

A Proposal for a Parameterized Circulating Vector Field Guidance for Fixed Wing  
Unmanned Aerial Vehicles

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This thesis titled  
A Proposal for a Parameterized Circulating Vector Field Guidance for Fixed Wing  
Unmanned Aerial Vehicles

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**ABSTRACT**

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ABSTRACT

*DED*

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## LIST OF SYMBOLS

$a$  Previous or Initial Axial Induction Factor (-)

## **LIST OF ACRONYMS**

AoA    Angle of Attack

# 1 INTRODUCTION

## 1.1 Motivation and Problem Statement

Fixed wing Unmanned Aerial Vehicles are used for long endurance missions such as surveillance that would fatigue pilots or put them in harms way [1]. Missions are typically built using waypoints navigation and loitering executed by path following [2]. Obstacles are not always known during path planning and once discovered, a new path must be generated. Planning obstacle free and flyable paths takes time and may be impossible to relay to a UAV if communication is not reliable. Guidance that follows mission paths while avoiding obstacles without the need for constant communication with a ground station may be beneficial. Gradient Vector Fields (GVF) produce heading guidance at any point in space by summing together convergence and circulation field components. Each component uses a static scalar weight. Obstacles have been represented as separate repulsive GVFs that are later summed to the path following GVF [Wilhelm, Wambold, Clem]. Static GVF weights do not consider the state of the UAV resulting in sub-optimal guidance. Modifying the GVF convergence and circulation weights to be functions of common UAV states may generate an optimal guidance. **The proposed research seeks to determine GVF weighting functions that construct optimal obstacle avoidance.**

## 1.2 Methods Overview

The proposed research will be conducted in three phases where singularities will be demonstrated, weighting functions will be investigated, and a developed GVF will be validated on a ground robot simulating a UAV. Phases I and II will be conducted in a simulation environment that combines mission paths and obstacles into a single GVF. Phase III will be conducted with a ground robot simulating a UAV guided by the modified GVF in real-time. Dubins fixed wing constraints will be imposed in simulations and experiments.

### 1.3 Phase I

**Recreate vector fields for circular and elliptical obstacles and demonstrate singularities.** A simulation environment will be built that generates GVFs consisting of mission paths and obstacles. Circular and elliptical obstacles will be investigated and the resulting singularities will be characterized. Static weights will be used and the performance of the guidance measured in distance traveled and time of flight.

### 1.4 Phase II

**Investigate GVF weighting functions that influence obstacle avoidance.** UAV closing rate, position, and range will be used to develop dynamic GVF weights for convergence and circulation. The modified GVF will be compared against a static and strictly repulsive GVF. Distance traveled and time of flight will be used to compare the modified GVF to the unmodified GVF.

### 1.5 Phase III

**Validate modified GVF model with ground robot experiments.** The modified GVF developed in Phase II will be implemented on a differential drive ground robot simulating a fixed wing UAV. Guidance to guide the robot to a path while avoiding static obstacles will be demonstrated.

## 1.6 Summary of Phases

Each phases consists of a **goal** that will be accomplished by executing *objectives*. Completion of all objectives and phases will result in the final deliverable.

### **Phase I:** Demonstrate Gradient Vector Field Singularities

1. *Build a GVF simulation environment*
2. *Derive GVF for circular and elliptical obstacles*
3. *Identify path and obstacles where singularities are produced*

### **Phase II:** Investigate GVF weighting functions that influence obstacle avoidance

1. *Formulate circulation and convergence weights as functions of UAV state*
2. *Determine combination of GVF weights that produces optimal guidance in simulation*

### **Phase III:** Validate modified GVF model with ground robot experiments

1. *Build differential drive robot*
2. *Build robotic framework to take guidance commands*
3. *Repeat simulations performed in Phase II on ground robot*

