# Study Guide: Scientific software engineering for a simple ODE problem

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# 1 Creating user interfaces

- Never edit the program to change input!
- Set input data on the command line or in a graphical user interface
- How is explained next

## 1.1 Accessing command-line arguments

- All command-line arguments are available in sys.argv
- sys.argv[0] is the program
- sys.argv[1:] holds the command-line arguments
- Method 1: fixed sequence of parameters on the command line
- Method 2: -option value pairs on the command line (with default values)

```
Terminal> python myprog.py 1.5 2 0.5 0.8 0.4
Terminal> python myprog.py --I 1.5 --a 2 --dt 0.8 0.4
```

## 1.2 Reading a sequence of command-line arguments

The program decay\_plot\_mpl.py<sup>1</sup> needs this input:

- •
- a
- T
- an option to turn the plot on or off (makeplot)
- a list of  $\Delta t$  values

Give these on the command line in correct sequence

Terminal> python decay\_cml.py 1.5 2 0.5 0.8 0.4

#### 1.3 Implementation

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Note

- sys.argv[i] is always a string
- Must explicitly convert to (e.g.) float for computations
- List comprehensions make lists: [expression for e in somelist]

Complete program: decay\_cml.py2.

## 1.4 Working with an argument parser

Set option-value pairs on the command line if the default value is not suitable:

```
Terminal> python decay_argparse.py --I 1.5 --a 2 --dt 0.8 0.4
```

Code:

(metavar is the symbol used in help output)

## 1.5 Reading option-values pairs

 ${\tt argparse.ArgumentParser}\ {\tt parses}\ {\tt the}\ {\tt command-line}\ {\tt arguments};$ 

```
def read_command_line():
    parser = define_command_line_options()
    args = parser.parse_args()
    print 'I={}, a={}, T={}, makeplot={}, dt_values={}'.format(
        args.1, args.a, args.T, args.makeplot, args.dt_values)
    return args.I, args.a, args.T, args.makeplot, args.dt_values
```

Complete program: decay\_argparse.py<sup>3</sup>.

<sup>1</sup>http://tinyurl.com/jvzzcfn/decay/decay\_plot\_mpl.py

<sup>2</sup>http://tinyurl.com/jvzzcfn/decay/decay\_cml.py

<sup>3</sup>http://tinyurl.com/jvzzcfn/decay/decay\_argparse.py

## 1.6 A graphical user interface

# 

Normally very much programming required - and much competence on graphical user interfaces. Here: use a tool to automatically create it in a few minutes (!)

## 1.7 The Parampool package

- Parampool<sup>4</sup> is a package for handling a large pool of input parameters in simulation programs
- Parampool can automatically create a sophisticated web-based graphical user interface (GUI) to set parameters and view solutions

#### Remark.

The forthcoming material aims at those with particular interest in equipping their programs with a  ${
m GUI}$  - others can safely skip it.

## 1.8 Making a compute function

- Key concept: a *compute function* that takes all input data as arguments and returning HTML code for viewing the results (e.g., plots and numbers)
- What we have: decay\_plot\_mpl.py<sup>5</sup>
- main function carries out simulations and plotting for a series of  $\Delta t$  values

- Goal: steer and view these experiments from a web GUI
- What to do:
  - create a compute function
  - call parampool functionality

The compute function main\_GUI:

## 1.9 The hard part of the compute function: the HTML code

- The results are to be displayed in a web page
- Only you know what to display in your problem
- Therefore, you need to specify the HTML code

Suppose explore solves the problem, makes a plot, computes the error and returns appropriate HTML code with the plot. Embed error and plots in a table:

```
# Build HTML code for web page. Arrange plots in columns
    # corresponding to the theta values, with dt down the rows
    theta2name = {0: 'FE', 1: 'BE', 0.5: 'CN'}
   html text = '\n'
    for dt in dt_values:
       html_text += '\n'
       for theta in theta_values:
           E, html = explore(I, a, T, dt, theta, makeplot=True)
html_text += """
>
<center><b>%s, dt=%g, error: %s</b></center><br>
%s
""" % (theta2name[theta], dt, E, html)
       html text += '\n'
    html_text += '\n'
    return html_text
```

## 1.10 How to embed a PNG plot in HTML code

In explore:

```
import matplotlib.pyplot as plt
...
# plot
plt.plot(t, u, r-')
plt.xlabel('t')
plt.ylabel('u')
...
from parampool.utils import save_png_to_str
html_text = save_png_to_str(plt, plotwidth=400)
```

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If you know HTML, you can return more sophisticated layout etc.

