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function [xhat, meas] = filterTemplate(calAcc, calGyr, calMag)
% FILTERTEMPLATE Filter template
% This is a template function for how to collect and filter data
% sent from a smartphone live. Calibration data for the
% accelerometer, gyroscope and magnetometer assumed available as
% structs with fields m (mean) and R (variance).
% The function returns xhat as an array of structs comprising t
% (timestamp), x (state), and P (state covariance) for each
% timestamp, and meas an array of structs comprising t (timestamp),
% acc (accelerometer measurements), gyr (gyroscope measurements),
% mag (magnetometer measurements), and orint (orientation quaternions
% from the phone). Measurements not availabe are marked with NaNs.
% As you implement your own orientation estimate, it will be
% visualized in a simple illustration. If the orientation estimate
% is checked in the Sensor Fusion app, it will be displayed in a
% separate view.
% Note that it is not necessary to provide inputs (calAcc, calGyr,
calMag).
```

### Setup necessary infrastructure

```
import('com.liu.sensordata.*'); % Used to receive data.
% Filters used
magFilt = true;
accFilt = true;
```

### Filter settings

```
t0 = []; % Initial time (initialize on first data received)
nx = 4; % Assuming that you use q as state variable.
% Add your filter settings here.
T = 1/25;
```

```
% Gyroscope covariances
sigma_w = 1/10; % was 0.01
Rw = diag([sigma_w^2 sigma_w^2 sigma_w^2]);
sigma v = 0.0014;
Rv = diag([sigma_v^2 sigma_v^2 sigma_v^2]);
qyr old = [0; 0; 0];
% Accelerometer parameters and covariances
g_abs = 9.82; % 9.8908 from estimate using stationary data.
g_{lim} = [0.8 \ 1.2]*g_{abs};
                          % +- 20% marginal
sigma_a = 0.3; % From variance estimate using stationary data.
Ra = diag([sigma_a^2 sigma_a^2 sigma_a^2]);
% Magnetometer parameters and covariances
m abs = 39.1103; % 39.1103 from estimate using stationary data.
m_lim = [0.6 1.4]*m_abs; % +- 20% marginal
sigma_m = 0.9; % From variance estimate using stationary data.s
Rm = diag([sigma_m^2 sigma_m^2 sigma_m^2]);
% Current filter state.
x = [1; 0; 0; 0];
P = eye(nx, nx);
% Saved filter states.
xhat = struct('t', zeros(1, 0), ...
              'x', zeros(nx, 0),...
              'P', zeros(nx, nx, 0));
meas = struct('t', zeros(1, 0),...
              'acc', zeros(3, 0),...
              'gyr', zeros(3, 0),...
              'mag', zeros(3, 0),...
              'orient', zeros(4, 0));
try
```

#### **Create data link**

```
* SensorDataReader started on 10.0.161.113:3400
*************

ERROR: Failed to open port or no connection attempted.

Unsuccessful connecting to client!

Make sure to start streaming from the phone *after*running this function!
```

#### Filter loop

```
while server.status() % Repeat while data is available
      % Get the next measurement set, assume all measurements
      % within the next 5 ms are concurrent (suitable for sampling
      % in 100Hz).
      data = server.getNext(5);
      if isnan(data(1)) % No new data received
        continue;
                          % Skips the rest of the look
      t = data(1)/1000; % Extract current time
      if isempty(t0) % Initialize t0
        t0 = t;
      end
      qyr = data(1, 5:7)';
      % Gyroscope
      if ~any(isnan(gyr))
          w = gyr;
          x tmp = x;
          P_{tmp} = P_{i}
          [x, P] = tu_qw(x, P, gyr, T, Rw);
          [x, P] = mu\_normalizeQ(x, P);
          x_kmin1 = x_tmp;
          P kmin1 = P tmp;
      else
응
            x tmp = x;
응
            P_{tmp} = P;
            [w, x, P] = tu_qw_pred(x, P, x_kmin1, P_kmin1, w, T, Rw);
            [x, P] = mu\_normalizeQ(x, P);
            x \text{ kmin1} = x \text{ tmp};
            P_kmin1 = P_tmp;
      end
      acc = data(1, 2:4);
      if accFilt
          if ~any(isnan(acc)) % Acc measurements are available.
          % Approximate g, skip update if "outlier"
          a_abs = sqrt(sum(acc.^2));
              if (a_abs > g_lim(1)) && (a_abs < g_lim(2))</pre>
                  g0 = [0; 0; a_abs];
                   [x, P] = mu_g(x, P, acc, Ra, g0);
```

