# MLD2P4 User's and Reference Guide

A guide for the Multi-Level Domain Decomposition Parallel Preconditioners Package based on PSBLAS

Pasqua D'Ambra ICAR-CNR, Naples, Italy

**Daniela di Serafino** Second University of Naples, Italy

Salvatore Filippone University of Rome "Tor Vergata", Italy

> Software version: 1.0 June 25, 2008

#### Abstract

MLD2P4 (MULTI-LEVEL DOMAIN DECOMPOSITION PARALLEL PRE-CONDITIONERS PACKAGE BASED ON PSBLAS) is a package of parallel algebraic multi-level preconditioners. It implements various versions of one-level additive and of multi-level additive and hybrid Schwarz algorithms. In the multi-level case, a purely algebraic approach is applied to generate coarse-level corrections, so that no geometric background is needed concerning the matrix to be preconditioned. The matrix is required to be square, real or complex, with a symmetric sparsity pattern

MLD2P4 has been designed to provide scalable and easy-to-use preconditioners in the context of the PSBLAS (Parallel Sparse Basic Linear Algebra Subprograms) computational framework and can be used in conjuction with the Krylov solvers available in this framework. MLD2P4 enables the user to easily specify different aspects of a generic algebraic multilevel Schwarz preconditioner, thus allowing to search for the "best" preconditioner for the problem at hand. The package has been designed employing object-oriented techniques, using Fortran 95 and MPI, with interfaces to additional external libraries such as UMFPACK, SuperLU and SuperLU\_Dist, that can be exploited in building multi-level preconditioners.

The software is freely distributable, under the terms of the license in Appendix A.

This guide provides a brief description of the functionalities and the user interface of MLD2P4.

# Contents

1	General Overview	1
2	Notational Conventions	3
3	Configuring and Building MLD2P4	4
4	Getting Started 4.1 Examples	<b>5</b>
5	User Interface 5.1 Subroutine mld_precinit	11 16 17
6	Error Handling	19
A	License	20
В	Bibliography	21

#### 1 General Overview

The Multi-Level Domain Decomposition Parallel Preconditioners Package based on PSBLAS (MLD2P4) provides multi-level Schwarz preconditioners [14], to be used in the iterative solutions of sparse linear systems:

$$Ax = b, (1)$$

where A is a square, real or complex, sparse matrix with a symmetric sparsity pattern. These preconditioners have the following general features:

- both additive and hybrid multilevel variants are implemented, i.e. variants that are additive among the levels and inside each level, and variants that are multiplicative among the levels and additive inside each level; the basic Additive Schwarz (AS) preconditioners are obtained by considering only one level:
- a purely algebraic approach is used to generate a sequence of coarse-level corrections to a basic AS preconditioner, without explicitly using any information on the geometry of the original problem (e.g. the discretization of a PDE). The smoothed aggregation technique is applied as algebraic coarsening strategy [1, 18].

The package is written in Fortran 95, following an object-oriented approach through the exploitation of features such as abstract data type creation, functional overloading and dynamic memory management. The parallel implementation is based on a Single Program Multiple Data (SPMD) paradigm for distributed-memory architectures. Single and double precision implementations of MLD2P4 are available for both the real and the complex case, that can be used through a single interface.

MLD2P4 has been designed to implement scalable and easy-to-use multilevel preconditioners in the context of the PSBLAS (Parallel Sparse BLAS) computational framework [12]. PSBLAS is a library originally developed to address the parallel implementation of iterative solvers for sparse linear system, by providing basic linear algebra operators and data management facilities for distributed sparse matrices; it also includes parallel Krylov solvers, built on the top of the basic PSBLAS kernels. The preconditioners available in MLD2P4 can be used with these Krylov solvers. The choice of PSBLAS has been mainly motivated by the need of having a portable and efficient software infrastructure implementing "de facto" standard parallel sparse linear algebra kernels, to pursue goals such as performance, portability, modularity ed extensibility in the development of the preconditioner package. On the other hand, the implementation of MLD2P4 has led to some revisions and extentions of the PSBLAS kernels, leading to the recent PSBLAS 2.0 version [11]. The inter-process comunication required by MLD2P4 is encapsulated into the PSBLAS routines, except few cases where MPI [15] is explicitly called. Therefore, MLD2P4 can be run on any parallel machine where PSBLAS and MPI implementations are available.

