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# **DATA SCIENCE**

## **MODEL EVALUATION PROCEDURES**

Q: What's wrong with training error?

*Thought experiment:*

*Suppose we train our model using the entire dataset.*

*Q: How low can we push the training error?*

- We can make the model arbitrarily complex (effectively “memorizing” the entire training set).*

*A: Down to zero!*

Q: What's wrong with training error?

*Thought experiment:*

*Suppose we train our model using the entire dataset.*

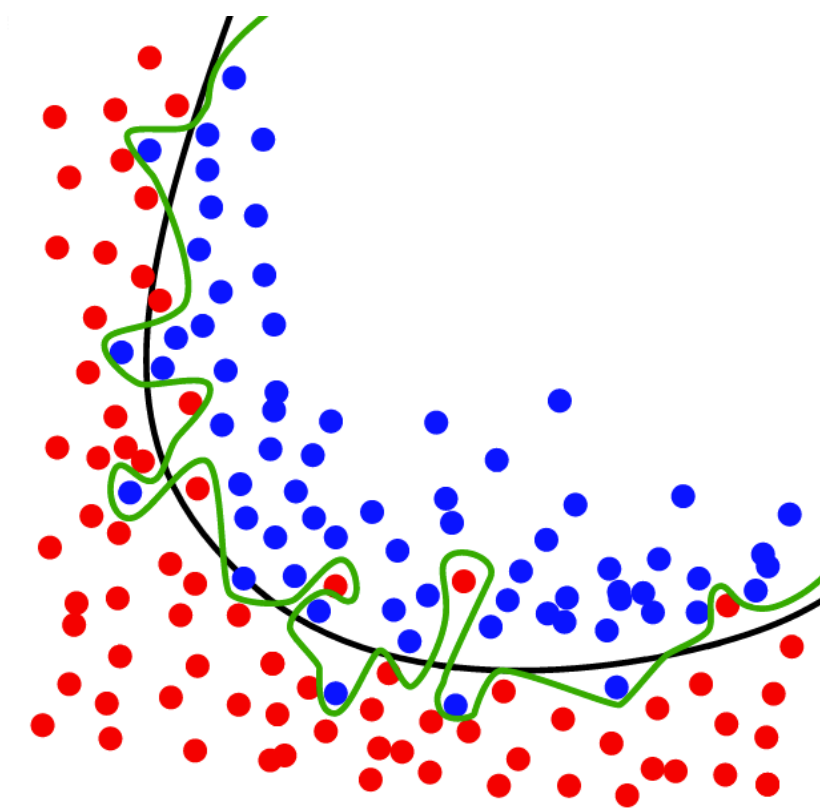
*Q: How low can we push the training error?*

