

INF1008
Data Structures & Algorithms

Group 10

CONTENTS

CHAPTER	QUESTION 2	PAGE 2
1.1	Problem Statement	2
1.2	Requirements/Specification	2
1.3	User Guide	2
1.4	Structure/Design	2
1.5	Limitations	3
1.6	Testing Invalid Inputs — 3	3
1.7	Listings Algorithm — 4 • Testing — 4	4

Chapter 1

Question 2

1.1 Problem Statement

Write a program that reads in a sequence of characters, and determines whether its parentheses, braces, and curly braces are “balanced.” Your program should read one line of input containing what is supposed to be a properly formed expression in algebra and tells whether it is in fact legal. The expression could have several sets of grouping symbols of various kinds, (), [], and {}. Your program needs to make sure that these grouping symbols match up properly. Analyse the efficiency of your implementation and provided a detailed discussion of its time and space complexity.

1.2 Requirements/Specification

Given any algebraic statement, (e.g. $-b \pm \left[\sqrt{\{b^2\} - (4)(a)(c)} \right] / 2(a)$), determine if the braces are balanced; That is, if the number of opening braces match the number of closing braces, and that the first closing brace matches with the last opening brace. The algorithm expects a properly formed expression in algebra as a string and outputs either **True** or **False**.

1.3 User Guide

To run the program, simply type `python main.py` in a terminal window. The program then prompts the user for an algebraic statement. If the statement is balanced, the program returns **True** and vice versa. No external libraries other than the standard `Python 3` libraries are required.

1.4 Structure/Design

The algorithm works by pushing opening brackets to a stack by looping through all bracket characters in the original statement. When encountering a closing bracket, it pops the last element of the stack and compares if they are complementary. If at any point the check fails, the algorithm returns **False** and ends the loop prematurely. At the end of the loop, the algorithm checks that the stack is empty. If it is, it returns **True** and **False** otherwise.

Algorithm 1: Bracket balance checker

Input: str statement

```
1 Function is_balanced(statement: str) is
2   statement  $\leftarrow$  all brackets from statement;
3   bracket_pairings  $\leftarrow$  {opening_bracket : closing_bracket};
4   if len(statement) mod 2  $\neq$  0 then
5     | return False;
6   end
7   stack = [];
8   foreach character in statement do
9     | if character is an opening bracket then
10    |   stack.push(character);
11    | end
12    | else if bracket_pairing[stack.pop()]  $\neq$  character then
13    |   | return False;
14    | end
15  end
16  return len(stack) == 0;
17 end
```

As the algorithm iterates through the input string only once, the time complexity is $O(n)$ for a given input string of length n . The opening brackets are iteratively pushed to and popped from a stack, so the space complexity is $O(n)$ as well.

Note:-

The time complexity of **Regular Expressions** and **Stack Operations** for insertion and deletion are known to be $O(n)$ and $O(1)$ respectively, so the time and space complexity of the algorithm remains at $O(n)$.

1.5 Limitations

While the algorithm determines perfectly if the brackets within any given algebraic statement are balanced, it does not check if the statement itself is a properly formed algebraic statement. Furthermore, it does not check that brackets on two sides of a given equality are balanced, as it only checks for bracket placement relative to other brackets in the entire input string (i.e. $([0]\{=\}2)$ will be evaluated as balanced).

1.6 Testing

Testing is handled by the `tests.py` file, which generates t number of input strings of up to length l , of which $n/2$ inputs are valid, and the other half are invalid. To generate valid inputs, the generator randomly selects an opening bracket or a closing bracket that matches the last opening bracket until reaching the halfway point of the string length, at which point it iteratively closes all the remaining open brackets.

1.6.1 Invalid Inputs

Invalid inputs are a superset of valid inputs, thus the selection of brackets to insert at any given point is expanded to include all invalid closing brackets as well. The generator then selects a random index i to insert random brackets until the max length is reached. Then, the generator checks if the number of opening brackets match the number of closing brackets for each type of bracket. If they match, a random index is selected again to either insert or remove a bracket. This ensures that we also deal with the case that the length of the input string is odd. The generator then provides the input string and whether the string is valid to a checker function, which compares the output of the developed algorithm with the validity of the input string. To run the tests, a user may run `python test.py -tests {number of tests} -length {max length of input strings}`. The output will show how many tests the algorithm passes, and what the generated input strings were for each test.

