

Homework 4

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Part I: Written Exercises

1. (a) Answer:

$$\begin{aligned}\frac{\partial}{\partial w} E_{in} &= \frac{\partial}{\partial w} \|y - Xw\|^2 + \lambda \|w\|^2 \\ &= 2wX^T X - 2X^T y + 2\lambda w \\ &= 2w(X^T X + \lambda I) - 2X^T y\end{aligned}$$

1. (b) Answer:

Set above equation equals 0, then:

$$\begin{aligned}2w(X^T X + \lambda I) - 2X^T y &= 0 \\ w(X^T X + \lambda I) &= X^T y \\ w &= (X^T X + \lambda I)^{-1} X^T y\end{aligned}$$

So the closed form solution should be: $w = (X^T X + \lambda I)^{-1} X^T y$