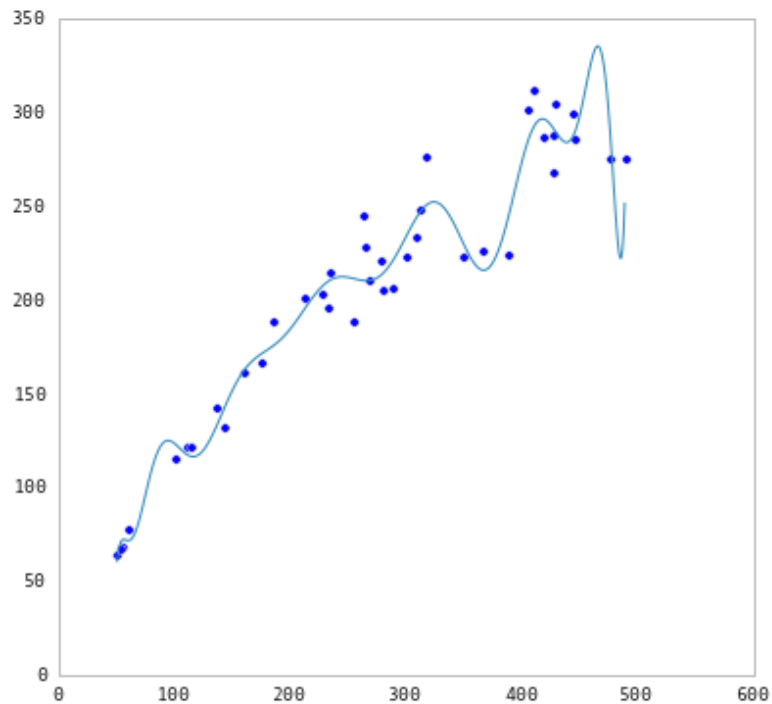
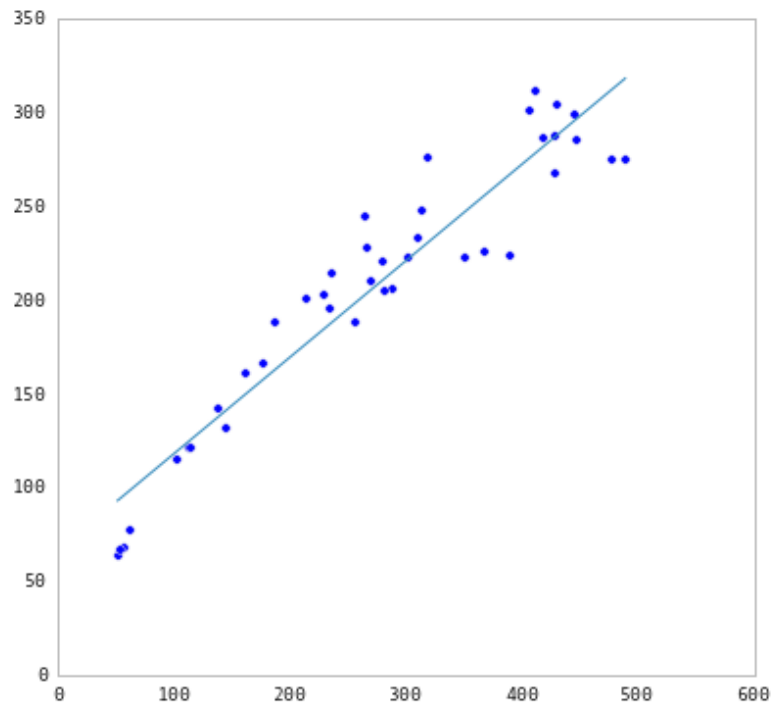
- We can make the model arbitrarily complex (effectively “memorizing” the entire training set).*

*A: Down to zero!*

**NOTE**

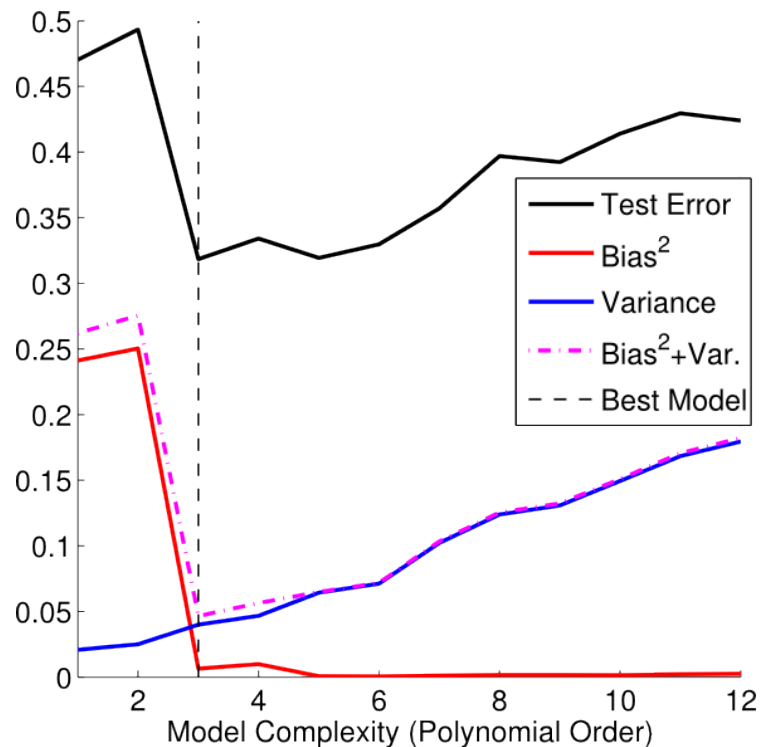
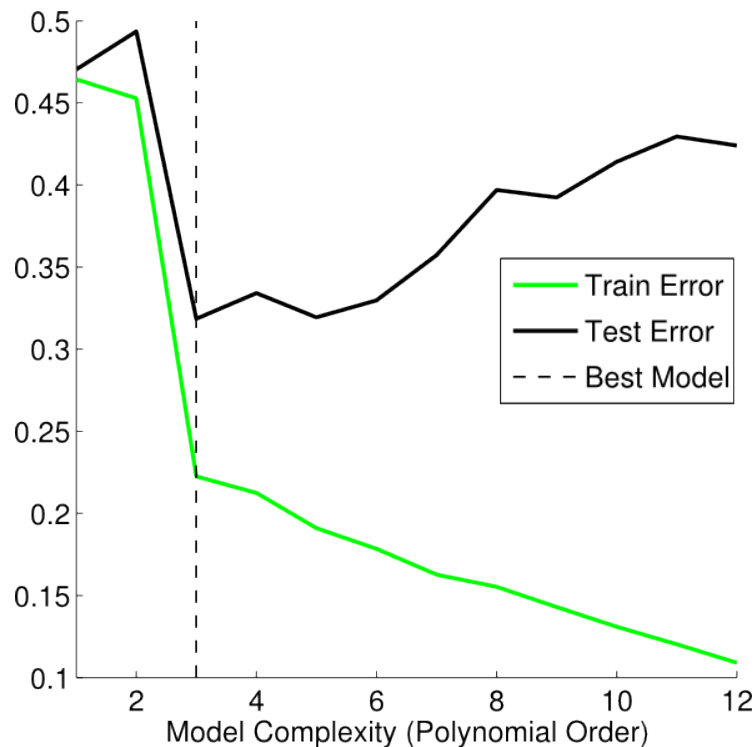
This phenomenon  
is called  
*overfitting*.