<sup>4</sup>https://github.com/hplgit/parampool

<sup>5</sup>http://tinyurl.com/jvzzcfn/decay/decay\_plot\_mpl.py

## 1.11 Generating the user interface

Make a file decay\_GUI\_generate.py:

```
\label{from parampool} \mbox{\tt generator.flask import generate} \\ \mbox{\tt from decay\_GUI import main}
generate (main,
               output_controller='decay_GUI_controller.py',
               output_template='decay_GUI_view.py',
output_model='decay_GUI_model.py')
```

Running decay\_GUI\_generate.py results in

- 1. decay\_GUI\_model.py defines HTML widgets to be used to set input data in the web interface.
- 2. templates/decay\_GUI\_views.py defines the layout of the web page,
- 3. decay\_GUI\_controller.py runs the web application.

Good news: we only need to run decay\_GUI\_controller.py and there is no need to look into any of these files!

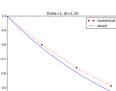
## 1.12 Running the web application

Start the GUI

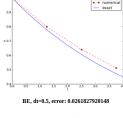
Terminal> python decay\_GUI\_controller.py

Open a web browser at 127.0.0.1:5000

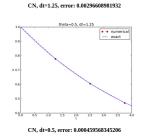




BE, dt=1.25, error: 0.062653947195









#### 1.13 More advanced use

- The compute function can have arguments of type float, int, string, list, dict, numpy array, filename (file upload)
- Alternative: specify a hierarchy of input parameters with name, default value, data type, widget type, unit (m, kg, s), validity check
- The generated web GUI can have user accounts with login and storage of results in a

## 2 Computing convergence rates

Frequent assumption on the relation between the numerical error E and some discretization parameter  $\Delta t$ :

$$E = C\Delta t^r, \tag{1}$$

- Unknown: C and r.
- Goal: estimate r (and C) from numerical experiments

## 2.1 Estimating the convergence rate r

Perform numerical experiments:  $(\Delta t_i, E_i)$ ,  $i = 0, \dots, m-1$ . Two methods for finding r (and C):

- 1. Take the logarithm of (1),  $\ln E = r \ln \Delta t + \ln C$ , and fit a straight line to the data points  $(\Delta t_i, E_i), i = 0, \dots, m-1.$
- 2. Consider two consecutive experiments,  $(\Delta t_i, E_i)$  and  $(\Delta t_{i-1}, E_{i-1})$ . Dividing the equation  $E_{i-1} = C\Delta t_{i-1}^r$  by  $E_i = C\Delta t_i^r$  and solving for r yields

$$r_{i-1} = \frac{\ln(E_{i-1}/E_i)}{\ln(\Delta t_{i-1}/\Delta t_i)} \tag{2}$$

for i = 1, = ..., m - 1.

Method 2 is best.

## 2.2 Implementation

Compute  $r_0, r_1, ..., r_{m-2}$ :

```
from math import log
def main():
    I, a, T, makeplot, dt_values = read_command_line()
    r = {} # estimated convergence rates
    for theta in 0, 0.5, 1:
        E values = []
        for dt in dt_values:
            E = explore(I, a, T, dt, theta, makeplot=False)
            E_values.append(E)
```

Complete program: decay\_convrate.py<sup>6</sup>.

#### 2.3 Execution

```
Terminal> python decay_convrate.py --dt 0.5 0.25 0.1 0.05 0.025 0.01 ...
Pairwise convergence rates for theta=0: 1.33 1.15 1.07 1.03 1.02

Pairwise convergence rates for theta=0.5: 2.14 2.07 2.03 2.01 2.01

Pairwise convergence rates for theta=1: 0.98 0.99 0.99 1.00 1.00
```

## Strong verification method.

Verify that r has the expected value!

## 2.4 Debugging via convergence rates

Potential bug: missing a in the denominator,

```
u[n+1] = (1 - (1-theta)*a*dt)/(1 + theta*dt)*u[n]
Running decay_convrate.py gives same rates.
```

Why? The value of a... (a = 1) 0 and 1 are bad values in tests! Better:

Pairwise convergence rates for theta=1: 0.21 0.12 0.06 0.03 0.01

Forward Euler works...because  $\theta = 0$  hides the bug. This bug gives  $r \approx 0$ :

```
u[n+1] = ((1-theta)*a*dt)/(1 + theta*dt*a)*u[n]
```

## 3 Software engineering

 $\label{eq:Goal:make more professional numerical software.}$  Topics:

- How to make modules (reusable libraries)
- Testing frameworks (doctest, nose, unittest)
- Implementation with classes

## 3.1 Making a module

- Previous programs: much repetitive code (esp. solver)
- DRY (Don't Repeat Yourself) principle: no copies of code
- A change needs to be done in one and only one place
- Module = just a file with functions (reused through import)

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- Let's make a module by putting these functions in a file:
  - solver
  - verify\_three\_steps
  - verify\_discrete\_solution
  - explore
  - define\_command\_line\_options
  - read\_command\_line
  - main (with convergence rates)
  - verify\_convergence\_rate

Module name: decay\_mod, filename: decay\_mod.py. Sketch:

<sup>6</sup>https://github.com/hplgit/INF5620/blob/gh-pages/src/decay/decay\_convrate.py

```
from numpy import *
from matplotlib.pyplot import *
import sys

def solver(I, a, T, dt, theta):
    ...

def verify_three_steps():
    ...

def verify_exact_discrete_solution():
    ...

def u_exact(t, I, a):
    ...

def explore(I, a, T, dt, theta=0.5, makeplot=True):
    ...

def define_command_line_options():
    ...

def read_command_line(use_argparse=True):
    ...

def main():
```

That is! It's a module decay\_mod in file decay\_mod.py.

