THE GRAINGER COLLEGE OF ENGINEERING

CS 521

Technological Foundations of Blockchain and Cryptocurrency

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Topic 2 – Basic Crypto Primitives

ILLINOIS

Thanks!

To Professors

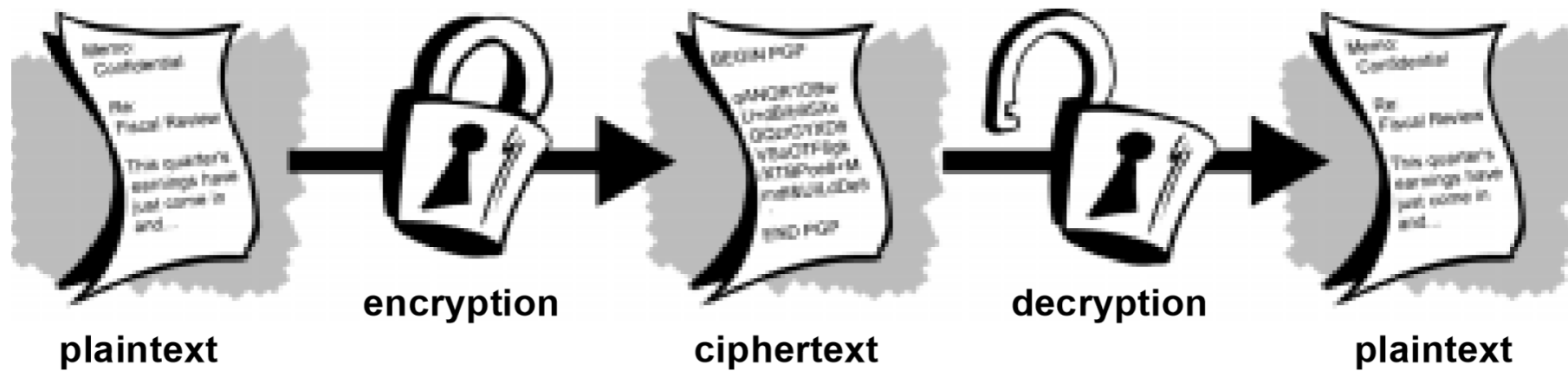David Tse (Stanford)

Sriram Viswanath (UT Austin)

Sreeram Kannan (UW – now at EigenLayer)