# UNDERFITTING AND OVERFITTING

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Q: What's wrong with training error?

*Thought experiment:*

*Suppose we train our model using the entire dataset.*

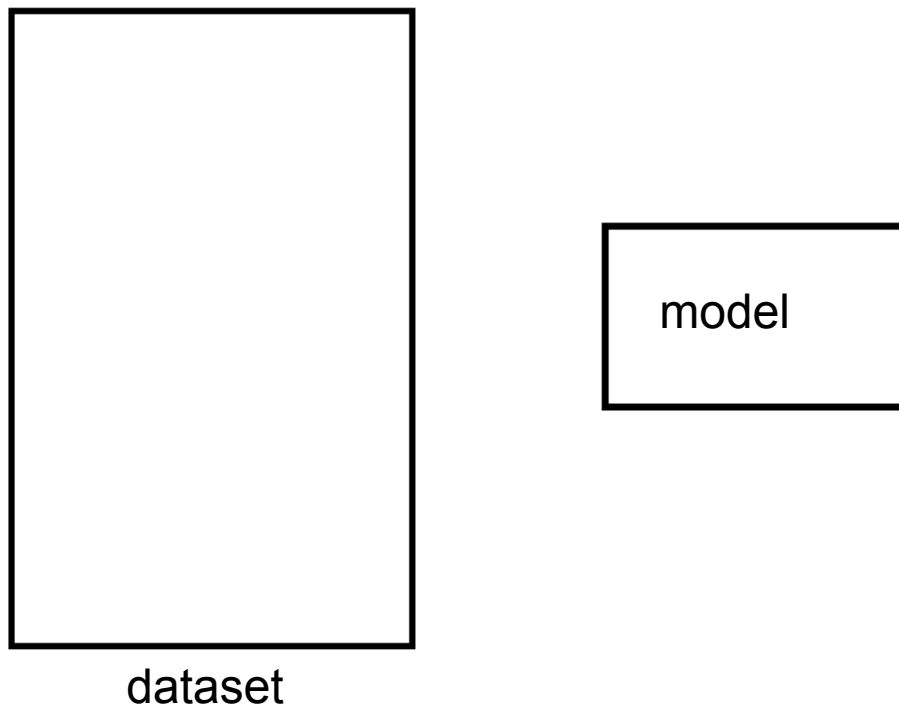
*Q: How low can we push the training error?*

- We can make the model arbitrarily complex (effectively “memorizing” the entire training set).*

*A: Down to zero!*

A: Training error is not a good estimate of accuracy beyond training data.

