Locally-Oriented Programming: A Simple Programming Model for Stencil-Based Computations on Multi-Level Distributed Memory Architectures

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Abstract. Emerging hybrid accelerator architectures for high performance computing are often suited for the use of a data-parallel programming model. Unfortunately, programmers of these architectures face a steep learning curve that frequently requires learning a new language (e.g., OpenCL). Furthermore, the distributed (and frequently multi-level) nature of the memory organization of clusters of these machines provides an additional level of complexity. This paper presents preliminary work examining how programming with a local orientation can be employed to provide simpler access to accelerator architectures. A locally-oriented programming model is especially useful for the solution of algorithms requiring the application of a stencil or convolution kernel. In this programming model, a programmer codes the algorithm by modifying only a single array element (called the local element), but has read-only access to a small sub-array surrounding the local element. We demonstrate how a locally-oriented programming model can be adopted as a language extension using source-to-source program transformations.

Keywords: domain specific language, stencil compiler, distributed memory parallelism

1 Introduction

Historically it has been hard to create parallel programs. The responsibility (and difficulty) of creating *correct* parallel programs can be viewed as being spread between the programmer and the compiler. Ideally we would like to have parallel languages that make it easy for the programmer to express correct parallel programs — and conversely it should be difficult to express incorrect parallel programs. Unfortunately, many current languages and standards place all of the responsibility on the user. The best example of this are programs written using MPI (Message Passing Interface), where the programmer expresses all parallelism in terms of calls to library routines and the serial C or Fortran compiler knows nothing about the parallel semantics of the combined language plus MPI library.

2 Locally-Oriented Programming

Of course one would hope that over time code complexity goes down as better languages allow compilers to take on a greater share of the parallel complexity burden. Multithreaded code written using OpenMP can be significantly simpler than the corresponding code in which the programmer explicitly manages a pool of threads themselves. This is somewhat true for distributed memory parallelism using Unified Parallel C (UPC) and Coarray Fortran. With these PGAS (Partitioned Global Address Space) extensions, C and Fortran compilers are now aware of parallelism and now generate message passing code that previously had been handled by the MPI library. In some instances the compiler is able to perform optimizations that it is not able to do with a library-based scheme like MPI [13].

However, in large part these languages are mostly syntactic sugar for message passing and do not provide a substantial decrease in code complexity when application performance is a goal [8]. While skilled programmers in the HPC community have become accustomed to the level of complexity of an MPI program, the problem for programmers is that hardware is changing in ways that increase the level of on-chip parallelism. Indeed, the current generation of machines could be the last to provide homogeneous multi-core parallelism [6]. For ultimate performance, programmers must envision coding for heterogeneous architectures with huge new levels of on-node parallelism, at the same time they account for off-node parallelism. Since languages have not evolved that allow the compiler to take up this increase, the complexity for a programmer has necessarily dramatically increased. Unfortunately, considering the complexity of large multiphysics code frameworks, it could take several person years to retarget an application for each new heterogeneous platform [7].

A reasonable solution given today's language limitations is to use MPI for distributed memory parallelism *plus* OpenMP for on-chip parallelism. This hybrid approach is taken by two successful, large-scale AMR multiphysics code frameworks, FLASH and Chombo; currently however, neither of these codes support hardware accelerators [7]. Other choices for expressing on-chip parallelism are OpenCL [10] and NVIDIA's CUDA. Unfortunately, achieving high performance using either of these two languages can be a daunting challenge and there are no guarantees that either language is suitable for future hardware generations.

In this paper we examine a language-based paradigm that allows the compiler to take on a larger portion of the code complexity burden. Anyone programming in OpenCL is aware that explicit loop structures over array elements in a serial program are removed and replaced by a kernel program that is run over all of the elements of the input arrays. We propose *Locally Orientated Programming extensions* (LOPe) to the Fortran and potentially C languages that formally adopt this programming model. The LOPe programming model explicitly separates numerical complexity from parallel complexity — leaving much of the staging and assembling of data to the compiler — and is applicable to the solution of stencil-based algorithms that provide data access patterns that are regular and spatially local.

