of trajectory generated by RRT-Path algorithm before it is optimized by Dubins curves. This solution also has big advantage in Dubins curves optimization because it results to shorter final path as will be shown in following experiment.

8.1 Influence of re-sampling on Dubins curves optimization

To demonstrate the optimization, I created map and let the RRT-Path algorithm find the trajectories for UAVs. The map with trajectories can be seen in 8.1. Obstacles are grey rectangles, AoI is green rectangle and each UAV has trajectory marked with different colour. For measuring of influence of re-sampling of path to Dubins curves optimization, I picked frequencies: 1 Hz (initial frequency used in RRT-Path algorithm), 2 Hz, 4 Hz, 6 Hz, 8 Hz, 10 Hz, 12 Hz, 14 Hz, 16 Hz, 18 Hz, 20 Hz.

The best result of Dubins curves optimization (re-sampling of 20Hz) is shown in 8.2. As we can see, trajectories are much shorter than trajectories before optimization in 8.1. On the beginning of trajectories, in the left upper corner of picture, we can see much smoother curves than

Figure 8.1: Path before Dubins curves optimization



before optimization. This is due to re-sampling to frequency 20Hz, which smooths trajectories.

In real flight, it is undesirable to have trajectories tight to obstacles, so obstacles are amplified before optimization. This can be seen in 8.2 where UAVs keep certain distance from the obstacles.

As stated above, due to time and memory consumption, each optimization is stopped after 150 iterations where optimization did not shorten the path or when speed of path shortening was slower than 5% of original path length per 1000 iterations.

For each frequency, the optimization process was run 100 times to obtain relevant results because of using random numbers during the optimization.

Following table shows average total, minimal and maximal distance of all trajectories from 100 optimizations after the re-sampling and optimization.

The results are also shown in graph 8.3. On the graph we can see that initial frequency 1 Hz has worst results and the frequency 20 Hz has best results. We can also see that in frequency 14 Hz and higher, all 100 iterations had same results, the minimum, maximum and mean value are the same. But the second best frequency in terms of minimal, maximal and mean value is 6 Hz and even the worst optimization in 6 Hz has smaller total distance than 8 to 18 Hz.

Depending on re-sampling frequency, the courses of optimization are also different.

In 8.4, 8.5 and 8.6 we can see mean values and standard deviations for different frequencies, divided into three graphs for better readability. The vertical lines are error bars, they show standard deviation during the optimization. Because the error bars would be too dense if they were shown for each iteration, only every 100th iteration is shown on graphs. For comparison, on each graph is shown also frequency 1 Hz, the initial frequency before re-sampling. As we can see, frequencies 14, 16, 18 and 20 Hz have almost zero standard deviation and converge to

