

# Modern Architectures & Optimization

Luca Tornatore - I.N.A.F.



**“Foundation of HPC” course**



DATA SCIENCE &  
SCIENTIFIC COMPUTING  
2020-2021 @ Università di Trieste

Optimization



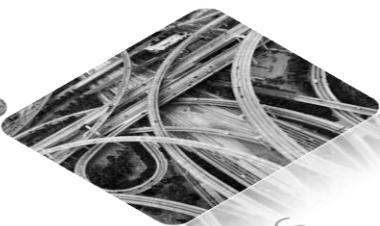
# Outline



First  
things  
first



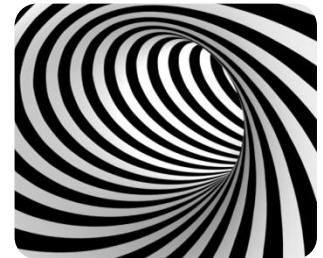
Cache &  
Memory



Branches



Pipelines



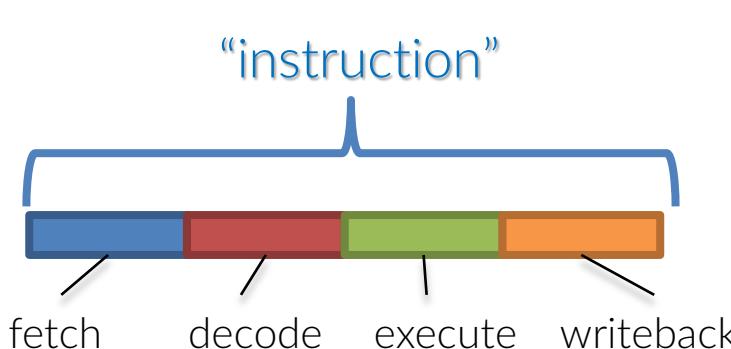
Loops



# Atomic instructions

It would be obvious to think that an “instruction” is a kind of *atomic* operation that the CPU perform as a whole. Indeed that was true until the mid of the 80s.

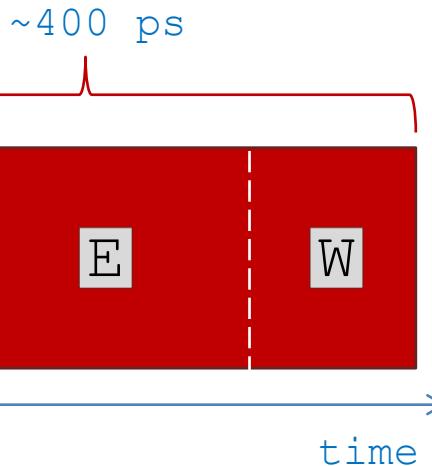
If you think carefully about it, it is easy to understand that actually an “instruction” involves at least the following *independent* steps:



1. ***Fetching***  
it must be recalled from memory/Icache
2. ***Decoding:***  
it must be “understood and interpreted”
3. ***Execution***
4. ***Writeback :***  
the result must be accounted in memory ()



# Atomic instructions ?



If all the four stages take ~400ps, we then would obtain a **throughput** of 2.5GIPS (giga-instructions per second).

400ps is also the total time required to get a result from an instruction, and so it is the **latency** of the instruction.

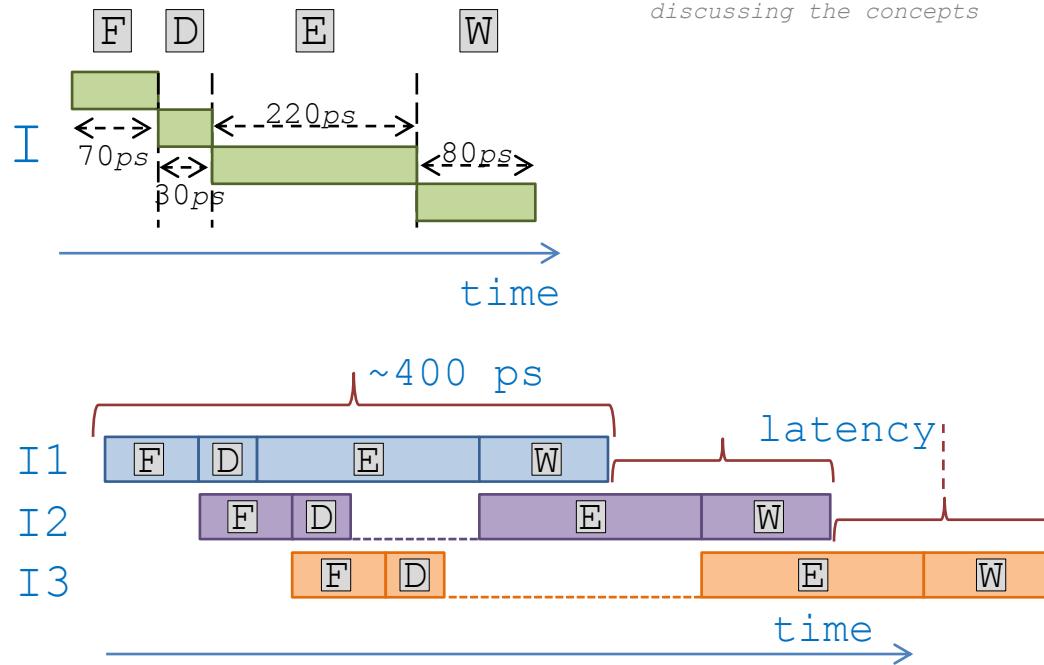
However, if we were able to “detach” the four stages, we could organize things differently, like in a car-building chain, or even at the mensa of the university.