1.7 Listings

1.7.1 Algorithm

```
1 import re
2
3 def main(statement:str):
4     return is_balanced(statement)
5
6 def is_balanced(statement:str) -> bool:
7     bracket_pairing = {
8         "{": "}" ,
9         "[": "]" ,
10        "(": ")"
11    }
12    # fast check
13    statement = re.sub(r"[A-Za-z0-9\*\-\+\^\~\/\=]", "", statement)
14    if len(statement) % 2 != 0: return False
15    brackets = [bracket for bracket in bracket_pairing.keys()] \
16        + [bracket for bracket in bracket_pairing.values()]
17    stack = []
18    for char in statement:
19        if char in brackets:
20            if char in bracket_pairing.keys():
21                stack.append(char)
22            else:
23                try:
24                    if bracket_pairing[stack.pop()] != char:
25                        return False
26                except IndexError:
27                    return False
28    return len(stack) == 0
29
30 if __name__ == "__main__":
31     res = main(input("Enter an algebraic statement: "))
32     print(res)
```

1.7.2 Testing

```
1 import argparse
2 import random
3 from main import is_balanced
4
5 def test_is_balanced(iters: int, max_length:int=10):
6     """Tests the is_balanced function over a given number of iterations.
7
8     Args:
9         iters (int): number of iterations
10    """
11    results = []
12    for i in range(iters):
13        statement, proper = statement_generator(random.randint(1, max_length))
14        print(f"Test {i+1}: \t{statement}", end=" ")
15        res = is_balanced(statement)
16        if res == proper:
17            print(f"Passed ({res})")
18        else:
19            print(f"Failed: {res} (should be {proper})")
20        results.append(res == proper)
21    print(f"Passed {results.count(True)} out of {iters} tests")
22
23 def statement_generator(length: int):
24     """Generates a random algebraic statement of a given length.
25
26     Args:
27         length (int): length of the statement
28    """
```

```

29 Returns:
30     str: random algebraic statement
31     ""
32     length // 2
33     bracket_pairing = {
34         "{": "}" ,
35         "[" : "]" ,
36         "(" : ")"
37     }
38     brackets = [bracket for bracket in bracket_pairing.keys()] \
39         + [bracket for bracket in bracket_pairing.values()]
40     ret = ""
41     state = random.choice([True, False])
42     ret += random.choice([bracket for bracket in bracket_pairing.keys()])
43     stack = [ret[0]]
44     for _ in range(length):
45         if state:
46             candidates = [b for b in bracket_pairing.keys()]
47             if ret[-1] in bracket_pairing.keys():
48                 candidates += [bracket_pairing[ret[-1]]]
49             ret += random.choice(candidates)
50             if ret[-1] in bracket_pairing.values():
51                 stack.pop()
52             else:
53                 stack.append(ret[-1])
54         else:
55             ret += random.choice(brackets)
56     for _ in range(len(stack)):
57         if state:
58             ret += bracket_pairing[stack.pop()]
59         else:
60             ret += random.choice(brackets)
61     if not state:
62         n_additions = random.randint(0, length)
63         insertion_index = random.randint(0, len(ret))
64         additions = [random.choice(brackets) for _ in range(n_additions)]
65         ret = ret[:insertion_index-1] + "".join(additions) + ret[insertion_index+1:len(ret)+1-
66         n_additions]
67     # count the number of bracket pairs
68     bracket_counts = {(k, v): 0 for k, v in bracket_pairing.items()}
69     for char in ret:
70         for k, v in bracket_pairing.items():
71             if char == k:
72                 bracket_counts[(k, v)] += 1
73             elif char == v:
74                 bracket_counts[(k, v)] -= 1
75     # if the statement is potentially balanced, either remove or add a random character.
76     if all([count == 0 for count in bracket_counts.values()]):
77         # remove a random character
78         if len(ret) > 2:
79             loc = random.randint(1, len(ret)-1)
80             ret = ret[:loc] + ret[loc+1:]
81         else:
82             ret += random.choice(brackets)
83     return (ret, state)
84
85 def main(tests: int=1000, max_length:int=10):
86     test_is_balanced(tests, max_length)
87
88 if __name__ == "__main__":
89     parser = argparse.ArgumentParser()
90     parser.add_argument("-t", "--tests", type=int, default=1000, help="number of tests to run")
91     parser.add_argument("-l", "--length", type=int, default=10, help="maximum length of the statement")
92     args = parser.parse_args()
93     main(args.tests, args.length)

```