# Study Guide: Scientific software engineering for a simple ODE problem

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# Creating user interfaces

- Never edit the program to change input!
- Set input data on the command line or in a graphical user interface
- How is explained next

# Accessing command-line arguments

- All command-line arguments are available in sys.argv
- sys.argv[0] is the program
- sys.argv[1:] holds the command-line arguments
- Method 1: fixed sequence of parameters on the command line
- Method 2: --option value pairs on the command line (with default values)

```
Terminal> python myprog.py 1.5\ 2\ 0.5\ 0.8\ 0.4 Terminal> python myprog.py --I\ 1.5\ --a\ 2\ --dt\ 0.8\ 0.4
```

# Reading a sequence of command-line arguments

The program decay\_plot\_mpl.py needs this input:

- 1
- a
- T
- an option to turn the plot on or off (makeplot)
- a list of  $\Delta t$  values

Give these on the command line in correct sequence Terminal> python decay\_cml.py 1.5 2 0.5 0.8 0.4

### **Implementation**

#### Note:

- sys.argv[i] is always a string
- Must explicitly convert to (e.g.) float for computations
- List comprehensions make lists:
   [expression for e in somelist]

Complete program: decay\_cml.py.

# Working with an argument parser

Set option-value pairs on the command line if the default value is not suitable:

Terminal> python decay\_argparse.py --I 1.5 --a 2 --dt 0.8 0.4 Code:

```
def define_command_line_options():
    import argparse
    parser = argparse.ArgumentParser()
    parser.add_argument('--I', '--initial_condition', type=float,
                        default=1.0, help='initial condition, u(0)'
                        metavar='I')
    parser.add_argument('--a', type=float,
                        default=1.0, help='coefficient in ODE',
                        metavar='a')
    parser.add_argument('--T', '--stop_time', type=float,
                        default=1.0, help='end time of simulation',
                        metavar='T')
    parser.add_argument('--makeplot', action='store_true',
                        help='display plot or not')
    parser.add_argument('--dt', '--time_step_values', type=float,
                        default=[1.0], help='time step values',
                        metavar='dt', nargs='+', dest='dt_values')
    return parser
```

(metavar is the symbol used in help output)

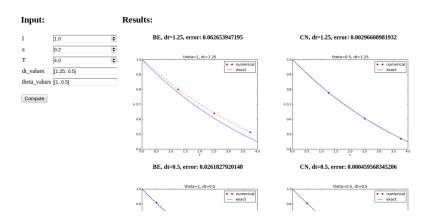
### Reading option-values pairs

argparse.ArgumentParser parses the command-line arguments:

```
def read_command_line():
    parser = define_command_line_options()
    args = parser.parse_args()
    print 'I={}, a={}, T={}, makeplot={}, dt_values={}'.format(
        args.I, args.a, args.T, args.makeplot, args.dt_values)
    return args.I, args.a, args.T, args.makeplot, args.dt_values
```

Complete program: decay\_argparse.py.

# A graphical user interface



Normally very much programming required - and much competence on graphical user interfaces.

Here: use a tool to automatically create it in a few minutes (!)

# The Parampool package

- Parampool is a package for handling a large pool of input parameters in simulation programs
- Parampool can automatically create a sophisticated web-based graphical user interface (GUI) to set parameters and view solutions

#### Remark.

The forthcoming material aims at those with particular interest in equipping their programs with a GUI - others can safely skip it.

# Making a compute function

- Key concept: a compute function that takes all input data as arguments and returning HTML code for viewing the results (e.g., plots and numbers)
- What we have: decay\_plot\_mpl.py
- main function carries out simulations and plotting for a series of Δt values
- Goal: steer and view these experiments from a web GUI
- What to do:
  - create a compute function
  - call parampool functionality

#### The compute function main\_GUI:

### The hard part of the compute function: the HTML code

- The results are to be displayed in a web page
- Only you know what to display in your problem
- Therefore, you need to specify the HTML code

Suppose explore solves the problem, makes a plot, computes the error and returns appropriate HTML code with the plot. Embed error and plots in a table:

```
def main_GUI(I=1.0, a=.2, T=4.0,
        dt_values=[1.25, 0.75, 0.5, 0.1],
        theta_values=[0, 0.5, 1]):
   # Build HTML code for web page. Arrange plots in columns
    # corresponding to the theta values, with dt down the rows
   theta2name = {0: 'FE', 1: 'BE', 0.5: 'CN'}
   html text = '\n'
   for dt in dt_values:
       html text += '\n'
       for theta in theta values:
           E, html = explore(I, a, T, dt, theta, makeplot=True)
           html_text += """
>
<center><b>%s, dt=%g, error: %s</b></center><br>
%s
% (theta2name[theta], dt, E, html)
       html_text += '\n'
```

# How to embed a PNG plot in HTML code

#### In explore:

```
import matplotlib.pyplot as plt
...
# plot
plt.plot(t, u, r-')
plt.xlabel('t')
plt.ylabel('u')
...
from parampool.utils import save_png_to_str
html_text = save_png_to_str(plt, plotwidth=400)
```

If you know HTML, you can return more sophisticated layout etc.

