

Introduction of Machine / Deep Learning

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Machine Learning ≈ Looking for Function

Speech Recognition

$$f($$
)= "How are you"

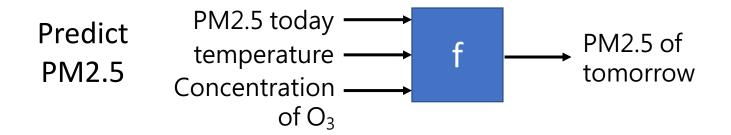
Image Recognition

Playing Go

$$f($$
 $)=$ "5-5" (next move)

Different types of Functions

Regression: The function outputs a scalar.

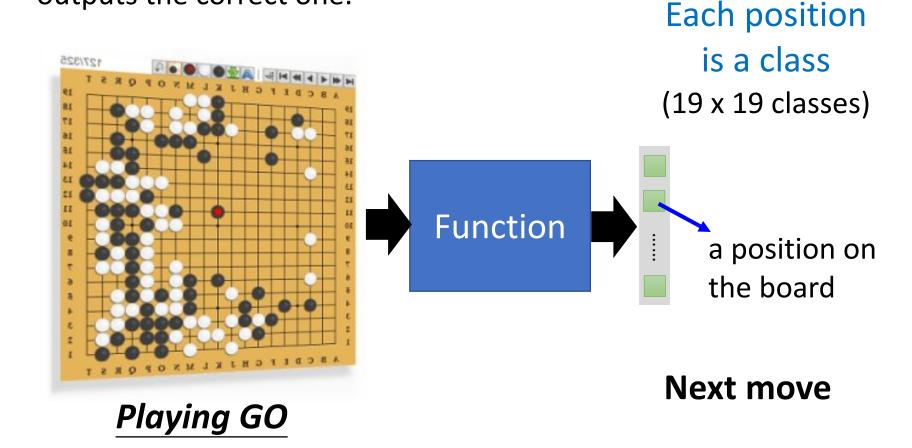


<u>Classification</u>: Given options (classes), the function outputs the correct one.



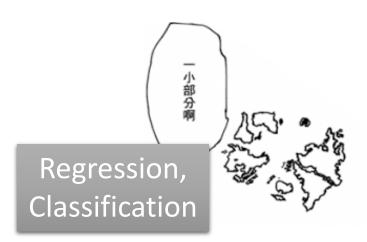
Different types of Functions

<u>Classification</u>: Given options (classes), the function outputs the correct one.



Structured Learning

create something with structure (image, document)





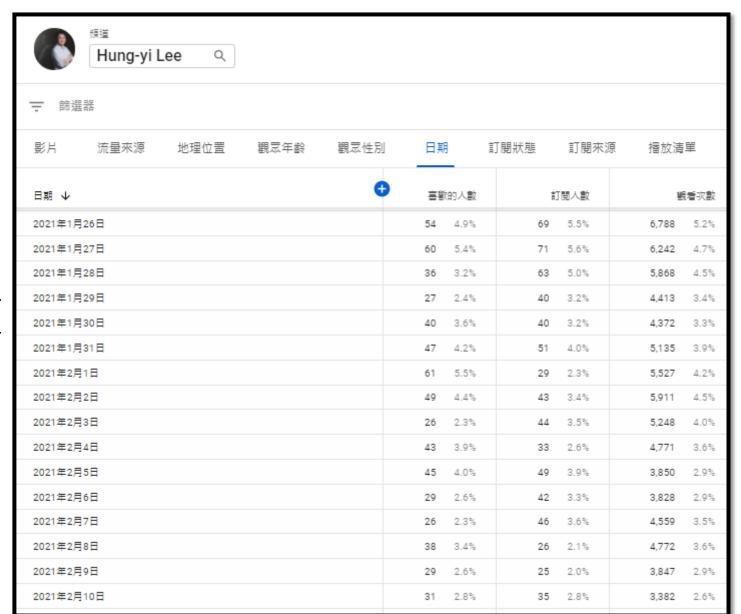
How to find a function?
A Case Study

YouTube Channel



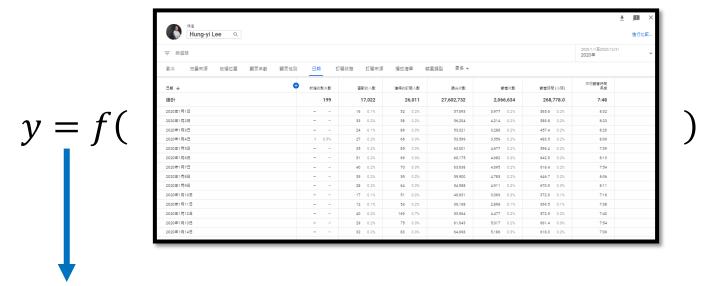
https://www.youtube.com/c/HungyiLeeNTU

The function we want to find ...



y = f(no. of views
on 2/26

1. Function with Unknown Parameters



Model $y = b + wx_1$ based on domain knowledge

feature

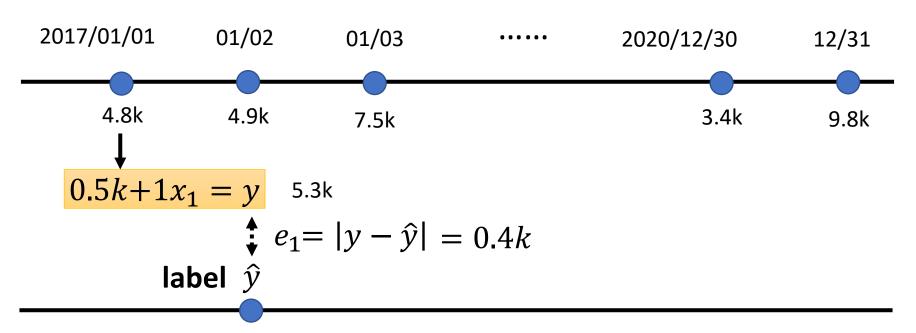
y: no. of views on 2/26, x_1 : no. of views on 2/25 w and b are unknown parameters (learned from data) weight bias

2. Define Loss from Training Data > Loss: how good a set of

- Loss is a function of parameters L(b, w)
- values is.

$$L(0.5k, 1)$$
 $y = b + wx_1 \longrightarrow y = 0.5k + 1x_1$ How good it is?

Data from 2017/01/01 – 2020/12/31

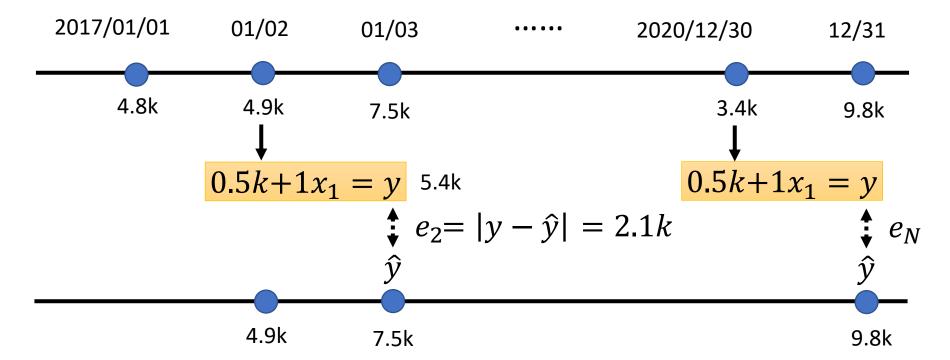


2. Define Loss from Training Data > Loss: how good a set of

- Loss is a function of parameters L(b, w)
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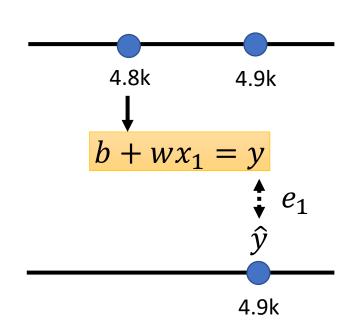
$$L(0.5k, 1)$$
 $y = b + wx_1 \longrightarrow y = 0.5k + 1x_1$ How good it is?