Some crypto primitives

- Encryption and Signatures

- Cryptographic Hash Functions

- Hash Accumulators
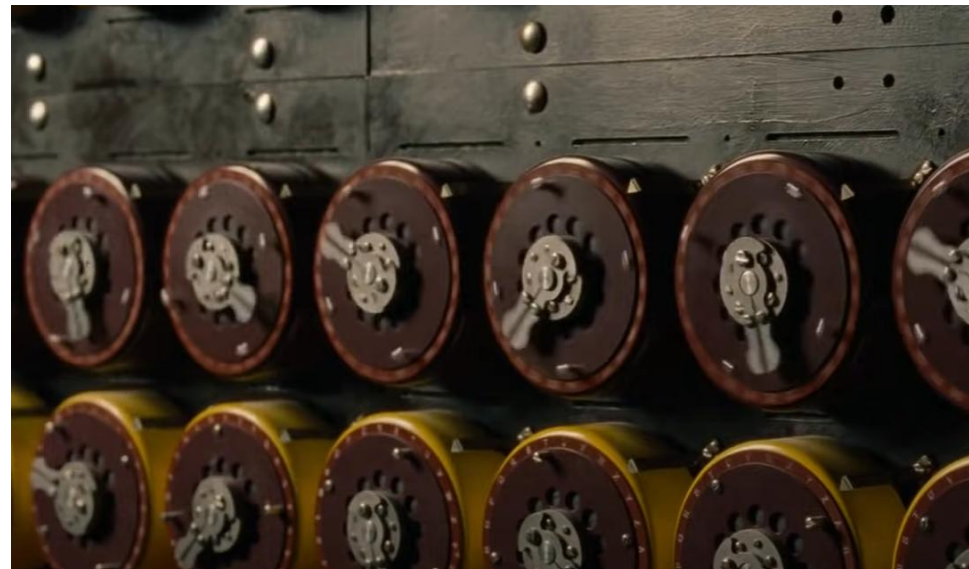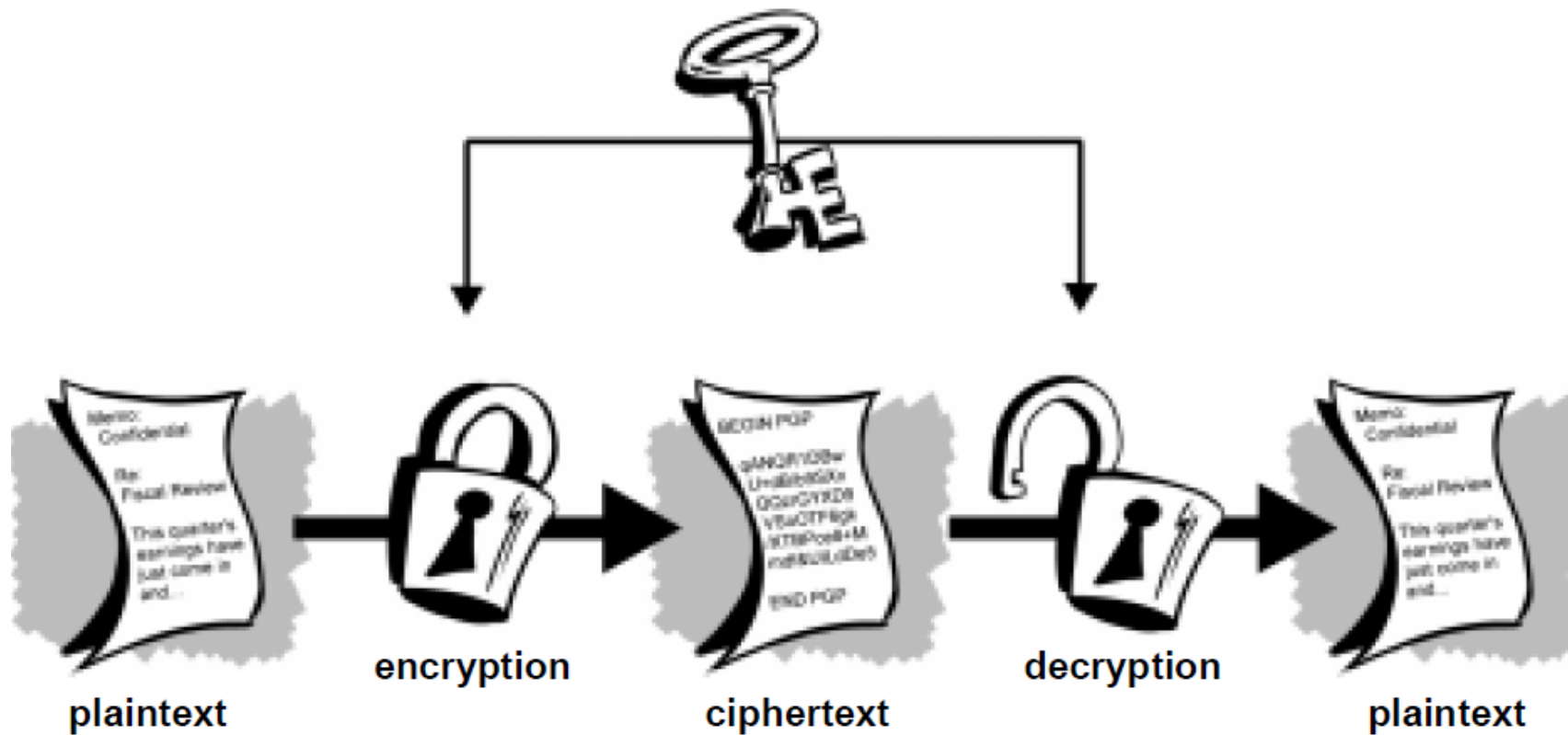 - Blockchain
  - Merkle trees