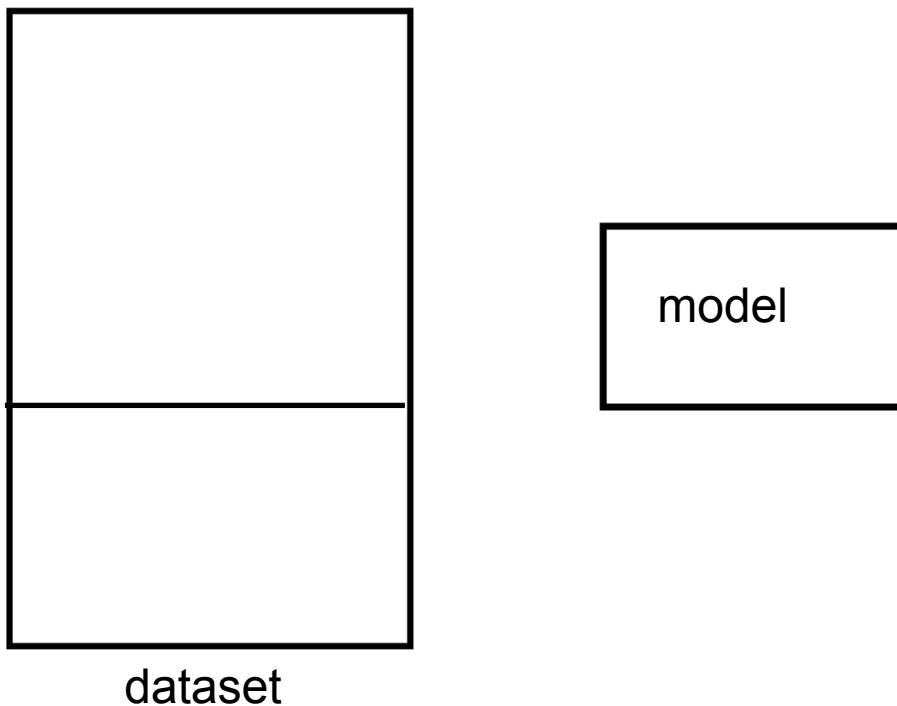
Q: How can we make a model that generalizes well?





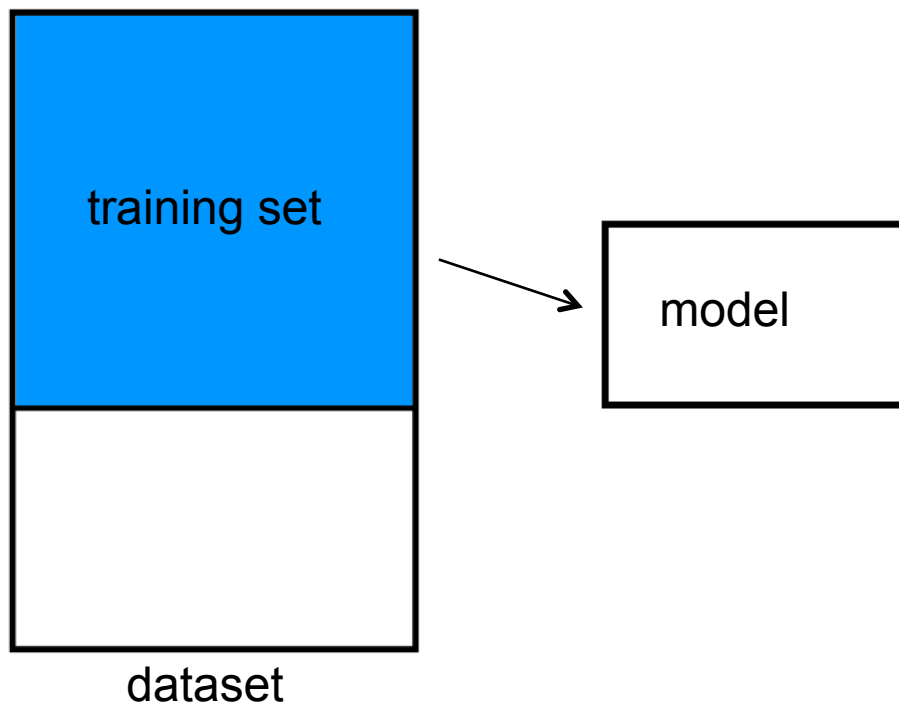
Q: How can we make a model that generalizes well?

