Practice 0

Activities solutions

1. Given the numbers $x = 14{,}32$, $y = 27{,}12$ and $z = 3{,}5$, calculate the value of the expression

$$\frac{8x + y^2}{2 - \sqrt[6]{x^3 - \frac{1}{z}}}$$

```
-->x=14.32; y=27.12; z=3.5;

-->(8*x+y^2)/(2-(x^3-1/z)^(1/6))

ans =

- 476.45685
```

2. Indicate how to introduce, in Scilab, the matrix $A = (a_{ij})$ of order 50×50 such that $a_{ii} = 10$ and $a_{ij} = 0$ for $i \neq j$.

There are several possibilities. For example,

```
-->for i=1:50 do

--> A(i,i)=10;

-->end

or, also,

-->A=10*eye(50,50);
```

3. Enter, by using blocks, in Scilab, the following matrix. Indicate the instructions that you use.

$$\mathsf{E} = \begin{pmatrix} 1 & 0 & 0 & 8 & 8 & 8 & 8 & 8 \\ 0 & 1 & 0 & 8 & 8 & 8 & 8 & 8 \\ 0 & 0 & 1 & 8 & 8 & 8 & 8 & 8 \\ -1 & 0 & 0 & 0 & 0 & 0 & 0 & 0 \\ 0 & -1 & 0 & 0 & 0 & 0 & 0 & 0 \\ 0 & 0 & -1 & 0 & 0 & 0 & 0 & 0 \end{pmatrix}$$

```
-->*E=[eye(3,3) 8*ones(3,5);-eye(3,3) zeros(3,5)]
```

4. Write the following loop to obtain the matrix $C = (c_{ij})$ of order 30×30 so that $c_{ij} = i \cdot j$.

```
C=Zeros (30,30);
for i=1:30 for j=1:30 do C(i,j)=i*j;
end end
```

Calculate the matrix $D=C^2-3C$ and indicate which is the element of the matrix D that there is in the position row 17 column 25.

```
-->C=Zeros(30,30);

-->for i=1:30 for j=1:30 do C(i,j)=i*j;

-->end end

-->D=C^2-3*C;

-->D(17,25)

ans =

4017100.
```

5. Write the instructions of Scilab that extract of the matrix $\sf C$ of the activity 4 the submatrix formed by the rows 3 and 7 and the columns 3 and 7. Write this submatrix.

```
-->C([3,7],[3,7])
ans =

9. 21.
21. 49.
```

6. Write the instructions of Scilab that extract of the matrix C of the activity 4 the submatrix formed by the rows 13 to 16 and the columns 17 to the 19. Write the matrix you obtain.

```
-->C([13:16],[17:19])
ans =

221. 234. 247.
238. 252. 266.
255. 270. 285.
272. 288. 304.
```

7. Given the vectors u = (1/4, -1/6, 5/6) and v = (1/5, 3/4, -2/3), calculate the scalar product of both and the angle that form. Write this angle in degrees.

8. Solve the matrix system $\left\{ \begin{array}{l} 3X+Y=A\\ 2X-5Y=B \end{array} \right. \ \, \text{being}$

$$\mathsf{A} = \begin{pmatrix} 1/2 & 0 & -1/3 \\ 0 & -2/3 & 3 \end{pmatrix}, \qquad \mathsf{B} = \begin{pmatrix} 1/5 & 1 & -1/6 \\ 1/6 & 1/5 & 2/3 \end{pmatrix}$$

We isolate the matrices unknowns: $\left\{ \begin{array}{l} 3X+Y=A \\ 2X-5Y=B \end{array} \right. \longrightarrow \left\{ \begin{array}{l} 3X+Y=A \\ 17X=5A+B \end{array} \right. \longrightarrow \left\{ \begin{array}{l} Y=A-3X \\ X=\frac{1}{17}(5A+B) \end{array} \right.$ And now we use Scilab:

```
-->X=1/17*(5*A+B)
X =
```

9. Given the matrix

$$A = \begin{pmatrix} 1 & 2 & 3 \\ 7 & 8 & 9 \\ 4 & 5 & 6 \end{pmatrix},$$

calculate the matrix $Z = A^3 - 16A^2 - 2I$, where I is the identity matrix of order 3.

```
-->A=[1 2 3; 7 8 9; 4 5 6]
          2.
                 3.
    1.
    7.
          8.
                 9.
    4.
-->I=eye(3,3)
I =
          0.
                 0.
    1.
    0.
                 0.
          1.
    0.
          0.
                 1.
-->Z=A^3-16*A^2-2*I
  - 20. - 15. - 12.
 - 36. - 53. - 66.
- 27. - 33. - 41.
```

10. Given the matrix V

$$\mathsf{V} = \begin{pmatrix} 1 \\ 7 \\ 6 \end{pmatrix},$$

Calculate the matrix ZV, where Z is the matrix of the previous activity. Write the matrix ZV as a linear combination of the columns of Z.

```
-->V=[1;7;6]
V =
1.
7.
6.
-->Z*V
ans =
- 197.
- 803.
- 504.
```

$$ZV = V(1) * Z(:,1) + V(2) * Z(:,2) + V(3) * Z(:,3)$$

if we enter it in Scilab,

```
-->ZV=V(1)*Z(:,1)+V(2)*Z(:,2)+V(3)*Z(:,3)
ZV =
- 197.
```

- 803.

- 504.

As we can check, we have obtained the same result.