2 Programming Model

The LOPe programming model restricts the programmer to a local view of the index space of an array. Within a LOPe function, only a single array element (called the local element) is mutable. In addition, a small halo region surrounding the local element is visible to the programmer, but this region is immutable. Restricting the programmer to a local index space serves to reduce complexity by separating all data- and task-decomposition concerns from the implementation of the element-level array calculations.

LOPe is a domain specific language (DSL) implemented as a small extension to the Fortran 2008 standard. Fortran was chosen as the base language for LOPe because it provides a rich array-based syntax. Although, in principle, the same techniques could be applied to languages such as C or C++.

2.1 Related work

LOPe builds upon prior work studying how to map Fortran to accelerator programming models like OpenCL. In the ForOpenCL project [14] we exploited Fortran's pure and elemental functions to express data-parallel kernels of an OpenCL-based program. In practice, array calculations for a given index i, j will require read-only access to a local neighborhood of size [M, N] around i, j. LOPe extends this work by introducing a mechanism for representing these neighborhoods as array declaration type annotations.

For OpenCL was based on concepts explored in the ZPL programming language [3] in which the programmer can define regions and operators that are applied over the index sets corresponding to the sub-array regions. This approach is quite powerful for compilation purposes since it provides a clean decoupling of the operators applied over an array from the decomposition of that array over a potentially complex distributed memory hierarchy. However, unlike the ZPL operations on entire sub-arrays, LOPe expresses operations based on a *single* local array-element.

2.2 LOPe Syntax Extensions

There are only a few syntactic additions required for a LOPe program. These additions include syntax for describing halo regions and concurrent procedures. In code examples that follow, language additions are highlighted by the usage of capitalization for keywords that are either new or that acquire new usage.

Halo regions. The principle semantic element of LOPe is the concept of a halo. A halo is an "artificial" or "virtual" region surrounding an array that contains boundary-value information. Halo (also called ghost-cell) regions are commonly employed to unify array indexing schemes in the vicinity of an array boundary so that an array may be referenced using indices that fall "outside" of the logical domain of the array. In LOPe, the halo region is given explicit syntax so that

the compiler can exploit this information for purposes of memory allocation, data replication and thread synchronization. For example, a halo region can be declared with a statement of the form,

```
real, allocatable, dimension(:), HALO(1:*:1) :: A
```

This statement indicates that A is a rank one array, will be allocated later, and has a halo region of one element surrounding the array on either side. The halo notation M:*: N specifies a halo of M elements to the left, N elements to the right, and an arbitrary number of "interior" array elements. When used to describe a formal parameter of a function, such as the type-declaration statement, real, HALO(:,:) :: U, the halo size is inferred by the compiler from the actual array argument provided at the calling site of the function.

Concurrent functions. The second keyword employed by LOPe is concurrent which already exists in the form of a do concurrent loop, whereby the programmer asserts that specific iterations of the loop body may be executed by the compiler in any order, even concurrently. LOPe allows a function with the attributes pure (assertion of no side effects) and concurrent (assertion of no dependencies between iterations) to be called from within a do concurrent loop. An example of a LOPe function is shown in Fig. 1 and an example calling this function will be provided later in the text. One should imagine that a LOPe function is called for each i, j index of the interior of the array U. Note that this usage introduces a race condition as new values of elements of U are created on the left-hand side of the assignment statement that may use new or old values of U on the right-hand side. LOPe requires the compiler to guarantee that race conditions won't occur by using, e.g., double-buffering techniques as needed.

```
pure CONCURRENT subroutine Laplacian(U)}
    real, HALO(:,:) :: U
    U(0,0) =
                              U(0,+1)
                U(-1,0)
                         -3*U(0, 0)
                                         U(+1,0)
                             U(0,-1)
end subroutine Laplacian
```

Fig. 1. A LOPe function implementing a Laplacian kernel in two dimensions.