Pipelines

# Pipelines

Note: all the timing estimates are hypothetical for the purpose of discussing the concepts



If many independent logical units exist to perform each step, they could operate subsequently on different instructions:

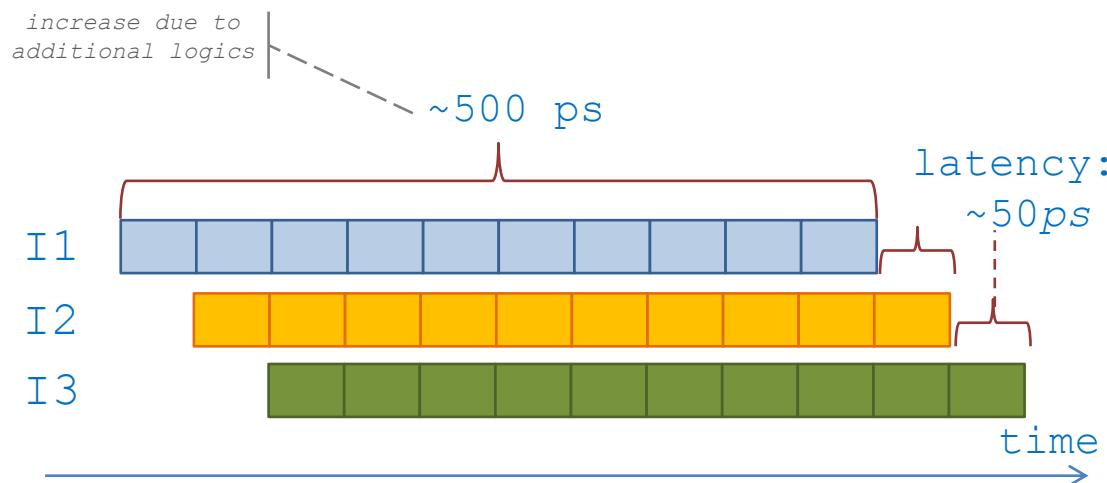
If the stage delays are not uniform, the throughput is limited by the latency  $F + (D+E) - (F+D) = E \sim 220\text{ps}$ , which means we have a throughput of **~4.5GIPS** just because of logic units separation.



# Pipelines

Therefore, introducing the instructions pipelining, we can increase the **throughput** of our system by a large factor.

However, the efficiency of the pipelines is limited by its longest stage: the better option would be to have all equal stages, for instance further subdividing each stage – especially the most demanding ones (\*).



Now the throughput of our system has increased to 1 instruction retired every 50ps, i.e. **20GIPS**

(\*) this is called *superpipelining*: modern CPUs may have 10-20 stages per pipeline.



| Pipelines are about throughput

Pipelining is then about increasing the throughput of a system, and as we have seen it could be really effective.

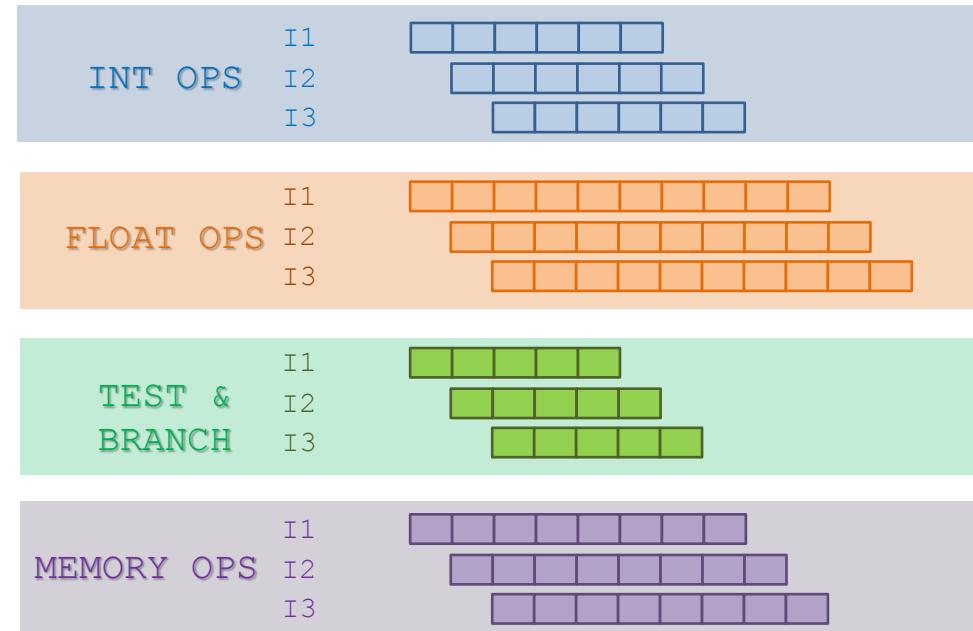
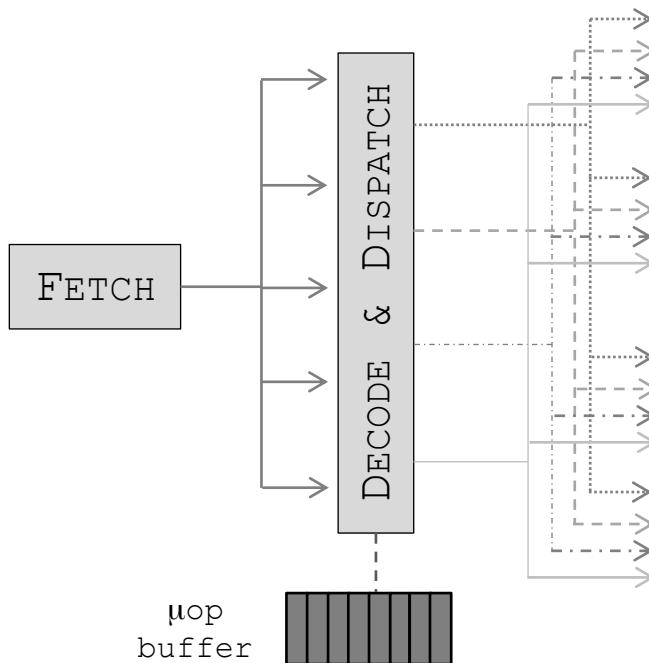
However, there is more that can be done working on the **execution stage** that, of course, encompasses a large number of different *functional units*, performing a **different and independent tasks**.

With an enhancement of the decode/dispatch stage, we can address multiple pipelines that can be active at the same time:



Pipelines

# Multiple pipelines





# Pipelines latency

The number of cycles between when an instruction's execution stage begins and when its result is available for other instructions usage, is the *latency* of the instruction and it grows with the pipeline deepness (the number of stages).

Typical latencies in modern processors (read the manual of yours) range from 1cyc for integer ops, to 3-6cyc for add and mul flop to  $\geq 10\text{-}20$  for div flop,  $\sim 50$  for trigonometric or exponential functions.

Latency for memory loads can be severely troublesome, because they are highly unpredictable and they block all other operations making it difficult to fill the delay with some other ops.