1) split dataset



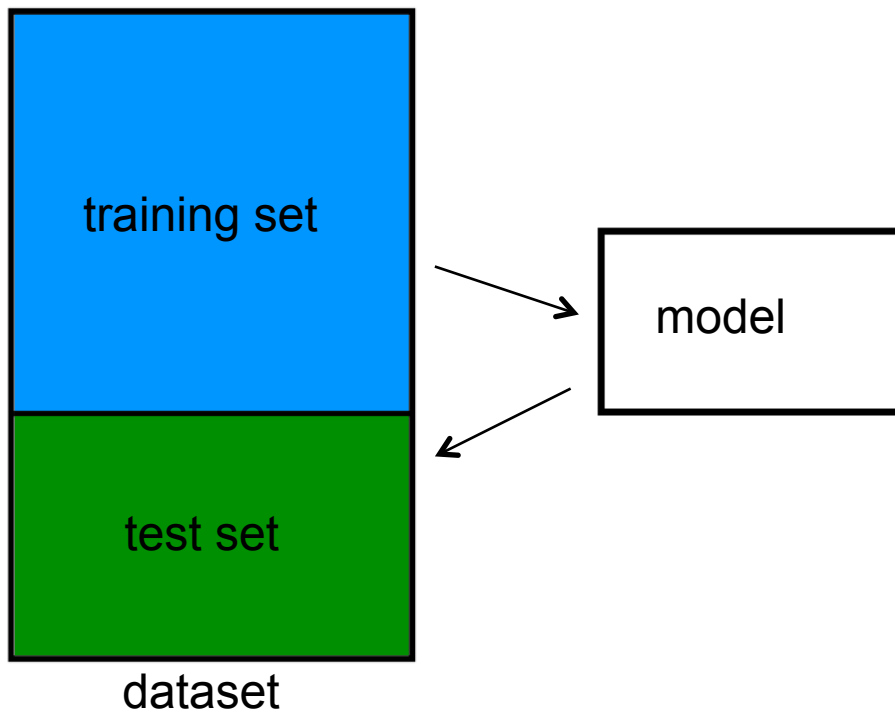
Q: How can we make a model that generalizes well?

- 1) split dataset
- 2) train model



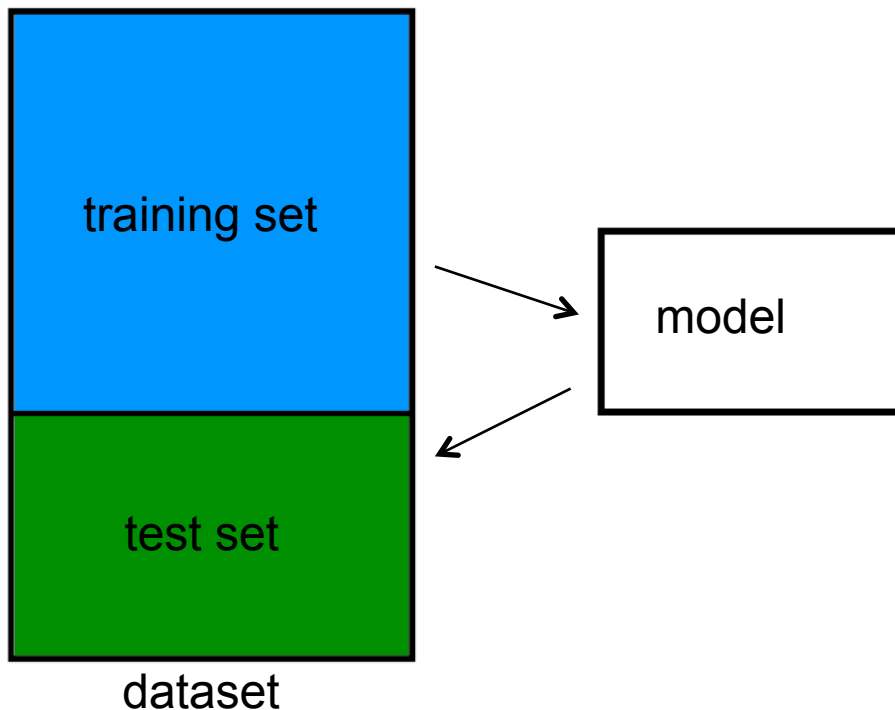
Q: How can we make a model that generalizes well?

