PHYS 2310 Engineering Physics I Formula Sheets

Chapters 1-18

Chapter 1/Important Numbers

Units for SI Base Quantities

Quantity	Unit Name	Unit Symbol
Length	Meter	M
Time	Second	S
Mass (not weight)	Kilogram	kg

Common Conversions

1 kg or 1 m	1000 g or m	1 m	$1 \times 10^6 \mu m$
1 m	100 cm	1 inch	2.54 cm
1 m	1000 mm	1 day	86400 seconds
1 second	1000 milliseconds	1 hour	3600 seconds
1 m	3.281 ft	360°	2π rad

Important Constants/Measurements

Mass of Earth	$5.98 \times 10^{24} \text{ kg}$
Radius of Earth	$6.38 \times 10^6 \text{m}$
1 u (Atomic Mass Unit)	$1.661 \times 10^{-27} \text{ kg}$
Density of water	$1 g/cm^3$ or $1000 kg/m^3$
g (on earth)	9.8m/s^2

Density Common geometric Formulas

Circumference	$C=2\pi r$	Area circle	$A = \pi r^2$
Surface area (sphere)	$SA = 4\pi r^2$	Volume (sphere)	$V = \frac{4}{3}\pi r^3$
Volume (rectangul	ar solid)	V = l $V = area$	· w · h thickness

Chapter 2

Velocity

Average Velocity	$V_{avg} = rac{displacement}{time} = rac{\Delta x}{\Delta t}$	2.2
Average Speed	$s_{avg} = \frac{total\ distance}{time}$	2.3
Instantaneous Velocity	$v = \lim_{\Delta t \to 0} \frac{\Delta \overline{x}}{\Delta t} = \frac{dx}{dt}$	2.4

Acceleration

Average Acceleration	$a_{avg} = \frac{\Delta v}{\Delta t}$	2.7
Instantaneous Acceleration	$a = \frac{dv}{dt} = \frac{d^2x}{dt^2}$	2.8 2.9

Motion of a particle with constant acceleration

$v = v_0 + at$	2.11
$\Delta x = \frac{1}{2}(v_0 + v)t$	2.17
$\Delta x = v_0 t + \frac{1}{2} a t^2$	2.15
$v^2 = v_0^2 + 2a\Delta x$	2.16

Adding Vectors Geometrically	$\vec{a} + \vec{b} = \vec{b} + \vec{a}$	3.2
Adding Vectors Geometrically (Associative Law)	$(\vec{a} + \vec{b}) + \vec{c} = \vec{a} + (\vec{b} + \vec{c})$	3.3
Components of Vectors	$a_x = a cos \theta$ $a_y = a sin \theta$	3.5
Magnitude of vector	$ a = a = \sqrt{a_x^2 + a_y^2}$	3.6
Angle between x axis and vector	$tan\theta = \frac{a_y}{a_x}$	3.6
Unit vector notation	$\vec{a} = a_x \hat{\imath} + a_y \hat{\jmath} + a_z \hat{k}$	3.7
Adding vectors in Component Form	$r_x = a_x + b_x$ $r_y = a_y + b_y$ $r_z = a_z + b_z$	3.10 3.11 3.12
Scalar (dot product)	$\vec{a} \cdot \vec{b} = abcos\theta$	3.20
Scalar (dot product)	$\vec{a} \cdot \vec{b} = (a_x \hat{\imath} + a_y \hat{\jmath} + a_z \hat{k}) \cdot (b_x \hat{\imath} + b_y \hat{\jmath} + b_z \hat{k})$ $\vec{a} \cdot \vec{b} = a_x b_x + a_y b_y + a_z b_z$	3.22
Projection of \vec{a} on \vec{b} or component of \vec{a} on \vec{b}	$\frac{\vec{a} \cdot \vec{b}}{ b }$	
Vector (cross) product magnitude	$c=absin\phi$	3.24
Vector (cross product)	$\vec{a}x\vec{b} = (a_x\hat{\imath} + a_y\hat{\jmath} + a_z\hat{k})x(b_x\hat{\imath} + b_y\hat{\jmath} + b_z\hat{k})$ $= (a_yb_z - b_ya_z)\hat{\imath} + (a_zb_x - b_za_x)\hat{\jmath}$ $+ (a_xb_y - b_xa_y)\hat{k}$ \mathbf{or} $\vec{a}x\vec{b} = \det \begin{vmatrix} \hat{\imath} & \hat{\jmath} & \hat{k} \\ a_x & a_y & a_z \\ b_x & b_y & b_z \end{vmatrix}$	3.26

