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1 %% Machine Learning
2 % Lab 11: K-Means Algorithm
3 % — K-Means and Image Compression —
4 %{
5 In this exercise, you will implement the K-means clustering algorithm and
6 apply it to compress an image.
7 %}
8
9 %% Initialization
10 clear ; close all; clc
11
12 %% ===== Part 1: Find Closest Centroids =====
13 % To help you implement K-Means, we have divided the learning algorithm
14 % into two functions — findClosestCentroids and computeCentroids. In this
15 % part, you should complete the code in the findClosestCentroids function.
16 %
17 fprintf('Finding closest centroids.\n\n');
18
19 % Load an example dataset that we will be using
20 load('ex7data2.mat');
21
22 % Select an initial set of centroids
23 K = 3; % 3 Centroids
24 initial_centroids = [3 3; 6 2; 8 5];
25
26 % Find the closest centroids for the examples using the
27 % initial_centroids
28 idx = findClosestCentroids(X, initial_centroids);
29
30 fprintf('Closest centroids for the first 3 examples: \n')
31 fprintf(' %d', idx(1:3));
32 fprintf('\n(the closest centroids should be 1, 3, 2 respectively)\n');
33
34 fprintf('Program paused. Press enter to continue.\n');
35 pause;
36
37 %% ===== Part 2: Compute Means =====
38 % After implementing the closest centroids function, you should now
39 % complete the computeCentroids function.
40 %
41 fprintf('\nComputing centroids means.\n\n');
42
43 % Compute means based on the closest centroids found in the previous part.
44 centroids = computeCentroids(X, idx, K);
45
46 fprintf('Centroids computed after initial finding of closest centroids: \n')
47 fprintf(' %f %f \n' , centroids);
48 fprintf('\n(the centroids should be\n');
49 fprintf(' [ 2.428301 3.157924 ]\n');
50 fprintf(' [ 5.813503 2.633656 ]\n');
51 fprintf(' [ 7.119387 3.616684 ]\n\n');
52
53 fprintf('Program paused. Press enter to continue.\n');
54 pause;
55
56

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57 %% ===== Part 3: K-Means Clustering =====
58 % After you have completed the two functions computeCentroids and
59 % findClosestCentroids, you have all the necessary pieces to run the
60 % kMeans algorithm. In this part, you will run the K-Means algorithm on
61 % the example dataset we have provided.
62 %
63 fprintf('\nRunning K-Means clustering on example dataset.\n\n');
64
65 % Load an example dataset
66 load('ex7data2.mat');
67
68 % Settings for running K-Means
69 K = 3;
70 max_iters = 10;
71
72 % For consistency, here we set centroids to specific values
73 % but in practice you want to generate them automatically, such as by
74 % settings them to be random examples (as can be seen in
75 % kMeansInitCentroids).
76 initial_centroids = [3 3; 6 2; 8 5];
77
78 % Run K-Means algorithm. The 'true' at the end tells our function to plot
79 % the progress of K-Means
80 [centroids, idx] = runkMeans(X, initial_centroids, max_iters, true);
81 fprintf('\nK-Means Done.\n\n');
82
83 fprintf('Program paused. Press enter to continue.\n');
84 pause;
85
86 %% ===== Part 4: K-Means Clustering on Pixels =====
87 % In this exercise, you will use K-Means to compress an image. To do this,
88 % you will first run K-Means on the colors of the pixels in the image and
89 % then you will map each pixel onto its closest centroid.
90 %
91 % You should now complete the code in kMeansInitCentroids.m
92 %
93
94 fprintf('\nRunning K-Means clustering on pixels from an image.\n\n');
95
96 % Load an image of a bird
97 A = double(imread('bird_small.png'));
98
99 % If imread does not work for you, you can try instead
100 % load ('bird_small.mat');
101
102 A = A / 255; % Divide by 255 so that all values are in the range 0 - 1
103
104 % Size of the image
105 img_size = size(A);
106
107 % Reshape the image into an Nx3 matrix where N = number of pixels.
108 % Each row will contain the Red, Green and Blue pixel values
109 % This gives us our dataset matrix X that we will use K-Means on.
110 X = reshape(A, img_size(1) * img_size(2), 3);
111
112 % Run your K-Means algorithm on this data
113 % You should try different values of K and max_iters here