Figure 8.2: Path after Dubins curves optimization

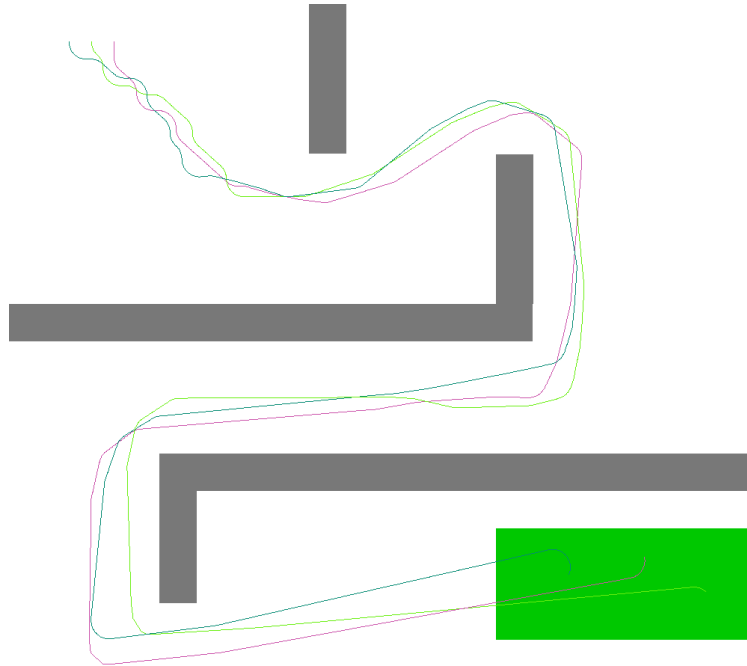


Table 8.1: Re-sampling and optimization results

Frequency [Hz]	Minimal distance [m]	Maximal distance [m]	Average distance [m]
1	8582.18	8849.7	8721.2904
2	8311.65	8548.81	8430.23
4	8366.88	8393.09	8379.985
6	8248.9	8275.7	8262.3