Chapter 4

Position vector	$\vec{r} = x\hat{\imath} + y\hat{\jmath} + z\hat{k}$	4.4
displacement	$\Delta \vec{r} = \Delta x \hat{\imath} + \Delta y \hat{\jmath} + \Delta z \hat{k}$	4.4
Average Velocity	$\vec{V}_{avg} = \frac{\Delta x}{\Delta t}$	4.8
Instantaneous Velocity	$\vec{v} = \frac{d\vec{r}}{dt} = v_x \hat{\imath} + v_y \hat{\jmath} + v_z \hat{k}$	4.10 4.11
Average Acceleration	$\vec{a}_{avg} = \frac{\Delta \vec{v}}{\Delta t}$	4.15
Instantaneous Acceleration	$\vec{a} = \frac{d\vec{v}}{dt}$ $\vec{a} = a_x \hat{\imath} + a_y \hat{\jmath} + a_z \hat{k}$	4.16 4.17

Projectile Motion

	$v_{y} = v_{0} sin\theta_{0} - gt$	4.23
Δx	$c = v_0 cos\theta t + \frac{1}{2}a_x t^2$	4.21
	$\Delta x = v_0 cos\theta t if a_x = 0$	
Δ	$y = v_0 sin\theta t - \frac{1}{2}gt^2$	4.22
v_y^2	$= (v_0 \sin \theta_0)^2 - 2g\Delta y$	4.24
	$v_{y} = v_{0} sin\theta_{0} - gt$	4.23
Trajectory	$y = (tan\theta_0)x - \frac{gx^2}{2(v_0cos\theta_0)^2}$	4.25
Range	$R = \frac{v_0^2}{g}\sin(2\theta_0)$	4.26

Relative Motion	$\overrightarrow{v_{AC}} = \overrightarrow{v_{AB}} + \overrightarrow{v_{BC}}$ $\overrightarrow{a_{AB}} = \overrightarrow{a_{BA}}$	4.44 4.45
Uniform Circular	$a = \frac{v^2}{T} = \frac{2\pi r}{T}$	4.34
Motion	r - v	4.35

Newton's Second Law

General	$ec{F}_{net}=mec{a}$	5.1
Component form	$egin{aligned} F_{net,x} &= ma_x \ F_{net,y} &= ma_y \ F_{net,z} &= ma_y \end{aligned}$	5.2

Gravitational Force

Gravitational Force	$F_g = mg$	5.8
Weight	W = mg	5.12

Chapter 6

Friction

Static Friction (maximum)	$\vec{f}_{s,max} = \mu_s F_N$	6.1
Kinetic Frictional	$\vec{f}_k = \mu_k F_N$	6.2

Drag Force	$D = \frac{1}{2}C\rho Av^2$	6.14
Terminal velocity	$v_t = \sqrt{rac{2F_g}{C ho A}}$	6.16

Centripetal acceleration	$a = \frac{v^2}{R}$	6.17
Centripetal Force	$F = \frac{mv^2}{R}$	6.18

Kinetic Energy	$K = \frac{1}{2}mv^2$	7.1
Work done by constant Force	$W = Fdcos\theta = \vec{F} \cdot \vec{d}$	7.7 7.8
Work- Kinetic Energy Theorem	$\Delta K = K_f - K_0 = W$	7.10
Work done by gravity	$W_g=mgdcos\phi$	7.12
Work done by lifting/lowering object	$\Delta K = W_a + W_g$ $W_a = applied \ Force$	7.15
Spring Force (Hooke's law)	$ec{F_S} = -kec{d}$ $F_{\chi} = -kx$ (along x-axis)	7.20 7.21
Work done by spring	$W_{s} = \frac{1}{2}kx_{i}^{2} - \frac{1}{2}kx_{f}^{2}$	7.25
Work done by Variable Force	$W = \int_{x_i}^{x_f} F_x dx + \int_{y_i}^{y_f} F_y dy + \int_{z_i}^{z_f} F_z dz$	7.36
Average Power (rate at which that force does work on an object)	$P_{avg} = \frac{W}{\Delta t}$	7.42
Instantaneous Power	$P = \frac{dW}{dt} = FV\cos\theta = \vec{F} \cdot \vec{v}$	7.43 7.47