# Pipelines hazards

Pipelining a system with *feedbacks* (i.e.: in which a result from an instruction can be the input of a following instruction, or can change the workflow) can expose the system to *hazards* when there are dependencies between successive instructions.

There are two forms of dependency:

1. *data dependency*: the result computed by the  $i$ th instruction are used by one or more following instructions;
2. *control dependency*: the result of an instruction determines the value of the pc, i.e. the location of the next instruction to be executed.

When a dependency can lead to a wrong result, it is called an *hazard*.



# Pipelines hazards

If a control hazard arises, the entire pipeline content has to be flushed away, and a new instruction has to start from the beginning, then wasting a lot of CPU cycles.

This is one of the main cause of performance loss in modern superscalar-superpipeline-out-of-order CPUs. The logics for the runtime branch predictor occupies a large space on processor chips but it definitely is worth it.



# Pipelines hazards

A very long pipeline, then, is not much more effective than a shorter one due to the real intrinsic nature of the codes that run on the CPUs.

The hazards we have just described are actually very common (very rarely a program is a stream of totally independent instructions with no jumps) and so the full exploitation of superscalarity + superpipelining is never reached.

Basically, that's the reason why we do not have 100-stage deep pipelines.

And the reason why branching is a performance-killer, too.



As we have seen, modern processor may be able to “perform more than one operations at a time”, through super-pipelining operations.

As for what concerns the programmer’s perspective, codes must be written so to make the pipelines saturation as effective as possible.

```
for (int i = 0; i < N; i++)  
    S += a[i] * b[i];
```

This way  $S$  is both read and written (the  $S$  as input in iteration  $i$  depends on  $S$  as output of iteration  $i-1$ ) and the FP pipeline is difficult to be exploited (iteration  $i$  must unavoidably wait for iteration  $i-1$  to end, which takes ~3-6 cycles at least)



Make things easier for the compiler and the CPU

```
for (i = 0; i < N; i += 2) {  
    sum0 += a[i] * b[i];  
    sum1 += a[i+1] * b[i+1]; }
```

Unrolling make it easier for the CPU to saturate the pipelines.

v. A

---

```
for (i = 0; i < N; i += 2) {  
    double tmp0 = a[i] * b[i];  
    double tmp1 = a[i+1] * b[i+1];  
    sum0 += tmp0;  
    sum1 += tmp1; }
```

Separate load and multiply from addition

v. B



Make things easier for the compiler and the CPU

```
for (i = 0; i < N; i += 4) {  
    sum0 += a[i] * b[i];  
    sum1 += a[i+1] * b[i+1];  
    sum2 += a[i+2] * b[i+2];  
    sum3 += a[i+3] * b[i+3]; }
```

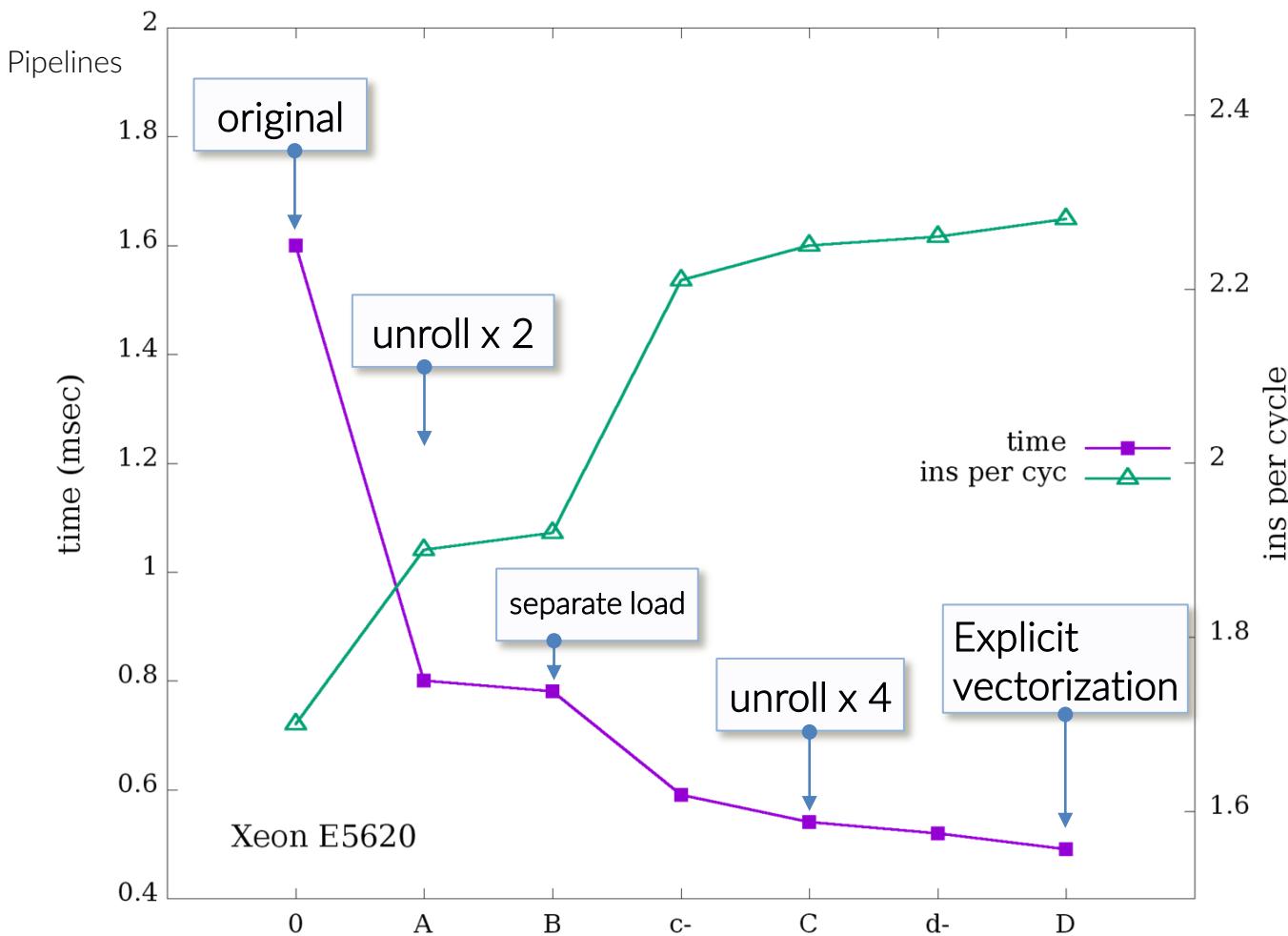
More unrolling may work even better

v. C

```
typedef double v4df __attribute__ ((vector_size (4*sizeof(double))));  
v4df array1, array2;  
v4df sum;  
for (i = 0; i < N/4; i++)  
    sum += array1[i] * array2[i];
```

Explicit vectorization

v. D





Let us now look in more detail to what happens at assembler level, so to understand in deeper details why some implementations are more effective than others.