8	8249.88	8378.51	8314.195
10	8286.22	8472.2	8379.21
12	8302.51	8309.2	8307.6613
14	8303.18	8303.18	8303.18
16	8363.92	8363.92	8363.92
18	8510.32	8510.32	8510.32
20	8194.22	8194.22	8194.22

Figure 8.3: Re-sampling and optimization results graph

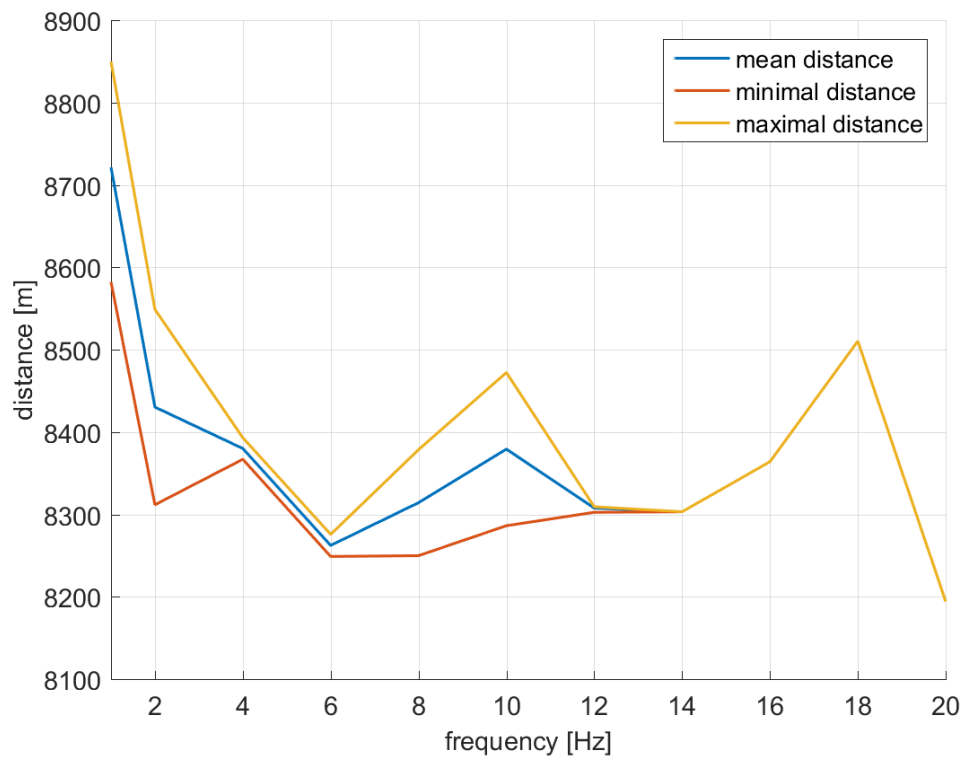
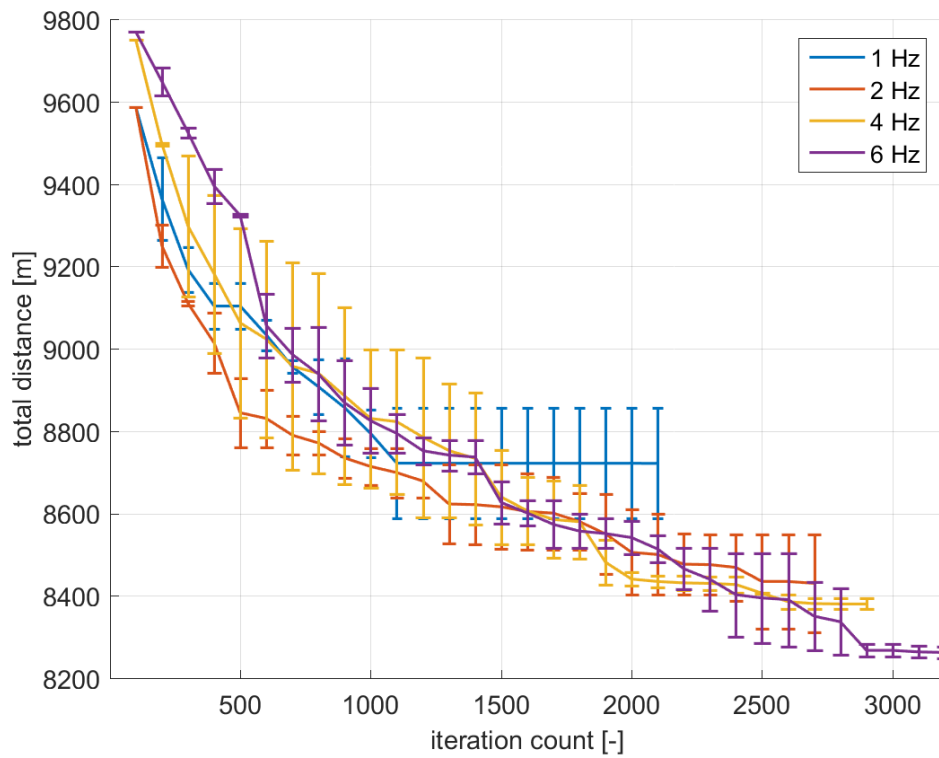