Data from 2017/01/01 – 2020/12/31



2. Define Loss from Training Data > Loss: how good a set of

- Loss is a function of parameters L(b, w)
- values is.



Loss:
$$L = \frac{1}{N} \sum_{n} e_n$$

$$e = |y - \hat{y}|$$
 L is mean absolute error (MAE)

$$e = (y - \hat{y})^2$$
 L is mean square error (MSE)

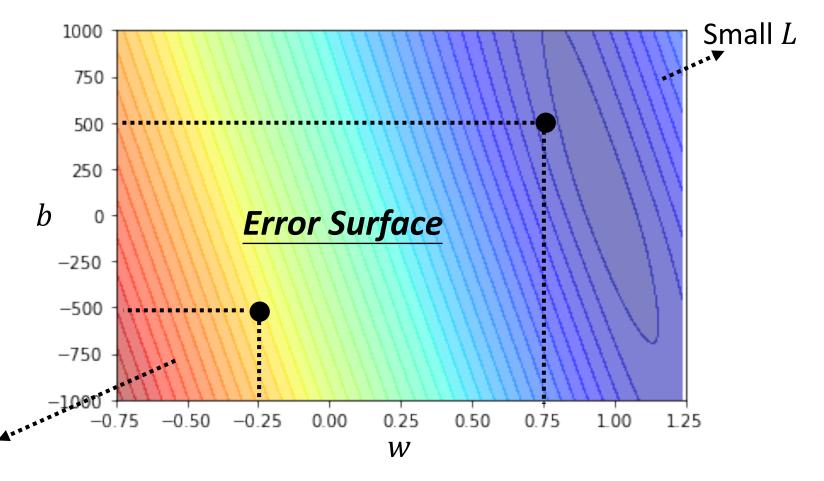
If y and \hat{y} are both probability distributions

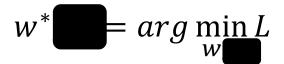


2. Define Loss from Training Data > Loss: how good a set of Model $y = b + wx_1$

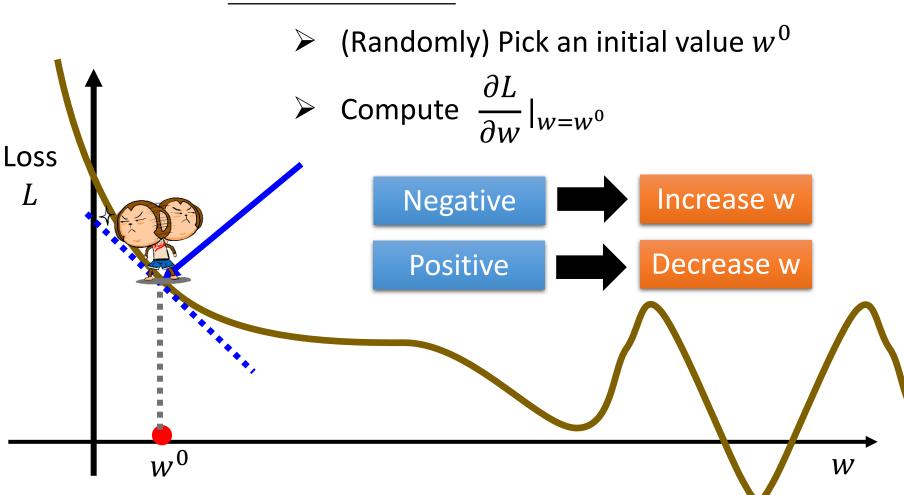
Large *L*

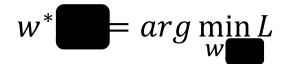
- Loss is a function of parameters L(b, w)
 - values is.



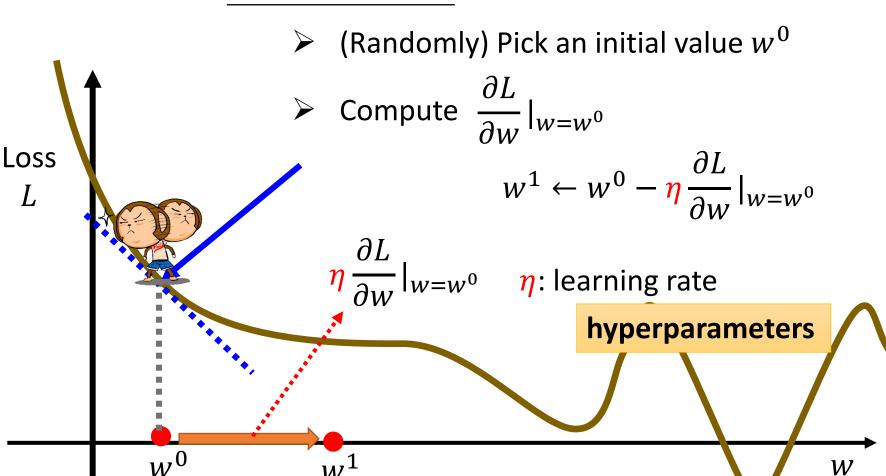


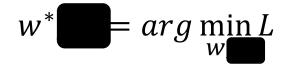
Gradient Descent



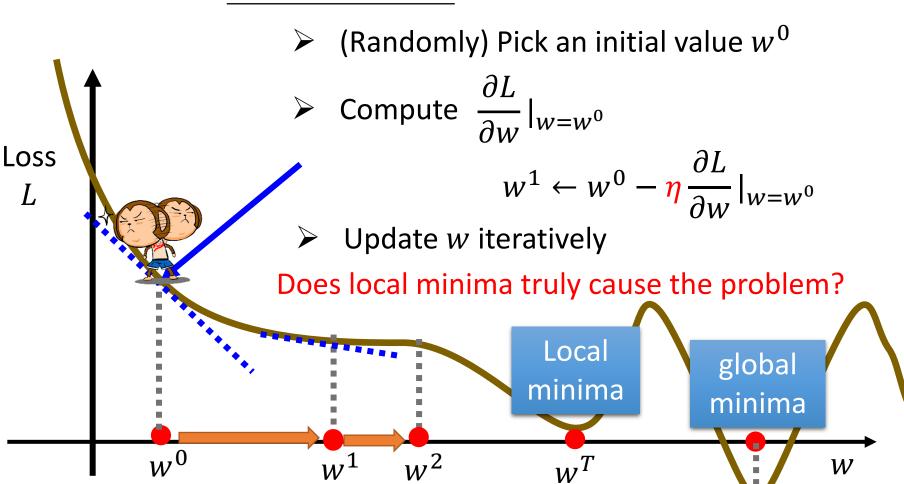


Gradient Descent





Gradient Descent



$$w^*, b^* = arg \min_{w,b} L$$

- \triangleright (Randomly) Pick initial values w^0 , b^0
- Compute

$$\frac{\partial L}{\partial w}|_{w=w^{0},b=b^{0}} \qquad w^{1} \leftarrow w^{0} - \eta \frac{\partial L}{\partial w}|_{w=w^{0},b=b^{0}}$$