Chapter 8

Potential Energy	$\Delta U = -W = -\int_{xi}^{xf} F(x)dx$	8.1 8.6
Gravitational Potential Energy	$\Delta U = mg\Delta y$	8.7
Elastic Potential Energy	$U(x) = \frac{1}{2}kx^2$	8.11
Mechanical Energy	$E_{mec} = K + U$	8.12
Principle of conservation of mechanical energy	$K_1 + U_1 = K_2 + U_2$ $E_{mec} = \Delta K + \Delta U = 0$	8.18 8.17
Force acting on particle	$F(x) = -\frac{dU(x)}{dx}$	8.22
Work on System by external force With no friction	$W = \Delta E_{mec} = \Delta K + \Delta U$	8.25 8.26
Work on System by external force With friction	$W = \Delta E_{mec} + \Delta E_{th}$	8.33
Change in thermal energy	$\Delta E_{th} = f_k dcos\theta$	8.31
Conservation of Energy *if isolated W=0	$W = \Delta E = \Delta E_{mec} + \Delta E_{th} + \Delta E_{int}$	8.35
Average Power	$P_{avg} = \frac{\Delta E}{\Delta t}$	8.40
Instantaneous Power	$P_{avg} = \frac{\Delta E}{\Delta t}$ $P = \frac{dE}{dt}$	8.41

^{**}In General Physics, Kinetic Energy is abbreviated to KE and Potential Energy is PE

Impulse and Momentum

Impulse	$ec{J} = \int_{t_i}^{t_f} ec{F}(t) dt$ $J = F_{net} \Delta t$	9.30
•	$J = F_{net} \Delta t$	9.35
Linear Momentum	$ec{p}=mec{v}$	9.22
Impulse-Momentum Theorem	$ec{J} = \Delta ec{p} = ec{p}_f - ec{p}_i$	9.31 9.32
meorem		9.32
Newton's 2 nd law	$\vec{F}_{net} = \frac{d\vec{p}}{dt}$	9.22
	$\vec{F} - m\vec{q}$	
	$ec{F}_{net} = m ec{a}_{com} \ ec{P} = M ec{v}_{com}$	9.14
System of Particles		9.25
,	$ec{F}_{net} = rac{d \overrightarrow{P}}{dt}$	9.27
	$r_{net} \equiv \frac{1}{dt}$	

Collision

Final Velocity of 2 objects in a head-on collision where one	$v_{1f} = \left(\frac{m_1 - m_2}{m_1 + m_2}\right) v_{1i}$	9.67
object is initially at rest 1: moving object 2: object at rest	$v_{2f} = \left(\frac{2m_1}{m_1 + m_2}\right) v_{1i}$	9.68
Conservation of Linear Momentum (in 1D)	$ec{P}=constant \ ec{P}_i=ec{P}_f$	9.42 9.43
Elastic Collision	$\vec{p}_{1i} + \vec{p}_{2i} = \vec{p}_{1f} + \vec{p}_{2f}$ $m_1 v_{i1} + m_2 v_{12} = m_1 v_{f1} + m_2 v_{f2}$ $K_{1i} + K_{2i} = K_{1f} + K_{2f}$	9.50 9.51 9.78

Collision continued...