Figure 8.4: Time course of optimization for 2 Hz, 4 Hz, 6 Hz



lower value than initial frequency. In frequency 10 Hz can be seen high standard deviation. That means the optimization got stuck in local optimum and did was not able to shorten any path for many iterations.

Figure 8.5: Time course of optimization for 8 Hz, 10 Hz, 12 Hz

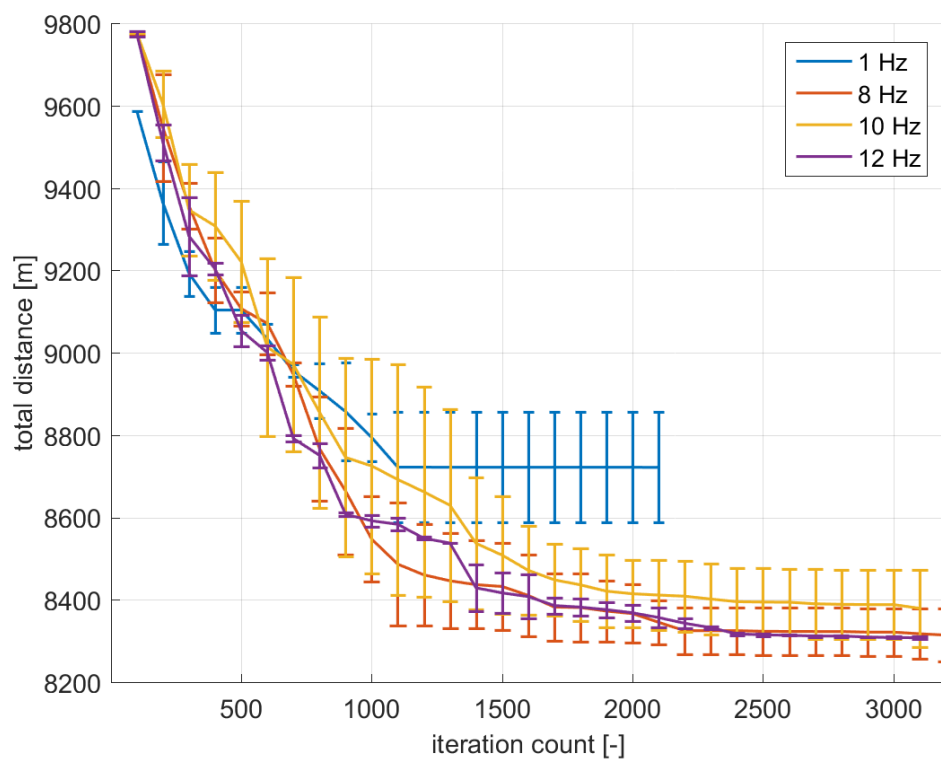
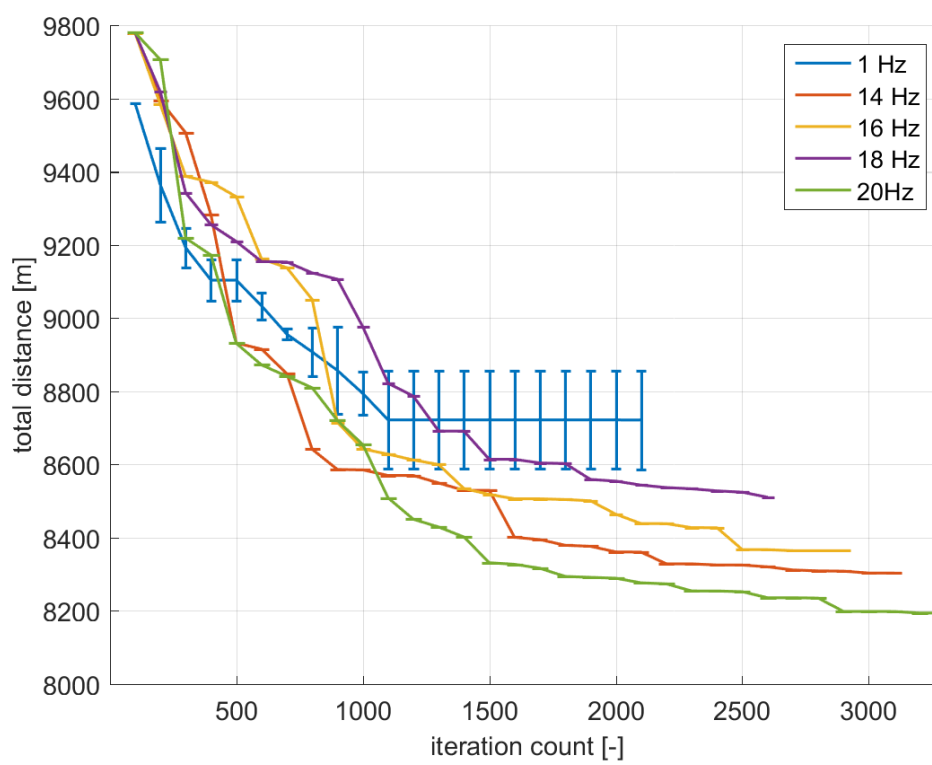


Figure 8.6: Time course of optimization for 14 Hz, 16 Hz, 18 Hz, 20 Hz



COVERING MORE AOIS WITH ONE SWARM

V-REP SIMULATIONS

V-REP is acronym for Virtual robot experimentation platform, a simulator developed by Coppelia Robotics, providing an advanced environment for testing and simulations of robots of all types. The V-REP environment is free and open-source for educational purposes and also has commercial licence. The environment takes in account certain physical laws like gravity, inertia or friction, which enables to truthfully verify applicability for deployment of UAVs in the real world. V-REP has many build-in models, but user can also create his own robot. V-REP enables to control robots over API and has API clients for C, C++, Python, Java, Lua, Matlab, Octave and Urbi.

10.1 UAV control and path simulation

Python is convenient for fast prototyping and has native functions for easy JSON parsing, which made it good choice for simulations of generated trajectories in V-REP.

