

Contents

1	Measuring Execution Time	1
1.1	How to Time Correctly	1
1.2	C++11 Example	2
1.3	Java Example	2
1.4	Python Example	2
2	Math Review	2
2.1	FLOOR: Largest int that is $\leq x$	2
2.2	CEILING: Smallest int that is $\geq x$	3
2.3	LOG	3
2.4	Log identities	3
2.5	ADDITION	3
	<code>#-- mode: org --</code>	

1 Measuring Execution Time

- It's difficult to measure correctly.
- Your computer is doing too much.
- I/O problems.
- May be too fast, hard to measure correctly.
- Run out of memory.

1.1 How to Time Correctly

- TIME MULTIPLE RUNS!
- Statistical significance: 29 or more.
- Use high resolution timers:
 - Use the smallest measure of time possible.
- Only time the important stuff.

1.2 C++11 Example

The following is c++11 only, it uses a high resolution timer rather than tick from C/C++.

```
double time_function()
{
    clock_t start, end, total;
    start = clock();
    for (int i=0; i<ITERS; i++)
        function_to_time();
    end = clock();
    total = end - start;;
    return (total / (float)CLOCKS_PER_SEC) / ITERS;
}
```

1.3 Java Example

```
public static float time_method()
{
    long start, end, total;
    start = System.nanoTime();
    // ITERS defined elsewhere
    for (int i=0; i<ITERS; i++)
        method_to_time()
    end = System.nanoTime();
    total = end - start;
    return total / (float) ITERS;
}
```

1.4 Python Example

Refer to python's Timeit Module (3.7).

2 Math Review

2.1 FLOOR: Largest int that is $\leq x$.

- $\text{floor}(3.2) \Rightarrow 3$
- $\text{floor}(-6.7) \Rightarrow -7$

2.2 CEILING: Smallest int that is $\geq x$.

- $\text{ceil}(3.2) \Rightarrow 4$
- $\text{ceil}(-6.7) \Rightarrow -6$

2.3 LOG

- Let $b > 1, x > 0$
- $\text{Log}_b(x) = L$ iff $b^L = x$
- $\text{Log}_{10}(1000) = 3$
- $\text{Log}_2(8) = 3$
- $\lg = \log_2$
- $\lg(16) \Rightarrow 4$
- $\text{floor}(\lg(10)) \Rightarrow 3$

2.4 Log identities

- $\text{log}_b(1) \Rightarrow 0$
- $\text{log}_b(b) \Rightarrow 1$
- $\text{log}_b(x \cdot y) \Rightarrow \text{log}_b(x) + \text{log}_b(y)$
- $\text{log}_b(x/y) \Rightarrow \text{log}_b(x) - \text{log}_b(y)$
- $\text{log}_b(x^g) \Rightarrow g \text{log}_b(x)$
- $\text{log}_a(x) \Rightarrow \text{log}_b(x) / \text{log}_b(a)$ [!]

2.5 ADDITION

- $1 + 2 + 3 + \dots + n \Rightarrow \text{sum}(1, n, 1)$
- $\text{sum}(1, n, 1) \Rightarrow n$
- $\text{sum}(1, n, i) \Rightarrow n(n+1)/2$
- $\text{sum}(1, n, i \cdot i) \Rightarrow [n(n+1)(2n+1)]/6$
- $\text{sum}(1, n, c^i) \Rightarrow (c^{n+1} - 1) / (c - 1)$ while $c \neq 1$