# Generating the user interface

#### Make a file decay\_GUI\_generate.py:

#### Running decay\_GUI\_generate.py results in

- decay\_GUI\_model.py defines HTML widgets to be used to set input data in the web interface,
- templates/decay\_GUI\_views.py defines the layout of the web page,
- decay\_GUI\_controller.py runs the web application.

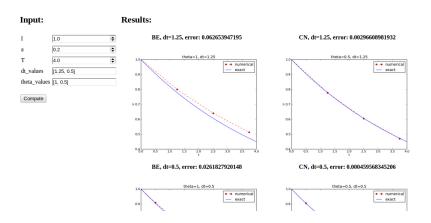
Good news: we only need to run decay\_GUI\_controller.py and there is no need to look into any of these files!

# Running the web application

#### Start the GUI

Terminal> python decay\_GUI\_controller.py

Open a web browser at 127.0.0.1:5000



### More advanced use

- The compute function can have arguments of type float, int, string, list, dict, numpy array, filename (file upload)
- Alternative: specify a hierarchy of input parameters with name, default value, data type, widget type, unit (m, kg, s), validity check
- The generated web GUI can have user accounts with login and storage of results in a database

# Computing convergence rates

Frequent assumption on the relation between the numerical error E and some discretization parameter  $\Delta t$ :

$$E = C\Delta t^r, \tag{1}$$

- Unknown: C and r.
- Goal: estimate r (and C) from numerical experiments

### Estimating the convergence rate r

Perform numerical experiments:  $(\Delta t_i, E_i)$ , i = 0, ..., m-1. Two methods for finding r (and C):

- Take the logarithm of (1),  $\ln E = r \ln \Delta t + \ln C$ , and fit a straight line to the data points  $(\Delta t_i, E_i)$ , i = 0, ..., m-1.
- ② Consider two consecutive experiments,  $(\Delta t_i, E_i)$  and  $(\Delta t_{i-1}, E_{i-1})$ . Dividing the equation  $E_{i-1} = C\Delta t_{i-1}^r$  by  $E_i = C\Delta t_i^r$  and solving for r yields

$$r_{i-1} = \frac{\ln(E_{i-1}/E_i)}{\ln(\Delta t_{i-1}/\Delta t_i)}$$
 (2)

for  $i = 1, = \dots, m - 1$ . Method 2 is best.

### **Implementation**

```
Compute r_0, r_1, ..., r_{m-2}:
    from math import log
    def main():
        I, a, T, makeplot, dt_values = read_command_line()
        r = {} # estimated convergence rates
        for theta in 0, 0.5, 1:
            E values = \Pi
            for dt in dt values:
                E = explore(I, a, T, dt, theta, makeplot=False)
                E_values.append(E)
            # Compute convergence rates
            m = len(dt_values)
            r[theta] = [log(E_values[i-1]/E_values[i])/
                        log(dt_values[i-1]/dt_values[i])
                         for i in range(1, m, 1)]
        for theta in r:
            print '\nPairwise convergence rates for theta=%g:' % theta
            print ' '.join(['%.2f' % r_ for r_ in r[theta]])
        return r
```

Complete program: decay\_convrate.py.

### Execution

```
Terminal> python decay_convrate.py --dt 0.5 0.25 0.1 0.05 0.025 0.01 ...

Pairwise convergence rates for theta=0:
1.33 1.15 1.07 1.03 1.02

Pairwise convergence rates for theta=0.5:
2.14 2.07 2.03 2.01 2.01

Pairwise convergence rates for theta=1:
0.98 0.99 0.99 1.00 1.00
```

#### Strong verification method.

Verify that r has the expected value!