MLD2P4 has a layered and modular software architecture where three main layers can be identified. The lower layer consists of the PSBLAS kernels, the middle one implements the construction and application phases of the preconditioners, and the upper one provides a uniform and easy-to-use interface to all the preconditioners. This architecture allows for different levels of use of

1 General Overview

2

the package: few black-box routines at the upper layer allow non-expert users to easily build any preconditioner available in MLD2P4 and to apply it within a PSBLAS Krylov solver. On the other hand, the routines of the middle and lower layer can be used and extended by expert users to build new versions of multi-level Schwarz preconditioners. We provide here a description of the upper-layer routines, but not of the medium-layer ones.

This guide is organized as follows: ORGANIZZAZIONE DELLA GUIDA

### 2 Notational Conventions

- caratteri tipografici usati nella guida (vedi guida ML recente e guida Aztec)
- convenzioni sui nomi di routine (differenza nei nomi tra high-level e medium-level), strutture dati, moduli, costanti, etc. (vedi guida psblas)
- versione reale e complessa, singola e doppia precisione

## 3 Configuring and Building MLD2P4

- uso di GNU autoconf e automake
- software di base necessario (MPI, BLACS, BLAS, PSBLAS, UMFPACK ? specificare versioni)
- software opzionale (SuperLU, SuperLUdist specificare versioni e opzioni di configure)
- sistemi operativi e compilatori su cui MLD2P4 e' stato costruito con successo
- sono previste opzioni di configurazione per il debugging o per il profiling?
- albero delle directory generato al momento dell'installazione

### 4 Getting Started

We describe the basics for building and applying MLD2P4 one-level and multilevel Schwarz preconditioners with the Krylov solvers included in PSBLAS [11]. The following steps are required:

- 1. Declare the preconditioner data structure. It is a derived data type, mld\_-xprec\_type, where x may be s, d, c or z, according to the basic data type of the sparse matrix (s = real single precision; d = real double precision; c = complex single precision; z = complex double precision). This data structure is accessed by the user only through the MLD2P4 routines, following an object-oriented approach.
- 2. Allocate and initialize the preconditioner data structure, according to a preconditioner type chosen by the user. This is performed by the routine mld\_precinit, which also sets defaults for each preconditioner type selected by the user. The defaults associated to each preconditioner type are listed in Table 1, where the strings used by mld\_precinit to identify the preconditioner types are also given.
- 3. Modify the selected preconditioner type, by properly setting preconditioner parameters. This is performed by the routine mld\_precset. This routine must be called only if the user wants to modify the default values of the parameters associated to the selected preconditioner type, to obtain a variant of the preconditioner. Examples of use of mld\_precset is given in Section 4.1; a complete list of all the preconditioner parameters and their allowed and default values is provided in Section 5, Tables 2-5.
- 4. Build the preconditioner for a given matrix. This is performed by the routine mld\_precbld.
- 5. Apply the preconditioner at each iteration of a Krylov solver. This is performed by the routine mld\_precaply. When using the PSBLAS Krylov solvers, this step is completely transparent to the user, since mld\_precaply is called by the PSBLAS routine implementing the Krylov solver (psb\_krylov).
- 6. Free the preconditioner data structure. This is performed by the routine mld\_precfree. This step is complementary to step 1 and should be performed when the preconditioner is no more used.

A detailed description of the above routines is given in Section 5.

Note that the Fortran 95 module mld\_prec\_mod must be used in the program calling the MLD2P4 routines; this requires also the use of the psb\_base\_mod for the sparse matrix and communication descriptor data types, as well as for the kind parameters for vectors, and the use of the module psb\_krylov\_mod for interfacing with the Krylov solvers. Note that the include path for MLD2P4 must override those for the base PSBLAS, e.g. they must come first in the sequence passed to the compiler, as the MLD2P4 version of the Krylov interfaces must override that of PSBLAS. This will change in the future when the support for the class statement becomes widespread in Fortran compilers. Examples showing the basic use of MLD2P4 are reported in Section 4.1.

**Remark.** The coarsest-level solver used by the default two-level preconditioner has been chosen by taking into account that, on parallel machines, it often leads

to the smallest execution time when applied to linear systems coming from finite-difference discretizations of basic elliptic PDE problems, considered as standard tests for multi-level Schwarz preconditioners [3, 4]. However, this solver does not necessarily to the smallest number of iterations of the preconditioned Krylov method, which is usually obtained by applying a direct solver, e.g. based on the LU factorization, on a matrix replicated at the coarsest level (see Section 5 for coarsest-level solvers available in MLD2P4).