LOPe index notation. In the Laplacian example the U(0,0) array element is the local array element and only the local element may be modified. This zerobased indexing for the local-array element differs from conventional Fortran, where by default, array indices start at 1. The use of zero-based indexing gives a clean symmetry for indices on either side of the central element at zero. The other array elements are in the halo region and are U(-1,0) and U(+1,0) (left and right of local, respectively) and U(0,-1) and U(0,+1) (below and above of local). The geometric positioning of the array elements can be seen by examining the arrangement of the expressions on the right-hand side of Fig. 1.

3 Coarray Fortran Extensions

Consider the Laplacian concurrent function in Fig. 1. In this section we demonstrate how this function can be called in the normal context of a program, one that allows full access to all of the interior elements of the array, as well as array elements within the logically exterior, halo-boundary region. Topics highlighted in this section are: 1. distributed memory array allocation; 2. explicit memory placement; 3. remote memory transfer; and 4. remote execution. This description is within the context of extensions to Fortran; as shorthand, these extensions are referred to as CAFe, for Coarray Fortran extensions. CAFe is complementary to previous work extending coarray Fortran [9,11].

3.1 Subimages

We must first introduce the important new concept of a CAFe subimage. Fortran images are a collection of distributed memory processes that all run the same program (image). LOPe extends the concept of a Fortran image by allowing images to be hierarchical. By this we mean that each image may have a subimage (or subimages), but this subimage is not visible to other regular Fortran images. Subimages also execute differently than normal images and may execute on different non-homogeneous hardware, e.g., an attached accelerator device. Subimages are task based while images all execute a Single Program but with different (Multiple) Data (SPMD). A task can be given to a subimage, but execution on the subimage terminates once the task is finished. Memory on a subimage is permanent, however, and must be explicitly allocated and deallocated.

One obtains a subimage by executing the new LOPe function call, <code>device = GET_SUBIMAGE(1)</code>, where the integer argument represents an attached hardware device (or a separate process). If the function fails (e.g., the requested device is unavailable) it returns the image number <code>this_image()</code> of the process that is executing the current program. Returning the current image allows program execution to proceed correctly even if there are no attached devices.

3.2 CAFe Example

We start with the declaration of an array with an explicit halo size and with two local dimensions (rank) and two distributed memory codimensions (corank),

The corank of the array is chosen to be identical to the rank of the array so that the logical process topology aligns in a way that allows a natural halo exchange between logically neighboring processes (this could not occur if corank and rank are not the same). For example, if the process location is [pcol,prow], then the right-hand halo for the local array U can be obtained by the assignment

U(M+1,:) = U(1,:)[pcol+1,prow] where the size and cosize of U are given by the allocation statement, allocate(U(0:M+1,0:N+1)[MP,*]). This allocation statement specifies (given the one element halo size provided earlier for U) that the left halo column is U(0,:), the right column is U(M+1,:), the bottom row is U(:,0) and the top row is U(:,N+1), leaving the interior region U(1:M,1:N).

In this allocation statement, the total number of process columns NP can be obtained at runtime, but may not be explicitly provided (according to Coarray Fortran (CAF) rules) because the actual number of participating processes (in Fortran called images) is variable, depending on how many processes are requested at program startup. In this discussion, it is assumed that there are no holes in the logical processor topology, thus MP * NP = P, where MP is the number of process rows and P is the total number of participating processes (images).

Once a subimage is obtained, memory on the device can be allocated,

```
if (device /= this_image()) then
   allocate(U[device], HALO_SRC=U) [[device]]
end if
```

There are four points to note regarding this memory allocation: 1. Memory is only allocated if a subimage has been obtained; 2. The location where memory is allocated is denoted by regular coarray notation U[device]; 3. The allocated size and halo attribute of the new array are obtained from the previously allocated local array U via the notation HALO_SRC=U (using HALO_SRC will also initially copy U to the subimage); and finally 4. The allocation itself is executed on the subimage device with the notation [[device]].