UAVs in V-REP can be controlled over remote API only by changing location of their target. Then UAV tries to reach the location of its target. Unfortunately, UAVs only follow location, with speed proportional to distance. UAVs do not try to reach target and simultaneously to have zero speed when reaching their target, which causes overshoot. This fact leads to another disadvantage of UAV controller. When keeping target in same distance and direction from UAV, the UAV increases its speed, which causes overshoot when target changes its direction to UAV. These overshoots were many times bigger than size of UAVs, so they could not be ignored and had to be fixed.

During first, naive implementation, position of next state was set as target position for UAV, but due to overshoot and large distances between states UAVs failed to follow the trajectory.

Another implementation linear interpolated trajectory between UAV and its next state position and calculated target placed in line between UAV and next state position, but in constant distance to UAV.

So the calculation was defined as follows

$$\mathbf{X}(k+1)_{target} = \mathbf{X}(k)_{UAV} + \frac{(\mathbf{X}(k)_{ns} - \mathbf{X}(k)_{UAV})}{\|\mathbf{X}(k)_{ns} - \mathbf{X}(k)_{UAV}\|} \cdot const$$

where $\mathbf{X}(k)_{UAV}$ is UAV position in k-th iteration of simulation, $\mathbf{X}(k)_{ns}$ is position of next state in planned path in k-th iteration, $\mathbf{X}(k+1)_{target}$ is position of UAV target in (k+1)-th iteration

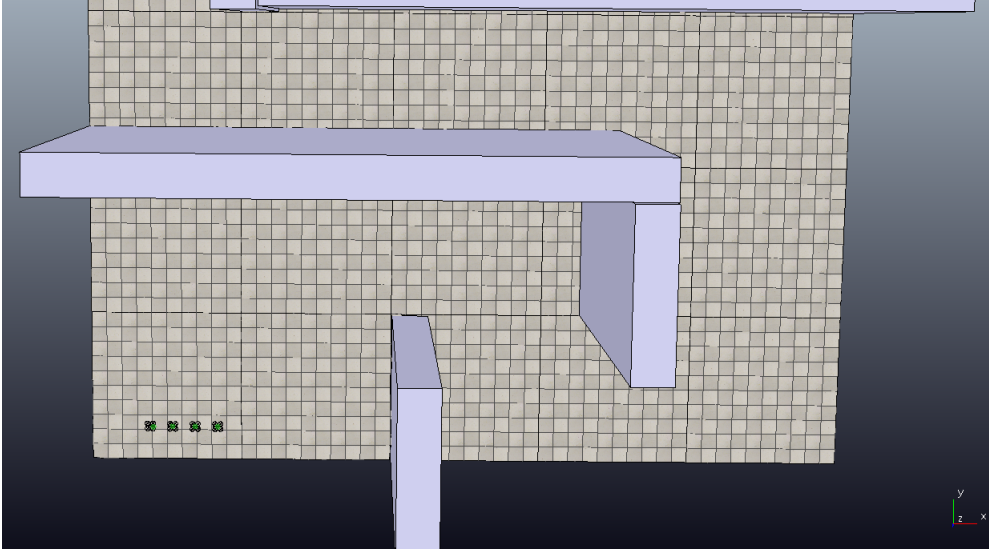


Figure 10.1: Map with UAV overshoot

and $const$ is constant experimentally tuned, so the UAV does not move too fast nor too slow. Too fast movements cause overshoot and too slow movements cause the simulation to run for needlessly long time.

But as mentioned earlier, even this approach did not go well. In long passages, where trajectory did not turn, UAVs increased their velocity and inertia, which made them harder to turn. The problem of overshooting is shown in figures 10.1 and 10.2. Overshoot is on the end of long passage in map 10.1. Red and violet balls represent positions of next states and green balls represent UAV targets. In the first image, we can see UAVs leaving the narrow passage. As you can see in second and third image, positions of next state are still, but because of constant distance of target and UAV, the target is dragged by UAV's inertia.