Usage in some other program:

```
from decay_mod import solver
u, t = solver(I=1.0, a=3.0, T=3, dt=0.01, theta=0.5)
```

#### 3.2 Test block

At the end of a module it is common to include a test block:

```
if __name__ == '__main__':
    main()
```

- If decay\_mod is imported, \_\_name\_\_ is decay\_mod.
- If decay\_mod.py is run, \_\_name\_\_ is \_\_main\_\_.
- Use test block for testing, demo, user interface, ...

Extended test block:

```
if __name__ == '__main__':
    if 'verify' in sys.argv:
        if verify_three_steps() and verify_discrete_solution():
            pass # ok
        else:
            print 'Bug in the implementation!'
    elif 'verify_rates' in sys.argv:
        sys.argv.remove('verify_rates')
        if not '--dt' in sys.argv:
            print 'Must assign several dt values'
```

```
sys.exit(1) # abort
if verify_convergence_rate():
    pass
else:
    print 'Bug in the implementation!'
else:
    # Perform simulations
    main()
```

## 3.3 Prefixing imported functions by the module name

```
from matplotlib.pyplot import *

This imports a large number of names (sin, exp, linspace, plot, ...).

Confusion: is a function from numpy? Or matplotlib.pyplot?

Alternative (recommended) import:

import numpy
import matplotlib.pyplot
```

Now we need to prefix functions with module name:

```
t = numpy.linspace(0, T, Nt+1)
u_e = I*numpy.exp(-a*t)
matplotlib.pyplot.plot(t, u_e)
```

Common standard:

from numpy import \*

```
import numpy as np
import matplotlib.pyplot as plt

t = np.linspace(0, T, Nt+1)
u_e = I*np.exp(-a*t)
plt.plot(t, u_e)
```

## 3.4 Downside of module prefix notation

A math line like  $e^{-at}\sin(2\pi t)$  gets cluttered with module names,

```
numpy.exp(-a*t)*numpy.sin(2(numpy.pi*t)
# or
np.exp(-a*t)*np.sin(2*np.pi*t)
```

Solution (much used in this course): do two imports

```
import numpy as np
from numpy import exp, sin, pi
...
t = np.linspace(0, T, Nt+1)
u_e = exp(-a*t)*sin(2*pi*t)
```

#### 3.5 Doctests

Doc strings can be equipped with interactive Python sessions for demonstrating usage and automatic testing of functions.

```
def solver(I, a, T, dt, theta):
    """
    Solve u'=-a*u, u(0)=I, for t in (0,T] with steps of dt.

>>> u, t = solver(I=0.8, a=1.2, T=4, dt=0.5, theta=0.5)
>>> for t_n, u_n in zip(t, u):
    ...    print 't=*\.If, u=\%.14f' % (t_n, u_n)
    t=0.0, u=0.80000000000000

    t=0.5, u=0.43076923076923
    t=1.0, u=0.23195266272189
    t=1.5, u=0.12489758761948
    t=2.0, u=0.06725254717972
    t=2.5, u=0.03621291001985
    t=3.0, u=0.01949925924146
    t=3.5, u=0.01049960113002
    t=4.0, u=0.00565363137770
    """
    ...
```

## 3.6 Running doctests

Automatic check that the code reproduces the doctest output:

```
Terminal> python -m doctest decay_mod_doctest.py
```

Report in case of failure:

```
Terminal> python -m doctest decay_mod_doctest.py
***************
File "decay_mod_doctest.py", line 12, in decay_mod_doctest....
Failed example:
   for t_n, u_n in zip(t, u):
      print 't=%.1f, u=%.14f' % (t_n, u_n)
   t=0.0, u=0.80000000000000
   t=0.5, u=0.43076923076923
   t=1.0, u=0.23195266272189
   t=1.5, u=0.12489758761948
   t=2.0, u=0.06725254717972
   t=0.0, u=0.80000000000000
   t=0.5, u=0.43076923076923
   t=1.0, u=0.23195266272189
   t=1.5, u=0.12489758761948
   t=2.0, u=0.06725254718756
****************
1 items had failures:
  1 of 2 in decay_mod_doctest.solver
***Test Failed*** 1 failures.
```

#### Floats are difficult to compare.

Limit the number of digits in the output in doctests! Otherwise, round-off errors on a different machine may ruin the test.