**Deliverable:** Modified GVF optimal guidance for path following and static obstacle avoidance.

## 2 LITERATURE REVIEW

### 2.1 Introduction to Literature Review

### 2.2 Fixed Wing Unmanned Aerial Vehicle

#### 2.2.1 Introduction to Fixed Wing UAV

Unmanned Aerial Vehicles (UAVs) operate without an on-board pilot making them ideal for high endurance and dangerous missions. Remotely piloted aircraft can trade-off pilots when they become fatigued allowing the aircraft to remain in service for longer periods of time. UAVs do not have cockpits or life support systems which free up space for additional equipment and reduces costs. The lack of an on-board pilot and low system costs also allows a UAV to be expendable. UAVs can be found in rotorcraft and fixed wing varieties. Fixed wing UAVs range widely in form factor and size, but typically fall under either hand-launched or large systems. Hand launched varieties can be carried on the back of a soldier and launched without the use of a runway and are typically battery powered. Large fixed wing UAVs are typically gas powered and require a runway to take-off and land.



(a)



(b)

Figure 2.1: Hand Launched Fixed Wing UAV and Global Hawk

Hand-launched UAVs are primarily tasked with surveilling the immediate area for soldiers on the ground. Cameras on-board relay video to the ground allowing soldiers to identify threats prior to engagement. Large UAVs are tasked with surveillance and can be used for armed reconnaissance [1]. Missions can be described in terms of a path that a UAV is required to fly on. The paths are typically constructed from simple primitives such as straight lines connecting waypoints and circular loiter paths. Obstacle free and flyable paths are generated at a ground station prior to flight and sent to the UAV. The UAVs autopilot uses the path as a reference and attempts to keep the UAV as close to the path as possible. The relationship between a ground station and a UAV is discussed in more detail in the following section.

### **2.2.2 Autopilot and Ground Station**

Autopilots are devices that control the position and attitude of a UAV by implementing guidance, navigation, and control systems. Accelerometers, gyroscopes, barometers, and compasses measure the state of a UAV and are passed to the navigation system. Measurements are often noisy and need to be fused together which is commonly done with a kalman filter [3]. The state estimates are used as feedback for both the guidance and control systems, depicted in Figure 2.2. Sensor uncertainty and wind disturbances cause the UAV to deviate from the reference path over time and needs to be corrected. The guidance system compares the estimated state of a UAV to the reference path and provides guidance commands in the form of a heading to the control system. State estimates are also fed into the control system as feedback along with guidance commands to produce pulse width modulation commands to actuators. The actuators produce a physical output that alters the state of the UAV which is again measured and estimated by the navigation system.

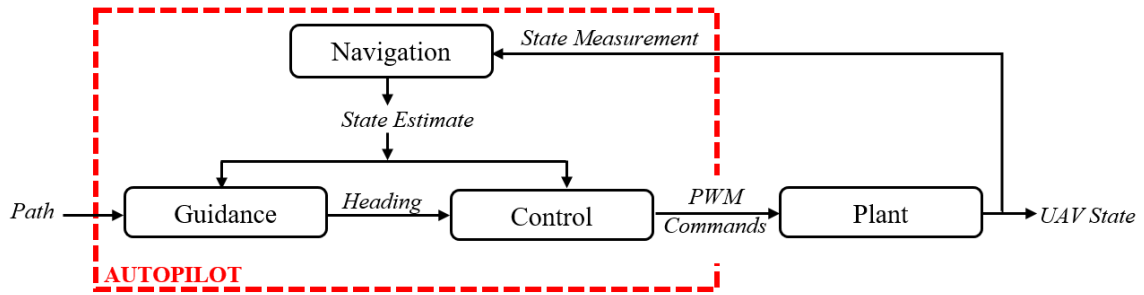


Figure 2.2: Autopilot Navigation Guidance and Control

A typical autopilot is shown in Figure 2.3 which is programmed with navigation, guidance, and control software. Accelerometers, gyroscopes, barometers and the compass are included inside the autopilot and makeup the inertial measurement unit (IMU). Additional sensors such as GPS and airspeed sensors can be connected as peripheral devices. Radios are connected to receive transmitter commands and communicate with a ground station.