We will use `-O0`, for the usual reason: with such simple kernels, compilers are very good (not all equally good..) in optimizing the code, and differences among improved version are more vagues.

*...that does NOT relieve you of knowing how to write not-that-bad code..*



v0

```
for (int i = 0; i < N; i++)
    S += a[i] * b[i];
```



# Comparison btw 2 compilers

v0

```
.LB3365:  
##      for ( int i = 0; i < N; i++ )  
    cmpl    %ebx, %r14d  
    jge     .LB3366  
## lineno: 185  
.LN20:  
  
    movslq  %r14d, %rax  
    movq    -72(%rbp), %rcx  
    vmovsd  (%rcx,%rax,8), %xmm0  
  
    vmovsd  -32(%rbp), %xmm1  
  
    vfmadd132sd    (%r12,%rax,8), %xmm1, %xmm0  
  
    vmovsd  %xmm0, -32(%rbp)  
  
    addl    $1, %r14d  
    jmp     .LB3365
```

```
.L8:  
# v0.c:185:    sum += array1[i] * array2[i];  
    mov    eax, DWORD PTR -136[rbp]          # tmp158, i  
    cdqe  
    lea    rdx, 0[0+rax*8]  
    mov    rax, QWORD PTR -96[rbp] # tmp159, array1  
    add    rax, rdx  
    vmovsd xmm1, QWORD PTR [rax]  
    mov    eax, DWORD PTR -136[rbp]  
    cdqe  
    lea    rdx, 0[0+rax*8] # _23,  
    mov    rax, QWORD PTR -88[rbp] # tmp161, array2  
    add    rax, rdx  
    vmovsd xmm0, QWORD PTR [rax]  
    vmulsd xmm0, xmm1, xmm0  
    vmovsd xmm1, QWORD PTR -104[rbp]        # tmp163, sum  
    vaddsd xmm0, xmm1, xmm0  
    vmovsd QWORD PTR -104[rbp], xmm0        # sum, tmp162  
    inc    DWORD PTR -136[rbp]          # i  
# v0.c:184:    for ( int i = 0; i < N; i++ )  
    mov    eax, DWORD PTR -136[rbp]          # tmp164, i  
    cmp    eax, DWORD PTR -148[rbp]          # tmp164, N  
    jl     .L8
```



# Comparison btw 2 compilers

```
.LB3365:  
##    for ( int i = 0; i < N; i++ )  
    cmpl    %rbx,%r14d  
    jge     .LB3366  
##  lineno: 185  
..LN20:  
  
    movsq  %r14d,%rax  
    movq   -72(%rbp),%rcx  
    vmovsd (%rcx,%rax,8),%xmm0  
    vfmaddsd (%r12,%rax,8),%xmm1,%xmm0  
    vmovsd %xmm0,-32(%rbp)  
  
    addl    $1,%r14d  
    jnp     .LB3365
```

```
luca@GGG:~/code/HPC_lectures/pipeline/2018% pgi/v0_papi_00 50000000  
generating 100000000 numbers..done  
sum is 1.24993e+07  
time is :0.176009 (min 0.175734, std dev 0.00054682, all 1.76643)  
transfer rate was 4.23 GB/sec ( 28.34% of theoretical max that is 15 GB/sec)
```



```
.LB:  
# v0.c:185:    sum += array1[i] * array2[i];  
    mov    eax,DWORD PTR -136(%rbp)    # tmp158, i  
    cdqe  
    lea    rdx,[0@+rax*8]  
    mov    rax,QWORD PTR -96(%rbp) # tmp159, array1  
    add    rax,rdx  
    vmovsd xmm1,QWORD PTR [rax]  
    mov    eax,DWORD PTR -136(%rbp)  
    cdqe  
    lea    rdx,[0@+rax*8] # _23,  
    mov    rax,QWORD PTR -88(%rbp) # tmp161, array2  
    add    rax,rdx  
    vmovsd xmm0,QWORD PTR [rax]  
    vmvnsd xmm0,xmm1,xmm0  
    vmvnsd xmm1,QWORD PTR -104(%rbp) # tmp163,sum  
    vaddsd xmm0,xmm1,xmm0  
    vmvnsd QWORD PTR -104(%rbp),xmm0# sum,tmp162  
    lnc    DWORD PTR -136(%rbp),# i  
    mov    eax,DWORD PTR -136(%rbp) # tmp164,i  
    cmp    eax,DWORD PTR -148(%rbp) # tmp164,N  
    jl     .LB
```

```
luca@GGG:~/code/HPC_lectures/pipeline/2018% ./v0_papi_00 50000000  
generating 100000000 numbers..done  
sum is 1.24993e+07  
time is :0.190236 (min 0.189567, std dev 0.000538453, all 1.90762)  
transfer rate was 3.92 GB/sec ( 26.22% of theoretical max that is 15 GB/sec)
```



Note: no optimization has been used in both cases



# *Comments on the previous slides*

The PGI compiler has opted for using specialised fused multiply-addition instruction (`fmaadd`) that allows for a more compact code, but an IPC of 1 (which basically means that the code occupies 1 pipeline at a time).

The gcc compiler, instead, opts for a redundant code (the 2 subsequent blocks `mov | cdqe | lea | mov | add | vmosd`) that can involve 2 pipelines, and separate multiplication and addition.

Both compilers could be induced to generate different and more efficient code playing with their options (the default behaviour can differ among different compilers).

The result is more or less equivalent from the point of view of the run-time due to the fact that the code generated by gcc is larger (more instructions) but it is dispatched to more pipelines (larger IPC).

NOTE: the IPC is a good metric, but it must be understood in a larger context. I.e. a larger IPC is good, but how good is the code depends on what instructions are being executed.