```
[x, P] = mu\_normalizeQ(x, P);
            end
        end
    end
    mag = data(1, 8:10)';
    if magFilt
        if ~any(isnan(mag)) % Mag measurements are available.
            % Approximate m, skip update if "outlier"
            m_abs = sqrt(sum(mag.^2));
            if (m abs > m lim(1)) \&\& (m abs < m lim(2))
                m0 = [0; 12; -36.09]; m0 = m0/norm(m0);
                [x, P] = mu m(x, P, mag, Rm, m0);
                [x, P] = mu\_normalizeQ(x, P);
            end
        end
    end
    orientation = data(1, 18:21)'; % Google's orientation estimate.
    % Visualize result
    if rem(counter, 10) == 0
      setOrientation(ownView, x(1:4));
      title(ownView, 'OWN', 'FontSize', 16);
      if ~any(isnan(orientation))
        if isempty(googleView)
          subplot(1, 2, 2);
          % Used for visualization.
          googleView = OrientationView('Google filter', gca);
        end
        setOrientation(googleView, orientation);
        title(googleView, 'GOOGLE', 'FontSize', 16);
      end
    end
    counter = counter + 1;
    % Save estimates
   xhat.x(:, end+1) = x;
   xhat.P(:, :, end+1) = P;
    xhat.t(end+1) = t - t0;
   meas.t(end+1) = t - t0;
    meas.acc(:, end+1) = acc;
   meas.gyr(:, end+1) = gyr;
   meas.mag(:, end+1) = mag;
    meas.orient(:, end+1) = orientation;
  end
catch e
  fprintf(['Unsuccessful connecting to client!\n' ...
```

## "tu\_qw"

```
function [x, P] = tu_qw(x, P, omega, T, Rw)
% EKF time update step
% Gyroscope measurement noise covariance (estimated from stationary
data)
sigma_v = 0.0014;
Rv = diag([sigma_v^2 sigma_v^2 sigma_v^2]);
% Process matrices
F = T/2*Somega(omega) + eye(4);
F \text{ tilde} = F;
G = T/2*Sq(x);
G_tilde = G;
% Prediction step
xp = F*x;
Pp = F_tilde*P*F_tilde' + G_tilde*Rw*G_tilde';
    % Update step
    % Equation: yk = H*xk + B*xkmin1_kmin1 + vk
    H = 2/T*pinv(Sq(x));
    B = -H;
    Bx = B*x;
    yhat = H*xp + Bx;
    S = H*Pp*H' + B*P*B' + Rv;
    K = Pp*H'*(S^{-1});
    x = xp + K*(omega - yhat);
    P = Pp - K*S*K';
end
```

# "tu\_qw\_pred"

```
function [w, x, P] = tu_qw_pred(x, P, x_kmin1, P_kmin1, omega, T, Rw)
% EKF time update step
% Estimate omega
H = 2/T*pinv(Sq(x_kmin1));
B = -H;
Bx = B*x_kmin1;
w = H*x + Bx;
% recalculate Process matrices
F = T/2*Somega(w) + eye(4);
F_{tilde} = F_{i}
G = T/2*Sq(x);
G_tilde = G;
% Prediction step
x = F*x;
P = F_tilde*P*F_tilde' + G_tilde*Rw*G_tilde';
end
```

## "mu\_g"

```
function [x, P] = mu_g(x, P, y, Ra, g0)
% EKF accelerometer measurement update

% Measurement matrices
hx = Qq(x)'*g0;
[dQ0, dQ1, dQ2, dQ3] = dQqdq(x);
Jhx = [dQ0'*g0 dQ1'*g0 dQ2'*g0 dQ3'*g0];

% Measurement update
S = Jhx*P*Jhx' + Ra;
K = P*Jhx'*(S^-1);

x = x + K*(y - hx);
P = P - K*S*K';
end
```

#### "mu m"

```
function [x, P] = mu_m(x, P, y, Rm, m0)
```

```
% EKF acclerometer measurement update
% normalize
ynorm = y/norm(y);
m0 = m0/norm(m0);
Rm = Rm/norm(y);

% Measurement matrices
hx = Qq(x)'*m0;
[dQ0, dQ1, dQ2, dQ3] = dQqdq(x);
Jhx = [dQ0'*m0 dQ1'*m0 dQ2'*m0 dQ3'*m0];

% Measurement update
S = Jhx*P*Jhx' + Rm;
K = P*Jhx'*(S^-1);

x = x + K*(y - hx);
P = P - K*S*K';
end
```

## "Project\_Implementation"

