Vector field path following and obstacle avoidance singularity mitigation via look-ahead flight envelope

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ABSTRACT

Problem Statement

Unmanned Aerial Vehicles (UAVs) conventially navigate a series of off-line generated and initially obstacle free waypoints that may have to be re-planned when encountering a previously unknown obstacle. Re-planning waypoints could be avoided by implementing a path following and obstacle avoidance vector field guidance. Guidance to converge and follow a pre-planned path is produced by an attractive vector field while obstacles are represented by a repulsive vector field. Summing together attractive goal and repulsive obstacle fields produce a guidance for tracking a pre-planned path while avoiding unplanned obstacles. Small regions of null guidance, called singularities, may be produced when summing attractive and repulsive fields together.

Method for path following, obstacle avoidance, and detection / mitigation of vector field singularities for UAVs etc **Motivation**

- Conventional waypoint guidance relies on a pre-planned, flyable, and obstacle free path
- Obstacles unaccounted for during planning may require a re-plan which may require communication with a ground station

Background

- Vector field guidance for path following has been shown to be both robust in the presence of external disturbances and produce low cross track error flight
- Obstacles can be represented as repulsive fields and summed with attractive fields to produce an obstacle avoidance guidance
- Summing vector field guidance my produce singularities, resulting in no guidance
- Repulsive fields currently provide no additional information on how to go around obstacle

Contribution

• Method for compensating for singularities that may be experienced (Lookahead or fast detection)

I. Nomenclature

VF = Vector Field

II. Introduction

Unmanned Aerial Vehicles are pilotless aircraft used by military, police, and civilian communities for tasks such as reconnaissance, damage assessment, natural disaster surveying, and target tracking [1, 2]. Tasks can be performed by a single UAV or with a team of other air, ground, or marine vehicles [3–5]. Missions are typically accomplished by following a series of pre-planned waypoints that are generated off-line at a ground station and relayed over radio. Obstacles such as buildings or terrain may be considered during planning to prevent collisions, as seen in Figure 1.

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Fig. 1 Series of waypoints avoiding static obstacle

The on-board guidance system directs the UAV towards the current active waypoint until a pre-defined radius around the waypoint is reached. When a waypoint has been reached the proceeding waypoint becomes active. An example of how a UAV follows waypoints can be shown in Figure 2



Fig. 2 UAV path from waypoint guidance

During waypoint navigation the UAV may encounter an obstacle unknown during planning or experience a change in the environment which may require a new obstacle free series of waypoints be generated. A highly uncertain or dynamic environment may require frequent waypoint re-planning which may be difficult or impossible if communication with the ground station is lost.

Potential field combines path planning, trajectory planning, and control into a single process [6] and is based on the principle of artificial attractive and repulsive forces [7]. A robot at an initially high potential is pulled towards a goal located at a globally minimum potential while being repelled by obstacles in close proximity by repulsive forces. Major drawbacks to potential field were pointed out in [8] consisting of local minimum and oscillations in corridors. The local minimum problem occurs when closely spaced obstacle's potential combine to produce a well on the descent gradient where a pre-mature stable point is found. Proposed solutions to local minimum include object clustering and virtual waypoint method [9], virtual escaping route [10], and use of navigation functions [11]. Oscillations in potential field were studied in [12], and [13].

The potential field method converges to a singular point which is not possible for fixed wing aircraft. Similar to conventional waypoint guidance, the active goal point would change as a function of proximity, however for certain UAV applications such as following a curved ground track or surveying it may be beneficial to follow an explicit path.

Such path following can be accomplished with vector fields which produce a heading guidance that asymptotically converges and circulates a path. A comparison between vector field and waypoint guidance techniques was presented in [14] where each method was evaluated based on its complexity, robustness, and cross-track error. Vector field produced guidance that was both robust to external wind disturbances while maintaining a low cross track error. The two most prominent methods for generating vector fields in literature consist of the Lyapunov [15–18] and Goncalves [19–22] method. A circular Lyapunov vector field can be generated by the methodology described in [15]. Given the Lyapunov function:

$$V(x,y) = (r^2 - r_d^2)^2$$
 (1)

where r is given by the equation

$$r = \sqrt{x^2 + y^2} \tag{2}$$

and the total time derivative of Equation 1 is

$$\dot{V}(x,y) = \nabla V \cdot [\dot{x}, \dot{y}]^T \tag{3}$$

Utilizing the following equation to select the desired relative velocity \dot{x} and \dot{y}

$$\vec{V}_{Lyapunov} = \begin{bmatrix} \dot{x}_d \\ \dot{y}_d \end{bmatrix} = \alpha \left(\frac{-v}{r} \right) \begin{bmatrix} x \frac{r^2 - r_d^2}{r^2 + r_d^2} + y \frac{2rr_d}{r^2 + r_d^2} \\ y \frac{r^2 - r_d^2}{r^2 + r_d^2} - x \frac{2rr_d}{r^2 + r_d^2} \end{bmatrix}$$
(4)

and assuming $\alpha = 1$ and r = 1, the final Lyapunov VF equation is generated:

$$\overrightarrow{V}_{Lyapunov} = \frac{v}{r^2 + r_d^2} \begin{bmatrix} -x(r^2 - r_d^2) - y(2rr_d) \\ -y(r^2 - r_d^2) + x(2rr_d) \end{bmatrix}$$
(5)