# Turning on the optimization

Let's have a preview of how the generated code changes..

```
.L8:  
# v0.c:185:    sum += array1[i] * array2[i];  
    mov    eax, DWORD PTR -136[rbp]      # tmp158, i  
    cdqe  
    lea    rdx, 0[0+rax*8]  
    mov    rax, QWORD PTR -96[rbp] # tmp159, array1  
    add    rax, rdx  
    vmovsd xmm1, QWORD PTR [rax]  
    mov    eax, DWORD PTR -136[rbp]  
    cdqe  
    lea    rdx, 0[0+rax*8] # _23,  
    mov    rax, QWORD PTR -88[rbp] # tmp161, array2  
    add    rax, rdx  
    vmovsd xmm0, QWORD PTR [rax]  
    vmulsd xmm0, xmm1, xmm0  
    vmovsd xmm1, QWORD PTR -104[rbp]      # tmp163,  
    vaddsd xmm0, xmm1, xmm0  
    vmovsd QWORD PTR -104[rbp], xmm0      # sum, tmp  
    inc    DWORD PTR -136[rbp]      # i  
# v0.c:184:        for ( int i = 0; i < N; i++ )  
    mov    eax, DWORD PTR -136[rbp]      # tmp164,  
    cmp    eax, DWORD PTR -148[rbp]      # tmp164,  
    jl     .L8
```

```
-00          for (int i = 0; i < N; i++)  
                      S += a[i] * b[i];  
  
-O3 -march=native  
  
.L8:  
# v0.c:55:    sum += array1[i] * array2[i];  
    vmovupd ymm5, YMMWORD PTR 0[r13+rax]  
    vmulpd  ymm0, ymm5, YMMWORD PTR [r15+rax]  
    add    rax, 32 # ivtmp.18,  
    vaddsd  xmm4, xmm0, xmm4  
    vunpckhpd   xmm1, xmm0, xmm0  
    vextractf128  xmm0, ymm0, 0x1  
    vaddsd  xmm1, xmm1, xmm4  
# v0.c:55:    sum += array1[i] * array2[i];  
    vaddsd  xmm1, xmm0, xmm1  
    vunpckhpd   xmm0, xmm0, xmm0  
    vaddsd  xmm4, xmm1, xmm0  
    cmp    rax, r12  
    jne    .L8    #,
```



# Turning on the optimization

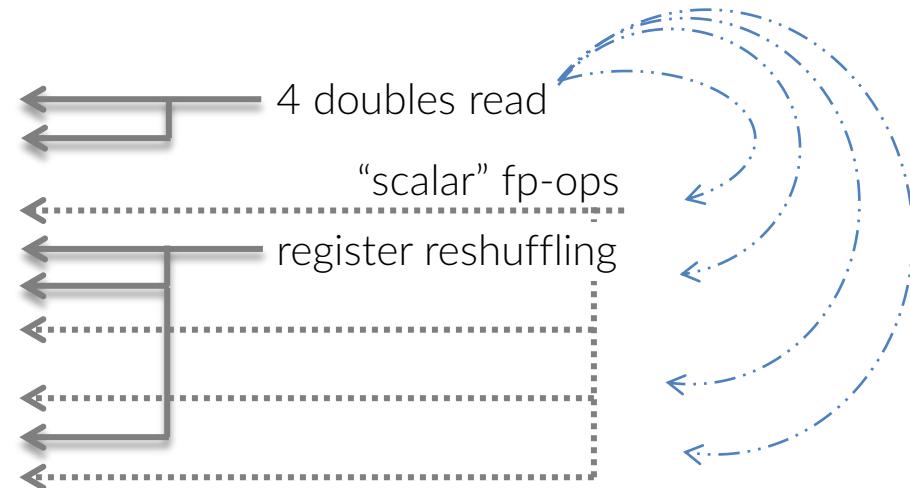
.L8:

```
# v0.c:55:      sum += array1[i] * array2[i];
    vmovupd ymm5, YMMWORD PTR 0[r13+rax]
    vmulpd  ymm0, ymm5, YMMWORD PTR [r15+rax]
    add     rax, 32 # ivtmp.18,
    vaddsd  xmm4, xmm0, xmm4
    vunpckhpd   xmm1, xmm0, xmm0
    vextractf128  xmm0, ymm0, 0x1
    vaddsd  xmm1, xmm1, xmm4
# v0.c:55:      sum += array1[i] * array2[i];
    vaddsd  xmm1, xmm0, xmm1
    vunpckhpd   xmm0, xmm0, xmm0
    vaddsd  xmm4, xmm1, xmm0
    cmp     rax, r12
    jne     .L8      #,
```

v0

```
for (int i = 0; i < N; i++)
    s += a[i] * b[i];
```

gcc 8.2 on SkyLake  
-O3 -march=native



HINT FOR IMPROVEMENT :

data are fetched with vector instructions,  
then processed in a mixed way

# Comments on the previous slides

Looking at the assembler generated by the compiler may be useful to understand where to direct optimization efforts.

In the previous slide, the compiler (with `-O3 -march=native`) chooses to fetch data from memory with a vector instruction, loading 4 doubles at a time (note that it uses the instruction for *unaligned memory*<sup>(\*)</sup>: `vmovupd`).

But however can not really exploit the ILP (Instruction-Level parallelism) due to the data dependency intrinsic in how we wrote the loop.

That's why the best first step is to exhibit the possible parallelism, for instance either by unrolling or by a different accumulation (`v1` and `v3` in the following slides).