Basic Encryption

plaintext   encryption   ciphertext   decryption   plaintext

hello $\xrightarrow{\text{Encryption}}$ lipps $\xrightarrow{\text{Decryption}}$ hello

plaintext   *ciphertext*   *plaintext*

Cypher: Offset the Alphabet
Key: 4

Scene from "Breaking the Enigma Code"

https://youtu.be/zZuqLLdx2YQ

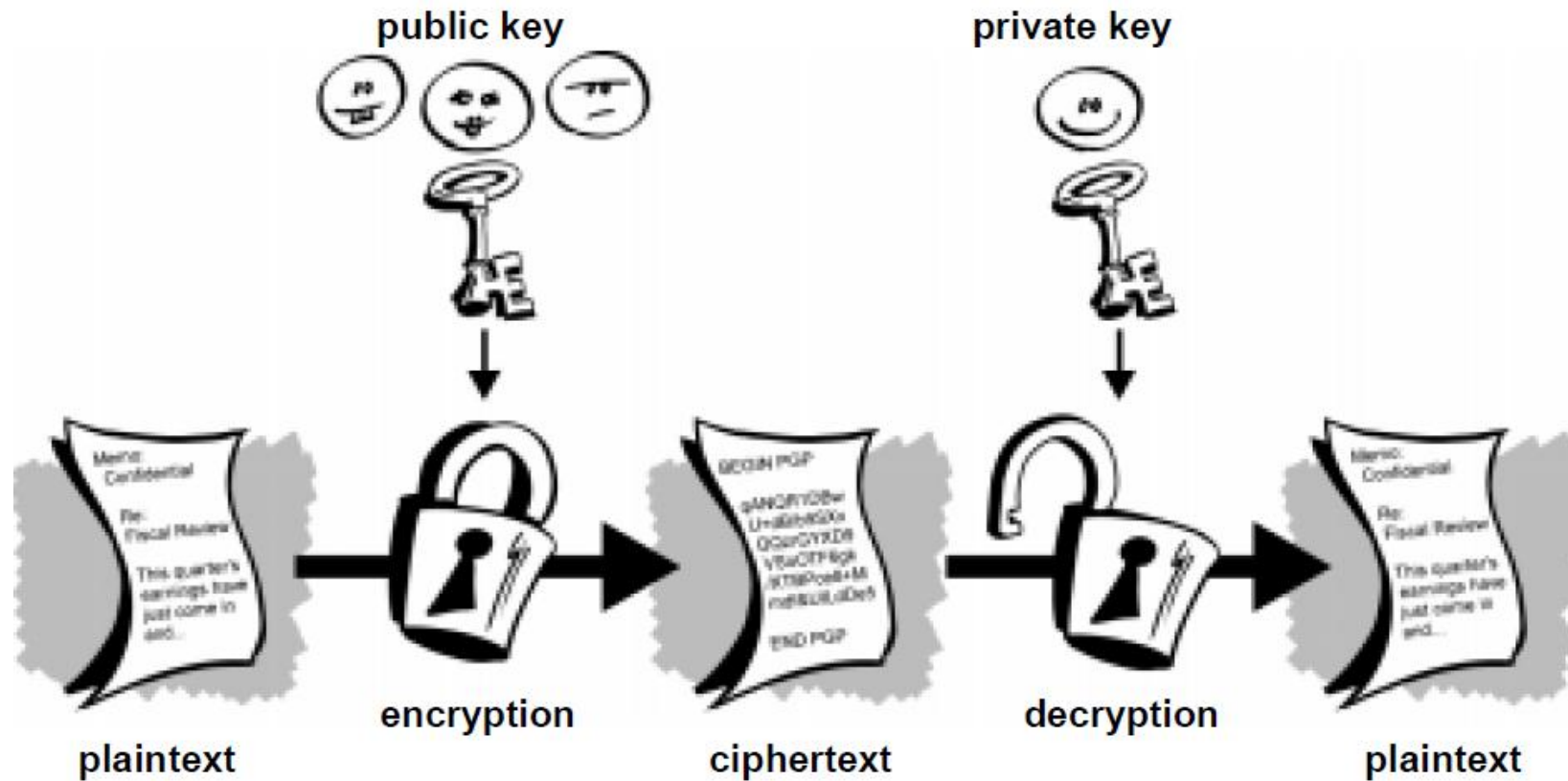# Symmetric (aka Secret-Key) Cryptography

How Secret-Key Cryptography Works

- **Single Shared Key** – Both sender and receiver use the same secret key for encryption and decryption

- **Key Distribution** – The shared key must be securely exchanged between parties before communication