Complete program: decay\_mod\_doctest.py7.

## 3.7 Unit testing with nose

- Nose is a very user-friendly testing framework
- Based on unit testing
- Identify (small) units of code and test each unit
- Nose automates running all tests
- Good habit: run all tests after (small) edits of a code
- Even better habit: write tests before the code (!)
- Remark: unit testing in scientific computing is not yet well established

#### 3.8 Basic use of nose

- 1. Implement tests in test functions with names starting with test\_.
- 2. Test functions cannot have arguments.
- Test functions perform assertions on computed results using assert functions from the nose.tools module.
- 4. Test functions can be in the source code files or be collected in separate files test\*.py.

## 3.9 Example on a nose test in the source code

Very simple module mymod (in file mymod.py):

```
def double(n):
    return 2*n
```

Write test function in mymod.py:

```
def double(n):
    return 2*n

import nose.tools as nt

def test_double():
    result = double(4)
    nt.assert_equal(result, 8)
```

Running

<sup>7</sup>http://tinyurl.com/jvzzcfn/decay/decay\_mod\_doctest.py

```
Terminal> nosetests -s mymod
```

makes the nose tool run all test\_\*() functions in mymod.py.

## 3.10 Example on a nose test in a separate file

Write the test in a separate file, say test\_mymod.py:

```
import nose.tools as nt
import mymod

def test_double():
    result = mymod.double(4)
    nt.assert_equal(result, 8)
```

Running

```
Terminal> nosetests -s
```

makes the nose tool run all test\_\*() functions in all files test\*.py in the current directory and in all subdirectories (recursevely) with names tests or \*\_tests.

## Tip.

Start with test functions in the source code file. When the file contains many tests, or when you have many source code files, move tests to separate files.

#### 3.11 The habit of writing nose tests

- Put test\_\*() functions in the module
- When you get many test\_\*() functions, collect them in tests/test\*.py

## 3.12 Purpose of a test function: raise AssertionError if failure

Alternative ways of raising AssertionError if result is not 8:

```
import nose.tools as nt

def test_double():
    result = ...

nt.assert_equal(result, 8)  # alternative 1

assert result == 8  # alternative 2

if result != 8:  # alternative 3
    raise AssertionError()
```

## 3.13 Advantages of nose

- Easier to use than other test frameworks
- Tests are written and collected in a compact and structured way
- Large collections of tests, scattered throughout a directory tree can be executed with one command (nosetests -s)
- Nose is a much-adopted standard

## 3.14 Demonstrating nose (ideas)

Aim: test function solver for u' = -au, u(0) = I.

We design three unit tests:

- 1. A comparison between the computed  $u^n$  values and the exact discrete solution
- 2. A comparison between the computed  $u^n$  values and precomputed verified reference values
- 3. A comparison between observed and expected convergence rates

These tests follow very closely the previous verify\* functions.

## 3.15 Demonstrating nose (code)

```
import nose.tools as nt
import decay_mod_unittest as decay_mod
import numpy as np
def exact_discrete_solution(n, I, a, theta, dt):
    """Return exact discrete solution of the theta scheme."""
    dt = float(dt) # avoid integer division
    factor = (1 - (1-theta)*a*dt)/(1 + theta*dt*a)
    return I*factor**n
def test_exact_discrete_solution():
    Compare result from solver against
    formula for the discrete solution
    theta = 0.8; a = 2; I = 0.1; dt = 0.8
    N = int(8/dt) # no of steps
    u, t = decay_mod.solver(I=I, a=a, T=N*dt, dt=dt, theta=theta)
    u_de = np.array([exact_discrete_solution(n, I, a, theta, dt)
                    for n in range(N+1)])
    diff = np.abs(u_de - u).max()
    nt.assert_almost_equal(diff, 0, delta=1E-14)
```

#### 3.16 Floats as test results require careful comparison

- Round-off errors make exact comparison of floats unreliable
- nt.assert\_almost\_equal: compare two floats to some digits or precision

```
def test_solver():
    Compare result from solver against
    precomputed arrays for theta=0, 0.5, 1.
    I=0.8; a=1.2; T=4; dt=0.5 # fixed parameters
   precomputed = {
        't': np.array([ 0. , 0.5, 1. , 1.5, 2. , 2.5, 3. , 3.5, 4. ]),
        0.5: np.array(
              0.8 , 0.43076923, 0.23195266, 0.12489759, 0.06725255, 0.03621291, 0.01949926, 0.0104996 ,
            8.0 ]
              0.00565363]),
        0: ...,
        1: ...
    for theta in 0, 0.5, 1:
        u, t = decay_mod.solver(I, a, T, dt, theta=theta)
        diff = np.abs(u - precomputed[theta]).max()
        # Precomputed numbers are known to 8 decimal places
        nt.assert_almost_equal(diff, 0, places=8,
                                msg='theta=%s' % theta)
```