This has been fixed by not updating the position of target when distance between UAV and next state is bigger than in previous iteration and the position of next state is still the same, so the equation describing target position is

$$\mathbf{X}(k+1)_{target} = \begin{cases} \text{if } \|\mathbf{X}(k)_{ns} - \mathbf{X}(k)_{UAV}\| < \|\mathbf{X}(k-1)_{ns} - \mathbf{X}(k-1)_{UAV}\| \\ \wedge \mathbf{X}(k)_{ns} = \mathbf{X}(k-1)_{ns} \\ \mathbf{X}(k)_{UAV} + \frac{(\mathbf{X}(k)_{ns} - \mathbf{X}(k)_{UAV})}{\|\mathbf{X}(k)_{ns} - \mathbf{X}(k)_{UAV}\|} \cdot const \\ else \\ \mathbf{X}(k)_{target} \end{cases}$$

. This prevents target from dragging by UAV with big inertia.

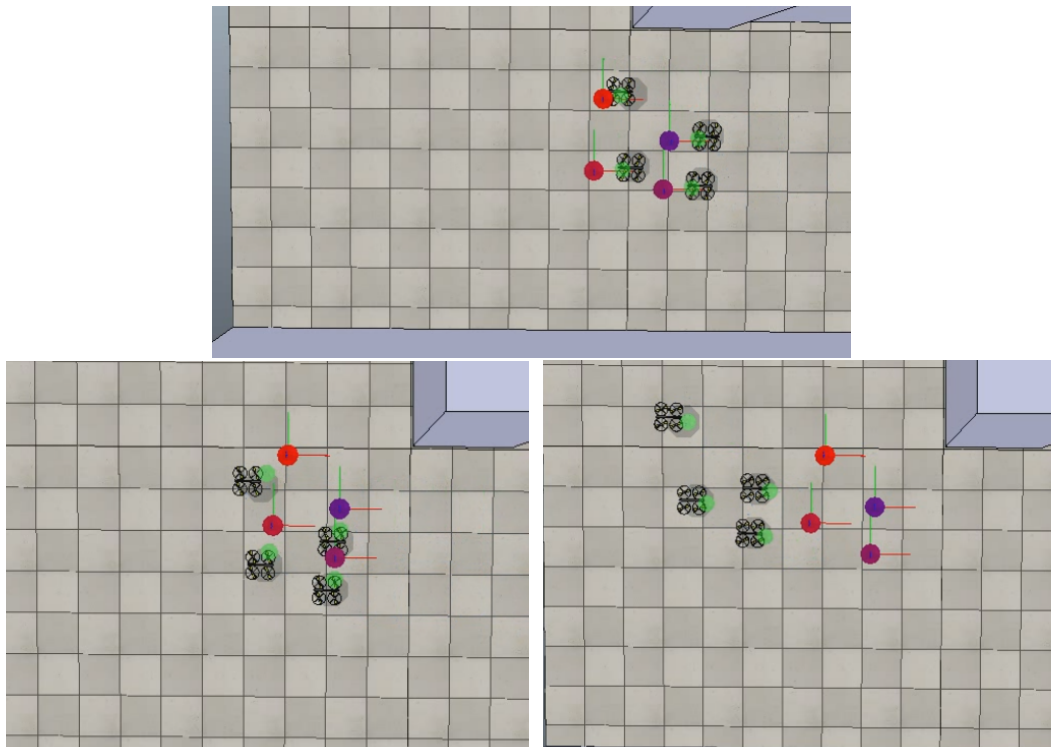


Figure 10.2: UAV overshoot
Here can be seen 3 iterations. Next state is changed during

IMPLEMENTATION

This part will cover implementation of algorithm, which was used for simulations. Whole codebase in C++ can be found at this [github repository](#). Next to the C++ program, I also created some CLI scripts in PHP, for drawing map and paths from the JSON representation, batch running of Dubins curves optimization and other useful stuff. These can be seen at this [github repository](#). V-REP simulations were made by communicating with V-REP through remote API, the client is written in Python and can be seen [here](#).

