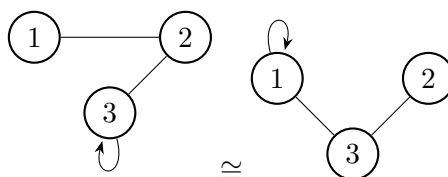


3.4

1. Which of the following describe equivalence relations? For those that are not equivalence relations, specify which of (R) , (S) , (T) fail and illustrate the failures with examples.
 - (a) $L_1 || L_2$ for straight lines in the plane if L_1 and L_2 are the same or are parallel.
.
 - (b) $L_1 \perp L_2$ for straight lines in the plane if L_1 and L_2 are perpendicular.
.
 - (c) $p_1 \sim p_2$ for Americans if p_1 and p_2 live in the same state.
.
 - (d) $p_1 \approx p_2$ for Americans if p_1 and p_2 live in the same state or in neighboring states.
.
 - (e) $p_1 \approx p_2$ for people if p_1 and p_2 have a parent in common.
.
 - (f) $p_1 \cong p_2$ for people if p_1 and p_2 have the same mother.
.
2. For each example of an equivalence relation in Exercise 1, describe the members of some equivalence class.
 - (a) DO WORK HERE
5. If G and H are both graphs with vertex set $\{1, 2, \dots, n\}$, we say that G is isomorphic to H , and write $G \cong H$, in case there is a way to label the vertices of G so that it becomes H .



- (a) Give a picture of another graph isomorphic to these two.
.
- (b) Find a graph with vertex set $\{1, 2, 3\}$ that is not isomorphic to the graphs yet has three edges and exactly one is a loop.
.

- (c) Find another example as in part(b) that isn't isomorphic to the answer of part(b) and the other two graphs.
.
- (d) Show that \cong is an equivalence relation on the set of all graphs with the vertex set $\{1, 2, \dots, n\}$.
.
- 8. (a) For $m, n \in \mathbb{Z}$, define $m \sim n$ in case $m - n$ is odd. Is the relation reflexive? symmetric? transitive? Is it an equivalence relation?
.
- (b) For a and b in \mathbb{R} , define $a \sim b$ in case $a - b \leq 1$. One could say that $a \sim b$ in case a and b are close enough or approximately equal. Answer the question in part (a).
.
- 17. (a) Verify that the relation \cong defined in Example 5b (the reachable Relation R on $V(G)$ by $(v, w) \in R$) is an equivalence relation on $V(G)$.
.
- (b) Given a vertex v in $V(G)$, describe in words the equivalence class containing v .
.

3.5

- 2. Find $nDIVm$ and $nMODm$ for the following values of n and m .
 - (a) $n = 20, m = 3$
.
 - (b) $n = 20, m = 4$
.
 - (c) $n = -20, m = 3$
.
 - (d) $n = -20, m = 4$
.
 - (e) $n = 371, 246, m = 265$
.
 - (f) $n = -371, 246, m = 265$
.
- 4. (a) List all equivalence classes of \mathbb{Z} for the equivalence relation congruence mod 4.
.

- (b) How many different equivalence classes of \mathbb{Z} are there with respect to congruence mod 73.

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