Figure 2.3: Pixhawk Autopilot

Ground stations are computers that run mission management software that allow users to configure vehicles and program missions. Missions are planned at the ground station where high level mission objectives are assigned to points on a map such as waypoints and loitering maneuvers. Ground station software generates obstacle free and flyable paths that connect mission objectives and relay paths to the autopilot over radio link.



Information collected by the UAV can be relayed back to the ground station for analysis. Transmitters can be used to control the UAVs movements directly. Ground stations and autopilots work together to form an Unmanned Aerial System (UAS) depicted in Figure 2.4.



Figure 2.4: Unmanned Aerial System

Once paths have been generated, such as that shown in Figure 2.5, they are sent to the UAV via radio link. The guidance system is then responsible for guiding the UAV to get on and follow the path. Common methods for guiding algorithms for getting on and following a path include carrot chasing, non-linear guidance law (NLGL), pure pursuit line of sight (PLOS), linear quadratic regulator (LQR) and vector field [2]. Benchmarks for how each guidance algorithm performs is commonly quantified in control effort and tracking error with respect to the reference path. Sujit et al. compared the above guidance laws and discussed the benefits and disadvantages of the guidance laws, and in terms of control effort and tracking error LQR and vector field performed the best respectively. LQR was shown

to have optimal control effort but exhibited large cross track error when subjected to high wind speeds. Vector field produced guidance with the lowest tracking error but experienced oscillations once on the path.



Figure 2.5: Ground Station Software QGroundControl

Low tracking error in the presence of wind and has led to the algorithm being used for

- What is an autopilot and a ground station
- What are their purposes
- Why one cannot exist without the other (lack of autonomy?)
- FIGURE of how they are connected
- Ground station

- Program or set of programs that provide interface for a pilot or operator to communicate with the UAV
  - Vehicle configurations
  - Mission planning (map, waypoints, loitering, altitude)
  - Missions decomposed into obstacle free and flyable paths that will be sent to the UAV
  - FIGURE of waypoints and loitering being decomposed into flyable paths
  - Unlike conventional robotic systems, path planning is chosen over trajectory planning (getting uav to certain point at certain time when there are constant wind disturbances is difficult)
  - OR maybe trajectory planning is difficult because too many unknowns such as wind disturbances. . .
  - Provides a way to collect data
  - Communicates with UAV through a radio link
- Autopilot
    - Receives instructions from ground station and implements navigation, guidance, and control algorithms to accomplish missions (to the best of its ability)
    - Navigation
      - \* Navigation is the process of measuring sensors, estimating data, .. . .etc
      - \* Use current material
    - Guidance
      - \* Purpose of guidance system (reference path to a command consumable to the controller)

- \* Guidance uses current position and reference path to determine deviation from path
  - \* Deviation from the path is used to calculate a heading command that will put the UAV back on the path
  - \* Methods for path following (Read Sujuits paper again)
  - \* Summary of findings, vector field has lowest cross track error, parameter tuning, and chattering
  - \* Parameter tuning . . . (ask jay)
  - \* More detailed discussion on different vector fields presented in section . . .
- Control
- \* Converts sensor information and guidance commands into actuator output
  - \* Read chapter 6 beard and McLain, find more sources
  - \* FIGURE of control loop

### **2.2.3 Guidance Navigation and Control Overview**

## **2.3 Potential Field**

Potential field was first introduced as a real-time robotic manipulator algorithm for obstacle avoidance [4]. The potential field algorithm represents a robots workspace as a gradient potential of attractive and repulsive artificial forces that drive the robot to a desired goal. Goals are given the lowest potential and act as attractive forces. Obstacles have high potential and act as repulsive forces. A simple example is depicted in Figure 2.6 consisting of an initial state, a goal, and a single obstacle. The initial state of the robot is at the edge of a gradient where the potential is maximum. In the lowest part of the gradient a goal exists at the global minimum. Obstacles are added to the potential field, but have limited effect due to a decay function.