- **Fast Performance** – Symmetric algorithms are computationally efficient, ideal for encrypting large amounts of data

- **Common Algorithms** – Examples include AES (Advanced Encryption Standard), DES, and 3DES

Pros and Cons of Secret-Key Cryptography

✓ High performing – fast, especially if the data is not going to be transmitted

✓ Can be implemented in hardware and software

✗ Secure key distribution is difficult, requires trust and secrecy between the parties as well as trust for the "distribution mechanism" if the parties are not in the same location

Asymmetric (aka Public-Key) Cryptography

How Public-Key Cryptography Works

- **Key Pair** – Each party has a public key (shared openly) and a private key (kept secret)

- **No Key Exchange Required** – Public keys can be freely distributed; only the private key must remain secret

- **Asymmetric Encryption** – Data encrypted with one key can only be decrypted with the other key in the pair

  - **Confidentiality** – Encrypt with recipient's public key; only they can decrypt with their private key

  - **Authentication** – Encrypt with your private key; anyone can verify it came from you using your public key

- **Common Algorithms** – Examples include RSA, Elliptic Curve Cryptography (ECC), and Diffie-Hellman

Pros and Cons of Public-Key Cryptography

✓ People can exchange messages securely without a security arrangement

✓ Makes secure message exchange available to a wider group of people

✗ Does not ensure foolproof identity of the sender

Digital Signatures

Digital Signatures
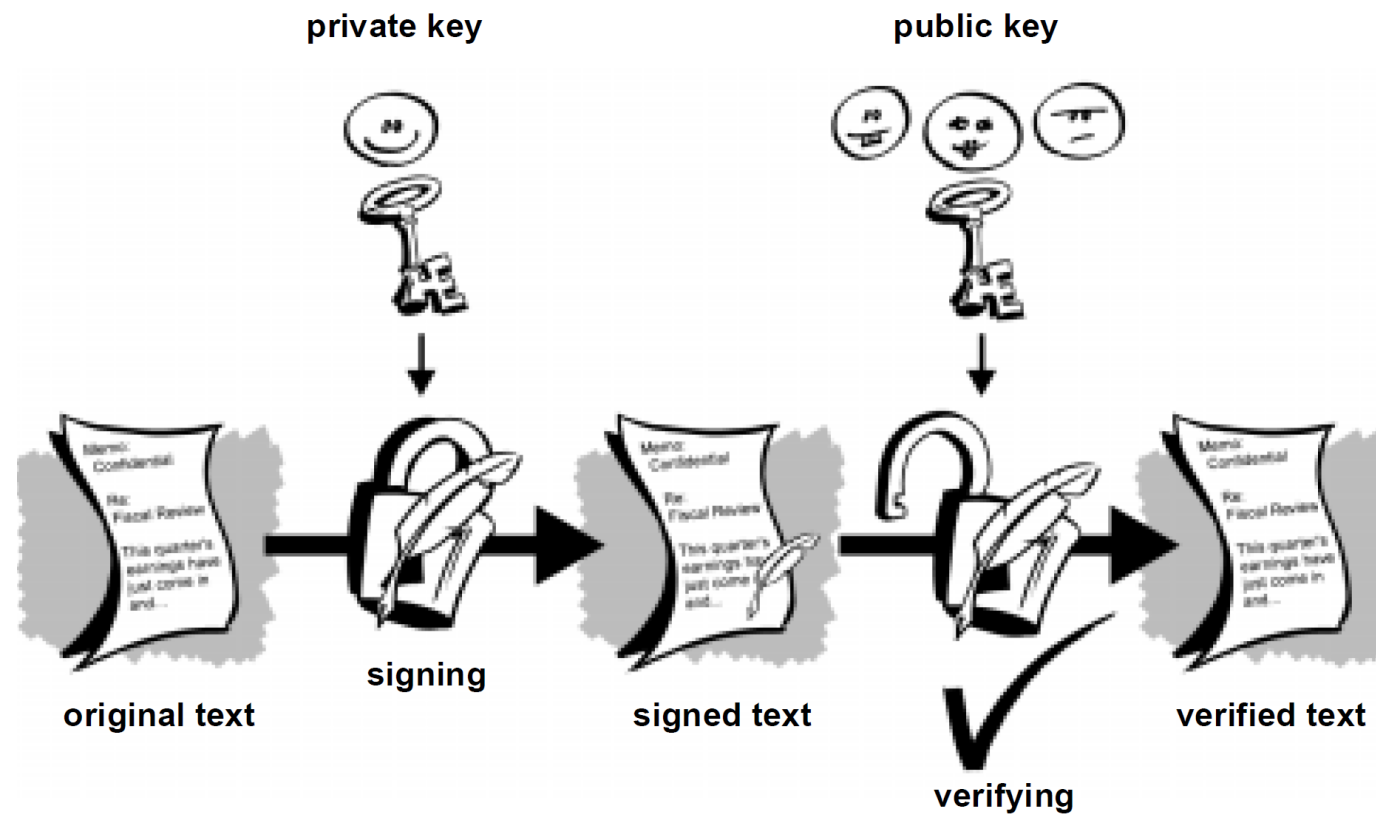
- **Key generation**
  (`secretkey`,`publickey`) =
  Generatekeys`(keysize)`