Type	String	Default preconditioner
No preconditioner	'NOPREC'	(Considered only to use the PSBLAS Krylov
		solvers with no preconditioner.)
Diagonal	'DIAG'	_
Block Jacobi	'BJAC'	Block Jacobi with ILU(0) on the local
		blocks.
Additive Schwarz	'AS'	Restricted Additive Schwarz (RAS), with overlap 1 and ILU(0) on the local blocks.
Multilevel	'ML'	Multi-level hybrid preconditioner (additive on the same level and multiplicative through the levels), with post-smoothing only. Number of levels: 2; post-smoother: RAS with overlap 1 and with ILU(0) on the local blocks; coarsest matrix: distributed among the processors; (approximate) coarse-level solver: 4 sweeps of the block-Jacobi solver, with the UMFPACK LU factorization on the blocks (double precision versions) or XXXXXXXXXXXXXXXXXXXXXXXXXXXXXXXXXXX

Table 1: Preconditioner types, corresponding strings and default choices.

#### 4.1 Examples

The code reported in Figure 1 shows how to set and apply the default multi-level preconditioner available in the real double precision version of MLD2P4 (see Table 1). This preconditioner is chosen by simply specifying 'ML' as second argument of mld\_precinit (a call to mld\_precset is not needed) and is applied with the BiCGSTAB solver provided by PSBLAS. The setup and application of the default multi-level preconditioners for the real single precision and the complex, single and double precision, versions are obtained with straightforward modifications of the example.

The part of the code concerning the reading and assembling of the sparse matrix and the right-hand side vector, performed through the PSBLAS routines for sparse matrix and vector management, is not reported here for brevity; the statements concerning the deallocation of the PSBLAS data structure are neglected too. The complete code can be found in the example program file example\_ml.f90 in the directory XXXXXXX (COMPLETARE. DIRE CHE I FILE IN REALTA' SONO DUE, UNO CON LA GENERAZIONE DELLA MATRICE ED UNO CON LA LETTURA). Note that the mod-

ules psb\_base\_mod and psb\_util\_mod at the beginning of the code are required by PSBLAS. O psb\_base\_mod E' RICHIESTO ANCHE DA MLD2P4?) For details on the use of the PSBLAS routines, see the PSBLAS User's Guide [11].

# LE FIGURE SONO DECENTRATE, NONOSTANTE IL CENTER. CI VUOLE UNA MINIPAGE?

Different versions of multilevel preconditioner can be obtained by changing the default values of the preconditioner parameters. The code reported in Figure 2 shows how to set a three-level hybrid Schwarz preconditioner, which uses block Jacobi with ILU(0) on the local blocks as post-smoother, a coarsest matrix replicated on the processors, and the LU factorization from UMF-PACK [8], version 4.4, as coarse-level solver. The number of levels is specified by using mld\_precinit; the other preconditioner parameters are set by calling mld\_precset. Note that the type of multilevel framework (i.e. multiplicative among the levels with post-smoothing only) is not specified since it is the default set by mld\_precinit. Figure 3 shows how to set a three-level additive Schwarz preconditioner, which applies RAS, with overlap 1 and ILU(0) on the blocks, as pre- and post-smoother, and five block-Jacobi sweeps, with the UMFPACK LU factorization on the blocks, as distributed coarsest-level solver. Again, mld\_precset is used only to set non-default values of the parameters (see Tables 2-5). In both cases, the construction and the application of the preconditioner are carried out as for the default multi-level preconditioner. The code fragments shown in Figures 2-3 are included in the example program file example\_ml.f90. LO STESSO PROGRAMMA CONTIENE I TRE ESEMPI, CON UN SWITCH TRA L'UNO E L'ALTRO O FACCIAMO 3 PROGRAMMI DISTINTI? NON RICORDO CHE COSA ABBIAMO DECISO. PASQUA: ABBIAMO DETTO CHE ERA PREFERIBILE UN UNICO PROGRAMMA CON SWITCH.

Finally, Figure 4 shows the setup of a one-level additive Schwarz preconditioner, i.e. RAS with overlap 2. The corresponding code, including also the application of the preconditioner is in the example program file example\_1lev.f90.