## 3.17 Test of wrong use

- $\bullet$  Find input data that may cause trouble and test such cases
- Here: the formula for  $u^{n+1}$  may involve integer division

Example:

```
theta = 1; a = 1; I = 1; dt = 2
```

may lead to integer division:

```
(1 - (1-theta)*a*dt)  # becomes 1
(1 + theta*dt*a)  # becomes 2
(1 - (1-theta)*a*dt)/(1 + theta*dt*a)  # becomes 0 (!)
```

Test that solver does not suffer from such integer division:

#### 3.18 Test of convergence rates

Convergence rate tests are very common for differential equation solvers.

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Complete program: test\_decay\_nose.py8.

## 3.19 Classical unit testing with unittest

- unittest is a Python module mimicing the classical JUnit class-based unit testing framework from Java
- This is how unit testing is normally done
- Requires knowledge of object-oriented programming

#### Remark.

You will probably not use it, but you're not educated unless you know what unit testing with classes is.

#### 3.20 Basic use of unittest

Write file test\_mymod.py:

```
import unittest
import mymod

class TestMyCode(unittest.TestCase):
    def test_double(self):
        result = mymod.double(4)
        self.assertEqual(result, 8)

if __name__ == '__main__':
    unittest.main()
```

#### 3.21 Demonstration of unittest

<sup>8</sup>http://tinyurl.com/jvzzcfn/decay/tests/test\_decay\_nose.py

```
import unittest
import decay_mod_unittest as decay
import numpy as np
def exact_discrete_solution(n, I, a, theta, dt):
   factor = (1 - (1-theta)*a*dt)/(1 + theta*dt*a)
    return I*factor**n
class TestDecay(unittest.TestCase):
    def test_exact_discrete_solution(self):
       diff = np.abs(u_de - u).max()
       self.assertAlmostEqual(diff, 0, delta=1E-14)
   def test_solver(self):
       for theta in 0, 0.5, 1:
            self.assertAlmostEqual(diff, 0, places=8,
                                  msg='theta=%s' % theta)
   def test_potential_integer_division():
       self.assertAlmostEqual(diff, 0, delta=1E-14)
   def test_convergence_rates(self):
       for theta in r:
            self.assertAlmostEqual(...)
if __name__ == '__main__':
   unittest.main()
```

Complete program: test\_decay\_unittest.py9.

## 4 Implementing simple problem and solver classes

- So far: programs are built of Python functions
- New focus: alternative implementations using classes
- Class-based implementations are very popular, especially in business/adm applications
- Class-based implementations scales better to large and complex scientific applications

## 4.1 What to learn

Tasks:

- Explain basic use of classes to build a differential equation solver
- Introduce concepts that make such programs easily scale to more complex applications
- Demonstrate the advantage of using classes

Ideas:

- Classes for Problem, Solver, and Visualizer
- Problem: all the physics information about the problem
- Solver: all the numerics information + numerical computations
- Visualizer: plot the solution and other quantities

## 4.2 The problem class

- Model problem: u' = -au, u(0) = I, for  $t \in (0, T]$ .
- Class Problem stores the physical parameters a, I, T
- May also offer other data, e.g.,  $u_e(t) = Ie^{-at}$

Implementation:

```
from numpy import exp

class Problem:
    def __init__(self, I=1, a=1, T=10):
        self.T, self.I, self.a = I, float(a), T

def u_exact(self, t):
    I, a = self.I, self.a  # extract local variables
    return I*exp(-a*t)
```

Basic usage:

```
problem = Problem(T=5)
problem.T = 8
problem.dt = 1.5
```

## 4.3 Improved problem class

More flexible input from the command line:

<sup>9</sup>http://tinyurl.com/jvzzcfn/decay/tests/test\_decay\_nose.py

```
'--T', '--stop_time', type=float, default=self.T,
help='end time of simulation', metavar='T')
return parser

def init_from_command_line(self, args):
    self.I, self.a, self.T = args.I, args.a, args.T

def exact_solution(self, t):
    I, a = self.I, self.a
    return I*exp(-a*t)
```

- Can utilize user's ArgumentParser, or make one
- None is used to indicate a non-initialized variable

#### 4.4 The solver class

- Store numerical data  $\Delta t$ ,  $\theta$
- Compute solution and quantities derived from the solution

Implementation:

```
class Solver:
   def __init__(self, problem, dt=0.1, theta=0.5):
       self.problem = problem
        self.dt, self.theta = float(dt), theta
   def define_command_line_options(self, parser):
       parser.add_argument(
'--dt', '--time_step_value', type=float,
            default=0.5, help='time step value', metavar='dt')
       parser.add_argument(
            '--theta', type=float, default=0.5,
            help='time discretization parameter', metavar='dt')
       return parser
   def init_from_command_line(self, args):
       self.dt, self.theta = args.dt, args.theta
   def solve(self):
       from decay_mod import solver
       self.u, self.t = solver(
            self.problem.I, self.problem.a, self.problem.T,
            self.dt, self.theta)
```

Note: reuse of the numerical algorithm from the decay\_mod module (i.e., the class is a wrapper of the procedural implementation).