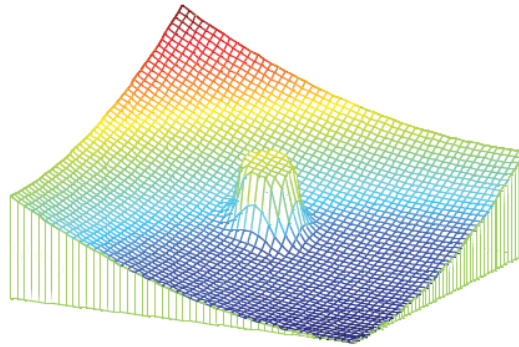


Figure 2.6: Single Obstacle Potential Field Gradient [5]

Potential field is unique in that path planning, trajectory planning, and control are lumped into a single system [6]. Transition from an initial state to a goal state traditionally occurred by executing three steps consisting of path planning, trajectory planning, and control. Path planning dealt with finding an obstacle free path from an initial state to a goal state. Trajectory planning time parametrized the obstacle free path with some high level vehicle constraints considered. Lastly, control attempts to reduce the tracking error with respect to the reference trajectory. Combining the three motion planning steps into a single algorithm has been shown to be computational inexpensive [7].

As pointed out in [8], robots using potential field are susceptible to local minimum. Encountering a local minimum prevents the robot from continuing down the gradient and into the global minimum because equilibrium has been reached prematurely. Figure 2.7 demonstrates local minimum by adding several obstacles into a goal field. Several methods have been developed to mitigate the effects of local minimums as pointed out in [7] through the use of navigation functions. Local minimum produced as a result of closely spaced obstacles as shown in Figure 2.7 have been addressed by grouping obstacles together into a cluster [5].

Several methods have been developed to mitigate the effects of local minimums as pointed out in [7] through the use of navigation functions. Local minimum produced

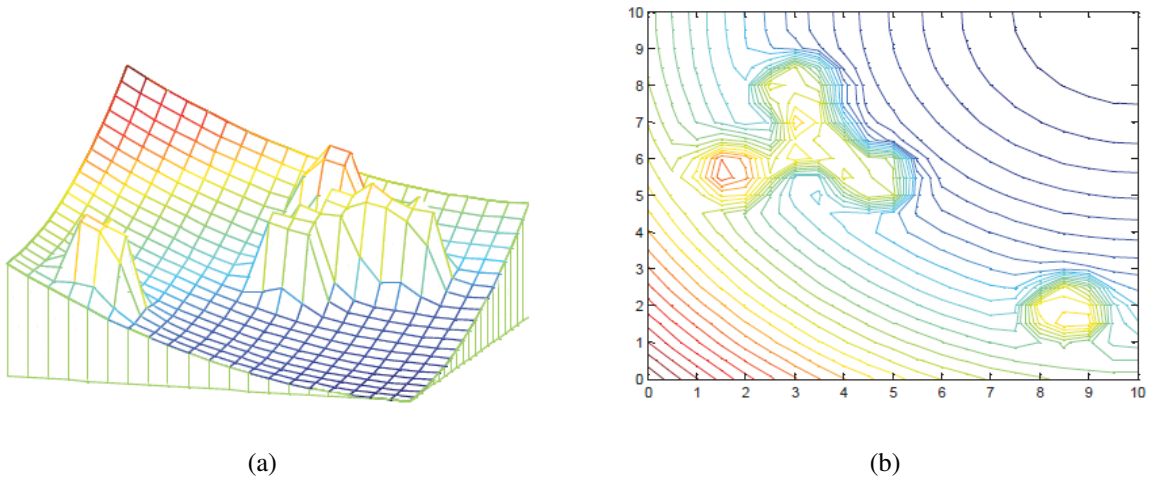


Figure 2.7: Potential Field Local Minimum [5]

as a result of closely spaced obstacles as shown in Figure 2.7 have been addressed by grouping obstacles together into a cluster [5]. Grouping obstacles addresses the risk of local minima before forming the potential field. If local minima are encountered after the field is generated, additional forces can be applied to push the robot away from the local minima.