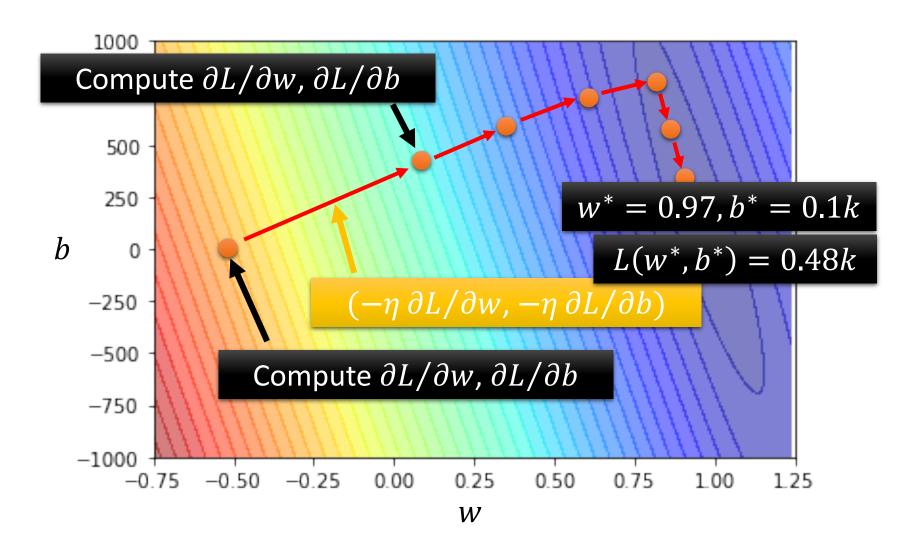
$$\frac{\partial L}{\partial b}|_{w=w^{0},b=b^{0}} \qquad b^{1} \leftarrow b^{0} - \eta \frac{\partial L}{\partial b}|_{w=w^{0},b=b^{0}}$$

Can be done in one line in most deep learning frameworks

 \triangleright Update w and b interatively

Model
$$y = b + wx_1$$

 $w^*, b^* = arg \min_{w,b} L$



Machine Learning is so simple

 $y = b + wx_1$

 $w^* = 0.97, b^* = 0.1k$ $L(w^*, b^*) = 0.48k$

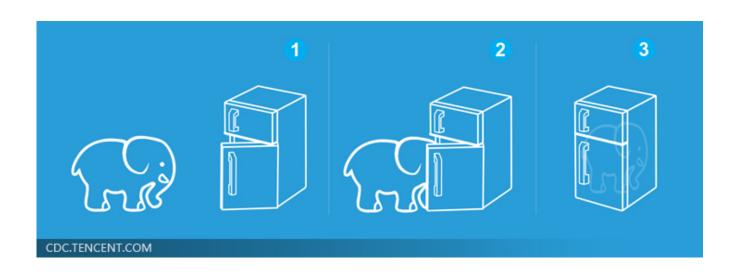
Step 1: function with unknown



Step 2: define loss from training data



Step 3: optimization



Machine Learning is so simple



Training

 $y = 0.1k + 0.97x_1$ achieves the smallest loss L = 0.48k on data of 2017 – 2020 (training data)

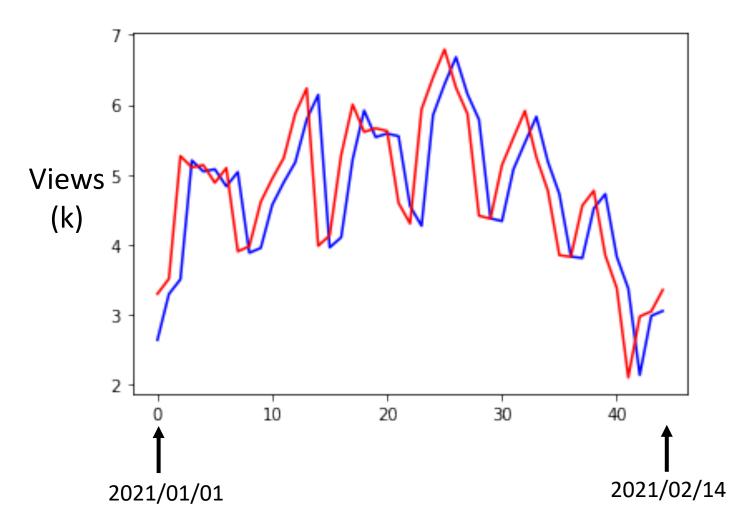
How about data of 2021 (unseen during training)?

$$L' = 0.58k$$

$$y = 0.1k + 0.97x_1$$

Red: real no. of views

blue: estimated no. of views



$$y = b + wx_1$$

$$L = 0.48k$$

$$L' = 0.58k$$

$$y = b + \sum_{i=1}^{r} w_i x_i$$

$$L = 0.38k$$

$$L' = 0.49k$$

b	w_1^*	w_2^*	w_3^*	w_4^*	w_5^*	w_6^*	w_7^*
0.05k	0.79	-0.31	0.12	-0.01	-0.10	0.30	0.18

$$y = b + \sum_{j=1}^{28} w_j x_j$$

$$L = 0.33k$$

$$L' = 0.46k$$

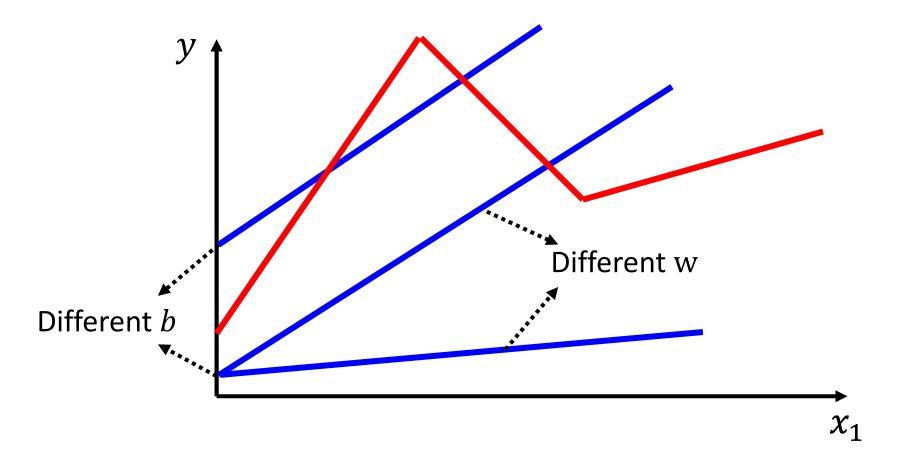
$$y = b + \sum_{i=1}^{56} w_i x_i$$

$$L = 0.32k$$

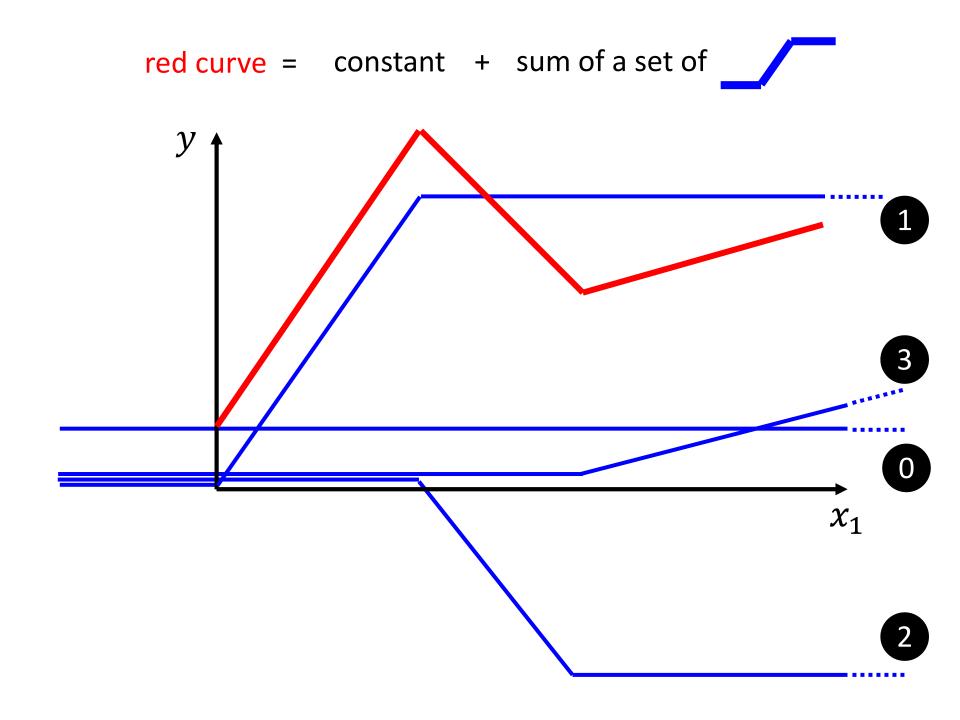
$$L'=0.46k$$

Linear models

Linear models are too simple ... we need more sophisticated modes.

