

\* this paper argues that there is a striking correspondence between the tasks on which human outperform current AI systems and the executive functions associated with the PFC

\* greater focus on the principles and inductive biases at work in the PFC may inspire novel architectures that can accomplish similar functions.

\* some functions of PFC: reasoning, representing abstract rules, control in novel environments, abstract planning.

# DEEP LEARNING NEEDS A PREFRONTAL CORTEX

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### ABSTRACT

Research seeking to build artificial systems capable of reproducing elements of human intelligence may benefit from a deeper consideration of the architecture and learning mechanisms of the human brain. In this brief review, we note a connection between many current challenges facing artificial intelligence and the functions of a particular brain area the prefrontal cortex (PFC). This brain area is known to be involved in executive functions such as reasoning, rule-learning, deliberate or controlled processing, and abstract planning. Motivated by the hypothesis that these functions provide a form of out-of-distribution robustness currently not available in state-of-the-art AI systems, we elaborate on this connection and highlight some computational principles thought to be at work in PFC, with the goal of enhancing the synergy between neuroscience and machine learning.



### INTRODUCTION

Deep learning, which has historically taken inspiration from the brain, has had unexpected and massive success in many applications. Though much progress has been made, new advances will be needed to meet the substantial challenges remaining on the path toward recreating the most powerful aspects of human intelligence. Stateof-the-art methods remain inferior to human learners in their ability to transfer knowledge to new domains (Lake et al., 2017), to capture compositional or systematic structure (Lake & Baroni, 2018), to plan efficiently (Hamrick, 2019), and to reason abstractly (Bhagavatula et al., 2019; Xu et al., 2020). All of these abilities share similarities with the collection of human capacities known as executive functions, and are often associated with conscious processing, i.e., they can be reported verbally by human subjects. The human brain must embody principles lacking in current deep learning systems that allow it to perform these powerful functions. This has led some to consider the possibility of taking inspiration from the architecture of the human brain to build more flexible learning systems (Marblestone et al., 2016; Hassabis et al., 2017). Here, we observe an intriguing correspondence between some of the current open questions in deep learning research and the functions of the human prefrontal cortex (PFC), a brain area known to be involved in executive functions such as planning (Duncan, 1986), abstract reasoning (Donoso et al., 2014), rule-learning (Wallis et al., 2001), and controlled or deliberate processing (Miller & Cohen, 2001). We explore this connection, and the potential of translating what is known about this brain area into architectural assumptions or inductive biases in deep learning (Marblestone et al., 2016; Battaglia et al., 2018). First, we elaborate on some of the current challenges in deep learning research mentioned above, and then briefly survey some findings from neuroscience about the PFC, noting connections to these current challenges. We then discuss some theoretical ideas about PFC function from cognitive and computational neuroscience, with the aim of stimulating a fruitful synergy between neurocience and deep learning research.

#### 2 THE NEED FOR NEURAL NETWORKS WITH EXECUTIVE FUNCTIONS

Current deep learning methods excel in perceptual tasks in which complicated patterns must be recognized in high-dimensional data. However, no one yet knows how to build learning machines which fare well on tasks that require deliberate, controlled processing over multiple steps or dealing with changes in distribution out-of-distribution. (Bengio, 2017; 2019; Lake et al., 2017; Marcus, 2018). In the following, we highlight some of the aspects of human cognition that have so far proven difficult for neural networks to reproduce, and have become active areas of research in deep learning.

**Reasoning** Bottou (2011) offers a helpful working definition of reasoning as "algebraically manipulating previously acquired knowledge in order to answer a new question." What this definition entails is the reuse of dynamically selected computational modules, with the results of recently produced computations feeding Abductive Commonsense Reasoning

lybrid computing using a NN with dynamic external memory.





I would add "catastrophic forgetting "as well which stands for that when the previous task.

the currently selected computation. Most of the tasks at the center of the rise of deep learning (e.g., object recognition, video-game playing, machine translation) generally do not require reasoning, i.e., algebraic manipulation of existing knowledge. Current neural nets involve composition of functions (e.g. layers) but in a fixed order. Recently, there has been growing interest and much progress on datasets and tasks that require reasoning over multiple steps (e.g. Bhagavatula et al., 2019; Johnson et al., 2017; Graves et al., 2016; Hudson & Manning, 2019; Weston et al., 2015; Xu et al., 2020; Barrett et al., 2018), with some cases of systems surpassing human performance (e.g. Hudson & Manning, 2018; Perez et al., 2018; Yi et al., 2018). However, as we discuss in the next section, most models trained on these tasks still fail to "answer new questions" in the sense of generalizing outside of the training distribution (Barrett et al., 2018; Bahdanau et al., 2019a).