- 1) split dataset
- 2) train model
- 3) test model



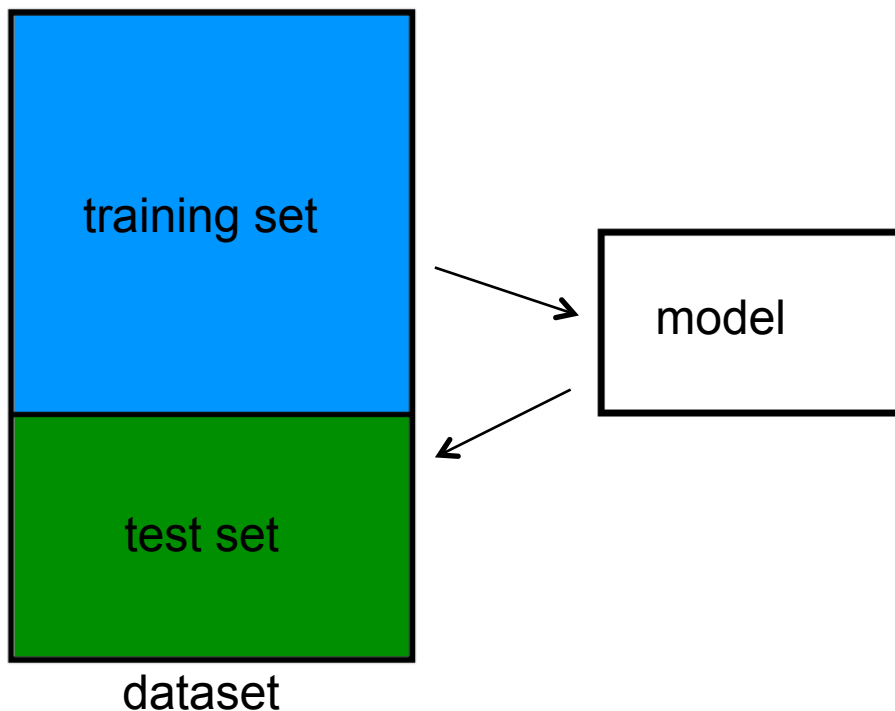
Q: How can we make a model that generalizes well?

- 1) split dataset
- 2) train model
- 3) test model
- 4) parameter tuning



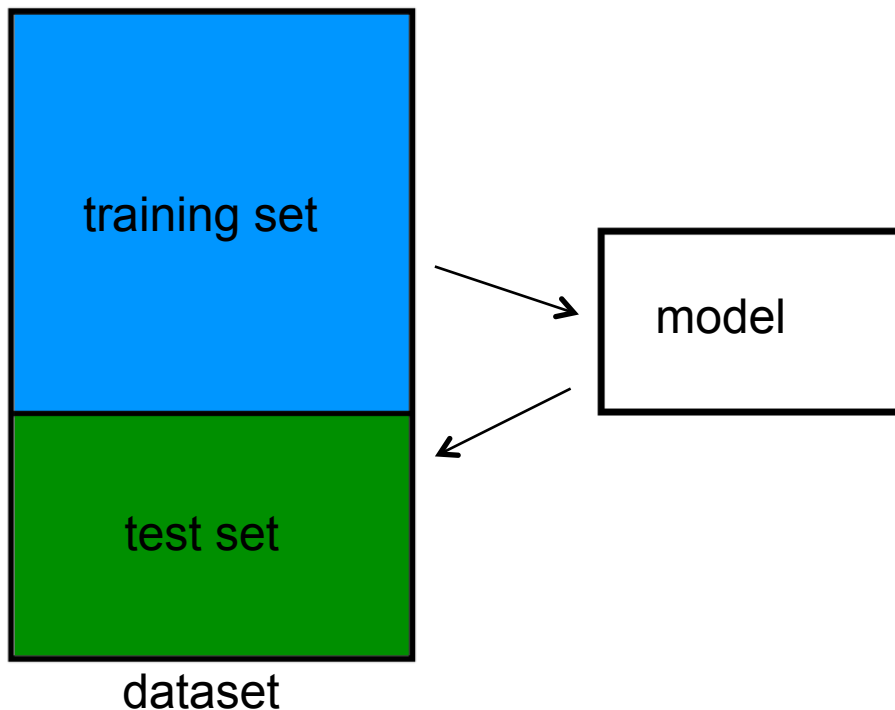
Q: How can we make a model that generalizes well?