(\*)you should remember what alignment is from the lecture about memory allocation



## V\* profile – 00

time is : 0.217358 (min 0.216092, std dev 0.000667496)			v0
transfer rate was 3.43 GB/sec ( 22.95% of theoretical max that is 15 GB/sec)			
503,469,659 cycles..	# 0.37 insn per cycle	( +- 12.99% )	
185,027,735 instructions..		( +- 17.44% )	
time is : 0.139794 (min 0.139124, std dev 0.000733397)			v1
transfer rate was 5.33 GB/sec ( 35.68% of theoretical max that is 15 GB/sec)			
394,225,210 cycles..	# 0.52 insn per cycle	( +- 9.57% )	
204,046,712 instructions..		( +- 27.62% )	
time is : 0.119491 (min 0.117614, std dev 0.00116417)			v3
transfer rate was 6.24 GB/sec ( 41.75% of theoretical max that is 15 GB/sec)			
1,183,361,839 cycles..	# 0.70 insn per cycle	( +- 6.59% )	
824,904,000 instructions..		( +- 8.66% )	
time is : 0.0805418 (min 0.0798115, std dev 0.00128884)			v6
transfer rate was 9.25 GB/sec ( 61.93% of theoretical max that is 15 GB/sec)			
288,211,800 cycles..	# 0.32 insn per cycle	( +- 1.80% )	
92,540,296 instructions..		( +- 3.80% )	



## V\* profile - O3

```
luca@GGG:~/code/HPC_lectures/pipeline/2018% ./v0_papi_03n 50000000
generating 100000000 numbers..done
sum is 1.24993e+07
time is : 0.104058 (min 0.103508, std dev 0.000375562, all 1.04728)
transfer rate was 7.16 GB/sec ( 47.94% of theoretical max that is 15 GB/sec)
    IPC: 0.65
    [ time: 0.1041sec - ins: 1.50004e+08 ]
luca@GGG:~/code/HPC_lectures/pipeline/2018% ./v1_papi_03n 50000000
generating 100000000 numbers..done ( 1.27 )
pipeline demonstrator, step 1:
- unroll 2 times

sum is 1.24993e+07
time is : 0.0755591 (min 0.0750261, std dev 0.000291917, all 0.762576)
transfer rate was 9.86 GB/sec ( 66.02% of theoretical max that is 15 GB/sec)
    IPC: 1.2
    [ time: 0.07556sec - ins: 1.93753e+08 ]
luca@GGG:~/code/HPC_lectures/pipeline/2018% ./v3_papi_03n 50000000
generating 100000000 numbers..done (in 1.08sec)
pipeline demonstrator, step 3:

sum is 1.24993e+07
time is : 0.0545231 (min 0.0544507, std dev 8.46002e-05, all 0.545244)
transfer rate was 13.7 GB/sec ( 91.49% of theoretical max that is 15 GB/sec)
    IPC: 1.1
    [ time: 0.0545sec - ins: 1.6e+08 ]%
luca@GGG:~/code/HPC_lectures/pipeline/2018% ./v3c_papi_03n 50000000
generating 100000000 numbers..done (in 1.27sec)
pipeline demonstrator, step 3:
- unroll 2 times +
- separate mul and sum
- separate accumulations

sum is 1.24993e+07
time is : 0.0527944 (min 0.0526688, std dev 0.000107074, all 0.53314)
transfer rate was 14.1 GB/sec ( 94.49% of theoretical max that is 15 GB/sec)
    IPC: 1.2
    [ time: 0.0528sec - ins: 1.75e+08 ]
```



## V\* profile – 03 + vectorisation

There's a lot of improvement in such a simple kernel, but why IPC even decreased?

Hint: the code becomes memory-bound (look at the memory transfer rate).

```
luca@GGG:~/code/HPC_lectures/pipeline/2018% ./v6_papi_03n 50000000
generating 100000000 numbers..done (in 1.27sec)
sum is 1.24993e+07
time is: 0.0647406 (min 0.0642672, std dev 0.00017916, all 0.654759)
transfer rate was 11.5 GB/sec ( 77.05% of theoretical max that is 15 GB/sec)
    IPC: 0.8
        [ time: 0.06475sec - ins: 1.00003e+08 ]
luca@GGG:~/code/HPC_lectures/pipeline/2018% ./v6_intrinsics_papi_03n 50000000
generating 100000000 numbers..done (in 1.1sec)
sum is 1.24993e+07
time is: 0.0504149 (min 0.0468492, std dev 0.00132376, all 0.509429)
transfer rate was 14.8 GB/sec ( 98.95% of theoretical max that is 15 GB/sec)
    IPC: 0.67
        [ time: 0.05042sec - ins: 7.50003e+07 ]
luca@GGG:~/code/HPC_lectures/pipeline/2018% ./v8_papi_03n 50000000
generating 100000000 numbers..done (in 1.11sec)
sum is 1.24993e+07
time is: 0.0499751 (min 0.0466076, std dev 0.00124928, all 0.499767)
transfer rate was 14.9 GB/sec ( 99.82% of theoretical max that is 15 GB/sec)
    IPC: 0.56
        [ time: 0.04998sec - ins: 6.25002e+07 ]
```

## | Comparison: v0 – v1

v0

```
for ( int i = 0; i < N; i++ )
    sum += array1[i] * array2[i];
```

v1

```
for ( int i = 0; i < N-1; i+=2 )
    // simply unrolling 2 times, exposes the fact that at least
    // 2 elements of the array can be processed independently
{
    sum1 += array1[ i ] * array2[ i ];
    sum2 += array1[ i+1 ] * array2[ i+1 ];
}
if ( N % 2 )
    sum = array1[ N-1 ] * array2[ N-1 ];
```



# Comparison:

v0

```
.L8:  
# v0.c:185:    sum += array1[i] * array2[i];  
    mov    eax, DWORD PTR -136[rbp]      # tmp158, i  
    cdqe  
    lea    rdx, 0[0+rax*8]  
    mov    rax, QWORD PTR -96[rbp] # tmp159, array1  
    add    rax, rdx  
    vmovsd xmm1, QWORD PTR [rax]  
    mov    eax, DWORD PTR -136[rbp]  
    cdqe  
    lea    rdx, 0[0+rax*8] # _23,  
    mov    rax, QWORD PTR -88[rbp] # tmp161, array2  
    add    rax, rdx  
    vmovsd xmm0, QWORD PTR [rax]  
    vmulsd xmm0, xmm1, xmm0  
    vmosd  xmm1, QWORD PTR -104[rbp]      # tmp163, sum  
    vaddsd xmm0, xmm1, xmm0  
    vmosd  QWORD PTR -104[rbp], xmm0      # sum, tmp162  
    inc    DWORD PTR -136[rbp]      # i  
# v0.c:184:    for ( int i = 0; i < N; i++ )  
    mov    eax, DWORD PTR -136[rbp]      # tmp164, i  
    cmp    eax, DWORD PTR -148[rbp]      # tmp164, N  
    jl     .L8
```

