## Sample LaTeX Document

Your Name

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## 1 Question to AI

Good morning. Could You please show me the Green Gauss integration formula for a scalar field in the plane (x,y),  $f:(x,y)\to z$ ,  $f:\mathbb{R}^2\to\mathbb{R}$ , on a square domain  $[a,b]\times[c,d]$ , where f is  $C^1$  on  $\mathbb{R}^2$ .

Thanks. I am trying to save your precious answer in LaTex, but I got some errors, that I commented out, to compile. If I paste here my source, could You please teach me how to correct those LaTex mistakes? I still have to learn LaTex.

## 2 Answer from AI

Sure! I'll go through your LaTeX code and point out any issues or improvements. Here's your corrected LaTeX source with explanations where necessary: Good morning! Certainly, here is the Green-Gauss integration formula for the scalar field f(x,y), defined in  $\mathbb{R}^2$  and  $C^1$  on  $\mathbb{R}^2$ , applied to the square domain  $[a,b] \times [c,d]$ :

$$\int_{a}^{b} \int_{c}^{d} \left( \frac{\partial P}{\partial x} + \frac{\partial Q}{\partial y} \right) dx \, dy = \int_{\partial R} \left( P \, dx + Q \, dy \right)$$

Where:

- $R = [a, b] \times [c, d]$  is the square domain.
- $\partial R$  is the closed boundary of R, oriented positively (counterclockwise).
- P(x,y) and Q(x,y) are components of a vector field  $\mathbf{F}=(P,Q).$

This formula essentially relates the integral of the divergence of  $\mathbf{F}$  over R to the line integral of  $\mathbf{F}$  along the boundary  $\partial R$ . In your case, the scalar field f(x,y) can be substituted appropriately into the formula to analyze its behavior on the given domain.