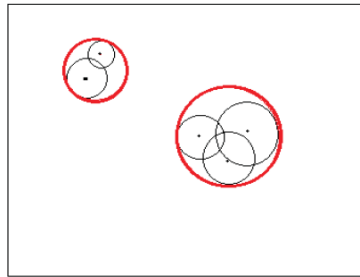


Figure 2.8: Obstacle Clustering [5]

Potential fields ability to avoid obstacles and combine path planning, trajectory planning, and control into a single system while being computationally inexpensive makes it an attractive option for many robotic systems. Fixed wing UAVs must maintain a

minimum forward velocity and cannot converge to a single point, making potential field difficult to implement.

## **2.4 Vector Field Guidance**

- Discussion on vector fields (what, uses, types....)
- Vector field description (Generation of vectors at any point in space)
- VF benefits (Guidance to established control system, continuous guidance, works well for disturbance rejection (wind))
- No need to modify existing autopilot controllers (let controllers reduce error, not track)
- Conclusion

### **2.4.1 Histogram Vector Field**

- Guidance method discretized space
- Obstacles detected and a confidence integer assigned to active cell
- Goal applied attractive force
- Obstacles applied repulsive force
- Similar to PF in that "artificial forces" are applied, however they are more guidance than actual states
- Problems with HVF (Discretization, fields point away from obstacles only, no parameters to guide around)
- Although no disturbances were modeled, for a UAV they could conceivably be added to the system

- Moving target not explored, only static case (conceivably could be extended to moving target)

#### **2.4.2 Lyapunov Vector Field**

- Unlike HVF, LVF has continuous guidance
- VF are constructed to follow path
- VF in literature have guided/followed paths that have been pre-defined
- Lyapunov arguments to show stability
- Path following with primitives, activate and deactivate fields, no summing together to prevent singularities
- Nelsons method of primitives extended to curved paths
- Tracking uncertain targets (uncertainty used for coordinate transformation to alter field)
- Tangent-plus-lyapunov used for path following and obstacle avoidance (Mixture of Dubins paths and VF)
- TPL relies on prior knowledge of obstacle for path planning (double check) essentially pp problem
- Genetic algorithm path planning (Jay)
- Obstacles discovered during flight need renewed path planning
- Cannot reach ground station or not enough time



### 2.4.3 Gradient Vector Field

- Gradient vector field
  - Intersection of surfaces, zero sets represent path
  - n-dimensions for any shapes (unlike some Lyapunov made of primitives)
  - Guaranteed vectors converge to path
  - Equations (convergence, circulation, tv)
  - Obstacles and paths are static, TV term is not considered
  - Examples of components FIGURES: (circulation,convergence,total)
  - Normalization of vectors gives each component equal influence on the total vector
  - After normalization a scalar weight influences how much influence each component has
  - Weights do not effect the guarantee of convergence (non zero and positive)
  - FIGURE: With normalization, without normalization (SIDE BY SIDE)
  - Dubins vehicle example of saturation
  - Static GVF weights do not consider state of the vehicle and provide sub-optimal guidance for obstacle avoidance
  - Dynamic GVF weights as a function of vehicle state may provide an optimal guidance for obstacle avoidance

## 2.5 Unmanned Aerial Vehicle Simulation

- Methods for testing UAVs
- SITL

- Actual flight tests
- Testing UAVs costly, setup, environment difficulties
- Simulation on ground robot (citations)
- Benefits, use as Dubins constraint vehicle to prove algorithm can run real time prior to flights
- Less expensive, saves resources, time, etc

## **2.6 Literature Review Summary**

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