**Remark.** Any PSBLAS-based program using the basic preconditioners implemented in PSBLAS 2.0, i.e. the diagonal and block-Jacobi ones, can use the diagonal and block-Jacobi preconditioners implemented in MLD2P4 without any change in the code. The PSBLAS-based program must be only recompiled and linked to the MLD2P4 library.

```
use psb_base_mod
 use psb_util_mod
 use mld_prec_mod
 use psb_krylov_mod
! sparse matrix
 type(psb_dspmat_type) :: A
! sparse matrix descriptor
 type(psb_desc_type) :: desc_A
! preconditioner
 type(mld_dprec_type) :: P
!
! initialize the parallel environment
 call psb_init(ictxt)
 call psb_info(ictxt,iam,np)
. . . . . .
! read and assemble the matrix {\tt A} and the right-hand
! side b using PSBLAS routines for sparse matrix /
! vector management
! initialize the default multi-level preconditioner,
! i.e. two-level hybrid Schwarz, using RAS (with
! overlap 1 and ILU(0) on the blocks) as post-smoother
! and 4 block-Jacobi sweeps (with UMFPACK LU on the
! blocks) as distributed coarse-level solver
 call mld_precinit(P,'ML',info)
! build the preconditioner
 call psb_precbld(A,P,desc_A,info)
!\ \mbox{set} the solver parameters and the initial guess
! solve Ax=b with preconditioned BiCGSTAB
 call psb_krylov('BICGSTAB',A,P,b,x,tol,desc_A,info)
! deallocate the preconditioner
 call mld_precfree(P,info)
! deallocate other data structures
 . . . . . .
! exit the parallel environment
 call psb_exit(ictxt)
 stop
```

Figure 1: Setup and application of the default multi-level Schwarz preconditioner.

```
! set a three-level hybrid Schwarz preconditioner,
! which uses block Jacobi (with ILU(0) on the blocks)
! as post-smoother, a coarsest matrix replicated on the
! processors, and the LU factorization from UMFPACK
! as coarse-level solver
    call mld_precinit(P,'ML',info,nlev=3)
    call_mld_precset(P,mld_smoother_type_,'BJAC',info)
    call mld_precset(P,mld_coarse_mat,'REPL')
    call mld_precset(P,mld_coarse_solve,'UMF')
```

Figure 2: Setup of a hybrid three-level Schwarz preconditioner.

```
! set a three-level additive Schwarz preconditioner,
! which uses RAS (with overlap 1 and ILU(0) on the blocks)
! as pre- and post-smoother, and 5 block-Jacobi sweeps
! (with UMFPACK LU on the blocks) as distributed
! coarsest-level solver
  call mld_precinit(P,'ML',info,nlev=3)
  call mld_precset(P,mld_ml_type_,'ADD',info)
  call_mld_precset(P,mld_smoother_pos_,'TWOSIDE',info)
  call mld_precset(P,mld_coarse_sweeps_,5)
```

Figure 3: Setup of an additive three-level Schwarz preconditioner.

```
! set RAS with overlap 2 and ILU(0) on the local blocks
call mld_precinit(P,'AS',info)
call mld_precset(P,mld_sub_ovr_,2,info)
```

Figure 4: Setup of a one-level Schwarz preconditioner.

#### 5 User Interface

The basic user interface of MLD2P4 consists of six routines. The four routines mld\_precinit, mld\_precset, mld\_precbld and mld\_precaply encapsulate all the functionalities for the setup and application of any one-level and multilevel preconditioner implemented in the package. The routine mld\_precfree deallocates the preconditioner data structure, while mld\_precdescr prints a description of the preconditioner setup by the user.

For each routine, the same user interface is overloaded with respect to the real/complex case and the single/double precision; arguments with appropriate data types must be passed to the routine, i.e.

- the sparse matrix data structure, containing the matrix to be preconditioned, must be of type mld\_xspmat\_type with x = s for real single precision, x = d for real double precision, x = c for complex single precision, x = c for complex double precision;
- the preconditioner data structure must be of type mld\_xprec\_type, with x = s, d, c, z, according to the sparse matrix data structure;
- the arrays containing the vectors v and w involved in the preconditioner application  $w = M^{-1}v$  must be of type  $type(kind\_parameter)$ , with type = real, complex and  $kind\_parameter = kind(1.e0)$ , kind(1.d0), according to the sparse matrix and preconditioner data structure; note that the PSBLAS module provides the constants  $psb\_spk\_ = kind(1.e0)$  and  $psb\_dpk\_ = kind(1.d0)$ ;
- real parameters defining the preconditioner must be declared according to the precision of the previous data structures (see Section 5.2).