#### 4.5 The visualizer class

```
class Visualizer:
    def __init__(self, problem, solver):
        self.problem, self.solver = problem, solver

def plot(self, include_exact=True, plt=None):
```

```
Add solver.u curve to the plotting object plt,
and include the exact solution if include_exact is True.
This plot function can be called several times (if
the solver object has computed new solutions).
if plt is None:
    import scitools.std as plt # can use matplotlib as well
plt.plot(self.solver.t, self.solver.u, '--o')
plt.hold('on')
theta2name = {0: 'FE', 1: 'BE', 0.5: 'CN'}
name = theta2name.get(self.solver.theta, '')
legends = ['numerical %s' % name]
if include exact:
   t_e = linspace(0, self.problem.T, 1001)
    u_e = self.problem.exact_solution(t_e)
    plt.plot(t_e, u_e, 'b-')
    legends.append('exact')
plt.legend(legends)
plt.xlabel('t')
plt.ylabel('u')
plt.title('theta=%g, dt=%g' %
          (self.solver.theta, self.solver.dt))
plt.savefig('%s_%g.png' % (name, self.solver.dt))
return plt
```

Remark: The plt object in plot adds a new curve to a plot, which enables comparing different solutions from different runs of Solver.solve

## 4.6 Combing the classes

Let Problem, Solver, and Visualizer play together:

```
def main():
    problem = Problem()
    solver = Solver(problem)
    viz = Visualizer(problem, solver)
    # Read input from the command line
    parser = problem.define_command_line_options()
    parser = solver. define_command_line_options(parser)
    args = parser.parse_args()
    problem.init_from_command_line(args)
    solver. init_from_command_line(args)
    # Solve and plot
    solver.solve()
    import matplotlib.pyplot as plt
    #import scitools.std as plt
    plt = viz.plot(plt=plt)
     E = solver.error()
    if E is not None:
   print 'Error: %.4E' % E plt.show()
```

Complete program: decay\_class.py<sup>10</sup>.

<sup>10</sup>http://tinyurl.com/jvzzcfn/decay/decay\_class.py

## 5 Implementing more advanced problem and solver classes

- The previous Problem and Solver classes soon contain much repetitive code when the number of parameters increases
- Much of such code can be parameterized and be made more compact
- Idea: collect all parameters in a dictionary self.prms, with two associated dictionaries self.types and self.help for holding associated object types and help strings
- Collect common code in class Parameters
- Let Problem, Solver, and maybe Visualizer be subclasses of class Parameters, basically defining self.prms, self.types, self.help

## 5.1 A generic class for parameters

```
class Parameters:
   def set(self, **parameters):
       for name in parameters:
           self.prms[name] = parameters[name]
   def get(self, name):
       return self.prms[name]
   def define_command_line_options(self, parser=None):
       if parser is None:
           import argparse
           parser = argparse.ArgumentParser()
       for name in self.prms:
           tp = self.types[name] if name in self.types else str
           help = self.help[name] if name in self.help else None
           parser.add_argument(
                '--' + name, default=self.get(name), metavar=name,
               type=tp, help=help)
       return parser
   def init_from_command_line(self, args):
       for name in self.prms:
           self.prms[name] = getattr(args, name)
```

Slightly more advanced version in class\_decay\_verf1.py<sup>11</sup>.

## 5.2 The problem class

```
class Problem(Parameters):
    """
Physical parameters for the problem u'=-a*u, u(0)=I,
    with t in [0,T].
    """

def __init__(self):
    self.prms = dict(I=1, a=1, T=10)
    self.types = dict(I=float, a=float, T=float)
```

## 5.3 The solver class

```
class Solver(Parameters):
   def __init__(self, problem):
       self.problem = problem
       self.prms = dict(dt=0.5, theta=0.5)
       self.types = dict(dt=float, theta=float)
        self.help = dict(dt='time step value',
                        theta='time discretization parameter')
   def solve(self):
        from decay_mod import solver
        self.u, self.t = solver(
           self.problem.get('I'),
            self.problem.get('a'),
           self.problem.get('T'),
            self.get('dt'),
           self.get('theta'))
   def error(self):
        try:
           u_e = self.problem.exact_solution(self.t)
            e = u_e - self.u
           E = np.sqrt(self.get('dt')*np.sum(e**2))
       except AttributeError:
           E = None
       return E
```

#### 5.4 The visualizer class

- No parameters needed (for this simple problem), no need to inherit class Parameters
- Same code as previously shown class Visualizer
- Same code as previously shown for combining Problem, Solver, and Visualizer

## 6 Performing scientific experiments

Goal: explore the behavior of a numerical method for a differential equation and show how scientific experiments can be set up and reported.