Compositionality and systematicity It has been argued that one of the most powerful aspects of human cognition is its systematicity: concepts can be composed in novel ways, so that the number of expressible combinations grows exponentially in the number of primitive concepts learned (Fodor & Pylyshyn, 1988; Lake et al., 2017; Lake & Baroni, 2018). This topic is closely related to reasoning, because "algebraic manipulation" requires that existing knowledge be represented in a form that is systematically composable. Interest in compositionality among deep learning researchers has grown over the past few years, where experiments have revealed that standard approaches in deep learning show weak generalization for compositions of known elements which are unlikely under the training distribution (Lake & Baroni, 2018; Bahdanau et al., 2019b;a; Keysers et al., 2020, but see also Hill et al. 2020). These experiments show that standard architectures fail to capture the compositional structure or systematic rules governing the data-generation process.

Control in novel environments Just as standard deep networks have weaker generalization outside of their training distribution in the settings described above, they are less efficient than humans at transferring knowledge about learned environments to novel ones (Hagendorff & Wezel, 2019; Kansky et al., 2017; Lake et al., 2019b; 2017). For example, when trained on the Atari games, the generalization of standard methods in deep reinforcement learning is not robust to slight changes in the rules of the game or the layout of the inputs pre-trained model is fine-tuned (Kansky et al., 2017). Generalization to novel environments has continued to be an important topic in deep on new task, it tend to forget learning research, where an increased focus on one-shot learning (e.g. Vinyals et al., 2017), transfer (Weiss et al., 2016), and meta-learning (e.g. Finn et al., 2017; Bengio et al., 2019) has emerged. Much progress has been made in these areas, but human-level transfer remains elusive (Lansdell & Kording, 2019; Griffiths et al., 2019).

> Abstract planning It has long been recognized that the standard planning algorithms used in model-based reinforcement learning (RL) are too computationally expensive to be useful in many real-world domains (Barto & Mahadevan, 2003), and that humans and other animals seem to possess planning strategies that avoid much of this computational cost (Botvinick, 2008; Botvinick et al., 2009). In particular, it has been suggested that humans plan using temporally abstract representations, whereas model-based algorithms usually treat each time-step independently (Botvinick et al., 2009; Botvinick & Weinstein, 2014). The most successful algorithms in deep RL are model-free (Arulkumaran et al., 2017; Hamrick, 2019), and though model-based deep RL methods have had some recent success (Corneil et al., 2018; Finn & Levine, 2017; Nagabandi et al., 2018; Feinberg et al., 2018), most still plan each time step individually or lack the abstraction and compositionality displayed in human planning (Hamrick, 2019).

### SOME FUNCTIONS OF THE PREFRONTAL CORTEX

All of the challenges described above have been noted by others, and are active areas of research. The first of our main contributions is to draw connections between them and the functioning of the human PFC. The PFC comprises a large swath of the most anterior portion of the cerebral cortex and appears to have undergone a disproportionate amount of development over the course of human evolution (Schoenemann et al., 2005; Rilling, 2006; Semendeferi et al., 2001; Falk, 2012). It receives highly processed, multimodal information from perceptual areas, and sits at the top of the decision-making hierarchy (Fuster, 2009; Hunt & Hayden, 2017; O'Reilly et al., 2012). Much remains unknown about the PFC, and in particular there is ongoing investigation into functional differentiation between different areas within it (e.g. Hunt et al., 2018). However, it has been argued that much of the PFC retains a canonical computational role, with functional differentiation among subareas emerging due to differences in connectivity (Miller & Cohen, 2001; O'Reilly, 2010; Thompson-Schill, 2004). Here we highlight some aspects of the general functionality of the PFC.

Reasoning One of the most well-established findings about the PFC is that it is specialized for working memory, or the ability to maintain and manipulate information over short periods of time (Fuster & Alexander, 1971; Kubota & Niki, 1971; Miller & Desimone, 1994; Goldman-Rakic, 1995; Sommer & Wurtz, 2000; Lara & Wallis, 2015). Working memory can be seen as an important aspect of the capacity to reason, as it allows for 1) computation on information that is not currently observable in the environment, and 2) the integration of intermediate results in a larger reasoning process (e.g., in a serial summation of a list of numbers; Menon, 2016). Indeed, evidence of prefrontal engagement has been found in many experiments investigating the

· Towards AI-Complete QA · What Can NN Reason About? · Measuring abstract reasoning

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neural underpinnings of human reasoning (Donoso et al., 2014), including deductive (Goel, 2007), inductive (Crescentini et al., 2011), relational (Krawczyk et al., 2011), and analogical reasoning (Hampshire et al., 2011).

