

01204211 Discrete Mathematics

Lecture 2: Quantifiers and proofs

Jittat Fakcharoenphol

August 18, 2015

This lecture covers:

- ▶ More on quantifiers
- ▶ How to prove a proposition
- ▶ Basic proof techniques

Review: Quantifiers

- ▶ A *predicate* is a statement with variables, which can be either true or false, after all its variables are specified.
- ▶ If we quantify a predicate completely, the quantified expression now has a truth value, and it is called a quantified proposition.
- ▶ Two ways to quantify:
 - ▶ **Universal quantifier** (\forall) states that the quantified proposition is true when the predicate is true for every value of the variable in the specified set.
 - ▶ **Existential quantifier** (\exists) states that the quantified proposition is true when the predicate is true for at least one value of the variable in the specified set.
- ▶ Quantifiers can be nested. E.g.,
 - ▶ $\forall x \forall y P(x, y) \equiv \forall x (\forall y (P(x, y)))$
 - ▶ $\forall x \exists y P(x, y) \equiv \exists x (\forall y (P(x, y)))$