### Debugging via convergence rates

```
Potential bug: missing a in the denominator,
    u[n+1] = (1 - (1-theta)*a*dt)/(1 + theta*dt)*u[n]
Running decay_convrate.py gives same rates.
Why? The value of a... (a = 1)
0 and 1 are bad values in tests!
Better:
Terminal> python decay_convrate.py --a 2.1 --I 0.1 \
          --dt 0.5 0.25 0.1 0.05 0.025 0.01
Pairwise convergence rates for theta=0:
1.49 1.18 1.07 1.04 1.02
Pairwise convergence rates for theta=0.5:
-1.42 -0.22 -0.07 -0.03 -0.01
Pairwise convergence rates for theta=1:
0.21 0.12 0.06 0.03 0.01
Forward Euler works...because \theta = 0 hides the bug.
This bug gives r \approx 0:
    u[n+1] = ((1-theta)*a*dt)/(1 + theta*dt*a)*u[n]
```

# Software engineering

Goal: make more professional numerical software. Topics:

- How to make modules (reusable libraries)
- Testing frameworks (doctest, nose, unittest)
- Implementation with classes

# Making a module

- Previous programs: much repetitive code (esp. solver)
- DRY (Don't Repeat Yourself) principle: no copies of code
- A change needs to be done in one and only one place
- Module = just a file with functions (reused through import)
- Let's make a module by putting these functions in a file:
  - solver
  - verify\_three\_steps
  - verify\_discrete\_solution
  - explore
  - define\_command\_line\_options
  - read\_command\_line
  - main (with convergence rates)
  - verify\_convergence\_rate

Module name: decay\_mod, filename: decay\_mod.py.

#### Sketch:

```
from numpy import *
from matplotlib.pyplot import *
import sys

def solver(I, a, T, dt, theta):
```

# Prefixing imported functions by the module name

```
from numpy import *
from matplotlib.pyplot import *
```

This imports a large number of names (sin, exp, linspace, plot, ...).

Confusion: is a function from numpy? Or matplotlib.pyplot? Alternative (recommended) import:

```
import numpy
import matplotlib.pyplot
```

Now we need to prefix functions with module name:

```
t = numpy.linspace(0, T, Nt+1)
u_e = I*numpy.exp(-a*t)
matplotlib.pyplot.plot(t, u_e)
```

#### Common standard:

```
import numpy as np
import matplotlib.pyplot as plt

t = np.linspace(0, T, Nt+1)
u_e = I*np.exp(-a*t)
plt.plot(t, u_e)
```

# Downside of module prefix notation

A math line like  $e^{-at}\sin(2\pi t)$  gets cluttered with module names,

```
numpy.exp(-a*t)*numpy.sin(2(numpy.pi*t)
# or
np.exp(-a*t)*np.sin(2*np.pi*t)
```

Solution (much used in this course): do two imports

```
import numpy as np
from numpy import exp, sin, pi
...
t = np.linspace(0, T, Nt+1)
u_e = exp(-a*t)*sin(2*pi*t)
```

#### **Doctests**

Doc strings can be equipped with interactive Python sessions for demonstrating usage and *automatic testing* of functions.

```
def solver(I, a, T, dt, theta):
    Solve u'=-a*u, u(0)=I, for t in (0,T] with steps of dt.
    >>> u, t = solver(I=0.8, a=1.2, T=4, dt=0.5, theta=0.5)
    >>> for t_n, u_n in zip(t, u):
           print 't=%.1f, u=\%.14f' % (t_n, u_n)
    t=0.5, u=0.43076923076923
    t=1.0, u=0.23195266272189
    t=1.5, u=0.12489758761948
    t=2.0, u=0.06725254717972
    t=2.5. u=0.03621291001985
    t=3.0, u=0.01949925924146
    t=3.5, u=0.01049960113002
    t=4.0, u=0.00565363137770
    . . .
```

### Running doctests

```
Automatic check that the code reproduces the doctest output:
    Terminal> python -m doctest decay_mod_doctest.py
Report in case of failure:
Terminal> python -m doctest decay_mod_doctest.py
File "decay_mod_doctest.py", line 12, in decay_mod_doctest....
Failed example:
    for t_n, u_n in zip(t, u):
        print 't=%.1f, u=%.14f' % (t_n, u_n)
Expected:
    t=0.0, u=0.80000000000000
    t=0.5, u=0.43076923076923
    t=1.0, u=0.23195266272189
    t=1.5, u=0.12489758761948
    t=2.0, u=0.06725254717972
Got:
    t=0.0, u=0.80000000000000
    t=0.5. u=0.43076923076923
    t=1.0, u=0.23195266272189
    t=1.5, u=0.12489758761948
    t=2.0, u=0.06725254718756
1 items had failures:
   1 of 2 in decay_mod_doctest.solver
***Test Failed*** 1 failures.
```

#### Floats are difficult to compare.

# Unit testing with nose

- Nose is a very user-friendly testing framework
- Based on unit testing
- Identify (small) units of code and test each unit
- Nose automates running all tests
- Good habit: run all tests after (small) edits of a code
- Even better habit: write tests *before* the code (!)
- Remark: unit testing in scientific computing is not yet well established

### Basic use of nose

- Implement tests in test functions with names starting with test\_.
- 2 Test functions cannot have arguments.
- Test functions perform assertions on computed results using assert functions from the nose.tools module.
- Test functions can be in the source code files or be collected in separate files test\*.py.

