91)
$$T(n) = 3T (n/2) + n^2$$

 $\rightarrow T(n) = aT(n/6) + f(n^2)$
 $\rightarrow a > 1, b > 1$
On compaining
 $a = 3, b = 2, f(n) = n^2$
Now, $c = laga = laga = 1.584$
 $n^2 = n^{1.584} \le n^2$
 $f(n) > n^2$
 $f(n) > n^2$
 $f(n) > n^2$
 $f(n) > n^2$

92)
$$T(n) = 4T(n/2) + n^2$$

 $\rightarrow a/1, b/1$
 $a = 4, b = 2, f(n) = n^2$
 $c = \log_2 4 = 2$
 $n^2 = n^2 = f(n) = n^2$
 $\therefore T(n) = \theta(n^2 \log_2 n)$

93)
$$T(n)_2 T(n/2) + 2^n$$
 $A = 1$
 $b = 2$
 $f(n)_2 2^n$
 $C = laga = lagc = 0$
 $h^c = h^o = 1$
 $f(n) > h^c$
 $T(n)_2 \delta(2^n)$

95)
$$T(n) = 16 T(n/4) + n$$
 $\Rightarrow \alpha = 16, 6 = 4$
 $f(n) = n$
 $c = \log 16 = \log (4)^2 = 2 \log 4$
 $= 2 \log 16 = \log (4)^2 = 2 \log 4$
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36)
$$T(n)=2T(n/2)+n \log n$$

 $\rightarrow a=2, b=2$
 $f(n)=n \log n$
 $c=\log 2=1$
 $n'=n'=n$
 $n \log n > n$
 $f(n) > n'$
 $f(n) > n'$
 $f(n) > n'$

XV

97) T(n)2 2T(n/2) + n/lagn > a=2, b=2, f(n)= n/legn C= lag 2 = 1 nc=n1=n · n < n · · f(n) < nc :. T(n) = 0 (n) 98) T(n)=2T(n/4)+n0.51 → a = 2, b = 4, f(n)= n° 51 $C = \log_{10} a = \log_{12} 2 = 0.5$ $n^{c} = n^{0.5}$ $n^{0.5} < n^{0.5}$ f(n)>nc .. T(n) = 0 (nº.51) 99) T(n) 2 0.5 T (n/2) + 1/n -> a=0.5, b=2 a 1/1 but here a is 0.5 so me cannot apply Master's Theorem. 910) T(n)= 16T(n/4)+n! -> a=16, b=4, f(n)=n! · · · C = lag a z lag 16 2 2

 $n^{c} = n^{2}$ As n/ >n2 ... T(n) = 0(n!)

911) 4T(n/2) + lag n -, a=4, b=e, f(n)=lagn C = laga · laga = ne = n2 (In) · legn : lagn < n= 2(n) (nº T(n): 0 (nc) = 0 (n2) Q12) T(n) = squt(n) T(n/2) + logn -, a= In, b=2 C= logo = log In= 1 lag n · · - Legen < leg(n) 1. f(n)>nc T(n)= 0 (f(n)) = 0 (leg (n)) (13) T(n)=3T(n/2)+n a=3; b=2; f(n)=n C = lag a = lag 3 = 1.5849 $nc = n^{1.5489}$ n< n1.5842 > f(n) < nc T(n) = 0 (n 1.5841) Q14) T(n) = 3T(n/3) + sgrt(n) $\rightarrow a=3, b=3$ C = lega = leg3 = 1 $n^{c} = n^{2} = n$ As sgut (n) < n f(n) (no T(n) = 0 (n)

$$g(15)$$
 $T(n) = 4T(n/2) + n$
 $\rightarrow 0 = 4, b = 2$
 $C = \log_{0} a = \log_{2} 4 = 2$
 $h^{c} = n^{2}$
 $n < n^{2}$ (for any constant)
 $f(n) < n^{c}$
 $f(n) = 0 (n^{2})$

916)
$$T(n) = 3T(n/4) + n \log n$$

 $\rightarrow a = 3, b = 4, f(n) = n \log n$
 $C = \log_b a = \log_4 3 = 0.792$
 $n^c = n^{0.792}$
 $n^{0.792} < n \log n$
 $T(n) = 0 (n \log n)$

$$g_{17}$$
) $T(n)=3T(n/3)+n/2$
 $\rightarrow a=3;b=3$
 $c=laga=lag_3=1$
 $f(n)=n/2$
 $n^c=n'=n$
 $As n/2 < n$
 $f(n) < nc$
 $f(n) < nc$
 $f(n) < nc$
 $f(n) = 0 < n$

$$g_{18}$$
) $T(n) = GT(n/3) + n^2 \log n$
 $A = G; b = 3$
 $C = \log_b a = \log_3 G = 1.6309$
 $n^c = n^{1.6300}$
 $A = n^{1.6300} \le n^2 \log n$
 $\therefore T(n) \ge 0 (n^2 \log n)$

gin) T(n)=4T(np) may + n/logn

\[
\rightarrow a=4,b=2,f(n)=n \\
\rightarrow a=\lag{4-2} \\
\lag{a} = \lag{4-2} \\
\lag{a} nc=n^2 \\
\lag{a} \lag{a} \lag{a} \lag{a} \\
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 $\begin{array}{c}
g20) T(n) = 64T(n/8) - n^{2} lagn \\
\rightarrow \alpha = 64 b = 8 \\
C = laga = lag 64 = lag (8)^{2} \\
C = 2 \\
N^{c} = n^{2} \\
\therefore n^{2} lagn > n^{2} \\
T(n) = 0 (n^{2} lagn)
\end{array}$

 $\begin{array}{c} g_{21} \rangle T(n) = 7T(n/3) + n^{2} \\ \rightarrow a = 7; b = 3; f(n) = n^{2} \\ C = log_{b}a = log_{3}7 = 1.7712 \\ \dot{n}^{c} = n^{1.7712} \\ \dot{n}^{1.7712} < n^{2} \\ T(n) = 0 (n^{2}) \end{array}$

Do