A description of each routine is given in the remainder of this section.

#### 5.1 Subroutine mld\_precinit

```
mld_precinit(p,ptype,info)
mld_precinit(p,ptype,info,nlev)
```

This routine allocates and initializes the preconditioner data structure, according to the preconditioner type chosen by the user.

#### Arguments

```
p          type(mld_xprec_type), intent(inout).
          The preconditioner data structure. Note that x must be chosen according
          to the real/complex, single/double precision version of MLD2P4 under use.
ptype     character(len=*), intent(in).
          The type of preconditioner. Its values are specified in Table 1.
info     integer, intent(out).
          Error code. See Section 6 for details.
nlev     integer, optional, intent(in).
          The number of levels of the multilevel preconditioner. If nlev is not present and ptype='ML'/'ml', then nlev=2 is assumed. Otherwise, nlev is ignored.
```

#### 5.2 Subroutine mld\_precset

mld\_precset(p,what,val,info)

This routine sets the parameters defining the preconditioner. More precisely, the parameter identified by what is assigned the value contained in val.

#### Arguments

p type(mld\_xprec\_type), intent(inout).

The preconditioner data structure. Note that x must be chosen according to the real/complex, single/double precision version of MLD2P4 under use.

what integer, intent(in).

The number identifying the parameter to be set. A mnemonic constant has been associated to each of these numbers, as reported in Tables 2-5.

val integer or character(len=\*) or real(psb\_spk\_) or real(psb\_dpk\_),
 intent(in).

The value of the parameter to be set. The list of allowed values and the corresponding data types is given in Table ??.

info integer, intent(out).

Error code. See Section 6 for details.

A variety of (one-level and multi-level) preconditioner can be obtained by a suitable setting of the preconditioner parameters. These parameters can be logically divided into four groups, i.e. parameters defining

- 1. the type of multi-level preconditioner;
- 2. the one-level preconditioner to be used as smoother;
- 3. the aggregation algorithm;
- 4. the coarse-space correction at the coarsest level.

A list of the parameters that can be set, along with their allowed and default values, is given in Tables 2-5. CORREGGERE LA ROUTINE E LA DOC INTERNA - ilev NON E' PIU' ACCESSIBILE ALL'UTENTE.

	aata type	val	default	comments
mld_ml_type_ c]	character(len=*)	'ADD'	,MULT,	basic multi-level framework: additive or mul-
		'MULT'		tiplicative among the levels always additive in-
				side a level)
mld_smoother_type_ c	character(len=*)	'DIAG'	$^{\prime}\mathrm{AS}^{\prime}$	basic one-level preconditioner (i.e. smoother)
		'BJAC'		of the multi-level preconditioner
		$^{\prime}\mathrm{AS}^{\prime}$		
mld_smoother_pos_ c	character(len=*)	'PRE'	'POST'	"position" of the smoother: pre-smoother,
		'POST'		post-smoother, pre-/post-smoother
		'TWOSIDE'		

Table 2: Parameters defining the type of multi-level preconditioner.

what	data type	val	default	comments
mld_sub_ovr	integer	any number	1	number of overlap in the basic Schwarz pre-
		0 <1		conditioner
mld_sub_restr_	character(len=*)	'HALO'	'HALO'	type of restriction operator used in basic
		'NONE'		Schwarz preconditioner: 'HALO' for taking
				into account contributions from the overlap
mld_sub_prol_	character(len=*)	'SUM'	'NONE'	type of prolongator operator used in basic
		'NONE'		Schwarz preconditioner: 'NONE' for neglect-
				ing contributions from the overlap
mld_sub_solve_	character(len=*)	JLU,	'UMF'	available local solver: 'ILU' for incomplete
		'MILU'		LU, 'MILU' for modified incomplete LU,
		'ILUT'		'ILUT' for incomplete LU with threshold,
		'UMF'		'UMF' for complete LU using UMFPACK [8]
		SLU'		version 4.4, 'SLU' for complete LU using Su-
				perLU $[9]$ , version 3.0
mld_sub_fillin_ integer	integer	any number 0	0	fill-in level for 'ILU', 'MILU' and 'ILUT' of
		0 <		local blocks
mld_sub_thresh_	real	any number $0$ .	0.	drop tolerance for 'ILUT'
		∨ 0.		
mld_sub_ren_	character(len=*)	'RENUM_NONE',	臣',	reordering algorithm for the local blocks
		'RENUM_GL\(\phi\)BAL'	BAL'	

Table 3: Parameters defining the basic one-level preconditioner (smoother).

