Simplicial surfaces in GAP

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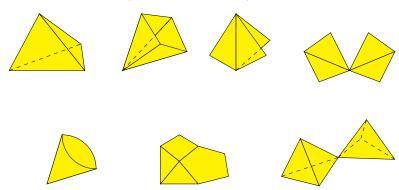
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2 Edge colouring and group properties

Edge colouring and group properties

Motivation

Goal: simplicial surfaces (and generalisations) in GAP



→ examples of polygonal complexes

No embedding

We do not work with embeddings (mostly)

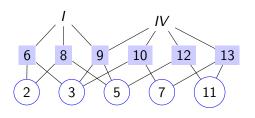
- is very hard to compute
- if often unknown for an abstractly constructed surface
- is different from intrinsic structure
- ⇒ lengths and angles are not important
- → incidence structure is intrinsic

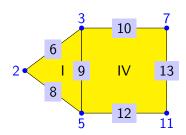
Incidence structure

- set of vertices V
- ullet set of edges ${\cal E}$

- 8 9 10 12 13

- ullet set of faces ${\cal F}$
- transitive relation $\subseteq (\mathcal{V} \times \mathcal{E}) \uplus (\mathcal{V} \times \mathcal{F}) \uplus (\mathcal{E} \times \mathcal{F})$

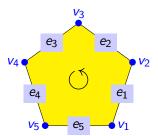




Polygonal complexes

A **polygonal complex** is a two–dimensional incidence structure of vertices, edges and faces, such that:

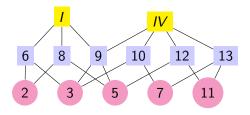
- Every edge has exactly two vertices. 2 6
- Every face is a polygon.



- Every vertex lies in an edge
- Every edge lies in a face

Isomorphism testing

Incidence geometry allows "easy" isomorphism testing. Incidence structure can be interpreted as a coloured graph:



General properties

Some properties can be computed for all polygonal complexes:

- Connectivity
- Euler-Characteristic

Orientability is **not** one of them. Counterexample:



- ⇒ every edge lies in at most two faces (for well–definedness)
- → ramified polygonal surfaces

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