```
multiplier_32b is a 32-bit multiplier leveraging both optimization structures: bit-pair
       recoding and carry-save addition.
 3
           It accepts M and Q as the multiplication and multiplier, respectively.
 4
5
6
7
8
      module multiplier_32b (
           input [31:0] M, Q,
 9
           output [63:0] result
10
11
           // All relevant variations of M for booth augend selection.
12
13
           wire [32:0] Q_shifted = {Q, 1'b0}; // Left shifted Q by 1 such that the i-1 Booth check
       is valid_with_i = 0.
           wire [31:0] negM = -M;
wire [32:0] Mx2 = {M, 1'b0};
wire [32:0] negMx2 = {negM, 1'b0};
15
16
17
18
19
           // Augends.
           reg [63:0] partial_products [15:0];
20
21
22
           integer i;
           // Perform Booth Augend Selection
23
           always @(*) begin
for (i = 0; i < 31; i = i+2) begin
24
25
                   // Choose variant of M based on partial_products
26
27
                   case ({Q_shifted[i+2], Q_shifted[i+1], Q_shifted[i]})
                       // All values are properly sign-extended.
3'b000: partial_products[i>>1] = 64'b0; // 0 x M
3'b001: partial_products[i>>1] = {{32{M[31]}}}, M}; // +1 x M
3'b010: partial_products[i>>1] = {{32{M[31]}}}, M}; // +1 x M
3'b011: partial_products[i>>1] = {{31{Mx2[32]}}}, Mx2}; // +2 x M
3'b100: partial_products[i>>1] = {{31{negMx2[32]}}}, negMx2}; // -2 x M
3'b101: partial_products[i>>1] = {{32{negM[31]}}}, negM}; // -1 x M
3'b110: partial_products[i>>1] = {{32{negM[31]}}}, negM}; // -1 x M
3'b111: partial_products[i>>1] = 64'b0: // 0 x M
28
29
30
31
32
33
34
35
36
37
                        3'b111: partial_products[i>>1] = 64'b0; \frac{1}{1} 0 x M
                       default: partial_products[i>>1] = 64'b0;
38
                   endcase
39
                   // Apply appropriate shift before addition.
40
                   partial_products[i>>1] = partial_products[i>>1] << i;</pre>
41
42
           end
43
44
           // Final operands after reduction process
45
           wire [63:0] reduced1, reduced2;
46
47
           // 16-to-2 CSA reducer.
48
           CSA_tree_16to2 reduction (.augends(partial_products), .reduced1(reduced1), .reduced2(
       reduced2));
49
50
           // Final carry-propagate stage, with no carry-in, nor carry-out (result for 32-bit mult.
       is 64-bits)
51
           adder_64b carry_propagate (.cin(\frac{1'b0}{b}), .x(reduced1), .y(reduced2), .s(result)); // No
       cout.
52
53
       endmodule
54
55
56
57
       `timescale 1ns / 1ps
58
59
       module multiplier_32b_tb;
            reg [31:0] M, Q;
            wire [63:0] result;
60
61
62
            // Instantiate the multiplier
63
            multiplier_32b dut (M, Q, Result);
64
65
            // Test procedure
initial begin
66
67
                  // Test cases
                  M = 32'd0; Q = 32'd0; #10; // 0 * 0
68
                  $display("M=%d, Q=%d, result=%d", M, Q, result);
69
70
```

```
71
72
73
74
75
77
77
77
78
81
82
83
84
88
89
99
99
99
                                                                                                         M = -32'd15; Q = 32'd10; #10; // -15 * 10 $display("M=%d, Q=%d, result=%d", M, Q, result);
                                                                                                         M = \frac{32'd15}{Q}; Q = -\frac{32'd10}{Q}; \#10; \#10; \#10; \#10; \#10; \#10; \#10; \#10; \#10; \#10; \#10; \#10; \#10; \#10; \#10; \#10; \#10; \#10; \#10; \#10; \#10; \#10; \#10; \#10; \#10; \#10; \#10; \#10; \#10; \#10; \#10; \#10; \#10; \#10; \#10; \#10; \#10; \#10; \#10; \#10; \#10; \#10; \#10; \#10; \#10; \#10; \#10; \#10; \#10; \#10; \#10; \#10; \#10; \#10; \#10; \#10; \#10; \#10; \#10; \#10; \#10; \#10; \#10; \#10; \#10; \#10; \#10; \#10; \#10; \#10; \#10; \#10; \#10; \#10; \#10; \#10; \#10; \#10; \#10; \#10; \#10; \#10; \#10; \#10; \#10; \#10; \#10; \#10; \#10; \#10; \#10; \#10; \#10; \#10; \#10; \#10; \#10; \#10; \#10; \#10; \#10; \#10; \#10; \#10; \#10; \#10; \#10; \#10; \#10; \#10; \#10; \#10; \#10; \#10; \#10; \#10; \#10; \#10; \#10; \#10; \#10; \#10; \#10; \#10; \#10; \#10; \#10; \#10; \#10; \#10; \#10; \#10; \#10; \#10; \#10; \#10; \#10; \#10; \#10; \#10; \#10; \#10; \#10; \#10; \#10; \#10; \#10; \#10; \#10; \#10; \#10; \#10; \#10; \#10; \#10; \#10; \#10; \#10; \#10; \#10; \#10; \#10; \#10; \#10; \#10; \#10; \#10; \#10; \#10; \#10; \#10; \#10; \#10; \#10; \#10; \#10; \#10; \#10; \#10; \#10; \#10; \#10; \#10; \#10; \#10; \#10; \#10; \#10; \#10; \#10; \#10; \#10; \#10; \#10; \#10; \#10; \#10; \#10; \#10; \#10; \#10; \#10; \#10; \#10; \#10; \#10; \#10; \#10; \#10; \#10; \#10; \#10; \#10; \#10; \#10; \#10; \#10; \#10; \#10; \#10; \#10; \#10; \#10; \#10; \#10; \#10; \#10; \#10; \#10; \#10; \#10; \#10; \#10; \#10; \#10; \#10; \#10; \#10; \#10; \#10; \#10; \#10; \#10; \#10; \#10; \#10; \#10; \#10; \#10; \#10; \#10; \#10; \#10; \#10; \#10; \#10; \#10; \#10; \#10; \#10; \#10; \#10; \#10; \#10; \#10; \#10; \#10; \#10; \#10; \#10; \#10; \#10; \#10; \#10; \#10; \#10; \#10; \#10; \#10; \#10; \#10; \#10; \#10; \#10; \#10; \#10; \#
                                                                                                         M = -32'd15; Q = -32'd10; \#10; \#10; \#10; \#10; \#10; \#10; \#10; \#10; \#10; \#10; \#10; \#10; \#10; \#10; \#10; \#10; \#10; \#10; \#10; \#10; \#10; \#10; \#10; \#10; \#10; \#10; \#10; \#10; \#10; \#10; \#10; \#10; \#10; \#10; \#10; \#10; \#10; \#10; \#10; \#10; \#10; \#10; \#10; \#10; \#10; \#10; \#10; \#10; \#10; \#10; \#10; \#10; \#10; \#10; \#10; \#10; \#10; \#10; \#10; \#10; \#10; \#10; \#10; \#10; \#10; \#10; \#10; \#10; \#10; \#10; \#10; \#10; \#10; \#10; \#10; \#10; \#10; \#10; \#10; \#10; \#10; \#10; \#10; \#10; \#10; \#10; \#10; \#10; \#10; \#10; \#10; \#10; \#10; \#10; \#10; \#10; \#10; \#10; \#10; \#10; \#10; \#10; \#10; \#10; \#10; \#10; \#10; \#10; \#10; \#10; \#10; \#10; \#10; \#10; \#10; \#10; \#10; \#10; \#10; \#10; \#10; \#10; \#10; \#10; \#10; \#10; \#10; \#10; \#10; \#10; \#10; \#10; \#10; \#10; \#10; \#10; \#10; \#10; \#10; \#10; \#10; \#10; \#10; \#10; \#10; \#10; \#10; \#10; \#10; \#10; \#10; \#10; \#10; \#10; \#10; \#10; \#10; \#10; \#10; \#10; \#10; \#10; \#10; \#10; \#10; \#10; \#10; \#10; \#10; \#10; \#10; \#10; \#10; \#10; \#10; \#10; \#10; \#10; \#10; \#10; \#10; \#10; \#10; \#10; \#10; \#10; \#10; \#10; \#10; \#10; \#10; \#10; \#10; \#10; \#10; \#10; \#10; \#10; \#10; \#10; \#10; \#10; \#10; \#10; \#10; \#10; \#10; \#10; \#10; \#10; \#10; \#10; \#10; \#10; \#10; \#10; \#10; \#10; \#10; \#10; \#10; \#10; \#10; \#10; \#10; \#10; \#10; \#10; \#10; \#10; \#10; \#10; \#10; \#10; \#10; \#10; \#10; \#10; \#10; \#10; \#10; \#10; \#10; \#10; \#10; \#10; \#10; \#10; \#10; \#10; \#10; \#10; \#10; \#10; \#10; \#10; \#10; \#10; \#10; \#10; \#10; \#10; \#10; \#10; \#10; \#10; \#10; \#10; \#10; \#10; \#10; \#10; \#10; \#10; \#10; \#10; \#10; \#10; \#10; \#10; \#10; \#10; \#10; \#10; \#10; \#10; \#10; \#10;
                                                                                                          M = 32'h7FFFFFFF; Q = 32'h00000001; #10; // Largest positive * 1
                                                                                                           $display("M=%d, Q=%d, result=%d", M, Q, result);
                                                                                                         M = 32'h80000000; Q = 32'd1; #10; // Smallest negative * 1 $display("M=%d, Q=%d, result=%d", M, Q, result);
                                                                                                          M = 32'hffffffff; Q = 32'hfffffffff; \#10; // -1 * -1
                                                                                                           $display("M=%d, Q=%d, result=%d", M, Q, result);
                                                                                                           $stop;
93
94
                                                                         end
                                         endmodule
  95
  96
```