 $\underline{\textbf{5}\ User\ Interface}$ 

what	$data \ type$	val	default	comments
mld_aggr_alg_	character(len=*)	'DEC'	'DEC'	define the aggregation scheme. Now, only de-
				coupled aggregation is available
mld_aggr_kind_	character(len=*)	'SMOOTH',	'SMOOTH'	define the type of aggregation technique
		'RAW'		(smoothed or nonsmoothed).
mld_aggr_thresh_	real	any number	0.	dropping threshold in aggregation
		$\in [0, 1]$		
mld_aggr_eig_	character(len=*)	'A_NORMI'		define the algorithm to evaluate the maximum
				eigenvalue of $D^{-1}A$ for smoothed aggregation.
				Currently only the infinity norm of the matrix
				A is available

Table 4: Parameters defining the aggregation algorithm.

mld_coarse_mat_ char	character(len=*)		· CECTO	
		'DISTR', 'REPL'	DISTR	Coarse matrix: distributed or replicated
mld_coarse_solve_ char	character(len=*)	'BJAC'	'BJAC'	VEDI OSSERVAZIONI EMAIL 15-
		'UMF'		16/06/08 available solver for coarse system. Only 'B.IAC' and 'SLIIDIST' can be used
				for distributed coarse matrix. 'BJAC' cor-
				responds to some sweeps of a block-Jacobi
				solver, while 'SLUDIST' corresponds to the
				use of the external package SuperLU_Dist [13],
				version 2.0, for distributed sparse factorization
mld coarse subsolve char	character(len=*)	'ILU'	'UMF'	VEDI OSSERVAZIONI EMAIL 15-
		'MILU'		16/06/08 available solver for diagonal local
		'ILUT'		blocks of the coarse matrix, when BJAC is
		'UMF'		used as coarse solver
		STU,		
mld_coarse_sweeps_ inte	integer	any number	4	number of Block-Jacobi sweeps when 'BJAC'
		0 <		is used as coarse solver
mld_coarse_fillin_ inte	integer	any number	0	fill-in level in incomplete factorization of lo-
		0 <		cal diagonal blocks of the coarse matrix, when
				'BJAC' is used as coarse solver and 'ILU' or
				'MILU' is used as local solver MODIFICA
				NOME PARAM. NEL SW
mld_coarse_thresh_ real		any number	0.	drop tolerance in incomplete factorization of
				local diagonal blocks of the coarse matrix,
				when 'BJAC' is used as coarse solver and
				'ILUT' is used as local solver

Table 5: Parameters defining the coarse-space correction at the coarsest level.

#### 5.3 Subroutine mld\_precbld

mld\_precbld(a,desc\_a,p,info)

This routine builds the preconditioner according to the requirements made by the user through the routines mld\_precinit and mld\_precset.

#### Arguments

a type(psb\_xspmat\_type), intent(in).

The sparse matrix structure containing the local part of the matrix to be preconditioned. Note that x must be chosen according to the real/complex, single/double precision version of MLD2P4 under use. See the PSBLAS User's Guide for details [11].

desc\_a type(psb\_desc\_type), intent(in).

The communication descriptor of a. See the PSBLAS User's Guide for details [11].

p type(mld\_xprec\_type), intent(inout).

The preconditioner data structure. Note that x must be chosen according to the real/complex, single/double precision version of MLD2P4 under use.

info integer, intent(out).

Error code. See Section 6 for details.

#### 5.4 Subroutine mld\_precaply

mld\_precaply(p,x,y,desc\_a,info)
mld\_precaply(p,x,y,desc\_a,info,trans,work)

This routine computes  $y = op(M^{-1})x$ , where M is a previously built preconditioner, stored in the p data structure, and op denotes the preconditioner itself or its transpose, according to the value of trans. Note that, when MLD2P4 is used with a Krylov solver from PSBLAS, mld\_precaply is called within the PSBLAS routine mld\_krylov and hence is completely transparent to the user.