- Randomized function

- **Signature**
  `Sig =`
  sign`(secretkey, message)`

- **Verification**
  verify`(publickey,Sig,message)`

Unforgeable Signatures

- **Unforgeable**

Computationally hard to generate a verifiable signature without knowing the secret key

- **ECDSA**

Elliptic Curve Digital Signature Algorithms

Cryptographically secure against an adaptive adversary

Decentralized Identity Management

- Public keys are your identity
  - *address* in Bitcoin/blockchain terminology

- Can create multiple identities
  - (`publickey`, `secretkey`) pairs
  - Publish `publickey`
  - Sign using `secretkey`

- Can create oneself

- Verifiable by others

Hash Functions
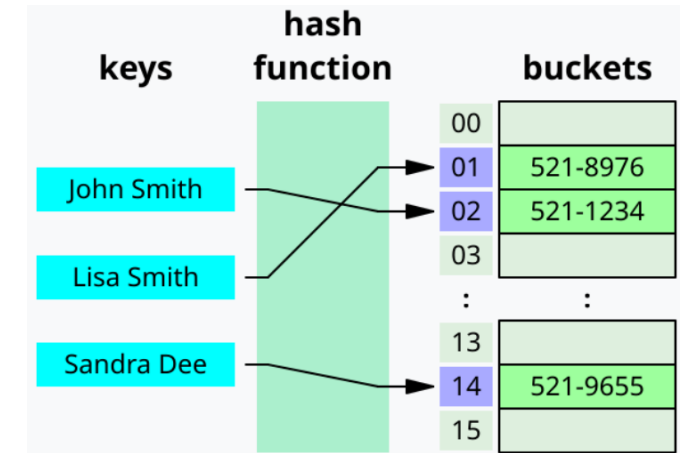
Defining Properties:

- Arbitrary sized inputs
- Fixed size deterministic output
- Efficiently computable
- Minimize collisions

Canonical application:

- Hash Tables
- Store and retrieve data records

Example: Hash Functions

- Division hashing

$$y = x \mod 2^{256}$$

- Uniform output

- Simple deterministic function

- Collision resistant

Cryptographic Hash Functions

Extra Properties:

- Adversarial collision resistance
  - Birthday paradox
- One way function
- Specialized one way function

Canonical applications:

- Message digest
- Commitments
- Puzzle generation
- Mining process

Hashing Algorithms

NSA 2001

No Collisions (yet)

SHA2 (Secure Hashing Algorithm)
- SHA2 takes strings of arbitrary length and generates a unique and irreversible 256 (SHA256) or 512 (SHA512) bit strings (SHA2 is the successor to SHA1 that generated 160 bit strings)
- SHA1 was derived from MD4

MD5 (Message Digest)
- MD5 is also a "child" of MD4 and produces a 128 bit output string
- MD5 works by chaining a "compression function

Collisions found!