### Example on a nose test in the source code

```
Very simple module mymod (in file mymod.py):
    def double(n):
        return 2*n
Write test function in mymod.py:
    def double(n):
        return 2*n
    import nose.tools as nt
    def test_double():
        result = double(4)
        nt.assert_equal(result, 8)
Running
Terminal> nosetests -s mymod
makes the nose tool run all test_*() functions in mymod.py.
```

### Example on a nose test in a separate file

Write the test in a separate file, say test\_mymod.py:

```
import nose.tools as nt
import mymod

def test_double():
    result = mymod.double(4)
    nt.assert_equal(result, 8)
```

#### Running

```
Terminal> nosetests -s
```

makes the nose tool run all test\_\*() functions in all files test\*.py in the current directory and in all subdirectories (recursevely) with names tests or \*\_tests.

#### Tip.

Start with test functions in the source code file. When the file contains many tests, or when you have many source code files, move tests to separate files.

# The habit of writing nose tests

- Put test\_\*() functions in the module
- When you get many test\_\*() functions, collect them in tests/test\*.py

### Purpose of a test function: raise AssertionError if failure

Alternative ways of raising AssertionError if result is not 8:

```
import nose.tools as nt

def test_double():
    result = ...

    nt.assert_equal(result, 8)  # alternative 1
    assert result == 8  # alternative 2

if result != 8:  # alternative 3
    raise AssertionError()
```

# Advantages of nose

- Easier to use than other test frameworks
- Tests are written and collected in a compact and structured way
- Large collections of tests, scattered throughout a directory tree can be executed with one command (nosetests −s)
- Nose is a much-adopted standard

# Demonstrating nose (ideas)

Aim: test function solver for u' = -au, u(0) = I. We design three unit tests:

- lacktriangledown A comparison between the computed  $u^n$  values and the exact discrete solution
- ② A comparison between the computed  $u^n$  values and precomputed verified reference values
- A comparison between observed and expected convergence rates

These tests follow very closely the previous verify\* functions.

# Demonstrating nose (code)

```
import nose.tools as nt
import decay_mod_unittest as decay_mod
import numpy as np
def exact_discrete_solution(n, I, a, theta, dt):
    """Return exact discrete solution of the theta scheme."""
    dt = float(dt) # avoid integer division
    factor = (1 - (1-\text{theta})*a*dt)/(1 + \text{theta}*dt*a)
    return T*factor**n
def test_exact_discrete_solution():
    Compare result from solver against
    formula for the discrete solution.
    theta = 0.8; a = 2; I = 0.1; dt = 0.8
    N = int(8/dt) # no of steps
    u, t = decay_mod.solver(I=I, a=a, T=N*dt, dt=dt, theta=theta)
    u_de = np.array([exact_discrete_solution(n, I, a, theta, dt)
                     for n in range(N+1)])
    diff = np.abs(u_de - u).max()
    nt.assert_almost_equal(diff, 0, delta=1E-14)
```

# Floats as test results require careful comparison

- Round-off errors make exact comparison of floats unreliable
- nt.assert\_almost\_equal: compare two floats to some digits or precision

```
def test_solver():
    Compare result from solver against
    precomputed arrays for theta=0, 0.5, 1.
    I=0.8; a=1.2; T=4; dt=0.5 # fixed parameters
    precomputed = {
        't': np.array([ 0. , 0.5, 1. , 1.5, 2. , 2.5,
                        3., 3.5, 4.]),
        0.5: np.array(
            [ 0.8
                        , 0.43076923, 0.23195266, 0.12489759,
              0.06725255, 0.03621291, 0.01949926, 0.0104996,
              0.005653631).
        0: ...,
        1: ...
    for theta in 0, 0.5, 1:
        u, t = decay_mod.solver(I, a, T, dt, theta=theta)
        diff = np.abs(u - precomputed[theta]).max()
        # Precomputed numbers are known to 8 decimal places
        nt.assert_almost_equal(diff, 0, places=8,
                           max = 2 + h + a = \sqrt{a} \sqrt{a} \sqrt{a} \sqrt{a}
```

## Test of wrong use

- Find input data that may cause trouble and test such cases
- Here: the formula for  $u^{n+1}$  may involve integer division