- 1) split dataset
- 2) train model
- 3) test model
- 4) parameter tuning
- 5) choose best model



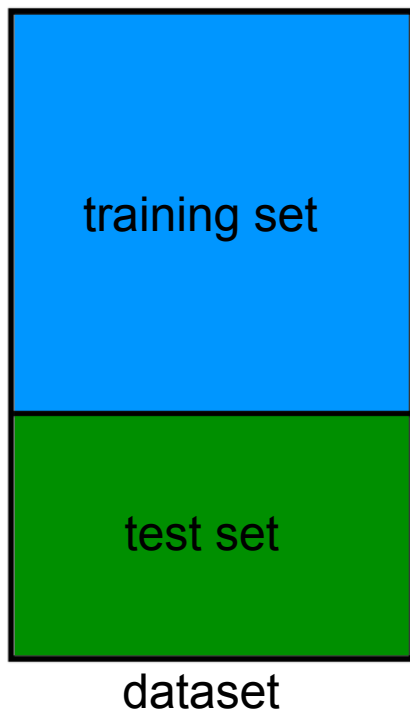
Q: How can we make a model that generalizes well?

- 1) split dataset
- 2) train model
- 3) test model
- 4) parameter tuning
- 5) choose best model
- 6) train on **all** data

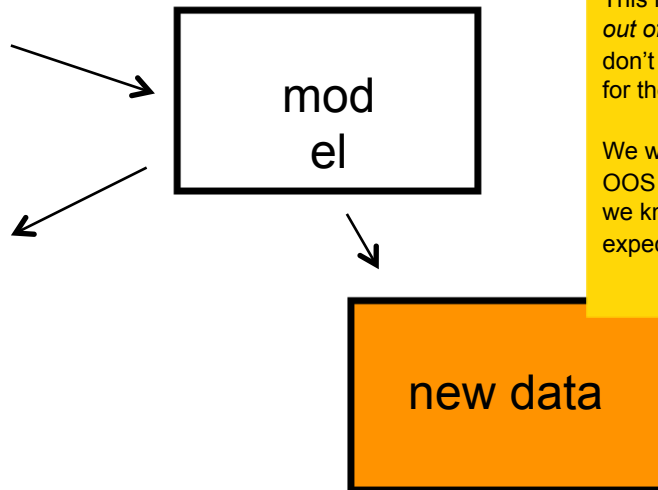


Q: How can we make a model that generalizes well?

- 1) split dataset
- 2) train model
- 3) test model
- 4) parameter tuning
- 5) choose best model
- 6) train on **all** data



- 7) make predictions on new data



### NOTE

This new data is called *out of sample* data. We don't know the labels for these OOS records!

We want to estimate OOS prediction error so we know what to expect from our model.

Suppose we do the train/test split.

Q: How well does test set error predict OOS accuracy?

*Thought experiment:*

*Suppose we had done a different train/test split.*

*Q: Would the test set error remain the same?*

*A: Of course not!*

A: On its own, not very well.



Something is still missing!

Q: How can we do better?