Tasks:

- Write scripts to automate experiments
- Generate scientific reports from scripts

Tools to learn:

<sup>11</sup>http://tinyurl.com/jvzzcfn/decay/class\_decay\_verf1.py

- os.system for running other programs
- subprocess for running other programs and extracting the output
- List comprehensions
- Formats for scientific reports: HTML w/MathJax, IATEX, Sphinx, DocOnce

## 6.1 Model problem and numerical solution method

Problem:

$$u'(t) = -au(t), \quad u(0) = I, \ 0 < t \le T,$$
 (3)

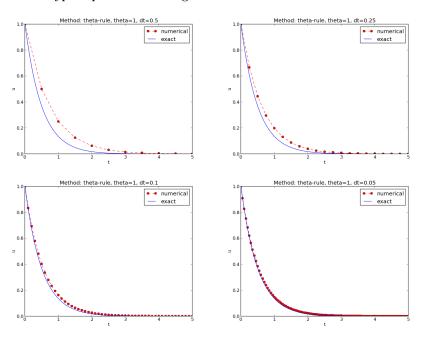
Solution method ( $\theta$ -rule):

$$u^{n+1} = \frac{1 - (1 - \theta)a\Delta t}{1 + \theta a\Delta t}u^n, \quad u^0 = I.$$

## 6.2 Plan for the experiments

- Plot  $u^n$  against  $u_e = Ie^{-at}$  for various choices of the parameters  $I, a, \Delta t$ , and  $\theta$
- How does the discrete solution compare with the exact solution when  $\Delta t$  is varied and  $\theta = 0.0.5, 1$ ?
- Use the decay\_mod.py<sup>12</sup> module (little modification of the plotting, see experiments/decay\_mod.py<sup>13</sup>)
- Make separate program for running (automating) the experiments (script)
  - 1. python decay\_mod.py --I 1 --a 2 --makeplot --T 5 --dt 0.5 0.25 0.1 0.05
  - Combine generated figures FE\_\*.png, BE\_\*.png, and CN\_\*.png to new figures with multiple plots
  - 3. Run script as python decay\_exper0.py 0.5 0.25 0.1 0.05 ( $\Delta t$  values on the command line)

## 6.3 Typical plot summarizing the results



## 6.4 Script code

Typical *script* (small administering program) for running the experiments:

<sup>12</sup>http://tinyurl.com/jvzzcfn/decay/decay\_mod.py

<sup>&</sup>lt;sup>13</sup>http://tinyurl.com/jvzzcfn/decay/experiments/decay\_mod.py

```
if failure:
        print 'Command failed:', cmd; sys.exit(1)
    # Combine images into rows with 2 plots in each row
    image_commands = []
   lmage_commands = []
for method in 'BE', 'CN', 'FE':
    pdf_files = ' '.join(['%s_%g.pdf' % (method, dt)
                                for dt in dt_values])
        png_files = ' '.join(['%s_%g.png' % (method, dt)
                                for dt in dt values])
        image_commands.append(
             'montage -background white -geometry 100%' +
             '-tile 2x %s %s.png' % (png_files, method))
        image commands.append(
             convert -trim %s.png %s.png' % (method, method))
        image_commands.append(
             'convert %s.png -transparent white %s.png' %
             (method, method))
        image_commands.append(
             'pdftk %s output tmp.pdf' % pdf_files)
        num_rows = int(round(len(dt_values)/2.0))
        image_commands.append(
             'pdfnup --nup 2x%d tmp.pdf' % num_rows)
         image_commands.append(
             'pdfcrop tmp-nup.pdf %s.pdf' % method)
   for cmd in image_commands:
        print cmd
        failure = os.system(cmd)
        if failure:
            print 'Command failed:', cmd; sys.exit(1)
    # Remove the files generated above and by decay_mod.py
    from glob import glob
   filenames = glob('*_*.png') + glob('*_*.pdf') + \
glob('*_*.eps') + glob('tmp*.pdf')
    for filename in filenames:
        os.remove(filename)
if __name__ == '__main__':
   run_experiments()
```

Complete program: experiments/decay\_exper0.py14.

