

Sum of forces:

$$\sum F_x = F_{fx} + F_{fx} \cdot \cos(\delta) - F_{fy} \cdot \sin(\delta)$$

$$\sum F_y = F_{fy} + F_{fy} \cdot \cos(\delta) + F_{fx} \cdot \sin(\delta)$$

$$\sum \tau = I \cdot \alpha = F \cdot d = L_r (F_{fy}) - L_f (F_{fx} \sin \delta + F_{fy} \sin \delta)$$

\downarrow moment of inertia \downarrow angular acceleration

Acceleration equations

$$\begin{aligned} \ddot{x} &= \frac{(F_{fx} + F_{fx} \cos(\delta) - F_{fy} \sin(\delta))}{m} + \dot{y} \dot{\psi} \\ \ddot{y} &= \frac{(F_{fy} + F_{fx} \sin(\delta) + F_{fy} \cos(\delta))}{m} - \dot{x} \dot{\psi} \\ \ddot{\psi} &= \frac{(L_r (F_{fy}) - L_f (F_{fx} \sin \delta + F_{fy} \sin \delta))}{I} \end{aligned}$$

Simulink structure

<3 Functions>

1. Calculating the $\ddot{x}, \ddot{y}, \ddot{\psi}$

Inputs: Steering angle (δ), F_{fx} , F_{fy} , F_{fx} , F_{fy}

Outputs: \ddot{x} , \ddot{y} , $\ddot{\psi}$

2. Deriving the slip angle using the steering angle

Inputs: Steering angle (δ), $\dot{\psi}$, \dot{x} , \dot{y}

Outputs: F_{fx} , F_{fy}

3. Changing to World coordinate system

Inputs: $\dot{\psi}$, \dot{x} , \dot{y}

Outputs: velocities & body slip angle

PID controllers (Proportional, Integral, Derivative)

K_p K_i K_d

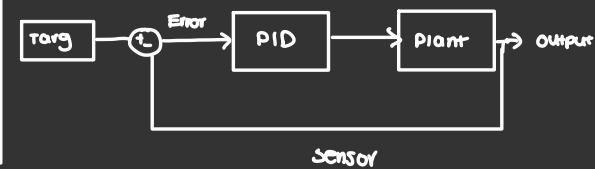
$$F_y = K_y a \cdot \alpha$$

$$F_x = K_x k \cdot \alpha$$

If current value = 700m,

Target value = 1000m

→ Error = 300



Simulink structure

<3 Functions>

1. Calculating the $\ddot{x}, \ddot{y}, \ddot{\psi}$

Inputs: Steering angle (δ), F_{fx} , F_{fy} , F_{rx} , F_{ry}

Outputs: $d\dot{\psi}$, $d\dot{p}_x$, $d\dot{p}_y$

2. Deriving the slip angle using the steering angle

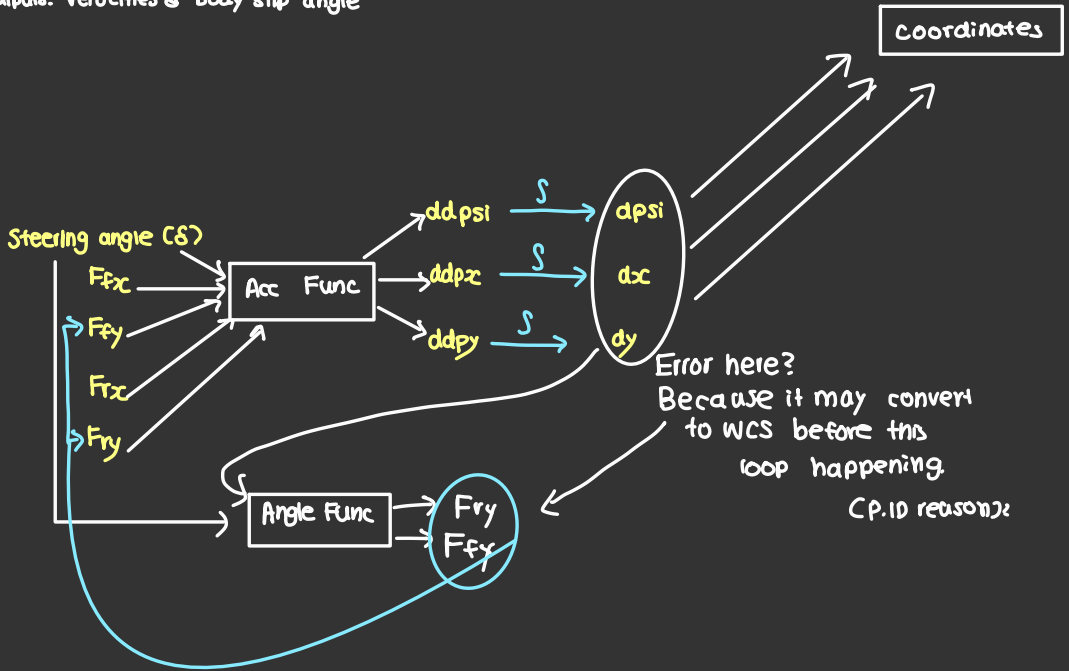
Inputs: Steering angle (δ), $d\psi$, $d\dot{x}$, $d\dot{y}$

Outputs: F_{ry} , F_{fy}

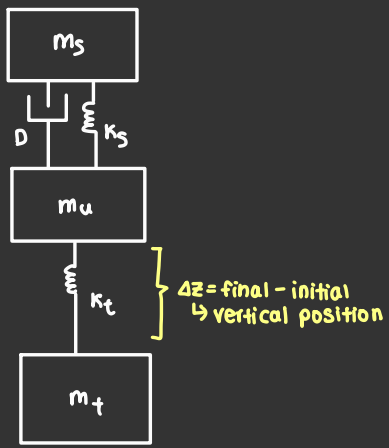
3. Changing to World coordinate system

Inputs: $d\psi$, $d\dot{y}$, $d\dot{x}$

Outputs: velocities & body slip angle

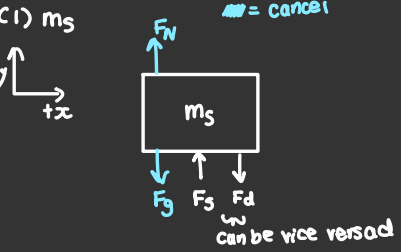


→ 1/4 of car
 → Focusing on vertical motion



Using Newton's second law to derive acceleration:

1) m_s



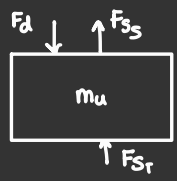
$\Rightarrow m a = \pm F_s \mp F_d$
 $m a = \pm k_s \Delta z \mp d \dot{z}$
 $m a = \frac{k_s (z_u - z_s) - d (z_u - z_s)}{m}$

spring equation ($k \Delta x$)

damper constant

추가 설명 필요

2)



$\Rightarrow m_u a = \pm F_{s_s} \pm F_{s_t} \mp F_d$
 $= \pm k_s \Delta z \pm k_t \Delta z \mp d \dot{z}$
 $= \frac{k_s (z_s - z_u) + k_t (z_u - z_t) - d (z_s - z_u)}{m}$

3)



$\Rightarrow m_t a = \pm F_{s_t}$
 $= \pm k_t \Delta z$
 $= \frac{k_t (z_t - z_u)}{m}$