#### Example:

```
may lead to integer division:

(1 - (1-theta)*a*dt)  # becomes 1
(1 + theta*dt*a)  # becomes 2
(1 - (1-theta)*a*dt)/(1 + theta*dt*a)  # becomes 0 (!)
```

theta = 1: a = 1: I = 1: dt = 2

Test that solver does not suffer from such integer division:

## Test of convergence rates

Convergence rate tests are very common for differential equation solvers.

```
def test_convergence_rates():
    """Compare empirical convergence rates to exact ones."""
    # Set command-line arguments directly in sys.argv
    import sys
    sys.argv[1:] = '--I 0.8 --a 2.1 --T 5 '\
                   '--dt 0.4 0.2 0.1 0.05 0.025'.split()
    r = decay_mod.main()
    for theta in r:
        nt.assert_true(r[theta]) # check for non-empty list
    expected_rates = {0: 1, 1: 1, 0.5: 2}
    for theta in r:
        r_final = r[theta][-1]
        # Compare to 1 decimal place
        nt.assert_almost_equal(expected_rates[theta], r_final,
                               places=1, msg='theta=%s' % theta)
```

Complete program: test\_decay\_nose.py.

# Classical unit testing with unittest

- unittest is a Python module mimicing the classical JUnit class-based unit testing framework from Java
- This is how unit testing is normally done
- Requires knowledge of object-oriented programming

#### Remark.

You will probably not use it, but you're not educated unless you know what unit testing with classes is.

## Basic use of unittest

```
Write file test_mymod.py:
    import unittest
    import mymod

class TestMyCode(unittest.TestCase):
        def test_double(self):
            result = mymod.double(4)
            self.assertEqual(result, 8)

if __name__ == '__main__':
    unittest.main()
```

### Demonstration of unittest

```
import unittest
import decay_mod_unittest as decay
import numpy as np
def exact_discrete_solution(n, I, a, theta, dt):
    factor = (1 - (1-\text{theta})*a*dt)/(1 + \text{theta}*dt*a)
    return T*factor**n
class TestDecay(unittest.TestCase):
    def test exact discrete solution(self):
        diff = np.abs(u_de - u).max()
        self.assertAlmostEqual(diff, 0, delta=1E-14)
    def test solver(self):
        for theta in 0, 0.5, 1:
            self.assertAlmostEqual(diff, 0, places=8,
                                    msg='theta=%s' % theta)
    def test_potential_integer_division():
        self.assertAlmostEqual(diff, 0, delta=1E-14)
    def test_convergence_rates(self):
```

# Implementing simple problem and solver classes

- So far: programs are built of Python functions
- New focus: alternative implementations using classes
- Class-based implementations are very popular, especially in business/adm applications
- Class-based implementations scales better to large and complex scientific applications

### What to learn

#### Tasks:

- Explain basic use of classes to build a differential equation solver
- Introduce concepts that make such programs easily scale to more complex applications
- Demonstrate the advantage of using classes

#### Ideas:

- Classes for Problem, Solver, and Visualizer
- Problem: all the physics information about the problem
- Solver: all the numerics information + numerical computations
- Visualizer: plot the solution and other quantities

## The problem class

- Model problem: u' = -au, u(0) = I, for  $t \in (0, T]$ .
- Class Problem stores the physical parameters a, I, T
- May also offer other data, e.g.,  $u_e(t) = Ie^{-at}$

#### Implementation:

```
from numpy import exp

class Problem:
    def __init__(self, I=1, a=1, T=10):
        self.T, self.I, self.a = I, float(a), T

    def u_exact(self, t):
        I, a = self.I, self.a  # extract local variables
        return I*exp(-a*t)
```

#### Basic usage:

```
problem = Problem(T=5)
problem.T = 8
problem.dt = 1.5
```

## Improved problem class

More flexible input from the command line: class Problem: def \_\_init\_\_(self, I=1, a=1, T=10): self.T, self.I, self.a = I, float(a), T def define\_command\_line\_options(self, parser=None): if parser is None: import argparse parser = argparse.ArgumentParser() parser.add\_argument( '--I', '--initial\_condition', type=float, default=self.I, help='initial condition, u(0)', metavar='I') parser.add\_argument( '--a', type=float, default=self.a, help='coefficient in ODE', metavar='a') parser.add\_argument( '--T', '--stop\_time', type=float, default=self.T, help='end time of simulation', metavar='T') return parser def init\_from\_command\_line(self, args): self.I, self.a, self.T = args.I, args.a, args.T def exact\_solution(self, t): I, a = self.I, self.a

------ Titi----- ( - it+)

#### The solver class

- Store numerical data  $\Delta t$ ,  $\theta$
- Compute solution and quantities derived from the solution