```
% SSY345 Project Implementation
% SECTION 4.1
% Task 2) See file Project_test.m. Measurement data loaded below.
load('data_FrassePhone_stationary.mat');
%% SECTION 4.2
% Task 3) Design the EKF time update step
% Implemented in file "tu_qw.m".
% Time between samples
T = 1/fs;
% Sizes
K = length(t);
n = 4;
% Gyroscope covariances
sigma_w = 0.01;
Rw = diag([sigma_w^2 sigma_w^2 sigma_w^2]);
sigma_v = 0.0014;
Rv = diag([sigma_v^2 sigma_v^2 sigma_v^2]);
% Accelerometer parameters and covariances
g_abs = 9.82; % 9.8908 from estimate using stationary data.
```

```
g_lim = [0.9 1.1]*g_abs;
                          % +- 10% marginal
sigma a = 0.03; % From variance estimate using stationary data.
Ra = diag([sigma_a^2 sigma_a^2 sigma_a^2]);
% Magnetometer parameters and covariances
m_abs = 39.1103; % 39.1103 from estimate using stationary data.
m_{lim} = [0.9 \ 1.1] * m_abs;
                           % +- 10% marginal
sigma m = 0.5; % From variance estimate using stationary data.s
Rm = diag([sigma_m^2 sigma_m^2 sigma_m^2]);
% Initial estimates and covariances
x_0 = [0; 0; 1; 0];
P = 0 = diag([1 1 1 1]);
% Visualisation stuff
figure(1)
ownView = OrientationView('Own filter', gca);
xw = zeros(4,K);
Pw = zeros(4,4,K);
xw(:,1) = x_0;
Pw(:,:,1) = P_0;
xa = zeros(4,K);
Pa = zeros(4,4,K);
xm = zeros(4,K);
Pm = zeros(4,4,K);
x = zeros(4,K);
P = zeros(4,4,K);
NaN_gyr = 1;
NaN_acc = 1;
for k = 2:K
    % Gyroscope measurement computations
    % Prediction:
    [xw(:,k), Pw(:,:,k)] = tu_qw(xw(:,k-1), Pw(:,:,k-1), y_qyr(:,k),
 T, Rw);
    % Include normalization of quaternion before using... where?
    [xw(:,k), Pw(:,:,k)] = mu_normalizeQ(xw(:,k), Pw(:,:,k));
    % Accelerometer computations
    % Measurement update:
    if ~isnan(y_acc(:,k))
        % Approximate q, skip update if "outlier"
        a_abs = sqrt(sum(y_acc(:,k).^2));
        if (a_abs > g_lim(1)) && (a_abs < g_lim(2))</pre>
            g0 = [0; 0; a_abs];
            [xa(:,k), Pa(:,:,k)] = mu_g(xw(:,k), Pw(:,:,k),
 y_acc(:,k), Ra, g0);
            [xa(:,k), Pa(:,:,k)] = mu_normalizeQ(xa(:,k), Pa(:,:,k));
        else
            xa(:,k) = xw(:,k);
```

```
Pa(:,:,k) = Pw(:,:,k);
        end
    else
        xa(:,k) = xw(:,k);
        Pa(:,:,k) = Pw(:,:,k);
    end
    % Magnetometer computations
    % Measurement update:
    if ~isnan(y_mag(:,k))
        % Approximate m, skip update if "outlier"
        m_abs = sqrt(sum(y_mag(:,k+1).^2));
        if (m abs > m lim(1)) && (m abs < m lim(2))</pre>
            m0 = [0; 19.18; -34.09];
            [xm(:,k), Pm(:,:,k)] = mu_m(xa(:,k), Pa(:,:,k),
y_mag(:,k), Rm, m0);
            [xm(:,k), Pm(:,:,k)] = mu_normalizeQ(xm(:,k), Pm(:,:,k));
        elseif ~isnan(y_acc(:,k))
            xm(:,k) = xa(:,k);
            Pm(:,:,k) = Pa(:,:,k);
        else
            xm(:,k) = xw(:,k);
            Pm(:,:,k) = Pw(:,:,k);
        end
    elseif ~isnan(y_acc(:,k))
        xm(:,k) = xa(:,k);
        Pm(:,:,k) = Pa(:,:,k);
    else
        xm(:,k) = xw(:,k);
        Pm(:,:,k) = Pw(:,:,k);
    end
    % Combine accelerometer and magnetometer information
    % Update:
    % Temporary for only gyroscope (Task 5)
응
     x(:,k+1) = xwp(:,k+1);
ુ
      P(:,:,k+1) = Pwp(:,:,k+1);
응
      x(2:4,k+1) = xa(:,k+1);
응
      P(2:4,2:4,k+1) = Pa(:,:,k+1);
      [x(:,k+1),P(:,:,k+1)] = mu normalizeQ(xwp(:,k+1), Pwp(:,:,k+1));
    setOrientation(ownView, xm(:,k));
    title(ownView, 'OWN', 'FontSize', 16);
    pause(0.01)
end
```