#### Arguments

p type( $mld_xprec_type$ ), intent(inout). The preconditioner data structure, containing the local part of M. Note that x must be chosen according to the real/complex, single/double precision

x type(kind\_parameter), dimension(:), intent(in).

The local part of the vector x. Note that type and kind\_parameter must be chosen according to the real/complex, single/double precision version of MLD2P4 under use.

y type(kind\_parameter), dimension(:), intent(out).

The local part of the vector y. Note that type and kind\_parameter must be chosen according to the real/complex, single/double precision version of MLD2P4 under use.

info integer, intent(out). Error code. See Section 6 for details.

version of MLD2P4 under use.

trans character(len=1), optional, intent(in). If trans = 'N', 'n' then  $op(M^{-1}) = M^{-1}$ ; if trans = 'T', 't' then  $op(M^{-1}) = M^{-T}$  (transpose of  $M^{-1}$ ); if trans = 'C', 'c' then  $op(M^{-1}) = M^{-C}$  (conjugate transpose of  $M^{-1}$ ).

work type(kind\_parameter), dimension(:), optional, target.
Workspace. Its size should be at least
4 \* psb\_cd\_get\_local\_cols(desc\_a) (see the PSBLAS User's Guide).
Note that type and kind\_parameter must be chosen according to the real/complex, single/double precision version of MLD2P4 under use.

#### 5.5 Subroutine mld\_precfree

mld\_precfree(p,info)

This routine deallocates the preconditioner data structure.

#### Arguments

p type(mld\_xprec\_type), intent(inout).

The preconditioner data structure. Note that x must be chosen according to the real/complex, single/double precision version of MLD2P4 under use.

info integer, intent(out).

Error code. See Section 6 for details.

#### 5.6 Subroutine mld\_precdescr

mld\_precdescr(p,iout)

This routine prints a description of the preconditioner to a file.

#### Arguments

p type(mld\_xprec\_type), intent(in).

The preconditioner data structure. Note that x must be chosen according to the real/complex, single/double precision version of MLD2P4 under use.

iout integer, intent(in), optional.

The id of the file where the preconditioner description will be printed, default is standard output.

<u>6 Error handling</u> 19

## 6 Error Handling

Error handling - Breve descrizione con rinvio alla guida di PSBLAS

A License 20

#### A License

The MLD2P4 is freely distributable under the following copyright terms:

MLD2P4 version 1.0

MultiLevel Domain Decomposition Parallel Preconditioners Package based on PSBLAS (Parallel Sparse BLAS version 2.3)

(C) Copyright 2008

Salvatore Filippone University of Rome Tor Vergata
Alfredo Buttari University of Rome Tor Vergata

Pasqua D'Ambra ICAR-CNR, Naples

Daniela di Serafino Second University of Naples

Redistribution and use in source and binary forms, with or without modification, are permitted provided that the following conditions are met:

- 1. Redistributions of source code must retain the above copyright notice, this list of conditions and the following disclaimer.
- 2. Redistributions in binary form must reproduce the above copyright notice, this list of conditions, and the following disclaimer in the documentation and/or other materials provided with the distribution.
- The name of the MLD2P4 group or the names of its contributors may not be used to endorse or promote products derived from this software without specific written permission.

THIS SOFTWARE IS PROVIDED BY THE COPYRIGHT HOLDERS AND CONTRIBUTORS
''AS IS'' AND ANY EXPRESS OR IMPLIED WARRANTIES, INCLUDING, BUT NOT LIMITED
TO, THE IMPLIED WARRANTIES OF MERCHANTABILITY AND FITNESS FOR A PARTICULAR
PURPOSE ARE DISCLAIMED. IN NO EVENT SHALL THE MLD2P4 GROUP OR ITS CONTRIBUTORS
BE LIABLE FOR ANY DIRECT, INDIRECT, INCIDENTAL, SPECIAL, EXEMPLARY, OR
CONSEQUENTIAL DAMAGES (INCLUDING, BUT NOT LIMITED TO, PROCUREMENT OF
SUBSTITUTE GOODS OR SERVICES; LOSS OF USE, DATA, OR PROFITS; OR BUSINESS
INTERRUPTION) HOWEVER CAUSED AND ON ANY THEORY OF LIABILITY, WHETHER IN
CONTRACT, STRICT LIABILITY, OR TORT (INCLUDING NEGLIGENCE OR OTHERWISE)
ARISING IN ANY WAY OUT OF THE USE OF THIS SOFTWARE, EVEN IF ADVISED OF THE
POSSIBILITY OF SUCH DAMAGE.