Fortran uses square bracket notation, e.g. [image], to specify on what process the memory reference is physically located. Square brackets are a visual clue to the programmer that the memory reference may be remote and therefore potentially suffer a performance penalty. CAFe extends this by employing double-bracket notation to indicate possibly remote subimage execution.

Execution of the Laplacian task is done using the do concurrent construct:

```
do while (.not. converged)
  do concurrent (i=1:M, j=1:N) [[device]]
     call Laplacian( U(i,j)[device] )
  end do
  call HALO_TRANSFER(U, BC=CYCLIC)
end do
```

There are several points that require highlighting: 1. Iteration occurs over the interior of the array domain, (i=1:M, j=1:N); 2. Execution of the loop body occurs on the specific subimage indicated by [[device]]; 3. Execution of the iterates may occur in any order, even *concurrently*; 4. The local element of the array (as defined above in reference to the definition of the concurrent procedure Laplacian) is given by the indices (i,j); 5. Location of memory for the task is to be taken from the subimage as noted by [device]; 6. All threads must finish

execution of the loop body before further execution of the program proceeds; and 7. Transfer of all requisite halo regions is effected by the call to the new LOPe intrinsic function HALO_TRANSFER(). This function is a synchronization event in that all images must complete the halo transfer before program execution continues.

Note that a transfer of halo memory is necessary after each completion of the do concurrent loop. This must be done in order for the halo region of a coarray on a given process to be consistent with the corresponding interior of the coarray on a logically neighboring process. Finally, memory for the entire array U can be copied from the subimage device with the statement, U = U[device], and memory deallocation (not shown) is similar to memory allocation.

3.3 Comparison to Coarray Fortran

LOPe provides a purely *local* viewpoint; the programmer is only provided read and write access to the local array element and read access to a small halo region surrounding the local element. There is simply no mechanism provided for the programmer to even know where the local element is in the context of the broader array. On a distributed memory architecture, the halo elements may not even be physically located on the same processor. If executed on a cluster containing hybrid processing elements (e.g. GPUs), the halo elements may be as far as three hops away: one to get to the host processor and another two to get to memory on the hybrid processor executing on another distributed memory node. LOPe provides a complete separation between algorithm development and memory management (synchronization between memory copies of the same logical array region covered by halos). By explicitly describing the existence and size of an array's halo region, the compiler is provided with enough information to manage most of the hard and detailed work involved in memory transfer and synchronization. Additionally, the semantics of the LOPe execution model remove the possibility of race conditions developing during execution of a concurrent procedure.

We emphasize some of these advantages by comparing the Laplacian implementation in Fig. 1 with the implementation of the same algorithm from the original Numrich and Reid paper [12] first describing coarrays in Fortran. We should point out that this comparison is somewhat unfair, because Numrich and Reid were introducing coarray notation for transferring memory on distributed memory architectures, not demonstrating how ideally one should use coarrays within a large application.

However this example serves to highlight some of the advantages of LOPe and CAFe as introduced above. Note that in the coarray example shown below, type declarations have been removed to save space:

```
subroutine Laplace (nrow,ncol,U)
  left = me-1    ! me refers to the current image
  if (me == 1) left = ncol
  right = me + 1
  if (me == ncol) right = 1
```

```
call sync all   ! Wait for left and right
new_u(1:nrow) = new_u(1:nrow) + u(1:nrow)[left] + u(1:nrow)[right]
call sync all
u(1:nrow) = new_u(1:nrow) - 4.0*u(1:nrow)
end subroutine
```

3.4 LOPe Advantages

A comparison of Fig. 1 to the CAF example suggests the following advantages:

- LOPe requires the implementation of the algorithm to be separate from the call to effect the halo transfer. Removing boundary condition specification from the algorithm allows the boundary conditions to be changed without changing algorithm code.
- LOPe applies the transfer of halo memory across possibly multiple levels of memory with the LOPe intrinsic TRANSFER_HALO function. Thus the LOPe algorithm can be run on a machine with many interconnected nodes, each containing hybrid processor cores.
- Algorithm implementation is separate from user-specified synchronization,
 e.g., call sync_all. In LOPe, synchronization is subsumed in the semantics of the CONCURRENT attribute and the TRANSFER_HALO function call.
- The algorithm implementation is separate from any specification as to where the array memory is located. The CAF example explicitly denotes where memory is located with the [left] and [right] syntax where left and right specify a processor topology.
- The algorithm implementation is separate from any specification as to where the algorithm is to be executed. The CAF example explicitly denotes where a statement is to be executed with the control flow construct if (me == 1).
- The LOPe implementation is easier to understand and frequently follows the mathematical algorithm directly. For example, the CAF implementation of Numrich and Reid adds 4 neighbors plus the center value to make the implementation with direct remote coarray access possible, while the LOPe example is able to implement the same algorithm with one statement and no intervening synchronization.
- The semantics of LOPe makes explicit management of array temporaries (e.g., u and new_u) by the programmer unnecessary. Because in LOPe the halo region is a language construct, the compiler is better able to manage temporary buffers than users on the target hardware platform.

3.5 LOPe Constraints

Constraints provided by the LOPe language extensions allow the compiler to catch several classes of errors that otherwise would be the programmer's responsibility:

• A programmer is not able to store data to the halo region during execution of a LOPe concurrent function. Neither are stores to the local element, followed by a read from the halo region of the same variable allowed. If these were allowed, one thread could overwrite another threads data at undefined times.

- A programmer can't make indexing errors in a concurrent routine by going out of bounds of the array plus halo memory.
- A programmer is not able to cause race conditions by forgetting to create and use temporary arrays properly.
- A programmer can't make synchronization errors in calls to LOPe functions as synchronization is implicit in the CONCURRENT attribute. A thread running a concurrent procedure is provided with a copy of its local array element plus halo that is consistent with the state of memory at the time of invocation of the procedure. Stores to an individual thread's local array element (by that thread) are never visible to other threads. Normal coarray programs (like MPI) require explicit synchronization to ensure that processes arrive at the same program location before a memory read occurs (for example). LOPE encourages the creation of small functions and lets the compiler fuse the functions together to improve performance and to provide necessary synchronization.

4 LOPe and CAFe Implementation

This section briefly describes how LOPe extensions to Fortran have been implemented as source-to-source transformations via rewrite rules (for expressing basic transformations) and rewriting strategies (for controlling the application of the rewrite rules). A LOPe file is transformed to Fortran and OpenCL files through generative programming techniques using Stratego/XT tools [2] and is accomplished in three phases: (1) parsing to produce a LOPe Abstract Syntax Tree (AST) represented in the Annotated Term Format (ATerm [15]); (2) transformations of LOPe AST nodes to Fortran and C AST nodes; and (3) pretty-printing to the base Fortran and OpenCL languages.

The foundation of LOPe is the syntax definition of the base language expressed in SDF (Syntax Definition Formalism) as part of the Open Fortran Project (OFP) [1]. LOPe is defined in a separate SDF module that extends the Fortran 2008 language standard with 15 context-free syntax rules. Parsing is implemented in Stratego/XT by a scannerless generalized-LR parser and the conversion of transformed AST nodes to text is accomplished with simple pretty-printing rules.

4.1 Transformations for Concurrent Procedures

A key component of code generation for LOPe is the targeting of a LOPe CONCURRENT procedure for a particular hardware architecture. The execution target can be one of several choices, including serial execution by the current process via inlining of the function, parallel execution by inlining with OpenMP compiler directives, or parallel execution by heterogeneous processing elements with a language like OpenCL.