The vector produced by 5 provides a guidance at position (x, y) for following a circular path, where v is the desired UAV velocity, r is the range to the center of the circular path, and r_d is the radius of the path. Additional vectors such as wind may also be added to the field for disturbance rejection.

The Goncalves method produces an-dimensional vector field that converges and circulates a static or time-varying path defined by (n-1) implicit surfaces $(\alpha_i : \mathbb{R}^n \to \mathbb{R} | i = 1, ..., n-1)$. The surface functions must satisfy the two conditions that 1) they are positive definite and 2 have bounded derivatives. Consider the space with dimensions in set q:

$$\mathbf{q} = \begin{bmatrix} x_1, x_2, ..., x_n \end{bmatrix} \tag{6}$$

The vector field can be calculated by the sum of three terms consisting of a convergence \vec{v}_{conv} , circulation \vec{v}_{circ} , and time-varying \vec{v}_{tv} term.

$$\vec{v} = \vec{v}_{conv} + \vec{v}_{circ} + \vec{v}_{tv} \tag{7}$$

Convergence is calculated by:

$$\vec{v}_{conv} = \sum_{i=1}^{n-1} \alpha_i \nabla_q \alpha_i \tag{8}$$

Circulation:

$$\vec{v}_{circ} = \wedge_{i=1}^{n-1} \nabla_q \alpha_i \tag{9}$$

$$\vec{v}_{circ} = \nabla_a \alpha_1 \times \nabla_a \alpha_2 \tag{10}$$

The time-varying component is calculated by:

$$\vec{\mathbf{v}}_{tv} = \mathbf{M}^{-1} a \tag{11}$$

$$M = \begin{bmatrix} \nabla \alpha_1^T \\ \nabla \alpha_2^T \\ (\nabla \alpha_1 \times \nabla \alpha_2)^T \end{bmatrix}$$
 (12)

$$a = \begin{bmatrix} \frac{\partial \alpha_1}{\partial t} & \frac{\partial \alpha_2}{\partial t} & 0 \end{bmatrix}^T \tag{13}$$

Gradient vector field (GVF) is a method that produces an *n*-dimensional vector field that converges and circulates a target path[19].

Paths can be static or time-varying and consist of points that lie at the intersection of surfaces defined by implicit functions.

The surface functions are used to calculate a total vector field that is a sum of a convergence, circulation, and time-varying term.

Convergence effectively attracts a robot to the target curve while circulation guides the robot to traverse the target curve.

Time-varying is a feed-forward term that accounts for changes in the target path as a function of time t. The total field \vec{v} is summarized in Equation 7.

A method for producing and stitching together straight and circular path vector fields was presented in [16]. Vector fields that converge and circulate an arbitrary path was investigated in [18]. Vector fields have been studied for standoff tracking and circumnavigation in [15],[17], [Wilhelm].

The standoff tracking scenario presented in [Wilhelm] tasked a fixed wing UAV with loitering around a moving ground target while adding obstacle avoidance constraints. A circular attractive vector field was attached to a moving ground target. Repulsive vector fields centered at the obstacles and weighted by hyperbolic tangent decay functions were summed with the attractive circular field to produce a target loitering and obstacle avoidance guidance. The performance of Lyapunov [15] and gradient vector field [19–21] were compared for their cross track error with respect to the loiter circle. Gradient vector field had favorable performance due to compensation for a time-varying vector field. The gradient vector field technique also has the benefit of decoupled weighting parameters for convergence, circulation, and time-varying terms, allowing for easy modification of field behavior.

Decay functions for avoidance fields were investigated in [Zhu] for obstacles present on a straight path. When summing attractive and repulsive vector fields there is the possibility of guidance singularities, where magnitude and direction are equal and opposite. The presence of singularities were not addressed in [Wilhelm] and [Zhu], mentioned briefly in [16] and observed in [23]. For fixed wing UAVs the lack of guidance may prevent the UAV from avoiding an obstacle, while multi-rotor UAVs may end up in a trap situation. Singularities may be present at any location where a goal field and obstacle field are of equal strength.