v1

```
.L10:  
# v1_aligned.c:91:    sum1 += array1[ i ] * array2[ i ];  
    movl   -148(%rbp), %eax      # i, tmp186  
    cltq  
    leaq   0(%rax,8), %rdx  
    movq   -96(%rbp), %rax # array1, tmp187  
    addq   %rdx, %rax  
    vmovsd (%rax), %xmm1  
    movl   -148(%rbp), %eax      # i, tmp188  
    cltq  
    leaq   0(%rax,8), %rdx  
    movq   -88(%rbp), %rax # array2, tmp189  
    addq   %rdx, %rax  
    vmovsd (%rax), %xmm0  
    vmulsd %xmm0, %xmm1, %xmm0  
    vmosd  -112(%rbp), %xmm1      # sum1, tmp191  
    vaddsd %xmm0, %xmm1, %xmm0  
    vmosd  %xmm0, -112(%rbp)      # tmp190, sum1  
    movl   -148(%rbp), %eax      # i, tmp192  
    cltq  
    incq   %rax  
    leaq   0(%rax,8), %rdx  
    movq   -96(%rbp), %rax # array1, tmp193  
    addq   %rdx, %rax  
    vmovsd (%rax), %xmm1  
    movl   -148(%rbp), %eax      # i, tmp194  
    cltq  
    incq   %rax  
    leaq   0(%rax,8), %rdx  
    movq   -88(%rbp), %rax # array2, tmp195  
    addq   %rdx, %rax  
    vmosd  (%rax), %xmm0  
    vmulsd %xmm0, %xmm1, %xmm0  
    vmosd  -104(%rbp), %xmm1      # sum2, tmp197  
    vaddsd %xmm0, %xmm1, %xmm0  
    vmosd  %xmm0, -104(%rbp)  
    addl   $2, -148(%rbp) #, i  
.L9:  
# v1_aligned.c:87:    for ( int i = 0; i < N-1; i+=2 )  
    movl   -164(%rbp), %eax      # N, tmp198  
    decl   %eax      # _42  
    cmpl   %eax, -148(%rbp)      # i  
    jl     .L10
```



# Comparison:

v0

```
.L8:  
# v0.c:185:    sum += array1[i] * array2[i];  
    mov    eax, DWORD PTR -136[rbp]      # tmp158, i  
    cdqe  
    lea    rdx, [0+rax*8]  
    mov    rax, QWORD PTR -96[rbp] # tmp159, array1  
    add    rax, rdx  
    vmovsd xmm1, QWORD PTR [rax]  
    mov    eax, DWORD PTR -136[rbp]  
    cdqe  
    lea    rdx, [0+rax*8] # _23,  
    mov    rax, QWORD PTR -88[rbp] # tmp161, array2  
    add    rax, rdx  
    vmovsd xmm0, QWORD PTR [rax]  
    vmulsd xmm0, xmm1, xmm0  
    vmovsd xmm1, QWORD PTR -104[rbp]      # tmp163, sum  
    vaddsd xmm0, xmm1, xmm0  
    vmovsd QWORD PTR -104[rbp], xmm0      # sum, tmp162  
    inc    DWORD PTR -136[rbp]      # i  
    .L8:  
        for ( int i = 0; i < N; i++ )  
            mov    eax, DWORD PTR -136[rbp]      # tmp164, i  
            cmp    eax, DWORD PTR -148[rbp]      # tmp164, N  
            jl     .L8
```

v1

```
.L10:  
# v1_aligned.c:91:    sum1 += array1[ i ] * array2[ i ];  
    movl   -148(%rbp), %eax      # i, tmp186  
    cltq  
    leaq   0(%rax,8), %rdx  
    movq   -96(%rbp), %rax # array1, tmp187  
    addq   %rdx, %rax  
    vmovsd (%rax), %xmm1  
    movl   -148(%rbp), %eax      # i, tmp188  
    cltq  
    leaq   0(%rax,8), %rdx  
    movq   -88(%rbp), %rax # array2, tmp189  
    addq   %rdx, %rax  
    vmovsd (%rax), %xmm0  
    vmulsd %xmm0, %xmm1, %xmm0  
    vmovsd -112(%rbp), %xmm1      # sum1, tmp191  
    vaddsd %xmm0, %xmm1, %xmm0  
    vmovsd %xmm0, -112(%rbp)      # tmp190, sum1  
    movl   -148(%rbp), %eax      # i, tmp192  
    cltq  
    incq   %rax  
    leaq   0(%rax,8), %rdx  
    movq   -96(%rbp), %rax # array1, tmp193  
    addq   %rdx, %rax  
    vmovsd (%rax), %xmm1  
    movl   -148(%rbp), %eax      # i, tmp194  
    cltq  
    incq   %rax  
    leaq   0(%rax,8), %rdx  
    movq   -88(%rbp), %rax # array2, tmp195  
    addq   %rdx, %rax  
    vmovsd (%rax), %xmm0  
    vmulsd %xmm0, %xmm1, %xmm0  
    vmovsd -104(%rbp), %xmm1      # sum2, tmp197  
    vaddsd %xmm0, %xmm1, %xmm0  
    vmovsd %xmm0, -104(%rbp)  
    addl   $2, -148(%rbp) #, i  
.L9:  
# v1_aligned.c:87:    for ( int i = 0; i < N-1; i+=2 )  
    movl   -164(%rbp), %eax      # N, tmp198  
    decl   %eax      # _42  
    cmpl   %eax, -148(%rbp)      # i  
.L10
```

The v1 version looks twice as longer (i.e.: more instructions to be executed), actually it really looks like the same code was copied & pasted below the original segment.

How does it come that the result is a faster execution?



