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function [a, e, i, RAAN, omega, M] = cart2kep(r,v,mu)
%-----%
% Converts ECI state orbit to Orbital elements
%-----%
% Inputs: r and v [m] and [m/s] of orbit
%         mu [m^3/s^2]
%
% Outputs: a [m] - semi major axis
%         e - eccentricity
%         i [deg] inclination
%         RAAN [deg] Right angle of ascending node
%         omega [deg] argument of perigee
%         M [deg] mean anomaly
%
%
h = cross(r,v);
h_mag = norm(h);
n = cross([0;0;1],h);
n_mag = norm(n);
e_vec = cross(v,h)/mu - r/norm(r);
e = norm(e_vec);
a = 1/(2/norm(r) - norm(v)^2/mu);
i = acos(h(3)/h_mag);
RAAN = atan2(h(1), -h(2));
omega = atan2(dot(cross(n,e_vec),h)/h_mag, dot(n,e_vec));
nu = atan2(dot(cross(e_vec,r),h)/h_mag, dot(e_vec,r));

if e < 1 - 1e-12           % elliptic
    % Compute eccentric anomaly E robustly from nu
    denom = 1 + e * cos(nu);
    cosE = (e + cos(nu)) ./ denom;
    sinE = sqrt(max(0, 1 - e^2)) .* sin(nu) ./ denom;
    E = atan2(sinE, cosE);
    E = mod(E, 2*pi);
    M = E - e .* sin(E);
    M = mod(M, 2*pi);      % normalized
elseif e > 1 + 1e-12       % hyperbolic
    % hyperbolic anomaly F (sometimes H)
    denom = 1 + e * cos(nu);
    if abs(denom) < eps
        warning('Denominator near zero when converting nu to hyperbolic anomaly; result may be unstable.');
    end
    sinhF = sqrt(e^2 - 1) .* sin(nu) ./ denom;
    F = asinh(sinhF);
    M = e .* sinh(F) - F;    % hyperbolic "mean anomaly" (signed)
    % do not normalize M to [0,2pi) for hyperbola
else
    error('Parabolic orbit (e ~ 1): mean anomaly is not defined; use Barker''s equation for time-of-flight.');
end

kep = [a; e; i; RAAN; omega; M];

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end