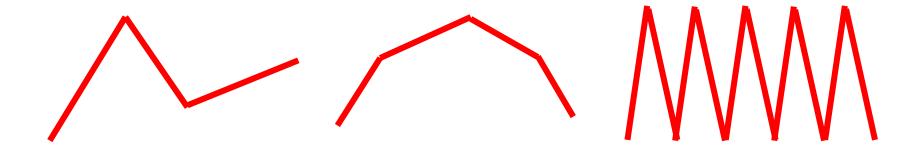


Linear models have severe limitation. *Model Bias*We need a more flexible model!



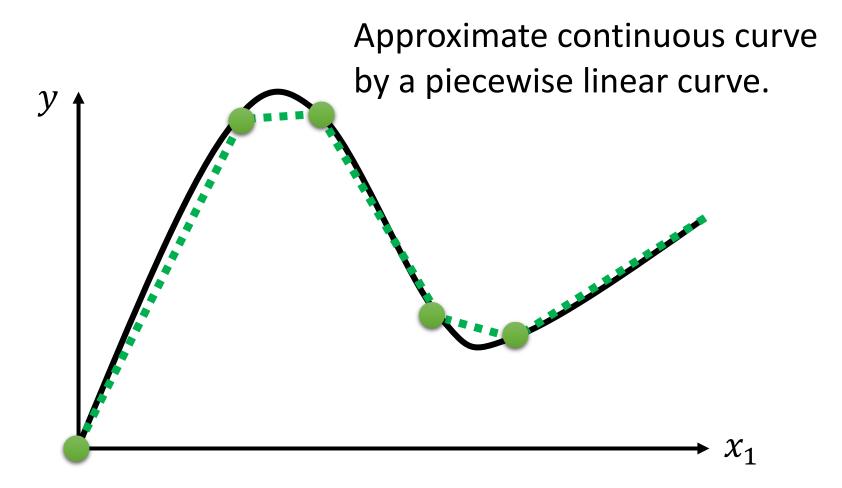
All Piecewise Linear Curves

= constant + sum of a set of



More pieces require more

Beyond Piecewise Linear?



To have good approximation, we need sufficient pieces.

red curve = constant + sum of a set of

How to represent this function?

Hard Sigmoid

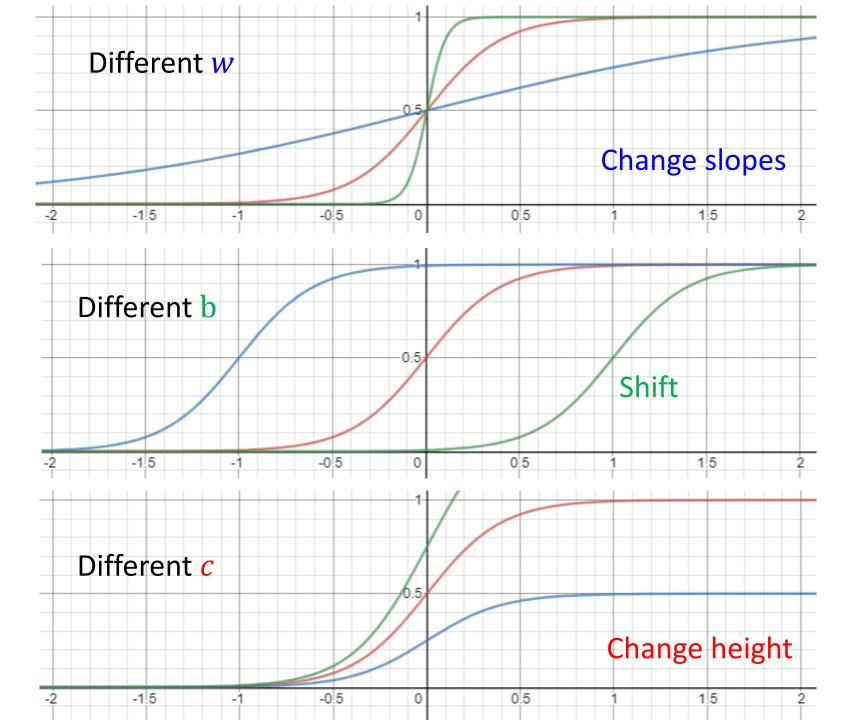
 \boldsymbol{x}_1

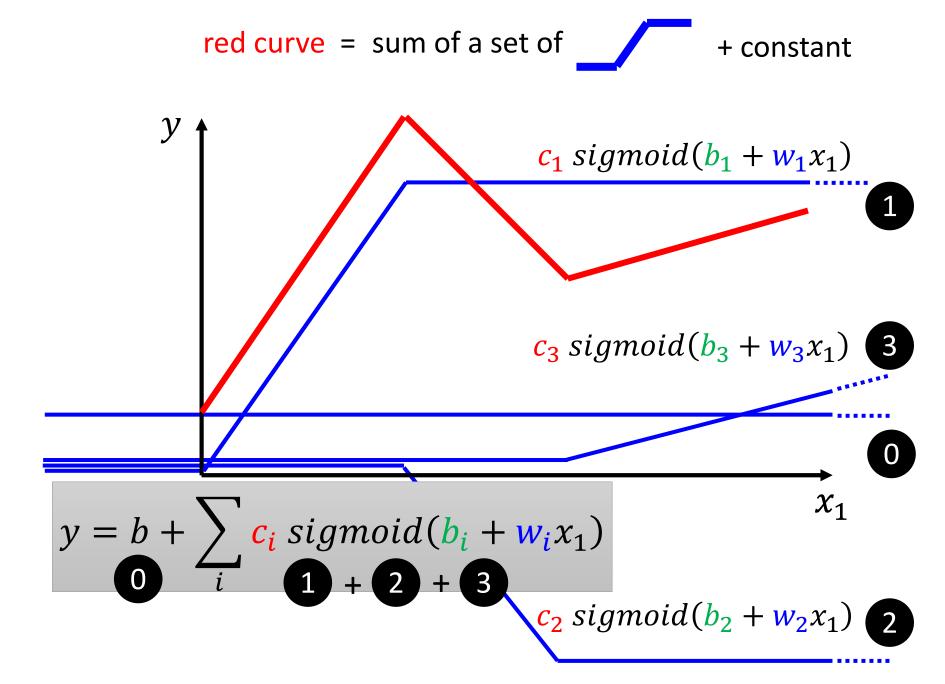
Sigmoid Function

$$y = c \frac{1}{1 + e^{-(b + wx_1)}}$$

$$= c sigmoid(b + wx_1)$$







New Model: More Features

$$y = b + wx_1$$

$$y = b + \sum_{i} c_{i} sigmoid(b_{i} + w_{i}x_{1})$$

$$y = b + \sum_{j} w_{j} x_{j}$$

$$y = b + \sum_{i} c_{i} sigmoid \left(\underbrace{b_{i} + \sum_{j} w_{ij} x_{i}}_{j} \right)$$

