
DATA SCIENCE

CLASS 2: LINEAR REGRESSION

0. BASIC FORM

II. CATEGORICAL VARIABLES

LINEAR REGRESSION

0. BASIC FORM

Q: What is the motivation for learning about linear regression?

- widely used
- runs fast
- easy to use (not a lot of tuning required)
- highly interpretable
- basis for many other methods

	continuous	categorical
supervised	????	?????
unsupervised	????	?????

	continuous	categorical
supervised	regression	classification
unsupervised	dimension reduction	clustering

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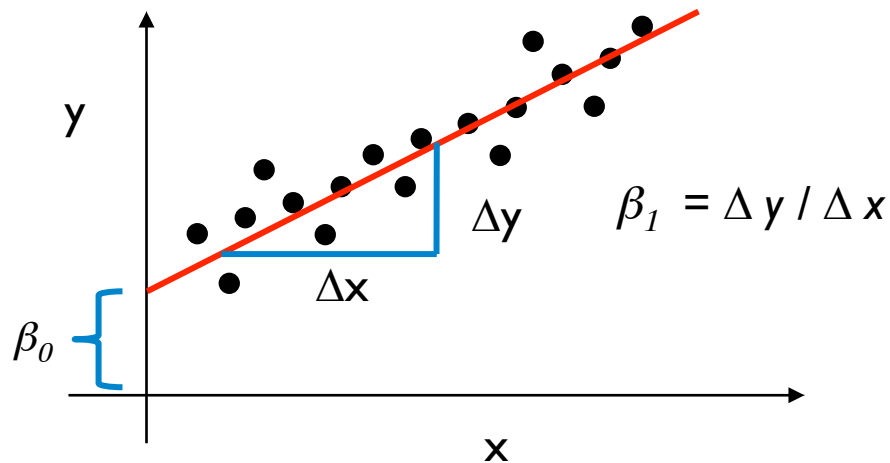
β_0 = intercept (where the line crosses the y-axis)

β_1 = regression coefficient (the model parameter)

ε = residual (the error)

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LINEAR REGRESSION

II. CATEGORICAL VARIABLES

Q: How do we deal with categorical variables?
(i.e., with k levels)

Major ($k=4$)
Computer Science
Engineering
Business
Literature
Business
Engineering

Q: How do we deal with categorical variables?
(i.e., with k levels)

A: Create a $k-1$ binary (“dummy”) variables.

Major (k=4)	Engineering	Business	Literature
Computer Science	0	0	0
Engineering	1	0	0
Business	0	1	0
Literature	0	0	1
Business	0	1	0
Engineering	1	0	0

Computer Science is the reference

Q: Why $k-1$ and not k ?

A: Because $k-1$ captures all possible outputs, and to avoid multicollinearity.

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Q: Does it matter which factor level I leave out?

A: Yes, this is the reference point for all other factor levels.

Q: Is this the only way to represent categorical data?

A: This is the conventional way to represent nominal data, however, ordinal data can be represented with integers.

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A: This is the conventional way to represent nominal data, however, ordinal data can be represented with integers.

Q: What does this mean?

A: Categories that can be ranked (i.e., strongly disagree, disagree, neutral, agree, strongly agree) can be represented as 1, 2, 3, 4, 5.