#### Implementation:

```
class Solver:
    def __init__(self, problem, dt=0.1, theta=0.5):
        self.problem = problem
        self.dt, self.theta = float(dt), theta
    def define_command_line_options(self, parser):
        parser.add_argument(
            '--dt', '--time_step_value', type=float,
            default=0.5, help='time step value', metavar='dt')
        parser.add_argument(
            '--theta', type=float, default=0.5,
            help='time discretization parameter', metavar='dt')
        return parser
    def init_from_command_line(self, args):
        self.dt, self.theta = args.dt, args.theta
    def solve(self):
        from decay_mod import solver
        self.u, self.t = solver(
            self.problem.I, self.problem.a, self.problem.T,
            self.dt, self.theta)
```

### The visualizer class

```
class Visualizer:
             def __init__(self, problem, solver):
                           self.problem, self.solver = problem, solver
             def plot(self, include_exact=True, plt=None):
                           Add solver.u curve to the plotting object plt,
                            and include the exact solution if include_exact is True.
                            This plot function can be called several times (if
                            the solver object has computed new solutions).
                           if plt is None:
                                         import scitools.std as plt # can use matplotlib as well
                           plt.plot(self.solver.t, self.solver.u, '--o')
                           plt.hold('on')
                           theta2name = {0: 'FE', 1: 'BE', 0.5: 'CN'}
                           name = theta2name.get(self.solver.theta, '')
                           legends = ['numerical %s' % name]
                           if include_exact:
                                         t_e = linspace(0, self.problem.T, 1001)
                                         u_e = self.problem.exact_solution(t_e)
                                         plt.plot(t_e, u_e, 'b-')
                                         legends.append('exact')
                           plt.legend(legends)
                           plt.xlabel('t')
                           plt.vlabel('u')
                           nl+ + i + l = (? + h + a = % d + = % d + a = % d + a = % d + a = % d + a = % d + a = % d + a = % d + a = % d + a = % d + a = % d + a = % d + a = % d + a = % d + a = % d + a = % d + a = % d + a = % d + a = % d + a = % d + a = % d + a = % d + a = % d + a = % d + a = % d + a = % d + a = % d + a = % d + a = % d + a = % d + a = % d + a = % d + a = % d + a = % d + a = % d + a = % d + a = % d + a = % d + a = % d + a = % d + a = % d + a = % d + a = % d + a = % d + a = % d + a = % d + a = % d + a = % d + a = % d + a = % d + a = % d + a = % d + a = % d + a = % d + a = % d + a = % d + a = % d + a = % d + a = % d + a = % d + a = % d + a = % d + a = % d + a = % d + a = % d + a = % d + a = % d + a = % d + a = % d + a = % d + a = % d + a = % d + a = % d + a = % d + a = % d + a = % d + a = % d + a = % d + a = % d + a = % d + a = % d + a = % d + a = % d + a = % d + a = % d + a = % d + a = % d + a = % d + a = % d + a = % d + a = % d + a = % d + a = % d + a = % d + a = % d + a = % d + a = % d + a = % d + a = % d + a = % d + a = % d + a = % d + a = % d + a = % d + a = % d + a = % d + a = % d + a = % d + a = % d + a = % d + a = % d + a = % d + a = % d + a = % d + a = % d + a = % d + a = % d + a = % d + a = % d + a = % d + a = % d + a = % d + a = % d + a = % d + a = % d + a = % d + a = % d + a = % d + a = % d + a = % d + a = % d + a = % d + a = % d + a = % d + a = % d + a = % d + a = % d + a = % d + a = % d + a = % d + a = % d + a = % d + a = % d + a = % d + a = % d + a = % d + a = % d + a = % d + a = % d + a = % d + a = % d + a = % d + a = % d + a = % d + a = % d + a = % d + a = % d + a = % d + a = % d + a = % d + a = % d + a = % d + a = % d + a = % d + a = % d + a = % d + a = % d + a = % d + a = % d + a = % d + a = % d + a = % d + a = % d + a = % d + a = % d + a = % d + a = % d + a = % d + a = % d + a = % d + a = % d + a = % d + a = % d + a = % d + a = % d + a = % d + a = % d + a = % d + a = % d + a = % d + a = % d + a = % d + a = % d + a = % d + a = % d + a = % d + a = % d + a = % d + a = % d + a = % d + a = % d + a = % d + a =
```

## Combing the classes

Let Problem, Solver, and Visualizer play together:

```
def main():
    problem = Problem()
    solver = Solver(problem)
    viz = Visualizer(problem, solver)
    # Read input from the command line
    parser = problem.define_command_line_options()
    parser = solver. define_command_line_options(parser)
    args = parser.parse_args()
    problem.init_from_command_line(args)
    solver. init_from_command_line(args)
    # Solve and plot
    solver.solve()
    import matplotlib.pyplot as plt
    #import scitools.std as plt
    plt = viz.plot(plt=plt)
    E = solver.error()
    if E is not None:
        print 'Error: %.4E' % E
    plt.show()
```

Complete program: decay\_class.py.