- Transition to Vector Field - Such path following can be accomplished with vector fields which are a continuous source of guidance for converge to and following paths.
 - Start of VF -
- Sujit compared vector field guidance to other guidance laws in [] and found that robust against wind disturbances Low cross track error
- VF produced for straight line and circular arc primitives in [Nelson] Method expanded in [Griffiths] for VF following curved paths Circular fields modified for standoff tracking in frew another Wilehlm
- Standoff tracking of a moving ground target while avoiding obstacles was presented in [Wilhelm] Fixed wing UAV tasked with tracking a moving ground target Circular attractive vector field guided UAV to track ground target while compensating for ground target velocity Repulsive vector field centered at obstacles and weighted by a hyperbolic tangent decay function Fields summed together to produce a combined guidance Two methods compared, Lyapunov and Goncalves Goncalves lower tracking error due to accounting for time varying nature of target
 - Activation / decay functions for obstacles were investigated in [Zhu]
- Singularities produced when summing together attractive and repulsive fields mentioned in [nelson] "deadzones, sinks, singularities" Observed in Panagou Expected at any VF location where an attractive field and obstacle field are of equal strength
- VF use existing path planning methods to generate a guidance that minimizes distance to a path while also avoiding obstacles and singularities in obstacle fields —- Final Contribution —-
 - UAS consists of vehicle, autopilot, ground station, radios
 - Missions typically pre-planned on ground station where flyable and obstacle free paths can be generated. (Figure of conventional waypoints)
 - Waypoints are sent to the autopilot over a radio and received and interpreted by the vehicles autopilot
 - Autopilot responsible for navigating waypoints while maintaining vehicle stability

- Due to turn rate constraints or external disturbances, a vehicle may not follow the path perfectly where it may encounter an obstacle previously planned for
- Demonstrate the above with dubins
 - Introduce dubins as a way to approximate a UAVs dynamics, assume control working (cite)
 - Equations
 - Demonstrate Dubin's UAV not perfectly following path
 - Demonstrate Dubin's with wind not following path
- Reduced error for straight line and circular path following has been achieved by using vector field guidance (sujit)
- Continuous vectors that asymptotically converge and follow straight and circular paths are both robust and produce guidance that results in low cross track error
- Lyapunov VF primitives introduced (Nelson). Nelson stitched together primitives to produce complex paths similar to navigating waypoints
- Curved path vector field was introduced in (griffiths)
- Goncalves VF
 - Path of any shape
 - Accounts for TV nature of paths
 - Field is produced by summing convergence and circulation terms that are easily accessable
 - Integral lines guaranteed to converge
- Obstacles considered in standoff tracking scenario Wilhelm
 - TV field loiter around moving ground target
 - obstacles represented by repulsive field
 - Did not consider or identify singularities present in summed fields
 - Singularities are small regions or wells of no guidance where UAV may be trapped
 - No information on how to go around obstacle
 - Field used as a high level specification for avoidance
 - Hyperbolic activation function
- Activation functions of obstacle avoidance investigated in Zhu
- Determining VF parameters that influence performance and singularity location

III. Methodology

A. Singularity Detection

- Present VF equations for straight path following
- Present VF equations for circular obstacle and obstacle definitions
 - Repulsion, small 'path' radius
 - Decay function
 - No circulation versus circulation (side by side figure)
- Sum fields together and show stages of normalization
- Identify pre normalization singularity
 - Surface plot (x,y,magnitude)
 - Identify undefined region and singularity (Evaluating entire space)
 - Find minimum of guidance function by evaluating several initial conditions
 - Method for finding all singularities as a reference to future look-ahead methods
- Look-ahead and singularity detection
- Location of all singularities not important if UAV is not going to encounter them
- Introduce UAV flight envelope
- Time, turn rate, constant velocity, produces possible locations of UAV
- Evaluate ICs on flight envelope when near obstacle

B. Modifying VF to avoid singularities

- Cause and location of singularities
 - Adding circulation to the repulsive obstacle field reduces /removes singularity

- Singularities will occur where both fields have equal strength
- Prediction of singularity location based on decay function
- Side by side repulsion and repulsion+circ singularity locations
- Singularity detected, modify field to remove singularity from flight envelope
- Objective function is:
 - Avoid obstacle
 - Avoid singularities
 - Minimize deviation from path

IV. Simulation

- Dubins UAV following a pre-planned straight path
- · Obstacle encountered
- A guidance solution must be determined that:
 - Determines location of singularities if present (inside flight envelope)
 - Solve VF parameters to remove / mitigate singularities
 - Solve VF parameters that result in guidance that minimize error from path
- Various UAV speeds
- Worse case scenario presented (on path)
- Multiple obstacles on path (sequential)
- Compare non-modified guidance with modified guidance
 - Deviation from path
 - Yes/no obstacle avoided
 - singularity avoided in flight envelope

V. Conclusion

Appendix

Acknowledgments

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