Programming Assignment #1 Due: October 9, 2018 11:59pm

# Programming Assignment #1

Programming assignments are to be done individually. You may discuss the problem and general concepts with other students, but there should be no sharing of code. You may not submit code other than that which you write yourself or is provided with the assignment. This restriction specifically prohibits downloading code from the Internet. If any code you submit is in violation of this policy, you will receive no credit for the entire assignment.

The goals of this lab are:

- Familiarize you with programming in Java
- Show an application of the stable matching problem
- Understand the difference between the two optimal stable matchings.

## **Problem Description**

In this project, you will implement a variation of the stable marriage problem adapted from the textbook Chapter 1, Exercise 4, and write a small report. We have provided Java code skeletons that you will fill in with your own solution. Please read through this document and the documentation in the starter code thoroughly before beginning.

Gale and Shapley published their paper on the Stable Matching Problem in 1962, but a version of their algorithm had already been in use for ten years by the National Resident Matching Program, for the problem of assigning medical residents to hospitals.

The situation was the following: There were n medical students graduating in a given year, each interested in joining one of the hospitals. Each hospital had a ranking of the students in order of preference, and each student had a ranking of the hospitals in order of preference. We will assume that there were more students graduating than there were slots available in the m hospitals. The interest was in finding a way of assigning each student to at most one hospital, in such a way that all available positions in all hospitals were filled. (Since we are assuming a surplus of students, there would be some students who do not get assigned to any hospital)

We say that an assignment of students to hospitals is *stable* if neither of the following situations arises:

- First type of instability: There are students s and s', and a hospital h, such that
  - -s is assigned to h, and
  - -s' is assigned to no hospital, and
  - -h prefers s' to s
- Second type of instability: There are students s and s', and hospitals h and h', so that

- -s is assigned to h, and
- -s' is assigned to h', and
- -h prefers s' to s, and
- -s' prefers h to h'.

So we basically have the Stable Matching Problem as presented in class, except that (i) hospitals generally want more than one resident, and (ii) there is a surplus of medical students. There are several parts to the problem.

## Part 1: Write a report [20 points]

Write a short report that includes the following information:

- (a) Give an algorithm in pseudocode (either an outline or paragraph works) to find a stable assignment that is **hospital** optimal. *Hint: it should be very similar to the Gale-Shapley algorithm, with hospitals taking the role of the men, and residents of the women.*
- (b) Give the runtime complexity of your algorithm in (a) in Big O notation and explain why. Note: Full credit will be given to solutions that have a complexity of O(mn).
- (c) Give an algorithm in pseudocode (either an outline or paragraph works) to find a stable assignment that is **resident** optimal *Hint:* it should be very similar to the Gale-Shapley algorithm, with residents taking the role of the men, and hospitals of the women.
- (d) Give the runtime complexity of your algorithm in (c) in Big O notation and explain why. Note: Try to make your algorithm as efficient as you can, but you may get full credit even if it is not O(mn) as long as you clearly explain your running time and the difficulty of optimizing it further.
- (e) Use the Brute Force Implementation (see below) to verify that your algorithm is indeed resident optimal.

In the following two sections you will implement code for a brute force method to find the resident optimal solution and an efficient algorithm to find both resident and hospital solutions. Note: For the programming assignment, you don't need to submit a proof that your algorithm returns a stable matching, or of hospital or resident optimality.

## Part 2: Implement a Brute Force Solution that is Resident Optimal [20 points]

A brute force solution to this problem involves generating all possible permutations of students and hospitals, and checking whether each one is a stable matching. To find the stable matching that is Resident Optimal, you need to find the matching where every resident gets their best valid partner. For this part of the assignment, you are to implement a function that verifies whether or not a given matching is stable and find the resident optimal one. We have provided most of the brute force solution already, including input, function skeletons, abstract classes, and a data structure. Your code will go inside a function called stableMarriageBruteForce\_residentoptimal() inside Program1.java. A file named Matching.java contains the data structure for a matching. See the instructions section for more information.

Inside Program1.java is a placeholder for a verify function called isStableMatching(). Implement this function to complete the Brute Force Resident Optimal algorithm (Note: a brute force algorithm is already provided, but the provided function returns the first stable matching).

Of the files we have provided, please only modify Problem1.java, so that your solution remains compatible with ours. However, feel free to add any additional Java files (of your own authorship) as you see fit.

## Part 3: Implement an Efficient Algorithm [60 points]

We can do better than the above using an algorithm similar to the Gale-Shapley algorithm. Implement the efficient algorithm you devised in your report for resident optimal and hospital optimal solutions. Again, you are provided several files to work with. Implement the function that yields a resident optimal solution stableMarriageGaleShapley\_residentoptimal() and hospital optimal solution stableMarriageGaleShapley\_hospitaloptimal() inside of Program1.java.