For this work we have developed rewrite rules and strategies in Stratego/XT to rewrite Fortran AST nodes to C AST nodes (extended with necessary OpenCL keywords). The C AST ATerms have mostly a one-to-one correspondence with Fortran terms: a CONCURRENT procedure is transformed to an OpenCL kernel; Fortran formal parameters are transformed to C parameters (with a direct mapping of types); and local Fortran variable declarations are rewritten as C declarations. Similarly, Fortran executable statements are rewritten as C statements. The only minor complication is mapping the LOPe local, array index view to the global C index space. This translation is facilitated by a Fortran symbol table that stores array shape and halo size information.

4.2 Transformations at the Calling Site

Transformations of a LOPe procedure call site are more difficult, though technically straight forward. The Fortran function call must be transformed to a call to run the OpenCL kernel (generated as described above). This is facilitated by use of the ForOpenCL library which provides Fortran bindings to the OpenCL runtime [14]. However, this usage requires the declaration of extra variables, allocation of memory on the OpenCL device (subimage), transfer of memory, marshalling of kernel arguments, and synchronization.

These transformations are accomplished using several rewrite stages using Stratego/XT strategies: (1) a symbol table is produced in the first pass to store information related to arrays including, array shape, halo size, and allocation status; (2) additional variables are declared that are used to maintain the OpenCL runtime state, including the OpenCL device, the OpenCL kernel, and OpenCL variables used to marshall kernel arguments; and (3) all CAFe code related to subimage usage is desugared (lowered) to standard Fortran with calls to the ForOpenCL library as needed.

Though not yet available, similar rewrite strategies are planned for targeting programming models other than OpenCL including parallel execution with OpenMP directives. In addition, simple serial execution with function inlining (if desired) will be performed by the regular Fortran compiler once all CAFe and LOPe code has been desugared to standard Fortran.

5 Conclusions

Fortran is a general-purpose programming language and as such it provides limited facilities for expressing concepts useful for stencil operations. For example, halo regions must be expressed in terms of the existing syntax of the language and there is no way to specify that the "interior" of an array is in any way special from an "outside" region. By not providing support for stencils in the language, the programmer must make specific choices regarding data-access patterns and the order of operations on the data. These choices often hide the opportunity for optimizations by the compiler [5]. For example, if the compiler had knowledge of the semantic intent of halo regions, it could reorder operations so that border

regions were computed *before* interior regions, allowing the transfer of data in halo regions to overlap with computations on the interior.

Just as Coarray Fortran originally extended Fortran to include domain specific knowledge (parallel computation) replacing MPI library routines [12], LOPe seeks to extend Fortran by providing domain specific knowledge of stencil operations. Specifically, LOPe and CAFe together provide: (1) a local view of stencil operations on data that allows a complete separation of the implementation of a stencil algorithm with data-access patterns; (2) memory placement via allocation routines that allow the specification of allocation location; (3) task execution placement with double-bracket syntax specifying which subimage is to execute a particular operation; and (4) memory exchange via the TRANSFER_HALO intrinsic procedure.

Benefits. LOPe proposes to formalize the common, halo software pattern in language syntax, thus providing the compiler with access to halo information in order to spread computation over more hardware resources, improve performance, and to reduce complexity for the programmer. Furthermore, LOPe semantics provide important *language restrictions* that remove the possibility of race conditions that occur when multiple threads have write access to overlapping data regions.

Limitations. LOPe only supports regular structured grids through Fortran multi-dimensional arrays and a corresponding multi-dimensional processor layout. It does not allow the composability of stencils required by non-linear physics operators, nor does it provide automatic support for the storage of intermediate results resulting from multiple intermediate update steps. Adaptive Mesh Refinement (AMR) Shift Calculus provides a generalized abstraction that addresses many of these concerns (see [5] and references therein). However, it may be possible to support AMR in LOPe through locally-structured grid methods based on the work of Berger and Oliger [4]. In this instance, LOPe could be used to update the regular array regions in each rectangular patch.

By implementing LOPe we have demonstrated that LOPe can be used to easily and succinctly code the stencil algorithms that are common to many areas of science, and furthermore, that LOPe is suitable for transformation to languages like OpenCL that support heterogeneous computing. It remains to history to ascertain if LOPe is sufficiently general purpose to be included in a general-purpose programming language or if it is better suited to remain as a DSL and to be used as a special-purpose preprocessing tool.

