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92 What should be time complexity of:
         for (inti-1 to u)
             i=i*2; \rightarrow o(1)

  for i → 1, 2, 4, 6, 8 . . . . n times

       ie Series is a GP
   So a=1, u=2/1
    Kth value of GIP:
             th = ank-1
             t_h = 1(2)^{k-1}
              2n=2k
          lag_2(2n) = k lag 2
            lag 2 + lag n = le
            leg 2 n+1 = h (Neglecting '1')
  So, Time Complexity T(n) > 0 (lag, n) - Ans.
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3. T(n) = [3T(n-1) \text{ if } n > 0 \text{ otherwise } 1

4 ie T(n) \Rightarrow 3T(n-1) - (1)

T(n) \Rightarrow 1

put n \Rightarrow n-1 in (1)

T(n-1) \Rightarrow 3T(n-2) - (2)

put (2) in (1)

T(n) \Rightarrow 3 \times 3T \cdot (n-2)

T(n) \Rightarrow 9T(n-2) \rightarrow (3)

put n \Rightarrow n-2 in (1)

T(n-2) = 3T \cdot (n-3)

put in (3).

T(n) = 27T \cdot (n-3) \rightarrow 4
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Generalising series,

T(h) = 3^{k} T(n-k) - (5)

for leth terms, Let n-k=1 (Base (ase)
k = n-1
put in (5)
T(n) = 3^{n-1} T(1)
T(n) = 3^{n-1} \qquad (neglecting 3')
T(n) = 0 (3^{n})
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84.
$$T(n) = \begin{cases} 2T(n-1)-1 & \text{if } n > 0, \\ 0 + 1 + 1 + 1 + 1 + 1 \end{cases}$$

$$T(n) = 2T(n-1)-1 \rightarrow (1)$$

put $n = n-1$

$$T(n-1) = 2T(n-2)-1 \rightarrow (2)$$

put $in(1)$

$$T(n) = 2x(2T(n-2)-1)-1$$

$$= 4T(n-2)-2-1 \rightarrow (3)$$

put $n = n-2$ in (1)

$$T(n-2) = 2T(n-3)-1$$

T(n-2) = 2T(n-3)-1Put in (1) T(n) = 8T(n-3)-4-2-1 - (4)

Generalizing series $T(n) = 2^{k} T(n-k) - 2^{k-1} - 2^{k-2} \dots 2^{n}$ $\frac{k^{+n} \text{ term}}{k} \text{ Let } n-k=1$ k=n-1

R = n-1 $T(n) = 2^{\frac{n}{2}-1} T(1) - 2^{k} \left(\frac{1}{2} + \frac{1}{2^{2}} + \dots + \frac{1}{2^{k}}\right)$ $= 2^{\frac{n}{2}-1} - 2^{\frac{n}{2}-1} \left(\frac{1}{2} + \frac{1}{2^{2}} + \dots + \frac{1}{2^{k}-1}\right)$ in Suius in GP. $a = \frac{1}{2}, \quad n = \frac{1}{2}.$

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50,

T(n) = 2^{n-1} (1 - (1/2)^{n-1})

= 2^{n-1} (1 - 1 + (1/2)^{n-1})

= \frac{2^{n-1}}{2^{n-1}}

= T(n) = O(1) Ans
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Is what should be time complexity of
           int i=1, s=1;
            while (s(=n)
             i i++;
               8 = s+ i;
             2 printf ("#");
-) i=1 2 3 4 5 6 ...
   8= 1+3+6+10+15+ ....
  Sum of s= 1+3+6+10+ ... + n - 1)
  Also 5 = 1+3+6+10+11. Tn-1+Tn -> 2)
   0= 1+2+3+4+ ... n-Tn
   Tk = 1+2+3+4+ ... + K
   TK = 1 K (K+1)
    for K iterations
    1+2+3+ ... k (= n
    \frac{k(k+1)}{2} < = w
      \frac{k^2+K}{2} < = n
      O(k2) <= N
        K = 0( Jn)
       T(n) = O(JN) Que.
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Ste Time Camplexity of

void f (int n)

int i, count = 0;

fac(i=0.1; i \neq i \leq n; i+i)

3

Ly As i^2 = n

i = \sqrt{n}

i = 1, 2, 3, 4, ... \sqrt{n}

= 1, 3, 4, ... \sqrt{n}

= 1
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Frine Complexity of

void f (int n)

int i, j, h, count = 0;

for (int i = n/2; i (= n; ++il))

for (j=1; j (= n; j=j*2)

for (h=1; h (= n; h= k+2)

count ++;

3

4 Since, for h=h²

k=1,2,4,8,... h

"Stries is in GP

×0, a=1, n=2

 $\frac{A(N^{n}-1)}{N-1}$ = $\frac{1(2^{k}-1)}{1}$ $N = 2^{k}-1$ $N + 1 = 2^{k}$ $\log_{2}(n) = k$

Du

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i j h

! lag(n) lag(n)*lag(n)

2 lag(n) lag(n)*lag(n)*

.:

n lag(n) lag(n)*lag(n)

T.C \Rightarrow O(n*lag^2(n)) \rightarrow 9hs

mu Camplexity of
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88. Time Complexity of
          void function ( int n)
             of (n==1) return;
             for (i=1 ten) [
             for (j=1 to n) {
             3 printf (" * "),
         function (n-3);
  4 fu (i = 1 to n)
      me get j = n times every turn
            · · · i * j = n2
    hth, Now, T(n) = n2+T(n-3);
               T(n-3) = (n23)2 + T(n-6);
               T(n-6)= (n 6)2 + T(n-9);
              and T(1)=1;
       Now, substitute each value in T(n)
         T(n) = n^2 + (n-3)^2 + (n-6)^2 + \dots + 1
               h = (n-1)/3 total tums = k+1
    T(n) = n^2 + (n-3)^2 + (n-6)^2 + \dots + 1
     T(n) = ~ 4 n2
      T(n)~(h-1)/3 # n2
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50, T(n) 20(n3) - Ans

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9. Time Camplexity of :-
     vaid function ( int n)
        for (int i= 1 to n) {
         for (intj=1; j <= n; j=j+i) [
           prints (" * "),
                j=1+2+... (n),j+i)
4 for i = 1
                j=1+3+5...(n)/j+i)
       i = 2
                j=1+4+7...(n),j+i)
      nth term of AP is
         T(n)= a+d* m
         T(m) = 1 + d xm
         (n-1)/d=n
      for i=1
                (n-1)/1 times
          i=2 (n-1)/2 times
   me get,
        T(n) 2 izj 1 + Lzj 2+... in-1 jn-1
             2(n-1)+(n-2)+(n-3)+\cdots
            2 n+n/2 + n/3 + .. n/n-1 - nx1
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2 n [1+1/2+1/3+ ··· 1/n-1] - n+1 znxlagn-n+1 Since 1 1/2 = lag x

T(n) = O(nlegn) + Ans.

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For the Function n' R & C", what is the asymptotic Relationship b/00 these functions?

Assume that h>=1 & C>1 are constants. Find out the value of C & no. of which relationship helds.

Is a given nh and c"

Relationship b/w nh & C" is

nh = 0 (C")

nh & a CC")

V n > no A constant, a>0

for no=1; C=2

no=1 & C-2 - Ans
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