Of the files we have provided, please only modify Problem1.java, so that your solution remains compatible with ours. However, feel free to add any additional Java files (of your own authorship) as you see fit.

#### Instructions

- Download and import the code into your favorite development environment. We will be grading in Java 1.8. Therefore, we recommend you use Java 1.8 and NOT other versions of Java, as we can not guarantee that other versions of Java will be compatible with our grading scripts. It is YOUR responsibility to ensure that your solution compiles with Java 1.8. If you have doubts, email a TA or post your question on Piazza.
- If you do not know how to download Java or are having trouble choosing and running an IDE, email a TA, post your question on Piazza or visit the TAs during Office Hours.
- There are several .java files, but you only need to make modifications to Program1.java. Do not modify the other files. However, you may add additional source files in your solution if you so desire. There is a lot of starter code; carefully study the code provided for you, and ensure that you understand it before starting to code your solution. The set of provided files should compile and run successfully before you modify them.
- The main data structure for a matching is defined and documented in Matching.java. A Matching object includes:
  - m: The number of hospitals
  - **n**: Number of students
  - hospital\_preference: An ArrayList of ArrayLists containing each of the hospital's preferences of students, in order from most preferred to least preferred. The hospitals are in order from 0 to m-1. Each hospital has an ArrayList that ranks its preferences of students who are identified by numbers 0 through n-1.
  - **resident\_preference**: An ArrayList of ArrayLists containing each of the student's preferences for hospitals, in order from most preferred to least preferred. The students are in order from 0 to n-1. Each student has an ArrayList that ranks its preferences of hospitals who are identified by numbers 0 to m-1.

- hospital\_slots: An ArrayList that specifies how many slots each hospital has. The
  index of the value corresponds to which hospital it represents.
- resident\_matching: An ArrayList to hold the final matching. This ArrayList (should) hold the number of the hospital each student is assigned to. This field will be empty in the Matching which is passed to your functions. The results of your algorithm should be stored in this field either by calling setResidentMatching(<your\_solution>) or constructing a new Matching(marriage, <your\_solution>), where marriage is the Matching we pass into the function. The index of this ArrayList corresponds to each student. The value at that index indicates to which hospital he/she is matched. A value of -1 at that index indicates that the student is not matched up. For example, if student 0 is matched to hospital 55, student 1 is unmatched, and student 2 is matched to hospital 3, the ArrayList should contain {55, -1, 3}.
- You must implement the methods stableMarriageBruteForce\_residentoptimal(), isStableMatching(), stableMarriageGaleShapley\_residentoptimal() and stableMarriageGaleShapley\_hospitaloptimal() in the file Program1.java. You may add methods to this file if you feel it necessary or useful. You may add additional source files if you so desire.
- The file Permutation.java is provided to help you generate matchings for the brute force solution. You should only have to use getNextMatching(Matching data) in your solution. See the function stableMarriageBruteForce(Matching marriage) in AbstractProgram1.java.
- Driver.java is the main driver program. Use command line arguments to choose between brute force and your efficient algorithms and to specify an input file. Use -b for brute force, -br for brute force resident optimal, -gr for the efficient resident optimal algorithm, -gh for the efficient hospital optimal algorithm and input file name for specified input (i.e. java -classpath . Driver [-gr] [-gh] [-b] [-br] <filename> on a linux machine). As a test, the 3-10-3.in input file should output the following for both a hospital and resident optimal efficient solution:
  - Resident 0 Hospital -1
  - Resident 1 Hospital 1
  - Resident 2 Hospital -1
  - Resident 3 Hospital -1
  - Resident 4 Hospital -1
  - Resident 5 Hospital -1
  - Resident 6 Hospital -1
  - Resident 7 Hospital 2
  - Resident 8 Hospital 0
  - Resident 9 Hospital -1

- When you run the driver, it will tell you if the results of your efficient algorithm pass the isStableMatching() function that you coded for this particular set of data. When we grade your program, however, we will use our implementation of isStableMatching() to verify the correctness of your solutions.
- Make sure your program compiles on the LRC machines before you submit it.
- We will be checking programming style. A penalty of up to 10 points will be given for poor programming practices (e.g. do not name your variables foo1, foo2, int1, and int2).
- Before you submit, be sure to turn your report into a PDF and name your PDF file eid\_lastname\_firstname.pdf.

#### What To Submit

You should submit a single zip file titled eid\_lastname\_firstname.zip that contains all of your java files and pdf report eid\_lastname\_firstname.pdf. Do not put these files in a folder before you zip them (i.e. the files should be in the root of the ZIP archive). Your solution must be submitted via Canvas BY 11:59 am on October 9, 2018.