11.1 External libraries

In implementation are used some external libraries. Every used library is mentioned here. Boost libraries is used for smart pointers, libraries for Dubins curves are from Master Thesis by Petr Váňa[4]. Generating of JSON from C++ object is done via Json Spirit library. Another external library is V-Collide from The University of North Carolina at Chapel Hill.

Because V-Collide sources were written in 1997 and because I used C++11 compiler to compile my source codes, I had to rewrite part of this library for compatibility and to make public API easier to use. Modifications can be seen in this [github repository](#).

Last used external library is QT, which was used to create platform independent GUI.

11.2 Code structure and services

Here is shown brief UML scheme demonstrating dependency diagram of codebase. To keep diagram simple, only services are displayed, other classes, which are not services, were left out for lucidity. Diagram was generated using software StarUML

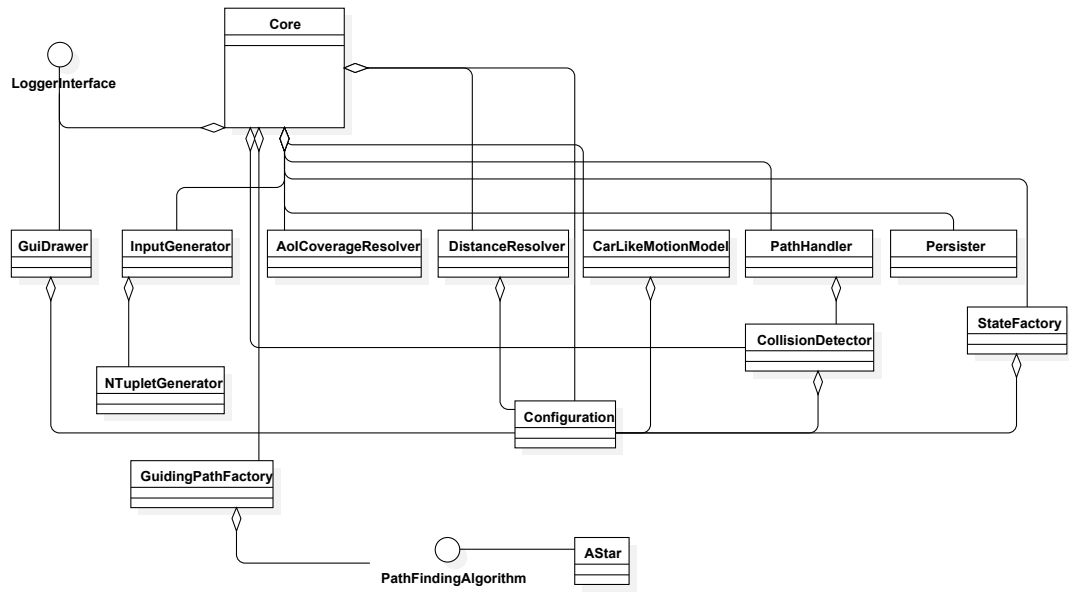
Core class holds core of whole Application and has all other classes as dependencies, as is shown in image 11.1.

As mentioned in 2 chapter Configuration is DTO for all configuration variables, but to keep reasonable amount of classes, Configuration is also service, which delegates all configuration changes from GUI to Core class. Configuration and GuiDrawer implementation LoggerInterface are the only connections between Core and GUI.

State factory creates State classes according to Factory pattern. State class represents state in RRT-Path algorithm. State has coordinates and rotations for all UAVs.

Persister persists found path to JSON using Json Spirit library.

Figure 11.1: Dependency diagram



PathHandler serves as utils class for manipulations with path (vector of State classes).

CarLikeMotionModel holds motion model algorithm.

InputGenerator is used to generate inputs to motion model.

NTupletGenerator only generates variation with repeating for given input.

DistanceResolver counts distances between two states and distance of path.

AoICoverageResolver determines cost function for states, where all UAVs are in AoIs.

GuidingPathFactory is wrapper for **PathFindingAlgorithm** interface and is used by **Core** to find guiding path.

Implementation of **PathFindingAlgorithm** is **AStar** class.

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