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114 K = 16;
115 max_iters = 10;
116
117 % When using K-Means, it is important the initialize the centroids
118 % randomly.
119 % You should complete the code in kMeansInitCentroids.m before proceeding
120 initial_centroids = kMeansInitCentroids(X, K);
121
122 % Run K-Means
123 [centroids, idx] = runkMeans(X, initial_centroids, max_iters);
124
125 fprintf('Program paused. Press enter to continue.\n');
126 pause;
127
128
129 %% ===== Part 5: Image Compression =====
130 % In this part of the exercise, you will use the clusters of K-Means to
131 % compress an image. To do this, we first find the closest clusters for
132 % each example. After that, we
133
134 fprintf('\nApplying K-Means to compress an image.\n\n');
135
136 % Find closest cluster members
137 idx = findClosestCentroids(X, centroids);
138
139 % Essentially, now we have represented the image X as in terms of the
140 % indices in idx.
141
142 % We can now recover the image from the indices (idx) by mapping each pixel
143 % (specified by its index in idx) to the centroid value
144 X_recovered = centroids(idx,:);
145
146 % Reshape the recovered image into proper dimensions
147 X_recovered = reshape(X_recovered, img_size(1), img_size(2), 3);
148
149 % Display the original image
150 subplot(1, 2, 1);
151 imagesc(A);
152 title('Original');
153
154 % Display compressed image side by side
155 subplot(1, 2, 2);
156 imagesc(X_recovered)
157 title(sprintf('Compressed, with %d colors.', K));
158
159
160 fprintf('Program paused. Press enter to continue.\n');
161 pause;

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findClosestCentroids.m

```

1 function idx = findClosestCentroids(X, centroids)
2 %FINDCLOSESTCENTROIDS computes the centroid memberships for every example
3 %   idx = FINDCLOSESTCENTROIDS (X, centroids) returns the closest centroids
4 %   in idx for a dataset X where each row is a single example. idx = m x 1
5 %   vector of centroid assignments (i.e. each entry in range [1..K])
6
7 % Set K
8 K = size(centroids, 1);
9
10 % You need to return the following variables correctly.
11 idx = zeros(size(X,1), 1);
12
13 for i = 1:size(X,1)
14     distance = Inf;
15     for k = 1:K
16         temp2 = X(i,:)-centroids(k,:);
17         if (temp2*temp2') < distance
18             distance = (temp2*temp2');
19             temp1 = k;
20         end
21     end
22     idx(i) = temp1;
23 end
24
25 end

```

computeCentroids.m

```

1 function centroids = computeCentroids(X, idx, K)
2 %COMPUTECENTROIDS returns the new centroids by computing the means of the
3 %data points assigned to each centroid.
4
5 % Useful variables
6 [m n] = size(X);
7
8 % You need to return the following variables correctly.
9 centroids = zeros(K, n);
10
11 for k = 1:K
12     centroid = zeros(1, n);
13     Ck = 0;
14     for i = 1:m
15         if idx(i) == k
16             centroid = centroid + X(i, :);
17             Ck = Ck + 1;
18         end
19     end
20     centroids(k,:) = centroid.*(1/Ck);
21 end
22
23 end

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kMeansInitCentroids.m

```
1 function centroids = kMeansInitCentroids(X, K)
2 %KMEANSINITCENTROIDS This function initializes K centroids that are to be
3 %used in K-Means on the dataset X
4
5 % You should return this values correctly
6 centroids = zeros(K, size(X, 2));
7
8 % Initialize the centroids to be random examples
9 % Randomly reorder the indices of examples
10 randidx = randperm(size(X, 1));
11 % Take the first K examples as centroids
12 centroids = X(randidx(1:K), :);
13
14 end
```