Inelastic Collision	$m_1 v_{01} + m_2 v_{02} = (m_1 + m_2) v_f$	
Conservation of Linear Momentum (in 2D)	$\vec{P}_{1i} + \vec{P}_{2i} = \vec{P}_{1f} + \vec{P}_{2f}$	9.77
Average force	$F_{avg} = -\frac{n}{\Delta t} \Delta p = -\frac{n}{\Delta t} m \Delta v$ $F_{avg} = -\frac{\Delta m}{\Delta t} \Delta v$	9.37 9.40

Center of Mass

Center of mass location	$\vec{r}_{com} = \frac{1}{M} \sum_{i=1}^{n} m_i \vec{r}_i$	9.8
Center of mass velocity	$\vec{v}_{com} = \frac{1}{M} \sum_{i=1}^{n} m_i \vec{v}_i$	

Rocket Equations

Thrust (Rv _{rel})	$Rv_{rel} = Ma$	9.88
Change in velocity	$\Delta v = v_{rel} ln rac{M_i}{M_f}$	9.88

Angular displacement (in radians	$\theta = \frac{s}{r}$ $\Delta\theta = \theta_2 - \theta_1$	10.1 10.4
Average angular velocity	$\omega_{avg} = \frac{\Delta \theta}{\Delta t}$	10.5
Instantaneous Velocity	$\omega = \frac{d\theta}{dt}$	10.6
Average angular acceleration	$lpha_{avg} = rac{\Delta \omega}{\Delta t}$	10.7
Instantaneous angular acceleration	$\alpha = \frac{d\omega}{dt}$	10.8

Rotational Kinematics

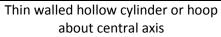
$\omega = \omega_0 + \alpha t$	10.12
$\Delta\theta = \omega_0 t + \frac{1}{2}\alpha t^2$	10.13
$\omega^2 = \omega_0^2 + 2\alpha\Delta\theta$	10.14
$\Delta\theta = \frac{1}{2}(\omega + \omega_0)t$	10.15
$\Delta\theta = \omega t - \frac{1}{2}\alpha t^2$	10.16

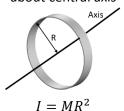
Relationship Between Angular and Linear Variables

Velocity	$v = \omega r$	10.18
Tangential Acceleration	$a_t = \alpha r$	10.19
Radical component of \vec{a}	$a_r = \frac{v^2}{r} = \omega^2 r$	10.23
Period	$T = \frac{2\pi r}{v} = \frac{2\pi}{\omega}$	10.19 10.20

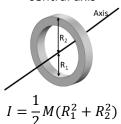
Rotation inertia	$I = \sum m_i r_i^2$	10.34
Rotation inertia (discrete particle system)	$I = \int r^2 dm$	10.35
Parallel Axis Theorem h=perpendicular distance between two axes	$I = I_{com} + Mh^2$	10.36
Torque	$\tau = rF_t = r_{\perp}F = rFsin\theta$	10.39- 10.41
Newton's Second Law	$ au_{net} = I lpha$	10.45
Rotational work done by a toque	$W=\int_{ heta_i}^{ heta_f} au d heta \ W= au \Delta heta \ (au ext{ constant})$	10.53 10.54
Power in rotational motion	$P = \frac{dW}{dt} = \tau \omega$	10.55
Rotational Kinetic Energy	$K = \frac{1}{2}I\omega^2$	10.34
Work-kinetic energy theorem	$\Delta K = K_f - K_i = \frac{1}{2} I \omega_f^2 - \frac{1}{2} I \omega_i^2 = W$	10.52

Moments of Inertia I for various rigid objects of Mass M

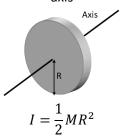




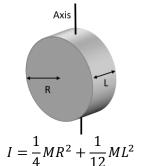
Annular cylinder (or ring) about central axis



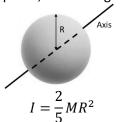
Solid cylinder or disk about central axis



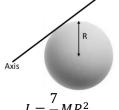
Solid cylinder or disk about central diameter



Solid Sphere, axis through center

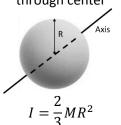


Solid Sphere, axis tangent to surface

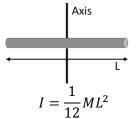


$$I = \frac{7}{5}MR^2$$

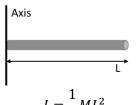
Thin Walled spherical shell, axis through center



Thin rod, axis perpendicular to rod and passing though center



Thin rod, axis perpendicular to rod and passing though end



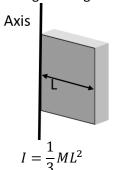
 $I = \frac{1}{3}ML^2$

Thin Rectangular sheet (slab), axis parallel to sheet and passing though center of the other edge