# Implementing more advanced problem and solver classes

- The previous Problem and Solver classes soon contain much repetitive code when the number of parameters increases
- Much of such code can be parameterized and be made more compact
- Idea: collect all parameters in a dictionary self.prms, with two associated dictionaries self.types and self.help for holding associated object types and help strings
- Collect common code in class Parameters
- Let Problem, Solver, and maybe Visualizer be subclasses of class Parameters, basically defining self.prms, self.types, self.help

# A generic class for parameters

```
class Parameters:
    def set(self, **parameters):
        for name in parameters:
            self.prms[name] = parameters[name]
    def get(self, name):
        return self.prms[name]
    def define_command_line_options(self, parser=None):
        if parser is None:
            import argparse
            parser = argparse.ArgumentParser()
        for name in self.prms:
            tp = self.types[name] if name in self.types else str
            help = self.help[name] if name in self.help else None
            parser.add_argument(
                '--' + name, default=self.get(name), metavar=name,
                type=tp, help=help)
        return parser
    def init_from_command_line(self, args):
        for name in self.prms:
            self.prms[name] = getattr(args, name)
```

Slightly more advanced version in class\_decay\_verf1.py.

## The problem class

```
class Problem(Parameters):
    11 11 11
    Physical parameters for the problem u'=-a*u, u(0)=I,
    with t in [0,T].
    .....
    def __init__(self):
        self.prms = dict(I=1, a=1, T=10)
        self.types = dict(I=float, a=float, T=float)
        self.help = dict(I='initial condition, u(0)',
                          a='coefficient in ODE',
                          T='end time of simulation')
    def exact_solution(self, t):
        I, a = self.get('I'), self.get('a')
        return I*np.exp(-a*t)
```

#### The solver class

```
class Solver(Parameters):
   def __init__(self, problem):
        self.problem = problem
        self.prms = dict(dt=0.5, theta=0.5)
        self.types = dict(dt=float, theta=float)
        self.help = dict(dt='time step value',
                         theta='time discretization parameter')
   def solve(self):
        from decay_mod import solver
        self.u, self.t = solver(
            self.problem.get('I'),
            self.problem.get('a'),
            self.problem.get('T'),
            self.get('dt'),
            self.get('theta'))
   def error(self):
        try:
            u_e = self.problem.exact_solution(self.t)
            e = u_e - self.u
            E = np.sqrt(self.get('dt')*np.sum(e**2))
        except AttributeError:
            E = None
        return E
```

### The visualizer class

- No parameters needed (for this simple problem), no need to inherit class Parameters
- Same code as previously shown class Visualizer
- Same code as previously shown for combining Problem,
   Solver, and Visualizer

# Performing scientific experiments

Goal: explore the behavior of a numerical method for a differential equation and show how scientific experiments can be set up and reported.

#### Tasks:

- Write scripts to automate experiments
- Generate scientific reports from scripts

#### Tools to learn:

- os.system for running other programs
- subprocess for running other programs and extracting the output
- List comprehensions
- Formats for scientific reports: HTML w/MathJax, LATEX, Sphinx, DocOnce

# Model problem and numerical solution method

Problem:

$$u'(t) = -au(t), \quad u(0) = I, \ 0 < t \le T,$$
 (3)

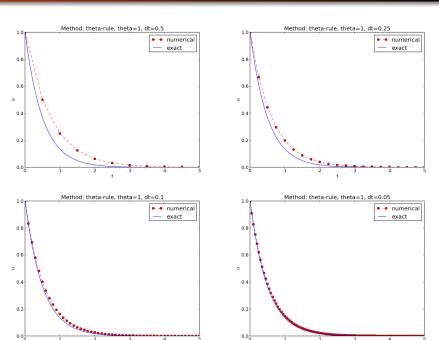
Solution method ( $\theta$ -rule):

$$u^{n+1} = \frac{1 - (1 - \theta)a\Delta t}{1 + \theta a\Delta t}u^n, \quad u^0 = I.$$