*Thought experiment:*

*Different train/test splits will give us different test set errors.*

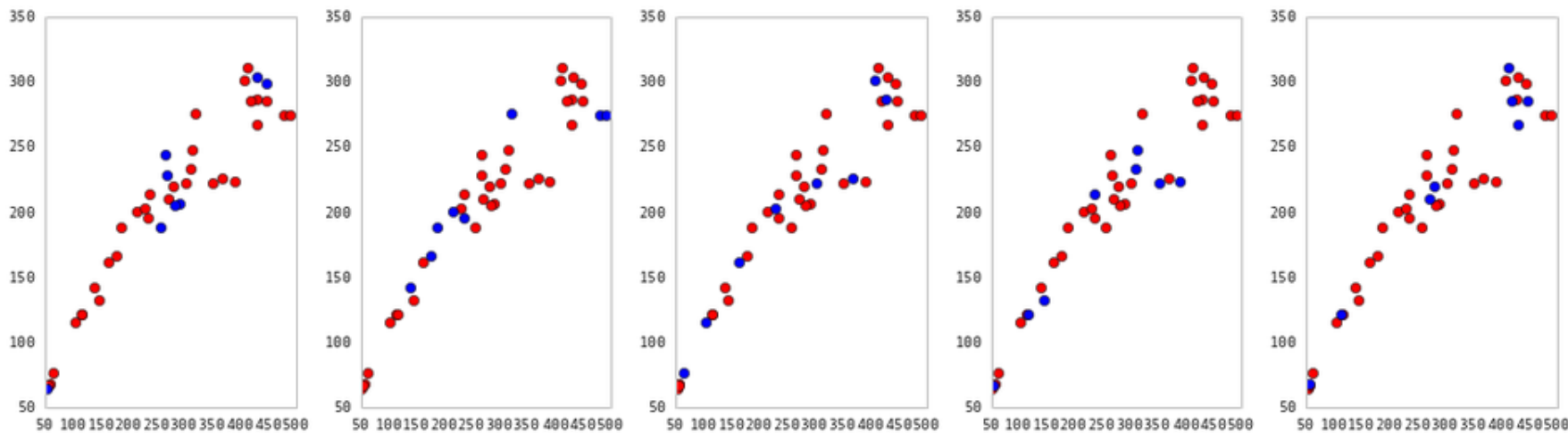
*Q: What if we did a bunch of these and took the average?*

*A: Now you're talking!*

A: Cross-validation.

## Steps for K-fold cross-validation:

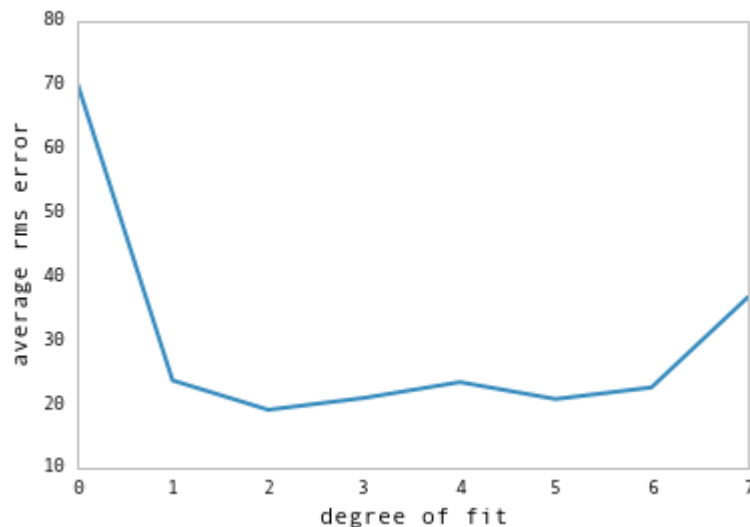
- 1) Randomly split the dataset into  $K$  equal partitions.
- 2) Use partition 1 as test set & union of other partitions as training set.
- 3) Calculate test set error.
- 4) Repeat steps 2-3 using a different partition as the test set at each iteration.
- 5) Take the average test set error as the estimate of OOS accuracy.



5-fold cross-validation: red = training folds,  
blue = test fold

## Features of K-fold cross-validation:

- 1) More accurate estimate of OOS prediction error.
- 2) More efficient use of data than single train/test split.
  - Each record in our dataset is used for both training and testing.
- 3) Presents tradeoff between efficiency and computational ex
  - 10-fold CV is 10x more expensive than a single train/test split
- 4) Can be used for parameter tuning and model selection.



Model selection using cross-validation:  
lowest predicted OOS error at  
degree = 2

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# DATA SCIENCE

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