Taller de Inferencia de Tipos Machete

PLP

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1 Algoritmo de inferencia

- $\mathbb{W}(x) \stackrel{\text{def}}{=} \{x:s\} \triangleright x:s, \quad s \text{ variable fresca}$
- $\mathbb{W}(\theta) \stackrel{\text{def}}{=} \emptyset \triangleright \theta : nat$
- $\mathbb{W}(true) \stackrel{\text{def}}{=} \emptyset \triangleright true : bool$
- $\mathbb{W}(false) \stackrel{\text{def}}{=} \emptyset \triangleright false : bool$
- $\mathbb{W}(succ(U)) \stackrel{\text{def}}{=} S\Gamma \triangleright S \, succ(M) : nat \text{ donde}$
 - $W(U) = \Gamma \triangleright M : \tau$
 - $-S = MGU\{\tau \doteq nat\}$
- $\mathbb{W}(pred(U)) \stackrel{\text{def}}{=} S\Gamma \triangleright S \, pred(M) : nat \, donde$
 - $W(U) = \Gamma \triangleright M : \tau$
 - $-S = MGU\{\tau \doteq nat\}$
- $\mathbb{W}(iszero(U)) \stackrel{\text{def}}{=} S\Gamma \triangleright S iszero(M) : bool \text{ donde}$
 - $\ \mathbb{W}(U) = \Gamma \triangleright M : \tau$
 - $-S = MGU\{\tau \doteq nat\}$
- $\mathbb{W}(if\ U\ then\ V\ else\ W)\stackrel{\mathrm{def}}{=} S\Gamma_1 \cup S\Gamma_2 \cup S\Gamma_3 \triangleright S(if\ M\ then\ P\ else\ Q): S\sigma$ donde
 - $W(U) = \Gamma_1 \triangleright M : \rho$
 - $\mathbb{W}(V) = \Gamma_2 \triangleright P : \sigma$
 - $\mathbb{W}(W) = \Gamma_3 \triangleright Q : \tau$
 - $-S = MGU\{\sigma \doteq \tau, \rho \doteq bool\} \cup \{\sigma_1 \doteq \sigma_2 \mid x : \sigma_1 \in \Gamma_i, x : \sigma_2 \in \Gamma_j, i \neq j\}$
- $\mathbb{W}(\lambda x.U) \stackrel{\text{def}}{=} \Gamma' \triangleright \lambda x : \tau'.M : \tau' \to \rho$ donde
 - $\ \mathbb{W}(U) = \Gamma \triangleright M : \rho$
 - $-\ \tau' = \left\{ \begin{array}{l} \alpha \ {\rm si} \ x : \alpha \in \Gamma \\ s \ {\rm con} \ s \ {\rm variable \ fresca \ en \ otro \ caso} \end{array} \right.$
 - $-\Gamma' = \Gamma \ominus \{x\}$
- $\mathbb{W}(U\,V) \stackrel{\text{def}}{=} S\Gamma_1 \cup S\Gamma_2 \triangleright S(M\,N) : St \text{ donde}$
 - $\mathbb{W}(U) = \Gamma_1 \triangleright M : \tau$
 - $W(V) = \Gamma_2 \triangleright N : \rho$
 - t variable fresca
 - $-S = MGU\{\tau \doteq \rho \to t\} \cup \{\sigma_1 \doteq \sigma_2 \mid x : \sigma_1 \in \Gamma_1, x : \sigma_2 \in \Gamma_2\}$

Código auxiliar

2.1 Expresiones

```
data Exp a = VarExp Symbol |
            ZeroExp |
            SuccExp (Exp a) |
            PredExp (Exp a) |
             IsZeroExp (Exp a) |
             TrueExp |
             FalseExp |
             IfExp (Exp a) (Exp a) (Exp a) |
             LamExp Symbol a (Exp a) |
             AppExp (Exp a) (Exp a)
type Symbol = String
type PlainExp = Exp ()
type AnnotExp = Exp Type
2.2
    Tipos
data Type = TVar Int | TNat | TBool | TFun Type Type
2.3 Contexto
emptyEnv :: Env
extendE :: Env -> Symbol -> Type -> Env
removeE :: Env -> Symbol-> Env
evalE :: Env -> Symbol -> Type
joinE :: [Env] -> Env
domainE :: Env -> [Symbol]
```

2.4 Sustituciones

```
emptySubst :: Subst
extendS :: Int -> Type -> Subst -> Subst
class Substitutable a where
   (<.>) :: Subst -> a -> a
   instance Substitutable Type \,\, -- subst <.> t
```

2.5 Unificación

```
type UnifGoal = (Type, Type)
data UnifResult = UOK Subst | UError Type Type
mgu :: [UnifGoal] -> UnifResult
```