#### 6.5 Comments to the code

Many useful constructs in the previous script:

- [float(arg) for arg in sys.argv[1:]] builds a list of real numbers from all the command-line arguments
- failure = os.system(cmd) runs an operating system command (e.g., another program)
- sys.exit(1) aborts the program
- ['%s\_%s.png' % (method, dt) for dt in dt\_values] builds a list of filenames from a list of numbers (dt\_values)
- All montage commands for creating composite figures are stored in a list and thereafter executed in a loop

- glob.glob('\*\_\*.png') returns a list of the names of all files in the current folder where
  the filename matches the *Unix wildcard notation* \*\_\*.png (meaning "any text, underscore,
  any text, and then '.png'")
- os.remove(filename) removes the file with name filename

#### 6.6 Interpreting output from other programs

In decay\_exper0.py we run a program (os.system) and want to grab the output, e.g.,

#### Tasks:

- read the output from the decay\_mod.py program
- interpret this output and store the E values in arrays for each  $\theta$  value
- plot E versus  $\Delta t$ , for each  $\theta$ , in a log-log plot

## 6.7 Code for grabbing output from another program

Use the subprocess module to grab output:

```
from subprocess import Popen, PIPE, STDOUT
p = Popen(cmd, shell=True, stdout=PIPE, stderr=STDOUT)
output, dummy = p.communicate()
failure = p.returncode
if failure:
    print 'Command failed:', cmd; sys.exit(1)
```

## 6.8 Code for interpreting the grabbed output

- Run through the output string, line by line
- If the current line prints  $\theta$ ,  $\Delta t$ , and E, split the line into these three pieces and store the data
- Store data in a dictionary errors with keys dt and the three  $\theta$  values

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<sup>14</sup>http://tinyurl.com/jvzzcfn/decay/experiments/decay\_exper0.py

```
errors = {'dt': dt_values, 1: [], 0: [], 0.5: []}
for line in output.splitlines():
     words = line.split()
     if words[0] in ('0.0', '0.5', '1.0'): # line with E?
# typical line: 0.0 1.25: 7.463E+00
          theta = float(words[0])
          E = float(words[2])
          errors[theta].append(E)
```

Next: plot E versus  $\Delta t$  for  $\theta = 0, 0.5, 1$ 

Complete program: experiments/decay\_exper1.py<sup>15</sup>. Fine recipe for

- how to run other programs
- how to extract and interpret output from other programs
- how to automate many manual steps in creating simulations and figures

## 6.9 Making a report

- Scientific investigations are best documented in a report!
- $\bullet\,$  A sample report  $^{16}$
- How can we write such a report?
- First problem: what format should I write in?
- Plain HTML<sup>17</sup>, generated by decay\_exper1\_html.py<sup>18</sup>
- HTML with MathJax<sup>19</sup>, generated by decay\_exper1\_mathjax.py<sup>20</sup>
- LaTeX PDF<sup>21</sup>, based on LaTeX source<sup>22</sup>
- Sphinx HTML<sup>23</sup>, based on reStructuredText<sup>24</sup>
- Markdown, MediaWiki, ...
- DocOnce<sup>25</sup> can generate L<sup>A</sup>T<sub>E</sub>X, HTML w/MathJax, Sphinx, Markdown, MediaWiki, ... (DocOnce source<sup>26</sup> for the examples above, and Python program for generating the DocOnce source<sup>27</sup>)
- Examples on different report formats<sup>28</sup>

15http://tinyurl.com/jvzzcfn/decay/experiments/decay\_exper1.py

## 6.10 Publishing a complete project

- Make folder (directory) tree
- Keep track of all files via a version control system (Mercurial, Git, ...)
- Publish as private or public repository
- Utilize Bitbucket, Googlecode, GitHub, or similar
- See the intro to such tools<sup>29</sup>

<sup>16</sup>http://hplgit.github.com/INF5620/doc/writing\_reports/sphinx-cloud/ 17http://hplgit.github.com/INF5620/doc/writing\_reports/report\_html.html 18http://tinyurl.com/jvzzcfn/decay/experiments/decay\_exper1\_html.py 19http://hplgit.github.com/INF5620/doc/writing\_reports/report\_html\_mathjax.html 20http://tinyurl.com/jvzzcfn/decay/experiments/decay\_exper1\_html.py

<sup>21</sup>http://hplgit.github.com/INF5620/doc/writing\_reports/report.pdf

<sup>22</sup>http://hplgit.github.com/INF5620/doc/writing\_reports/report.tex.html

<sup>23</sup>http://hplgit.github.com/INF5620/doc/writing\_reports/sphinx-cloud/index.html

<sup>24</sup>http://hplgit.github.com/INF5620/doc/writing\_reports/report\_sphinx.rst.html

<sup>25</sup>https://github.com/hplgit/doconce

<sup>&</sup>lt;sup>26</sup>http://hplgit.github.com/INF5620/doc/writing\_reports/report.do.txt.html

<sup>27</sup> http://tinyurl.com/jvzzcfn/decay/experiments/decay\_exper1\_do.py

<sup>28</sup>http://hplgit.github.com/INF5620/doc/writing\_reports/

<sup>29</sup>http://hplgit.github.com/teamods/bitgit/html/

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