Representing abstract rules One domain in which humans excel at generalizing outside of the training distribution is the ability to apply known rules to novel elements (Lake et al., 2019a). The PFC has been found to be important for success on tasks that require the induction, maintenance, updating, or application of rules (Mian et al., 2014; Milner, 1963; Wallis et al., 2001; Shallice & Burgess, 1991). For example, patients with damage to PFC struggle to sort cards according to a changing rule (e.g., color or shape) (Milner, 1963; Buchsbaum et al., 2005; Berg, 1948). In a seminal electrophysiology study on rule application (Wallis et al., 2001), monkeys were trained to either select the picture that was a 'match' to the previously presented one, or select the 'nonmatch'. Single neurons in PFC were found to respond when invoking such abstract rules, regardless of the particular pictures presented on a given trial (Wallis et al., 2001). Some computational models (Rougier et al., 2005) have attempted to capture this important property of the PFC, showing, e.g., how indirection might be implemented in a canonical PFC circuit (Kriete et al., 2013, see also Hayworth & Marblestone 2018 and Müller et al. 2016).

Control in novel environments Overwhelming evidence implicates the PFC in decision-making and control processes (Domenech & Koechlin, 2015; Miller & Cohen, 2001). However, it is in general not crucial for the execution of habitual responses that have been trained extensively (as would be the case, e.g., in a model that had played an Atari game for hundreds of hours) — rather, it is required for *overriding* these habitual responses in novel situations, with new rules or in the pursuit of a novel goal (Miller & Cohen, 2001; Botvinick & Cohen, 2014). This function, generally termed "cognitive control," is illustrated well in studies using the classic Stroop task (Stroop, 1935). In this task, participants are presented with color words (e.g., 'red', 'blue') written in colored ink, which may or may not match the words. Patients with damage to PFC perform reliably poorly on this task, which requires them to override habitual responses (reading text) according to the color-naming rule (Perret, 1974; Vendrell et al., 1995). In general, it is thought that the functioning of the PFC is crucially important when a novel goal is being pursued in a familiar environment where habits have become entrenched, or in novel environments when no such habits yet exist (Miller & Cohen, 2001).

Abstract planning Humans and other mammals demonstrate evidence of both model-free and model-based RL (Momennejad et al., 2017; Daw et al., 2011; 2005), but the PFC has been implicated in model-based RL in particular (Daw et al., 2005; Smittenaar et al., 2013). Humans with damage to the PFC can exhibit deficits in routine behaviors that require planning and coordinating sequences of actions like cooking or making coffee (Miller & Cohen, 2001; Levine et al., 1998; Duncan, 1986; Shallice, 1982). Some have theorized that the planning processes in PFC are temporally abstract or hierarchical, as in, e.g., the options framework (Sutton et al., 1999; Botvinick, 2008; Botvinick et al., 2009; Botvinick & Weinstein, 2014; Frank & Badre, 2012). This idea accords well with experiments indicating that PFC represents actions at multiple timescales simultaneously (Hunt & Hayden, 2017; Botvinick et al., 2009; Sarafyazd & Jazayeri, 2019).

# 4 COMPUTATIONAL PRINCIPLES AND LEARNING MECHANISMS IN PFC

The section above describing some of the functions of the PFC was structured to draw out their connection to current challenges facing deep learning. However, the structure of this section is somewhat arbitrary, as all of these functions are related to one another. Here, we cover some theoretical ideas about the underlying computational mechanisms of PFC that can unify these various functions, with an eye toward principles that may be transferable to deep learning.

Top-down attention and modulation In an influential framework, Miller & Cohen (2001) argue that many of the cognitive capacities associated with the PFC, including reasoning, rule-learning, planning, and cognitive control, can be explained by its role in top-down attentional modulation of other brain areas. The PFC sends projections to much of neocortex, allowing it to modulate activity in other areas, possibly according to a current goal or in agreement with currently conscious contents. In the Stroop task, e.g., the PFC represents the instruction to name the colors rather than read the words, and modulates the activity of color features in higher-order visual areas of the brain to bias behavior toward naming them (Miller & Cohen, 2001).

Top-down attentional modulation has some analogues in deep learning research. The use of attention has become an increasingly popular approach in many tasks (e.g. Bahdanau et al., 2014; Xu et al., 2016; Hudson & Manning, 2018). One major difference with these mechanisms may be that PFC is thought to modulate activity through multiple brain areas at once, conditioned on the current goal. This kind of conditioning may be more similar to <a href="HyperNetworks">HyperNetworks</a> (Ha et al., 2016), <a href="Film">Film</a> (Perez et al., 2018), where the mapping learned by a single feedforward network can be modulated with transformations at each layer, or RIM, which tries explicitly to model a top-down attentional modulation mechanism (Goyal et al., 2019).

Film: Visual Reasoning with a General Conditioning Layer al

having a control in novel environment which has the rules which we are not used to encounter before.

multi scale
processing

(analogous to "attention
mechanism")

Hypernetworks: an approach of 1 using a one network (hypernetwork) to generate the weights for 1 another network.