Basic building blocks together
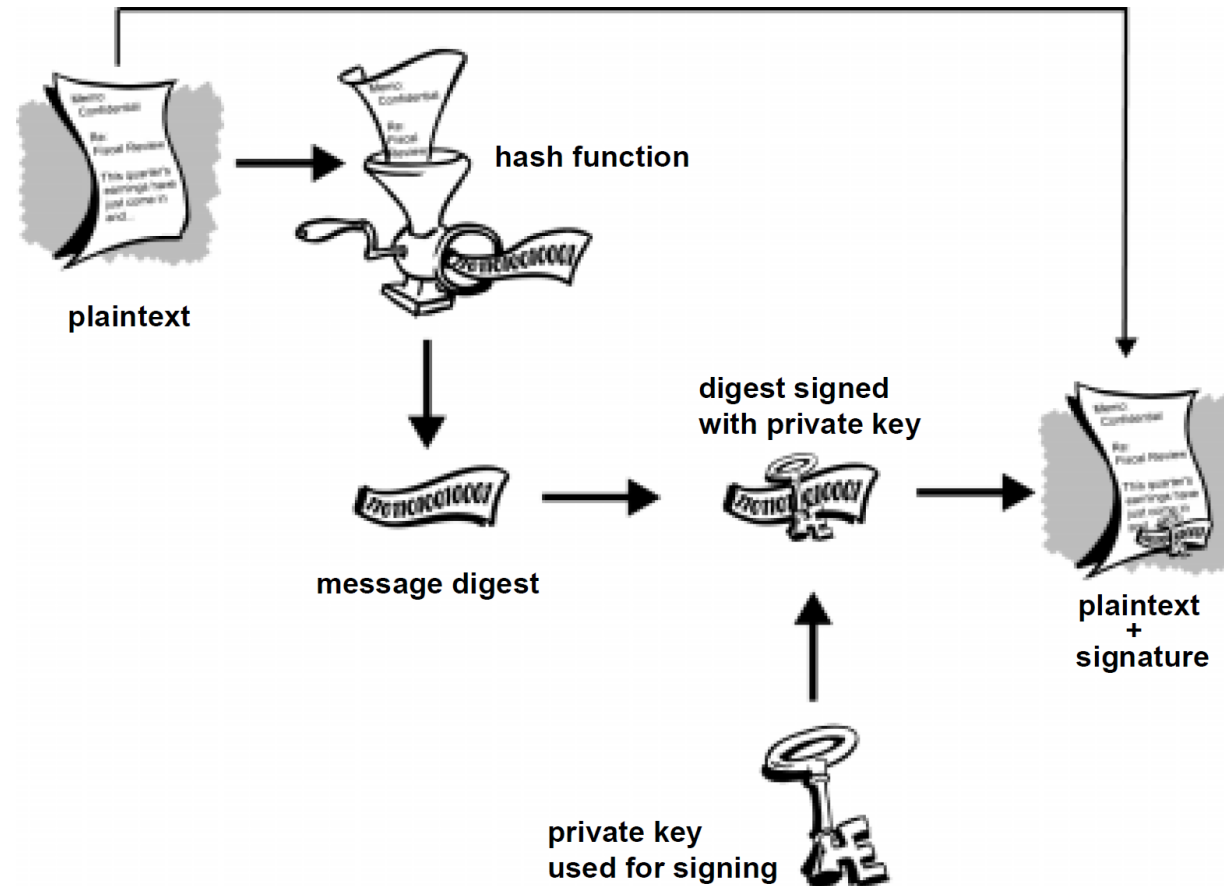
Hash Pointer

- **Pointer to:**

  location of information

  + hash of the information

- **Regular pointer**
  - retrieve information

- **Hash pointer**
  - retrieve information and verify the information has not changed

- Regular pointers
  - Used to build data structures
    - linked lists, binary trees, etc

- Hash pointers
  - Can also be used to build data structures
  - Crucially useful for blockchains!
    - Blockchain = hash pointer based data structure

Blockchain: a linked list via hash pointers

- **Block**: Header + Data
- **Header:** hash pointer to
     location of previous block
   + hash of the previous block
- **Data**: information specific to
   the block (e.g., transactions)

- **Application**: tamper evident information log
- Head of the chain being known is enough to find tamper evidence in any internal block
- Hence the phrase: **block chain blockchain**

Merkle Tree

Binary tree of hash pointers

- Retain only the tree root

- Tamper of any data in the bottom of the tree is evident

- **Proof of Membership**

- **Proof of Non-membership**

Merkle Trees

- **Block**: Header + Data

- **Header:** Pointer to
     location of previous block
  + hash of the previous block

- **Data**
  – block specific information