# Comparison: v0 – v1

The point is clearer considering the output of the PAPI instrumented code, that returns the IPC. Clearly, the 2fold unroll makes the CPU able to better exploit more than 1 logical units at a time.

```
luca@GGG:~/code/HPC_lectures/pipeline/2018% ./v0_papi_00 50000000
generating 100000000 numbers..done
sum is 1.24993e+07
time is :0.191208 (min 0.190616, std dev 0.00053432, all 1.91787)
transfer rate was 3.9 GB/sec ( 26.09% of theoretical max that is 15 GB/sec)
IPC: 1.9
[ time: 0.1912sec - ins: 1.00158e+09 ]
luca@GGG:~/code/HPC_lectures/pipeline/2018% ./v1_papi_00 50000000
generating 100000000 numbers..done ( 0.965)
pipeline demonstrator, step 1:
- unroll 2 times

sum is 1.24993e+07
time is :0.125749 (min 0.12396, std dev 0.00142263, all 1.26349)
transfer rate was 5.92 GB/sec ( 39.67% of theoretical max that is 15 GB/sec)
IPC: 2.8
[ time: 0.1258sec - ins: 9.76578e+08 ]
```



# Refining v1

v1

```
for ( int i = 0; i < N-1; i+=2 )
    // simply unrolling 2 times, exposes the fact that at least
    // 2 elements of the array can be processed independently
{
    sum1 += array1[ i ] * array2[ i ];
    sum2 += array1[ i+1 ] * array2[ i+1 ];
}
if ( N % 2 )
    sum = array1[ N-1 ] * array2[ N-1 ];
```

v1b

```
double register sum0 = 0;
double register sum1 = 0;

double register * restrict a1 = __builtin_assume_aligned(array1, 32);
double register * restrict a2 = __builtin_assume_aligned(array2, 32);

tstart = CPU_TIME;
#pragma ivdep
for( int i = 0 ; i < N-1; i+=2 )
{
    sum0 += *(a1++) * *(a2++);
    sum1 += *(a1++) * *(a2++);
}
if( N%2 )
    sum = *a1 * *a2;
```



# Refining v1

```
luca@GGG:~/code/HPC_lectures/pipeline/2018% ./v1_papi_00 50000000
generating 100000000 numbers..done ( 0.973)
pipeline demonstrator, step 1:
- unroll 2 times

sum is 1.24993e+07
time is 0.125593 (min 0.125287, std dev 0.000476174, all 1.26231)
transfer rate was 5.93 GB/sec ( 39.72% of theoretical max that is 15 GB/sec)
    IPC: 2.8
    [ time: 0.1256sec ins: 9.76578e+08 ]

luca@GGG:~/code/HPC_lectures/pipeline/2018% ./v1b_papi_00 50000000
generating 100000000 numbers.. done (in 0.973sec)
pipeline demonstrator, step 1b:
- unroll 2 times +
- align memory +
- minimize ptr arithmetic

sum is 1.24993e+07
time is 0.0977905 (min 0.0972945, std dev 0.000712555, all 0.977921)
transfer rate was 7.62 GB/sec ( 51.01% of theoretical max that is 15 GB/sec)
    IPC: 2.1
    [ time: 0.0978sec ins: 5.76578e+08 ]
```



# Refining: v3

Let's go further in trying to make it clear for the CPU about the possible ILP

```
#pragma ivdep
for ( int i = 0; i < N_4; i+=4 )
{
    sum += array1[i] * array2[i] +
           array1[i+1] * array2[i+1] +
           array1[i+2] * array2[i+2] +
           array1[i+3] * array2[i+3];
}
for ( int i = N_4; i < N; i++ )
    sum += array1[i] * array2[i];
```

## prefetching

v3b

```
double register a;
double register b;
a = array1[0] * array2[0];
ma ivdep
for ( int i = 0; i < N_4; i+=4 )
{
    DO_NOT_OPTIMIZE;
    b = array1[i+4] * array2[i+4];
    DO_NOT_OPTIMIZE;
    sum += a +
        array1[i+1] * array2[i+1] +
        array1[i+2] * array2[i+2] +
        array1[i+3] * array2[i+3];
    b
    a = b;
}
for ( int i = N_4; i < N; i++ )
sum += array1[i] * array2[i];
```



# Refining: vectorisation



With the following statement you can define a vector type in gcc

```
typedef double v4df __attribute__ ((vector_size (4*sizeof(double))));  
typedef union {  
    v4df  V;  
    double v[4];  
}v4df_u;
```

- By creating this union, you can access the single doubles within the vector
- This is the actual vector, made up by 4 doubles. You can not access the single elements.



# Refining: vectorisation



What is this  
strange stuff  
about ?

The loop is re-written  
here in its simplest  
form.

Now, however, the  
variables are vectors.

```
#ifdef _GNU_SOURCE
    v4df sum_ = {0, 0, 0, 0};
#else
    v4df sum_ = {0};
#endif
v4df register mytmp;
v4df register tmp = *((v4df*)&array1[0]) * *((v4df*)&array2[0]);

int N_4 = N/4;
int N_4 = N_4*4;
tstart = CPU_TIME;
#pragma ivdep
for( int i = 1; i <= N_4; i++)
{
    _DO_NOT_OPTIMIZE_BEGIN;
    mytmp = *((v4df*)array1 + i) * *((v4df*)array2 + i);
    _DO_NOT_OPTIMIZE_END;
    sum_ += tmp;
    tmp = mytmp;
}

for ( int i = N_4; i < N; i++ )
    sum += array1[ i ] * array2[ i ];
```



Vector type  
with 256bits  
(AVX)

You can  
initialize  
it as an  
array

The FMA in  
vector AVX  
flavour

Why am I  
defining those  
macros ?

With the following statements you prepare the ground to use  
intrinsics, both types and functions.

```
#elif defined ( __AVX__ ) || defined ( __AVX2__ )  
  
#define V_DSIZE 4  
typedef __m256d vd;  
vd _dzero_ = {0, 0, 0, 0};  
#define MUL_ADD( A1, A2, R ) _mm256_fmaddd_pd( (A1), (A2), (R) )
```

Intrinsics are an API, exposed by the compiler<sup>(\*)</sup>, that provide direct access to vector instructions and types.

(\*) they are no compiler-dependent: look at <https://software.intel.com/sites/landingpage/IntrinsicsGuide/> for Intel's intrinsics



As before, the loop is re-written here in its simplest form.

It also looks very similar to the previous one.

The variables are still vectors.

Note the usage of macros: the code is still valid both for AVX512 or SSE

```
vd sum__attribute__ ((aligned(64)));
sum_ = _dzero_;

vd * restrict A1 __attribute__ ((aligned(64)));
vd * restrict A2 __attribute__ ((aligned(64)));
A1 = (vd*)array1 ;
A2 = (vd*)array2 ;

int N__ = N / V_DSIZE;
int N_ = N__ * V_DSIZE;

tstart = CPU_TIME;

#pragma ivdep
for( int i = 0; i < N__; i++)
    sum_ = MUL_ADD( A1[i], A2[i], sum_ );

for ( int i = N__; i < N; i++)
    sum += array1[ i ] * array2[ i ];
```



that's all, have fun

"So long  
and thanks  
for all the fish"