Recurrence, gating, and seriality Recurrence is ubiquitous in the brain, but the PFC has a special role in maintaining information in working memory over longer timescales (Lara & Wallis, 2015). Work

in computational neuroscience examining the detailed biological mechanisms that would allow PFC to accomplish this has emphasized its interaction with the basal ganglia and the importance of LSTM-like gating operations (O'Reilly & Frank, 2006). Although computations in the brain are massively parallelized, the amount of information that can be maintained in working memory at a given time is notoriously small (Petri et al., 2017; Feng et al., 2014; Oberauer & Kliegl, 2006). This means that seriality is also an important aspect of how the PFC operates: top-down attention must be applied serially over the course of a planning or reasoning process, and intermediate results must be integrated over time. However, the serial processing of a few elements at a time can also be an advantage, as it enables arbitrary sequences of complex computational processing at each of these steps to be combined to obtain more powerful and compositional computation. This may be an important factor for supporting Turing-machine like universal computation (Graves et al., 2014; Newell, 1990), and for generalizing outside of the training distribution (Bengio, 2017; 2019).

Dopamine:
is a type of neurotransmitter.
Your body makes it, and your
nervous system uses it to send
messages between nerve cells.

Learning: Dopamine and reinforcement Recent proposals from deep learning researchers have encouraged neuroscientists to focus on the architectures, learning algorithms, and cost functions in the brain, as opposed to the more traditional approach of characterizing the low-level biological mechanisms or tuning properties of neurons or neuronal populations (Marblestone et al., 2016; Richards et al., 2019). This approach has been emphasized in research in connectionism and parallel distributed processing for decades (Rumelhart et al., 1986), but much remains unknown about the learning mechanisms and cost functions that might be at work in biological neurons (Richards et al., 2019). Reinforcement learning is thought to be especially important for learning in the PFC, which receives ample dopamine signals conveying reward prediction errors (O'Reilly & Frank, 2006), and is heavily involved in decision-making and planning (Rushworth & Behrens, 2008). A recent proposal shows that a number of empirical findings can be explained by a model in which the PFC implements a meta-reinforcement learning system, trained by dopamine to instantiate an RL procedure within the dynamics of its neural activity (Wang et al., 2018).

A PFC module for deep learning? Much remains unknown, but an overall picture of the PFC that has emerged in cognitive and computational neuroscience is one where it selects, maintains, and manipulates learned representations in other areas of the brain through a serial process of top-down attentional modulation (Miller & Cohen, 2001; O'Reilly & Frank, 2006; Hazy et al., 2007). This serial processing may be tuned through reinforcement or meta-reinforcement learning and dopamine signals to optimize performance on tasks that require reasoning, rule-like representations, sequential and dynamic recombination of computations, cognitive control, or temporally abstract planning. This kind of system may be critical to ensuring flexibility in familiar environments and controlled decision-making in novel ones, and may allow for efficient planning on multiple timescales.

Many of the current major challenges facing deep learning research involve tasks that require an extended notion of generalization, not just to examples from the same distribution as the past observations, but also to out-of-distribution inputs (Lake & Baroni, 2018; Bahdanau et al., 2019b; Bengio, 2019). The ability to handle such non-stationarities would naturally evolve because learning agents (who change their policy and thus end up visiting different states of the environment) naturally face them, and even more so in a social multi-agent context where the environment itself changes. Some of the paradigmatic cases in which humans are able to do this involve the application of known rules to novel elements (Lake et al., 2019a) — a cognitive function that has been associated with the PFC (Miller & Cohen, 2001; Wallis et al., 2001). This systematicity is natural in symbolic systems typical of classical approaches to AI, but these lack many of the powerful advantages brought by deep learning (such as the ability to learn efficiently on a large scale, to handle uncertainty, to generalize well across symbols through distributed representations, and to ground these symbols in a complex perceptual reality). These symbolic systems utilize the notions of indirection or of variables — arrays of memory that can be manipulated by computations that do not depend on the specific content stored there — ensuring the kind of abstraction necessary for this kind of systematic generalization to emerge. An analogous independence may exist between the PFC and posterior sensory and association areas: the PFC may be able to select and manipulate representational content in these areas according to learned rules that can be applied to many different elements (Russin et al., 2019; Kriete et al., 2013). This may provide the kind of abstraction and compositionality currently missing from standard architectures in deep learning (Bengio, 2017; Bengio et al., 2019).

# 5 CONCLUSION

We have argued that there is a striking correspondence between the tasks on which humans outperform current AI systems and the executive functions associated with the PFC. We believe that a greater focus on the principles and inductive biases at work in the PFC may inspire novel architectures that can accomplish similar functions. Much remains to be learned in making these principles more concrete and in implementing them in working systems, but we hope that we have taken a step in this direction and that this work will facilitate greater synergy between neuroscience and AI in the future.

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