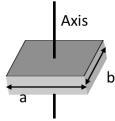


 $I = \frac{1}{12}ML^2$

Thin Rectangular sheet (slab, axis along one edge



Thin rectangular sheet (slab) about perpendicular axis through center



 $I = \frac{1}{12}M(a^2 + b^2)$

Rolling Bodies (wheel)

Speed of rolling wheel	$v_{com} = \omega R$	11.2
Kinetic Energy of Rolling Wheel	$K = \frac{1}{2}I_{com}\omega^2 + \frac{1}{2}Mv_{com}^2$	11.5
Acceleration of rolling wheel	$a_{com} = \alpha R$	11.6
Acceleration along x-axis extending up the ramp	$a_{com,x} = -\frac{gsin\theta}{1 + \frac{I_{com}}{MR^2}}$	11.10

Torque as a vector

Torque	$ec{ au}=ec{r} imesec{F}$	11.14
Magnitude of torque	$ au=rF_{\perp}=r_{\perp}F=rFsin\phi$	11.15- 11.17
Newton's 2 nd Law	$ec{ au}_{net} = rac{dec{\ell}}{dt}$	11.23

Angular Momentum

Angular Momentum	$v\vec{\ell} = \vec{r} \times \vec{p} = m(\vec{r} \times \vec{v})$	11.18
Magnitude of Angular Momentum	$\ell = rmvsin\phi \ \ell = rp_{\perp} = rmv_{\perp}$	11.19- 11.21
Angular momentum of a system of particles	$ec{L} = \sum_{i=1}^{n} ec{\ell}_i$ $ec{ au}_{net} = rac{dec{L}}{dt}$	11.26 11.29

Angular Momentum continued

Angular Momentum of a rotating rigid body	$L = I\omega$	11.31
Conservation of angular momentum	$ec{L} = constant \ ec{L}_i = ec{L}_f$	11.32 11.33

Precession of a Gyroscope

Precession rate	$\Omega = \frac{Mgr}{I\omega}$	11.31
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Static Equilibrium

	$\vec{F}_{net} = 0$	12.3
	$ec{ au}_{net}=0$	12.5
If forces lie on the	$\vec{F}_{net,x} = 0$, $\vec{F}_{net,y} = 0$	12.7 12.8
xy-plane	$\vec{ au}_{net,z}=0$	12.9

Stress (force per unit area) Strain (fractional change in length)	$stress = modulus \times strain$	12.22
Stress (pressure)	$P = \frac{F}{A}$	
Tension/Compression E: Young's modulus	$\frac{F}{A} = E \frac{\Delta L}{L}$	12.23
Shearing Stress G: Shear modulus	$\frac{F}{A} = G \frac{\Delta x}{L}$	12.24
Hydraulic Stress B: Bulk modulus	$p = B \frac{\Delta V}{V}$	

Chapter 13

		,
Gravitational Force (Newton's law of gravitation)	$F = G \frac{m_1 m_2}{r^2}$	13.1
Principle of Superposition	$ec{F}_{1,net} = \sum_{i=2}^{n} ec{F}_{1i}$	13.5
Gravitational Force acting on a particle from an extended body	$ec{F}_1 = \int dec{F}$	13.6
Gravitational acceleration	$a_g = \frac{GM}{r^2}$	13.11
Gravitation within a spherical Shell	$F = \frac{GmM}{R^3}r$	13.19
Gravitational Potential Energy	$U = -\frac{GMm}{r}$	13.21
Potential energy on a system (3 particles)	$U = -\left(\frac{Gm_1m_2}{r_{12}} + \frac{Gm_1m_3}{r_{13}} + \frac{Gm_2m_3}{r_{23}}\right)$	13.22
Escape Speed	$v = \sqrt{\frac{2GM}{R}}$	13.28
Kepler's 3 rd Law (law of periods)	$T^2 = \left(\frac{4\pi^2}{GM}\right)r^3$	13.34
Energy for bject in circular orbit	$U = -\frac{GMm}{r} \ K = \frac{GMm}{2r}$	13.21 13.38
Mechanical Energy (circular orbit)	$E = -\frac{GMm}{2r}$	13.40
Mechanical Energy (elliptical orbit)	$E = -\frac{GMm}{2a}$	13.42