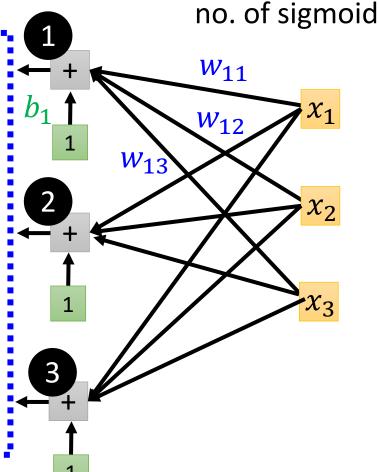
$$y=b+\sum_{i} c_{i} \ sigmoid \left(b_{i}+\sum_{j} w_{ij}x_{j}\right) \ \begin{array}{c} j:1,2,3 \\ \text{no. of features} \\ i:1,2,3 \end{array} \right)$$

 $r_1 = b_1 + w_{11}x_1 + w_{12}x_2 + w_{13}x_3$

 w_{ij} : weight for x_j for i-th sigmoid

$$r_2 = b_2 + w_{21}x_1 + w_{22}x_2 + w_{23}x_3$$

$$r_3 = b_3 + w_{31}x_1 + w_{32}x_2 + w_{33}x_3$$



$$y = b + \sum_{i} c_{i} \operatorname{sigmoid} \left(b_{i} + \sum_{i} w_{ij} x_{j} \right) \qquad i: 1, 2, 3$$
$$j: 1, 2, 3$$

$$r_1 = b_1 + w_{11}x_1 + w_{12}x_2 + w_{13}x_3$$

$$r_2 = b_2 + w_{21}x_1 + w_{22}x_2 + w_{23}x_3$$

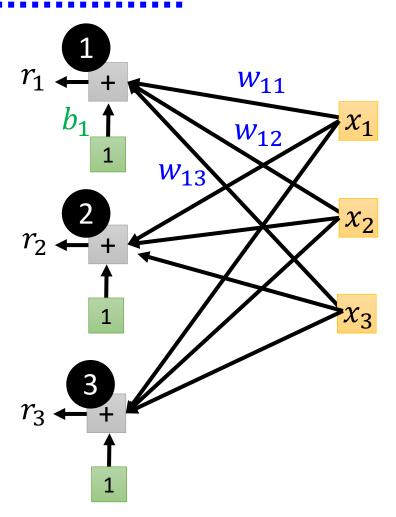
$$r_3 = b_3 + w_{31}x_1 + w_{32}x_2 + w_{33}x_3$$

$$\begin{bmatrix} r_1 \\ r_2 \\ r_3 \end{bmatrix} = \begin{bmatrix} b_1 \\ b_2 \\ b_3 \end{bmatrix} + \begin{bmatrix} w_{11} & w_{12} & w_{13} \\ w_{21} & w_{22} & w_{23} \\ w_{31} & w_{32} & w_{33} \end{bmatrix} \begin{bmatrix} x_1 \\ x_2 \\ x_3 \end{bmatrix}$$

$$|r| = |b| + |w|$$

$$y = b + \sum_{i} c_{i} \operatorname{sigmoid} \left(b_{i} + \sum_{j} w_{ij} x_{j} \right)$$
 i: 1,2,3 j: 1,2,3

$$|r| = |b| + |W| x$$



$$y = b + \sum_{i} \frac{c_{i}}{sigmoid} \left(\frac{b_{i}}{b_{i}} + \sum_{j} \frac{w_{ij}}{w_{ij}} x_{j} \right)$$
 i: 1,2,3 j: 1,2,3

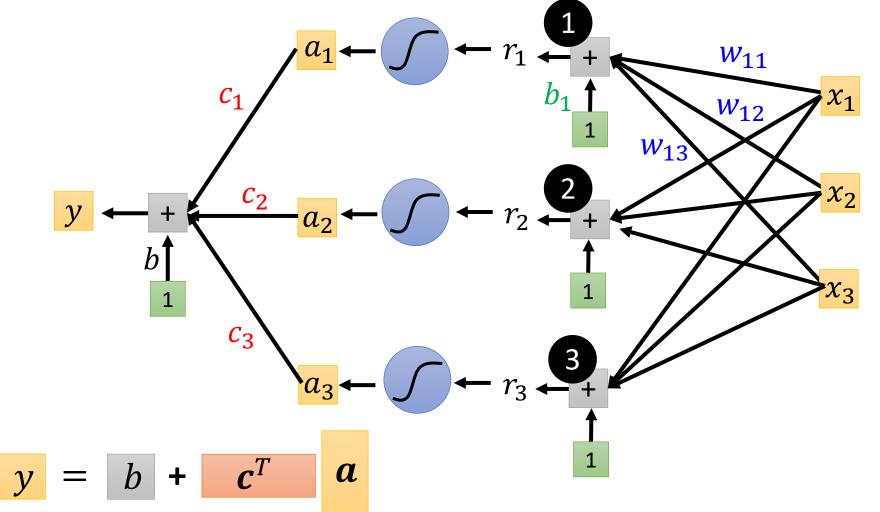
$$a_{1} \leftarrow r_{1} \leftarrow r_{1} \leftarrow r_{1} \leftarrow r_{1}$$

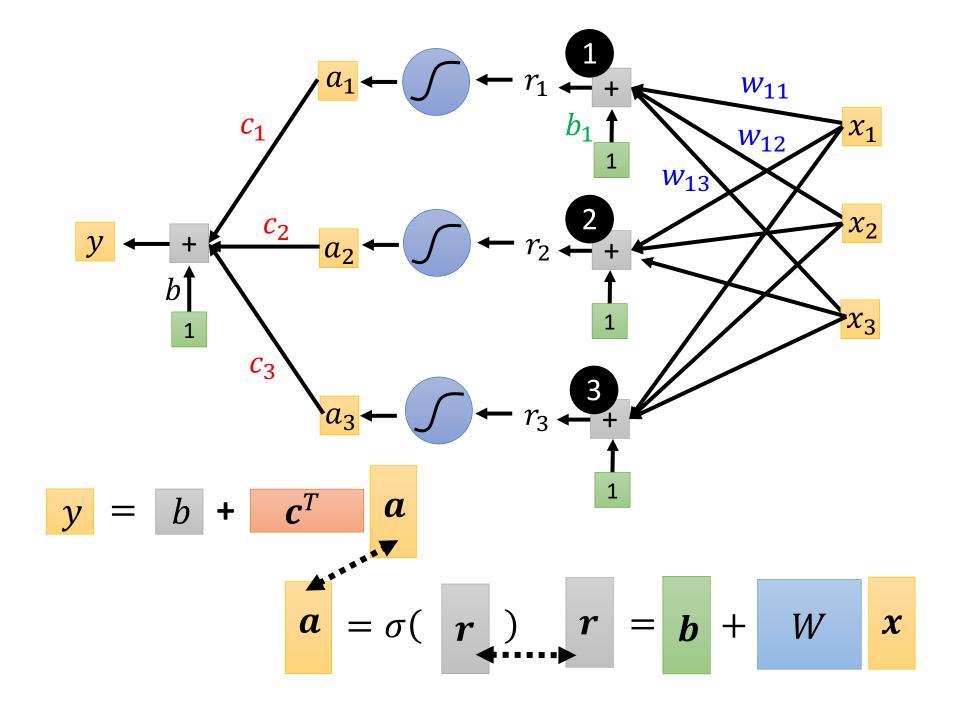
$$a_{1} = sigmoid(r_{1}) = \frac{1}{1 + e^{-r_{1}}}$$

