



MAX PLANCK INSTITUTE  
FOR DYNAMICS OF COMPLEX  
TECHNICAL SYSTEMS  
MAGDEBURG



COMPUTATIONAL METHODS IN  
SYSTEMS AND CONTROL THEORY

morgen (1.2)

Model Order Reduction for Gas and Energy Networks

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CSC





<https://git.io/morgen>



morgen (german for: tomorrow)

- **M**odel
- **O**rder
- **R**eduction

for **G**as

and **E**nergy

- **N**etworks



- Testing model-solver-reductor combinations
- Comparing models, solvers, or reductors
- Benchmarking reductors
- Prototyping algorithms
- Uncertainty quantification



- Open-source (BSD-2-Clause)
- High-Level (MATLAB and OCTAVE)
- Modular (Six modules)
- Configurable (Three-level configuration)
- Extensible (Contributions welcome)



1. Models (Discretizations)
2. Solvers (Integrators)
3. Reductors (Model Reduction Algorithms)
4. Networks (Topologies & Scenarios)
5. Tests (Simulation and Model Reduction Experiments)
6. Tools (Unit and Format Converters)



## Implemented:

- `ode_mid` – midpoint discretization
- `ode_end` – endpoint discretization (port-Hamiltonian)

```
discrete = model(network,config);
```

## `discrete` Structure:

- |  |   |
|--|---|
| ■ <code>.E</code> – Mass matrix function   | ■ <code>.J</code> – Vector field Jacobian       |
| ■ <code>.A</code> – System matrix          | ■ <code>.x0</code> – Initial state              |
| ■ <code>.B</code> – Input matrix           | ■ <code>.nP</code> – Number of pressure states  |
| ■ <code>.C</code> – Output matrix          | ■ <code>.nQ</code> – Number of mass-flux states |
| ■ <code>.f</code> – Nonlinear vector field | ■ <code>.nPorts</code> – Number of ports        |



## Implemented:

- `imex1` – 1st Order Implicit-Explicit (Euler-Euler)
- `imex2` – 2nd Order Implicit-Explicit (Runge-Kutta)
- `cnab2` – 2nd Order Crank-Nicolson/Adams-Bashforth
- `generic` – 2nd Order Adaptive Rosenbrock (`ode23s`)
- `rk4` – “Classic” 4th Order Explicit Runge-Kutta
- `rk2hyp` – 2nd Order Explicit Runge-Kutta with increased stability
- `rk4hyp` – 4th Order Explicit Runge-Kutta with increased stability

```
solution = solver(discrete,scenario,config);
```

## `solution` Structure:

- |  |   |
|--|---|
| ■ <code>.t</code> – Time instances       | ■ <code>steady_z0</code> – Mean compressibility       |
| ■ <code>.u</code> – Input time series    | ■ <code>steady_error</code> – Steady-state error      |
| ■ <code>.y</code> – Output time series   | ■ <code>steady_iter1</code> – Algebraic Iterations    |
| ■ <code>.runtime</code> – Solver runtime | ■ <code>steady_iter2</code> – Differential Iterations |





## Implemented:

- `pod_r` – Structured Proper Orthogonal Decomposition (POD)
- `eds_ro`, `eds_wx`, `eds_wz`,  
`eds_ro_l`, `eds_wx_l`, `eds_wz_l` – Structured Dominant Subspaces
- `mpod_ro`, `mpod_wx`, `mpod_wz`,  
`mpod_ro_l`, `mpod_wx_l`, `mpod_wz_l` – Structured Modified POD
- `bpod_ro`,  
`bpod_ro_l` – Structured Balanced POD
- `ebt_ro`, `ebt_wx`, `ebt_wz`,  
`ebt_ro_l`, `ebt_wx_l`, `ebt_wz_l` – Structured Balanced Truncation
- `gopod_r` – Structured Goal-Oriented POD
- `ebg_ro`, `ebg_wx`, `ebg_wz`,  
`ebg_ro_l`, `ebg_wx_l`, `ebg_wz_l` – Structured Balanced Gains
- `dmd_r` – Structured Dynamic Mode Decomposition Galerkin

```
[proj,name] = reductor(solver,discrete,scenario,config);
```

- `proj` – Cell array of projectors
- `name` – Full name of reductor



## Network and scenario data:

- Network data stored as decorated edge list in CSV format (`.net`).
- Scenario data stored as key-value pairs in INI format (`.ini`).
- Network base name determines associated scenario folder name.
- Each network has minimally a `training.ini` scenario.

## Types of tests:

- Prefix `sim_` – Simulate scenario by a model-solver combination.
- Prefix `mor_` – Reduce and test model-solver-reductor combination.



## Available:

- `xml2net` – Convert *GasLib* .xml to `morgen .net`
- `json2net` – Convert *MathEnergy* .json to `morgen .net`
- `csv2net` – Convert *SciGRID\_gas* .csv to `morgen .net`
- `vf2kgs` – Convert volume flow to mass flow in kg/s
- `psi2bar` – Convert pressure from psi to bar
- `cmp_friction` – Compare friction factors
- `cmp_compressibility` – Compare compressibility factors
- `randscen` – Generate random scenario from training scenario



## Available:

- optional arguments (`varargin`)
- configuration file (`morgen.ini`)
- fallback via hard-coded default values



```
R = morgen(network_id,scenario_id,model_id,solver_id,redutor_ids,varargin);
```

{string} network\_id – Network file (.net) base name

{string} scenario\_id – Scenario file (.ini) base name

{string} model\_id – Model function name

{string} solver\_id – Solver function name

{cell} redutor\_ids – Array of redutor names

{string} varargin – Adhoc configuration arguments ('key=val')



- `morgen` is open source (under BSD-2-Clause license),
- and compatible with MATLAB and Octave.
- A template model, solver and reductor are available.
- Currently, all reductors use `emgr`: <https://gramian.de>.
- See [README.md](#) for more info.
- This is research software!



morgen – **M**odel **O**rders **R**eduction for **G**as and **E**nergy **N**etworks

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C. Himpe, S. Grundel, P. Benner:

**Model Order Reduction for Gas and Energy Networks.**

Journal of Mathematics in Industry 11: 13, 2021.

<https://doi.org/10.1186/s13362-021-00109-4>



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