*Note: $G = 6.6704 \times 10^{-11} \ N \cdot m^2 / kg^2$

Density	$\rho = \frac{\Delta m}{\Delta V}$ $\rho = \frac{m}{V}$ ΔF	14.1 14.2
Pressure	$p=rac{\Delta F}{\Delta A}$ $p=rac{F}{A}$	14.3 14.4
Pressure and depth in a static Fluid P1 is higher than P2	$p_2 = p_1 + \rho g(y_1 - y_2)$ $p = p_0 + \rho g h$	14.7 14.8
Gauge Pressure	ho g h	
Archimedes' principle	$F_b = m_f g$	14.16
Mass Flow Rate	$R_m = \rho R_V = \rho A v$	14.25
Volume flow rate	$R_V = Av$	14.24
Bernoulli's Equation	$p + \frac{1}{2}\rho v^2 + \rho gy = constant$	14.29
Equation of continuity	$R_m = \rho R_V = \rho A v = constant$	14.25
Equation of continuity when $\rho_1=\rho_2$	$R_V = Av = constant$	14.24

Chapter 15

Frequency cycles per time	$f = \frac{1}{T}$	15.2
displacement	$x = x_m \cos(\omega t + \phi)$	15.3
Angular frequency	$\omega = \frac{2\pi}{T} = 2\pi f$	15.5
Velocity	$v = -\omega x_m \sin(\omega t + \phi)$	15.6
Acceleration	$a = -\omega^2 x_m \cos(\omega t + \phi)$	15.7
Kinetic and Potential Energy	$K = \frac{1}{2}mv^2 \ U = \frac{1}{2}kx^2$	
Angular frequency	$\omega = \sqrt{\frac{k}{m}}$	15.12
Period	$T = 2\pi \sqrt{\frac{m}{k}}$	15.13
Torsion pendulum	$T = 2\pi \sqrt{\frac{I}{k}}$	15.23
Simple Pendulum	$T = 2\pi \sqrt{\frac{L}{g}}$	15.28
Physical Pendulum	$T = 2\pi \sqrt{\frac{I}{mgL}}$	15.29
Damping force	$\vec{F}_d = -b\vec{v}$	
displacement	$x(t) = x_m e^{-\frac{bt}{2m}} \cos(\omega' t + \phi)$	15.42
Angular frequency	$\omega' = \sqrt{\frac{k}{m} - \frac{b^2}{4m^2}}$	15.43
Mechanical Energy	$E(t) \approx \frac{1}{2} k x_m^2 e^{-\frac{bt}{m}}$	15.44

Sinusoidal Waves

Mathematical form (positive direction)	$y(x,t) = y_m \sin(kx - \omega t)$	16.2
Angular wave number	$k = \frac{2\pi}{\lambda}$	16.5
Angular frequency	$\omega = \frac{2\pi}{T} = 2\pi f$	16.9
Wave speed	$v = \frac{\omega}{k} = \frac{\lambda}{T} = \lambda f$	16.13
Average Power	$P_{avg} = \frac{1}{2}\mu v\omega^2 y_m^2$	16.33

Traveling Wave Form	$y(x,t) = h(kx \pm \omega t)$	16.17
Wave speed on stretched string	$v = \sqrt{\frac{\tau}{\mu}}$	16.26
Resulting wave when 2 waves only differ by phase constant	$y'(x,t) = \left[2y_m \cos\left(\frac{1}{2}\phi\right)\right] \sin\left(kx - \omega t + \frac{1}{2}\phi\right)$	16.51
Standing wave	$y'(x,t) = [2y_m \sin(kx)]\cos(\omega t)$	16.60
Resonant frequency	$f = \frac{v}{\lambda} = n \frac{v}{2L} \text{ for n=1,2,}$	16.66