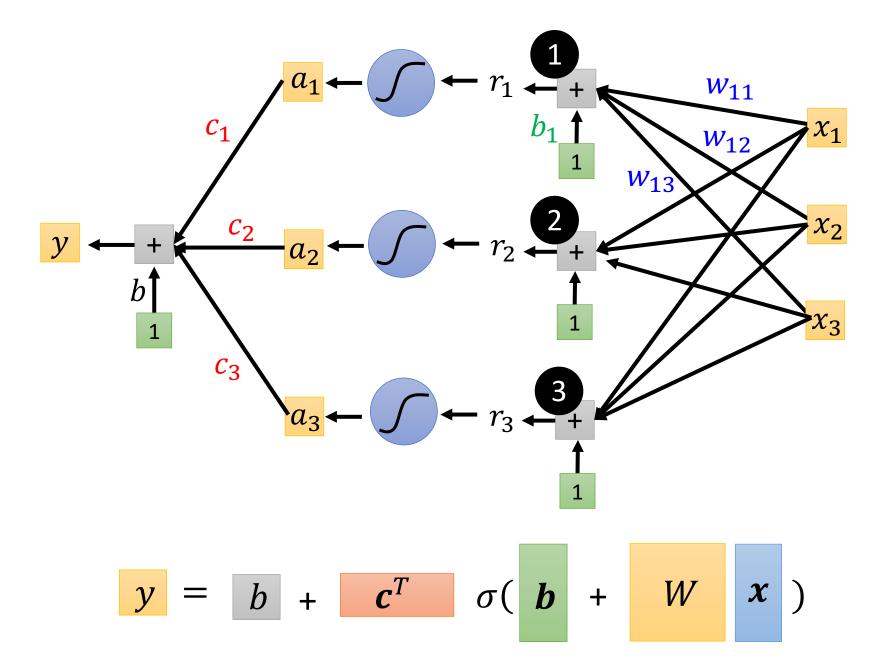
$$a_{2} \leftarrow r_{2} \leftarrow r_{2} \leftarrow r_{3} \leftarrow r_{3}$$

$$a_{3} \leftarrow r_{3} \leftarrow r_{3$$

$$y = b + \sum_{i} c_{i} \operatorname{sigmoid} \left(b_{i} + \sum_{j} w_{ij} x_{j} \right)$$
 i: 1,2,3 j: 1,2,3







Function with unknown parameters

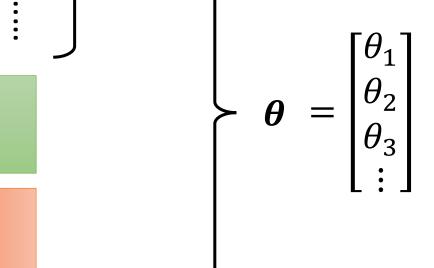
$$y = b + c^T \sigma(b + W x)$$

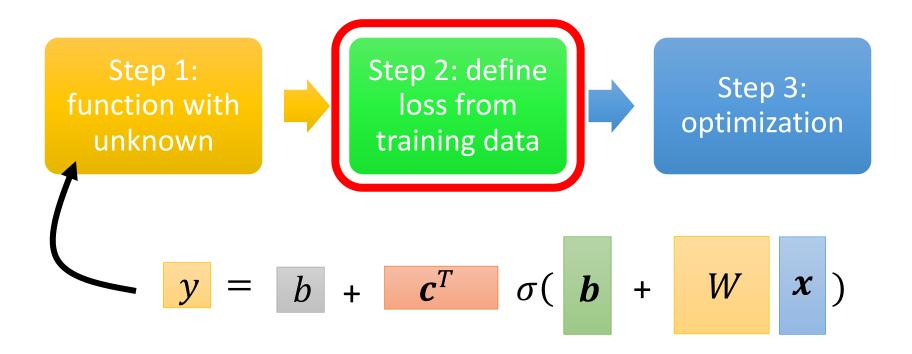
x feature

Unknown parameters

W b

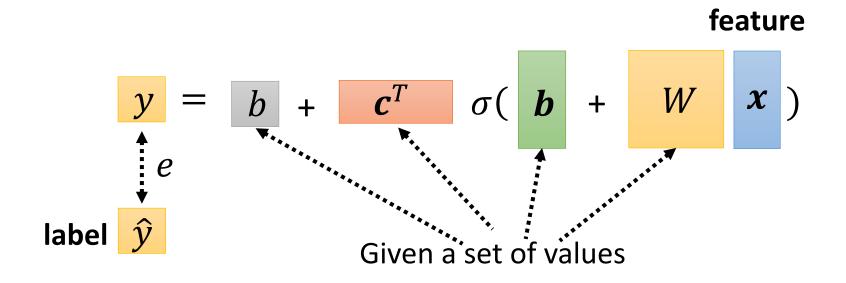
 c^T b



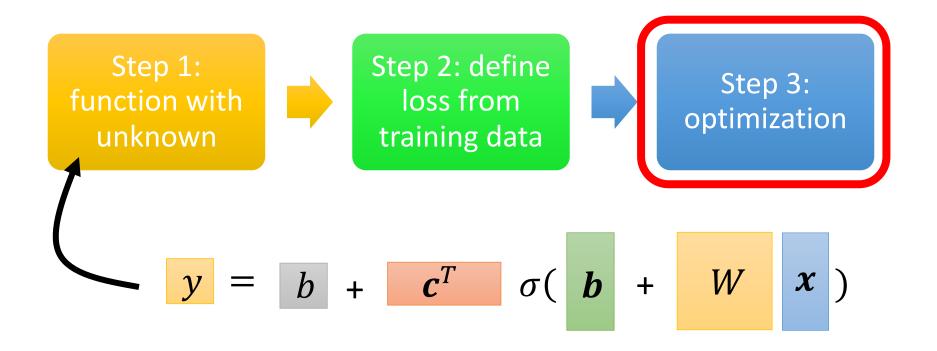


Loss

- \triangleright Loss is a function of parameters $L(\theta)$
- > Loss means how good a set of values is.



Loss:
$$L = \frac{1}{N} \sum_{n} e_n$$



$$\boldsymbol{\theta}^* = arg \min_{\boldsymbol{\theta}} L$$

$$oldsymbol{ heta} = egin{bmatrix} heta_1 \\ heta_2 \\ heta_3 \\ heta_3 \end{bmatrix}$$

(Randomly) Pick initial values $oldsymbol{ heta}^0$

$$\boldsymbol{g} = \begin{bmatrix} \frac{\partial L}{\partial \theta_1} |_{\boldsymbol{\theta} = \boldsymbol{\theta}^0} \\ \frac{\partial L}{\partial \theta_2} |_{\boldsymbol{\theta} = \boldsymbol{\theta}^0} \end{bmatrix}$$
 gradient \vdots

$$\mathbf{g} = \nabla L(\mathbf{\theta}^0)$$
 $\mathbf{\theta}^1 \leftarrow \mathbf{\theta}^0 - \mathbf{\eta} \mathbf{g}$

$$\boldsymbol{\theta}^* = arg \min_{\boldsymbol{\theta}} L$$

- \succ (Randomly) Pick initial values $oldsymbol{ heta}^0$
- ightharpoonup Compute gradient $g = \nabla L(\theta^0)$

$$\theta^1 \leftarrow \theta^0 - \eta g$$

ightharpoonup Compute gradient $g = \nabla L(\theta^1)$

$$\theta^2 \leftarrow \theta^1 - \eta g$$

ightharpoonup Compute gradient $g = \nabla L(\theta^2)$

$$\theta^3 \leftarrow \theta^2 - \eta g$$

$$m{ heta}^* = arg \min_{m{\theta}} L$$

> (Randomly) Pick initial values $m{ heta}^0$

B batch

Compute gradient $m{g} = \nabla L^1(m{\theta}^0)$

L batch

update $m{\theta}^1 \leftarrow m{\theta}^0 - \eta m{g}$

Compute gradient $m{g} = \nabla L^2(m{\theta}^1)$

update $m{\theta}^2 \leftarrow m{\theta}^1 - \eta m{g}$

batch

Compute gradient $m{g} = \nabla L^3(m{\theta}^2)$

update $m{\theta}^3 \leftarrow m{\theta}^2 - \eta m{g}$

batch

1 epoch = see all the batches once

Example 1

- \geq 10,000 examples (N = 10,000)
- \triangleright Batch size is 10 (B = 10)

How many update in **1 epoch**?

