

$$u(t) = 1 + \frac{1}{a} \int_0^t u(z) (\sin t \cos z - \cos t \sin z) dz$$

$$= 1 + \frac{1}{a} \left\{ \sin t \int_0^t u(z) \cos z dz - \cos t \int_0^t u(z) \sin z dz \right\}$$

$$= 1 + \frac{\sin t}{a} \int_0^t u(z) \cos z dz - \frac{\cos t}{a} \int_0^t u(z) \sin z dz$$

$$u'(t) = \frac{\cos t}{a} \int_0^t u(z) \cos z dz + \frac{\sin t}{a} u(t) \cos t$$

$$+ \frac{\sin t}{a} \int_0^t u(z) \sin z dz - \frac{\cos t}{a} u(t) \sin t$$

$$u''(t) = \left[-\frac{\sin t}{a} \int_0^t u(z) \cos z dz + \frac{\cos t}{a} u(t) \cos t + \frac{\cos t}{a} \int_0^t u(z) \sin z dz + \frac{\sin t}{a} u(t) \sin t \right] = \frac{u(t)}{a}$$

$$- (u(t) - 1)$$

$$\therefore u'' = -u + 1 + \frac{u}{a} = \left(\frac{1}{a} - 1\right)u + 1$$

$$u(0) = 1$$

$$u(\pi) = 1 + \frac{1}{a} \int_0^\pi u(z) \frac{\sin(\pi - z)}{\sin z} dz$$

No.

$$(i) a_i^T d \leq 0 (\forall i) \Rightarrow d = 0$$

Date

$$d \neq 0$$

$$\Rightarrow a_i^T d > 0 (\exists i)$$

$$\forall v \in P, x^1 \in P, x^2 \in P, v = \frac{1}{2}x^1 + \frac{1}{2}x^2, x^1 \neq x^2$$

$$a_i^T v \leq b_i$$

$$a_i^T x^1 \leq b_i \quad (i=1, \dots, m)$$

$$a_i^T x^2 \leq b_i$$

$$a_i^T v = b_i \quad (i \in I(v))$$

$$a_i^T x^1 = b_i \quad (i \in I(x^1))$$

$$a_i^T x^2 = b_i \quad (i \in I(x^2))$$

$$\frac{a_i^T (x^1 - x^2) \leq 0}{x^1 - x^2 \neq 0} \quad (i=1, \dots, m) \Rightarrow x^1 \succeq x^2$$

$$a_i^T \frac{1}{2}x^1 \leq \frac{1}{2}b_i$$

$$a_i^T \frac{1}{2}x^2 \leq \frac{1}{2}b_i$$

$$a_i^T \left(\frac{1}{2}x^1 + \frac{1}{2}x^2 \right) \leq b_i \quad (i \in I(x^1) \cap I(x^2))$$

$$a_i^T (x^1 - x^2) \neq 0 \quad (i \in I(x^1) \cap I(x^2))$$