Sound Waves

Speed of sound wave	$v = \sqrt{\frac{B}{\rho}}$	17.3
displacement	$s = s_m \cos(kx - \omega t)$	17.12
Change in pressure	$\Delta p = \Delta p_m \sin(kx - \omega t)$	17.13
Pressure amplitude	$\Delta p_m = (v\rho\omega)s_m$	17.14

Interference

Phase difference	$\phi = \frac{\Delta L}{\lambda} 2\pi$	17.21
Fully Constructive Interference	$\phi=m(2\pi)$ for m=0,1,2 $rac{\Delta L}{\lambda}=0$,1,2	17.22 17.23
Full Destructive interference	$\phi = (2m + 1)\pi$ for m=0,12 $\frac{\Delta L}{\lambda} = .5,1.5,2.5$	17.24 17.25
Mechanical Energy	$E(t) \approx \frac{1}{2} k x_m^2 e^{-\frac{bt}{m}}$	15.44

Sound Intensity

Intensity	$I = \frac{P}{A}$ $I = \frac{1}{2}\rho v\omega^2 s_m^2$	17.26 17.27
Intensity -uniform in all directions	$I = \frac{P_{\rm S}}{4\pi r^2}$	17.29
Intensity level in decibels	$\beta = (10dB)\log\left(\frac{I}{I_o}\right)$	17.29
Mechanical Energy	$E(t) \approx \frac{1}{2}kx_m^2 e^{-\frac{bt}{m}}$	15.44

Standing Waves Patterns in Pipes

Standing wave frequency (open at both ends)	$f = \frac{v}{\lambda} = \frac{nv}{2L} \text{ for n=1,2,3}$	17.39
Standing wave frequency (open at one end)	$f = \frac{v}{\lambda} = \frac{nv}{4L} $ for n=1,3,5	17.41

Doppler Effect

	20 Pic: 2::001	
Source Moving toward stationary observer	$f' = f \frac{v}{v - v_s}$	17.53
Source Moving <i>away</i> from stationary observer	$f' = f \frac{v}{v + v_s}$	17.54
Observer moving toward stationary source	$f' = f \frac{v + v_D}{v}$	17.49
Observer moving <i>away</i> from stationary source	$f' = f \frac{v - v_D}{v}$	17.51

Shockwave

Half-angle $ heta$ of Mach	$\sin\theta = \frac{v}{-}$	17 57
cone	v_{s}	17.57

Temperature Scales

Fahrenheit to Celsius	$T_C = \frac{5}{9} (T_F - 32)$	18.8
Celsius to Fahrenheit	$T_F = \frac{9}{5}T_C + 32$	18.8
Celsius to Kelvin	$T = T_C + 273.15$	18.7

Thermal Expansion

Linear Thermal Expansion	$\Delta L = L\alpha \Delta T$	18.9
Volume Thermal Expansion	$\Delta V = V \beta \Delta T$	18.10

Heat

Heat and temperature change	$Q = C(T_f - T_i)$ $Q = cm(T_f - T_i)$	18.13 18.14
Heat and phase change	Q = Lm	18.16
Power	P=Q/t	
Power (Conducted)	$P_{cond} = \frac{Q}{t} = kA \frac{T_H - T_C}{L}$	18.32
Rate objects absorbs energy	$P_{abs} = \sigma \epsilon A T_{env}^4$	18.39
Power from radiation	$P_{rad} = \sigma \epsilon A T^4$	18.38

$$\sigma = 5.6704 \times 10^{-8} \, W/m^2 \cdot K^4$$

First Law of Thermodynamics

First Law of	$\Delta E_{int} = E_{int,f} - E_{int,i} = Q - W$	18.26
Thermodynamics	$dE_{int} = dQ - dW$	18.27

Note:

 ΔE_{int} Change in Internal Energy

Q (heat) is positive when the system absorbs heat and negative when it loses heat. **W** (work) is work done by system. W is positive when expanding and negative contracts because of an external force

Applications of First Law

Adiabatic (no heat flow)	$\begin{array}{c} Q=0 \\ \Delta E_{int} = -W \end{array}$
(constant volume)	W =0 $\Delta E_{int} = Q$
Cyclical process	$\Delta E_{int} = 0$ Q=W
Free expansions	$Q = W = \Delta E_{int} = 0$

Misc.