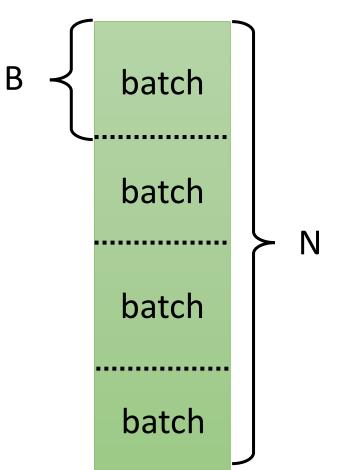
1,000 updates

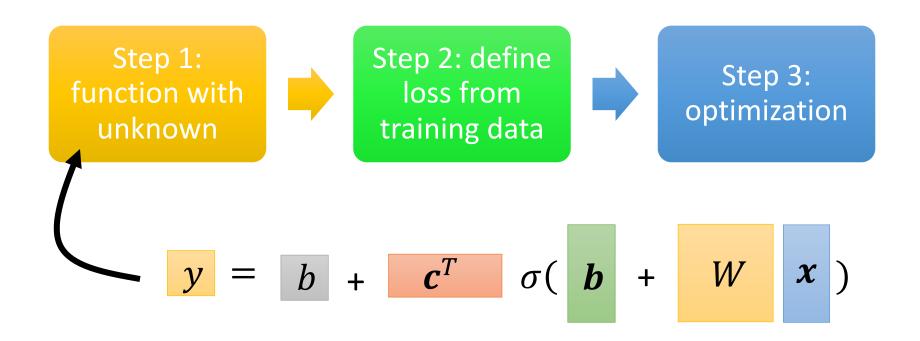
Example 2

- > 1,000 examples (N = 1,000)
- Batch size is 100 (B = 100)

How many update in 1 epoch?

10 updates





More variety of models ...

Sigmoid → ReLU

How to represent this function?

 $\rightarrow x_1$

Rectified Linear Unit (ReLU)

 $c \max(0, b + wx_1)$

 $c' max(0, b' + w'x_1)$

Sigmoid → ReLU

$$y = b + \sum_{i} c_{i} \underline{sigmoid} \left(b_{i} + \sum_{j} w_{ij} x_{j} \right)$$

Activation function

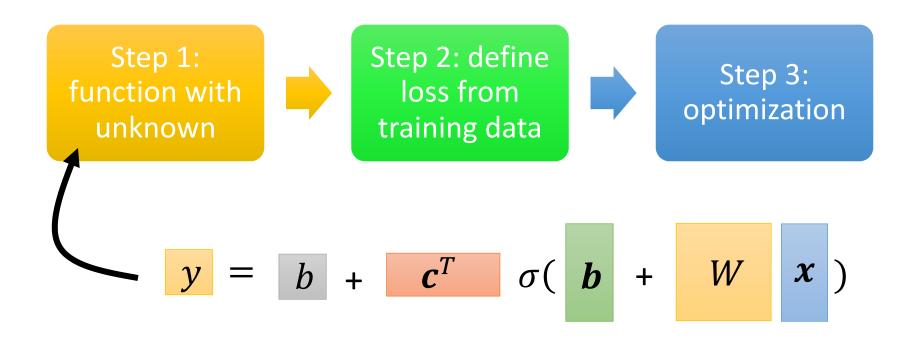
$$y = b + \sum_{i=1}^{\infty} c_i \max \left(0, b_i + \sum_{j=1}^{\infty} w_{ij} x_j\right)$$

Which one is better?

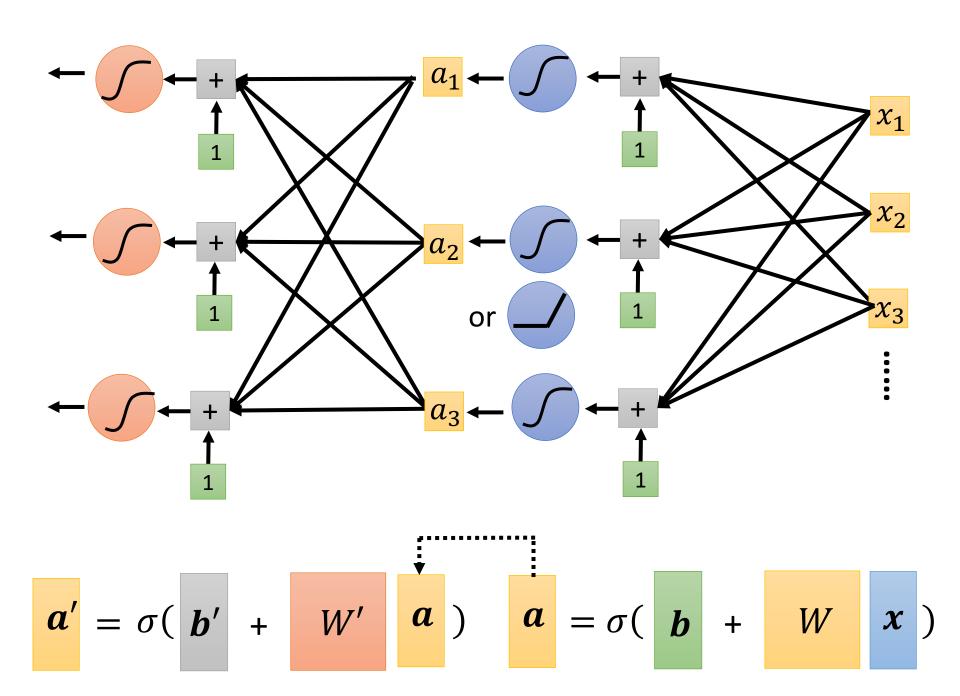
Experimental Results

$$y = b + \sum_{2i} c_i \max \left(0, b_i + \sum_j w_{ij} x_j\right)$$

	linear
2017 – 2020	0.32k
2021	0.46k



Even more variety of models ...



Experimental Results

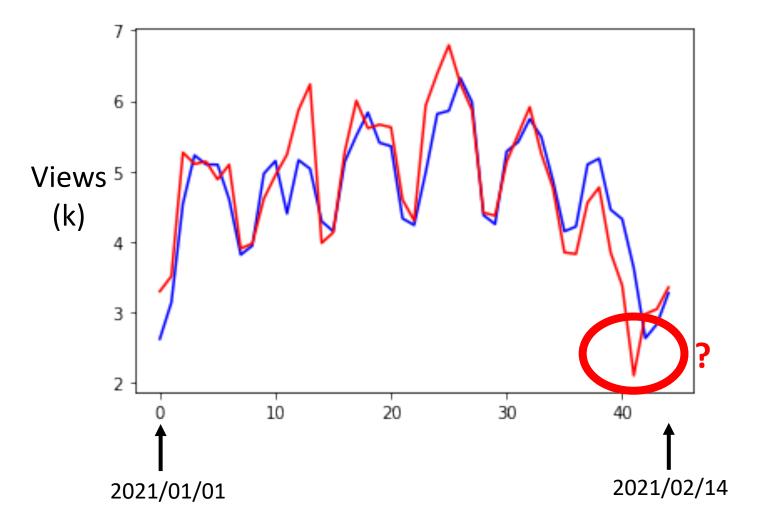
- Loss for multiple hidden layers
 - 100 ReLU for each layer
 - input features are the no. of views in the past 56 days