## Plan for the experiments

- Plot  $u^n$  against  $u_e = Ie^{-at}$  for various choices of the parameters I, a,  $\Delta t$ , and  $\theta$
- How does the discrete solution compare with the exact solution when  $\Delta t$  is varied and  $\theta = 0, 0.5, 1$ ?
- Use the decay\_mod.py module (little modification of the plotting, see experiments/decay\_mod.py)
- Make separate program for running (automating) the experiments (script)
  - python decay\_mod.py --I 1 --a 2 --makeplot --T 5 --dt 0.
  - Combine generated figures FE\_\*.png, BE\_\*.png, and CN\_\*.png to new figures with multiple plots
  - 3 Run script as python decay\_exper0.py 0.5 0.25 0.1 0.05 ( $\Delta t$  values on the command line)

# Typical plot summarizing the results



## Script code

Typical *script* (small administering program) for running the experiments:

```
import os, sys
def run_experiments(I=1, a=2, T=5):
    # The command line must contain dt values
    if len(sys.argv) > 1:
        dt_values = [float(arg) for arg in sys.argv[1:]]
    else:
        print 'Usage: %s dt1 dt2 dt3 ...' % sys.argv[0]
        sys.exit(1) # abort
    # Run module file as a stand-alone application
    cmd = 'python decay_mod.py --I %g --a %g --makeplot --T %g' % \
          (I, a, T)
    dt_values_str = ' '.join([str(v) for v in dt_values])
    cmd += ' --dt %s' % dt_values_str
    print cmd
    failure = os.system(cmd)
    if failure:
        print 'Command failed:', cmd; sys.exit(1)
    # Combine images into rows with 2 plots in each row
    image_commands = []
    for method in 'BE', 'CN', 'FE':
        pdf_files = ' '.join(['%s_%g.pdf' % (method, dt)
                              for dt in dt values])
```

### Comments to the code

#### Many useful constructs in the previous script:

- [float(arg) for arg in sys.argv[1:]] builds a list of real numbers from all the command-line arguments
- failure = os.system(cmd) runs an operating system command (e.g., another program)
- sys.exit(1) aborts the program
- ['%s\_%s.png' % (method, dt) for dt in dt\_values] builds a list of filenames from a list of numbers (dt\_values)
- All montage commands for creating composite figures are stored in a list and thereafter executed in a loop
- glob.glob('\*\_\*.png') returns a list of the names of all files in the current folder where the filename matches the *Unix* wildcard notation \*\_\*.png (meaning "any text, underscore, any text, and then '.png'")
- os.remove(filename) removes the file with name filename

# Interpreting output from other programs

In decay\_exper0.py we run a program (os.system) and want to grab the output, e.g.,

```
Terminal> python decay_plot_mpl.py
0.0     0.40:     2.105E-01
0.0     0.04:     1.449E-02
0.5     0.40:     3.362E-02
0.5     0.04:     1.887E-04
1.0     0.40:     1.030E-01
1.0     0.04:     1.382E-02
```

#### Tasks:

- read the output from the decay\_mod.py program
- $m{\bullet}$  interpret this output and store the E values in arrays for each  $m{\theta}$  value
- plot E versus  $\Delta t$ , for each  $\theta$ , in a log-log plot

## Code for grabbing output from another program

Use the subprocess module to grab output:

```
from subprocess import Popen, PIPE, STDOUT
p = Popen(cmd, shell=True, stdout=PIPE, stderr=STDOUT)
output, dummy = p.communicate()
failure = p.returncode
if failure:
    print 'Command failed:', cmd; sys.exit(1)
```

# Code for interpreting the grabbed output

- Run through the output string, line by line
- If the current line prints  $\theta$ ,  $\Delta t$ , and E, split the line into these three pieces and store the data
- $\bullet$  Store data in a dictionary errors with keys dt and the three  $\theta$  values

Next: plot E versus  $\Delta t$  for  $\theta=0,0.5,1$ Complete program: experiments/decay\_exper1.py. Fine recipe for

- how to run other programs
- how to extract and interpret output from other programs
- how to automate many manual steps in creating simulations and figures

# Making a report

- Scientific investigations are best documented in a report!
- A sample report
- How can we write such a report?
- First problem: what format should I write in?
- Plain HTML, generated by decay\_exper1\_html.py
- HTML with MathJax, generated by decay\_exper1\_mathjax.py
- LaTeX PDF, based on LaTeX source
- Sphinx HTML, based on reStructuredText
- Markdown, MediaWiki, ...
- DocOnce can generate LATEX, HTML w/MathJax, Sphinx, Markdown, MediaWiki, ... (DocOnce source for the examples above, and Python program for generating the DocOnce source)
- Examples on different report formats

# Publishing a complete project

- Make folder (directory) tree
- Keep track of all files via a version control system (Mercurial, Git, ...)
- Publish as private or public repository
- Utilize Bitbucket, Googlecode, GitHub, or similar
- See the intro to such tools