B Bibliography 21

## B Bibliography

[1] M. Brezina, P. Vaněk, A Black-Box Iterative Solver Based on a Two-Level Schwarz Method, Computing, 63, 1999, 233–263.

- [2] A. Buttari, P. D'Ambra, D. di Serafino, S. Filippone, Extending PSBLAS to Build Parallel Schwarz Preconditioners, in , J. Dongarra, K. Madsen, J. Wasniewski, editors, Proceedings of PARA 04 Workshop on State of the Art in Scientific Computing, Lecture Notes in Computer Science, Springer, 2005, 593–602.
- [3] A. Buttari, P. D'Ambra, D. di Serafino, S. Filippone, 2LEV-D2P4: a package of high-performance preconditioners, Applicable Algebra in Engineering, Communications and Computing, 18, 3, May, 2007, 223–239.
- [4] P. D'Ambra, S. Filippone, D. Di Serafino, On the Development of PSBLAS-based Parallel Two-level Schwarz Preconditioners, Applied Numerical Mathematics, Elsevier Science, 57, 11-12, 2007, 1181-1196.
- [5] X. C. Cai, M. Sarkis, A Restricted Additive Schwarz Preconditioner for General Sparse Linear Systems, SIAM Journal on Scientific Computing, 21, 2, 1999, 792–797.
- [6] X. C. Cai, O. B. Widlund, Domain Decomposition Algorithms for Indefinite Elliptic Problems, SIAM Journal on Scientific and Statistical Computing, 13, 1, 1992, 243–258.
- [7] T. Chan and T. Mathew, *Domain Decomposition Algorithms*, in A. Iserles, editor, Acta Numerica 1994, 61–143. Cambridge University Press.
- [8] T.A. Davis, Algorithm 832: UMFPACK an Unsymmetric-pattern Multifrontal Method with a Column Pre-ordering Strategy, ACM Transactions on Mathematical Software, 30, 2004, 196-199. (See also http://www.cise.ufl.edu/davis/)
- [9] J.W. Demmel, S.C. Eisenstat, J.R. Gilbert, X.S. Li and J.W.H. Liu, A supernodal approach to sparse partial pivoting, SIAM Journal on Matrix Analysis and Applications, 20, 3, 1999, 720–755.
- [10] E. Efstathiou, J. G. Gander, Why Restricted Additive Schwarz Converges Faster than Additive Schwarz, BIT Numerical Mathematics, 43, 2003, 945– 959.
- [11] S. Filippone, A. Buttari, PSBLAS-2.1 User's Guide. A Reference Guide for the Parallel Sparse BLAS Library, xxxxx.
- [12] S. Filippone, M. Colajanni, PSBLAS: A Library for Parallel Linear Algebra Computation on Sparse Matrices, ACM Transactions on Mathematical Software, 26, 4, 2000, 527–550.
- [13] X. S. Li, J. W. Demmel, SuperLU\_DIST: A Scalable Distributed-memory Sparse Direct Solver for Unsymmetric Linear Systems, ACM Transactions on Mathematical Software, 29, 2, 2003, 110–140.

B Bibliography 22

[14] B. Smith, P. Bjorstad, W. Gropp, Domain Decomposition: Parallel Multilevel Methods for Elliptic Partial Differential Equations, Cambridge University Press, 1996.

- [15] M. Snir, S. Otto, S. Huss-Lederman, D. Walker, J. Dongarra, *MPI: The Complete Reference. Volume 1 The MPI Core*, second edition, MIT Press, 1998.
- [16] K. Stüben, Algebraic Multigrid (AMG): an Introduction with Applications, in A. Schüller, U. Trottenberg, C. Oosterlee, editors, Multigrid, Academic Press, 2000.
- [17] R. S. Tuminaro, C. Tong, Parallel Smoothed Aggregation Multigrid: Aggregation Strategies on Massively Parallel Machines, in J. Donnelley, editor, Proceedings of SuperComputing 2000, Dallas, 2000.
- [18] P. Vaněk, J. Mandel and M. Brezina, Algebraic Multigrid by Smoothed Aggregation for Second and Fourth Order Elliptic Problems, Computing, 1996, 56, 179-196.