References

- 1. Open Fortran Project. https://github.com/OpenFortranProject/ofp-sdf.
- 2. Martin Bravenboer, Karl Trygve Kalleberg, Rob Vermaas, and Eelco Visser. Stratego/XT 0.17. a language and toolset for program transformation. Science of Computer Programming, 72(1–2):52 70, 2008.

- Bradford L. Chamberlain, Sung-Eun Choi, Steven J. Deitz, and Lawrence Snyder. The High-Level Parallel Language ZPL Improves Productivity and Performance. In Proceedings of the IEEE International Workshop on Productivity and Performance in High-End Computing, 2004.
- 4. Phillip Colella, John Bell, Noel Keen, Terry Ligocki, Michael Lijewski, and Brian Van Straalen. Performance and scaling of locally-structured grid methods for partial differential equations. In *Journal of Physics: Conference Series*, volume 78, page 012013. IOP Publishing, 2007.
- 5. Anshu Dubey. Stencils in scientific computations. In *Proceedings of the Second Workshop on Optimizing Stencil Computations*, WOSC '14, pages 57–57, New York, NY, USA, 2014. ACM.
- Anshu Dubey, Steve Brandt, Richard Brower, Merle Giles, Paul Hovland, Donald Lamb, Frank Lffler, Boyana Norris, Brian O'Shea, Claudio Rebbi, Marc Snir, Rajeev Thakur, and Petros Tzeferacos. Software abstractions and methodologies for hpc simulation codes on future architectures. *Journal of Open Research Software*, 2(1), 2014.
- Anshu Dubey and Brian van Straalen. Experiences from software engineering of large scale AMR multiphysics code frameworks. CoRR, abs/1309.1781, 2013.
- 8. Manuel Hasert, Harald Klimach, and Sabine Roler. Caf versus mpi applicability of coarray fortran to a flow solver. pages 228–236. Springer-Verlag, 2011.
- Guohua Jin, John M. Mellor-Crummey, Laksono Adhianto, William N. Scherer III, and Chaoran Yang. Implementation and performance evaluation of the HPC challenge benchmarks in coarray fortran 2.0. In 25th IEEE International Symposium on Parallel and Distributed Processing, IPDPS 2011, Anchorage, Alaska, USA, 16-20 May, 2011 - Conference Proceedings, pages 1089-1100, 2011.
- Khronos OpenCL Working Group. The OpenCL Specification Version: 1.1 Document Revision: 44, 2011.
- 11. John Mellor-Crummey, Laksono Adhianto, William N. Scherer, III, and Guohua Jin. A new vision for coarray fortran. In *Proceedings of the Third Conference on Partitioned Global Address Space Programing Models*, PGAS '09, pages 5:1–5:9, New York, NY, USA, 2009. ACM.
- 12. Robert W. Numrich and John Reid. Co-array fortran for parallel programming. SIGPLAN Fortran Forum, 17(2):1–31, 1998.
- 13. Robert Preissl, Nathan Wichmann, Bill Long, John Shalf, Stephane Ethier, and Alice Koniges. Multithreaded global address space communication techniques for gyrokinetic fusion applications on ultra-scale platforms. 2011 International Conference for High Performance Computing, Networking, Storage and Analysis, pages 1–11, 2011.
- Matthew J. Sottile, Craig E Rasmussen, Wayne N. Weseloh, Robert W. Robey, Daniel Quinlan, and Jeffrey Overbey. Foropencl: Transformations exploiting array syntax in fortran for accelerator programming. *Int. J. Comput. Sci. Eng.*, 8(1):47– 57, February 2013.
- 15. Mark van den Brand, H. A. de Jong, Paul Klint, and Pieter A. Olivier. Efficient annotated terms. *Softw.*, *Pract. Exper.*, 30(3):259–291, 2000.

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