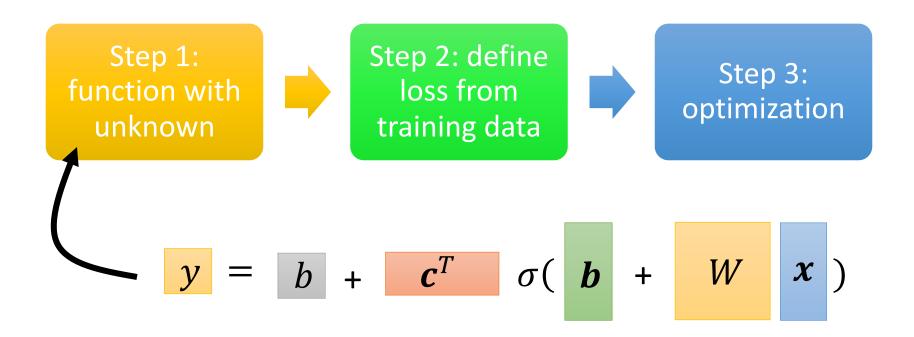
	1 layer
2017 – 2020	0.28k
2021	0.43k

3 layers

Red: real no. of views

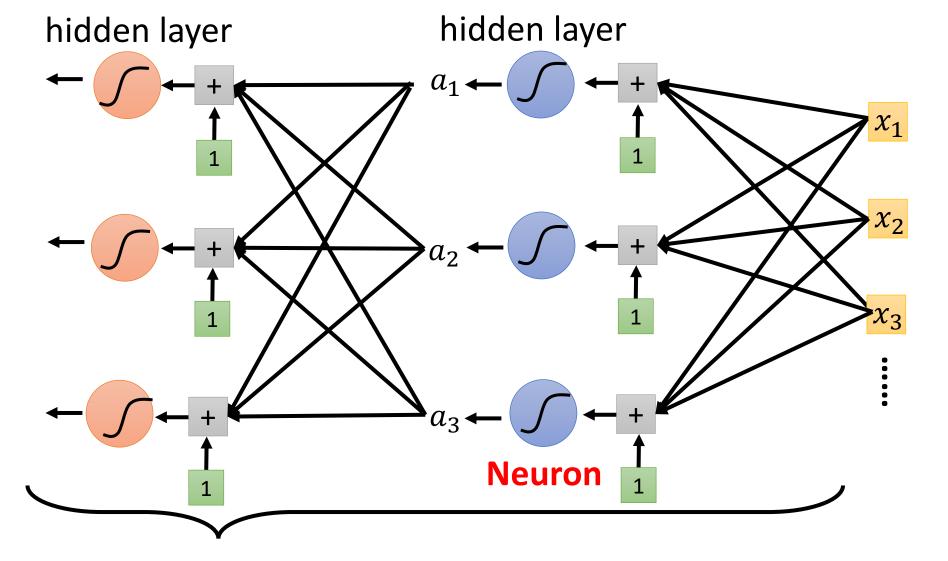
blue: estimated no. of views





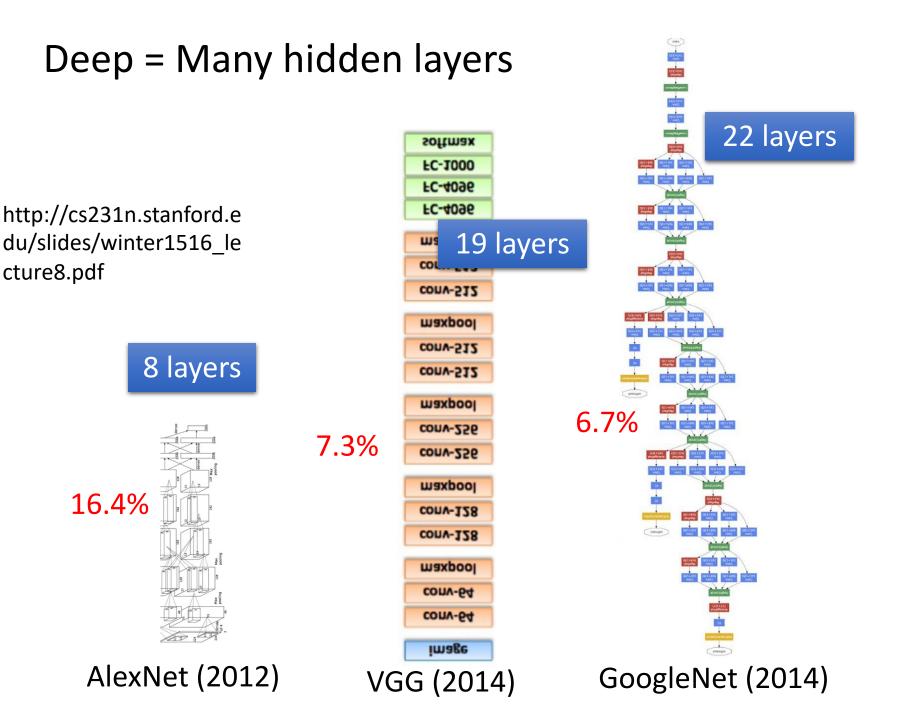
It is not *fancy* enough.

Let's give it a *fancy* name!

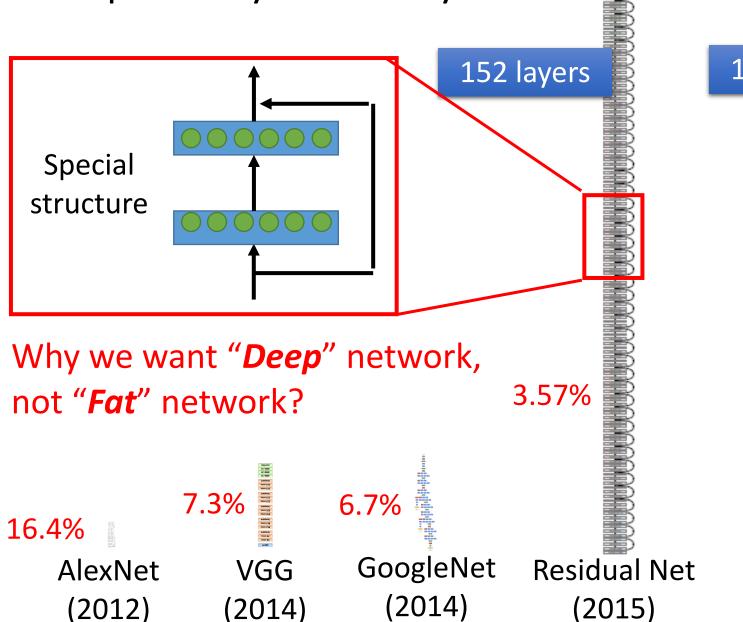


Neural Network This mimics human brains ... (???)

Many layers means **Deep** Deep Learning



Deep = Many hidden layers





101

Why don't we go deeper?

- Loss for multiple hidden layers
 - 100 ReLU for each layer
 - input features are the no. of views in the past 56 days

	1 layer	2 layer	3 layer
2017 – 2020	0.28k	0.18k	0.14k
2021	0.43k	0.39k	0.38k

Why don't we go deeper?

- Loss for multiple hidden layers
 - 100 ReLU for each layer
 - input features are the no. of views in the past 56 days

	1 layer	2 layer	3 layer	4 layer
2017 – 2020	0.28k	0.18k	0.14k	0.10k
2021	0.43k	0.39k	0.38k	0.44k

Better on training data, worse on unseen data



Let's predict no. of views today!

 If we want to select a model for predicting no. of views today, which one will you use?

	1 layer	2 layer	3 layer	4 layer
2017 – 2020	0.28k	0.18k	0.14k	0.10k
2021	0.43k	0.39k	0.38k	0.44k

We will talk about model selection next time. ©

To learn more

Basic Introduction



https://youtu.be/Dr-WRIEFefw

Backpropagation

Computing gradients in an efficient way



https://youtu.be/ibJpTrp5mcE