

## The Tetrahedral Engine

A Resolution-Independent Volumetric Rendering System

### 1. The Core Concept

The **Tetrahedral Engine** is a fundamental reimagining of 3D computer graphics.

For the last 50 years, 3D rendering has relied on the **Cartesian Grid** (X, Y, Z) and **Polygonal Meshes** (triangles). While effective, this approach suffers from a critical flaw: **Aliasing**. When you zoom in, the illusion breaks. Curves become jagged lines, and textures become pixelated blocks.

This engine changes the coordinate system.

Instead of an origin-based point perspective, we utilize a **Skew-Axis Coordinate System** based on the geometry of the Tetrahedron. This allows us to represent 3D volumes not as a stack of flat pictures, but as a continuous, resolution-independent field—similar to a vector file, but for volumetric matter.

### 2. How It Works

The "Inside-Out" Voxel

Traditional voxels are cubes. They stack poorly and hate rotation.

Our engine uses the **Rhombic Dodecahedron** as its atomic unit.

- **Geometric Dual:** It is the "inside-out" inversion of a Cube.
- **Integer Math:** It maintains a precise 2:1 volume ratio with Cartesian space.
- **Packing:** It tessellates 3D space perfectly with no gaps, like a 3D honeycomb.

The S, T, U Address Space

We replace the standard (X, Y, Z) coordinates with a dimensionless barycentric triplet: (S, T, U).

- **S (Slit 1):** Position along the horizontal edge of the root tetrahedron.
- **T (Slit 2):** Position along the opposing vertical edge.
- **U (Depth):** The barycentric balance between the two axes.

This coordinate system is **Affine Invariant**. You can stretch, squash, or scale the volume to the size of a galaxy, and the internal logic remains perfectly intact without floating-point errors.

### 3. Key Innovations

#### 1. Exocentric Rendering ("The Hologram")

Standard engines use an **Egocentric** camera (the world revolves around the eye).

The Tetra Engine uses an **Exocentric** model. The object broadcasts light rays in all directions.

The "Screen" is just a net that catches these rays.

- **Result:** You can move the screen closer to the object, and the detail increases naturally, exactly like looking closer at a real physical object.

#### 2. The 360° Singularity Solution

X-Slit projection traditionally suffers from "blind spots" (singularities) at 90-degree angles.

We solved this with a **Dynamic Axis Switching** mechanism. The engine automatically detects the view angle and "hands off" the rendering to the optimal pair of tetrahedral edges (Red, Green, or Blue axis pairs), ensuring a seamless, artifact-free image from any angle.

#### 3. Volumetric Compression

By organizing data into a recursive **Tetra-Tree** (similar to an Octree but geometrically superior), we can stream massive 3D assets over the web. The client device can display a low-res "proxy" instantly and fill in the details progressively, enabling "Holographic Streaming."

#### 4. Mathematical Validation

The coordinate system has been mathematically verified via Python simulation.

- **The Round-Trip Proof:** Cartesian points (X,Y,Z) can be converted to Tetra-Space (S,T,U) and back with zero loss of precision.

- **The Center Lock:** The Cartesian origin (0,0,0) maps perfectly to the Tetrahedral center (0.5, 0.5, 0.5).

See `/proofs/tetra_validation.py` for the validation script.

#### 5. Patent Status

This technology is currently **Patent Pending**.

The unique methods regarding the Rhombic Dodecahedral Voxel derivation, the Skew-Axis rendering pipeline, and the Exocentric viewing model are documented in the associated provisional specification.

© 2026. All Rights Reserved.