

ETC'S DELIVERABLE

Exercise 1.- A file takes 58,720,256 bytes. Give its size using both decimal and binary prefixes.

Solution:

- Decimal prefix: 58,720,256 KB = 58.720256 MB \approx 0.0587 GB \approx 0.00006 TB
- Binary prefix: 57.344 KiB = 56 MiB \approx 0.5469 GiB \approx 0.000053 TiB

Exercise 2.- A given hard disk has 4 sides (in two platters) and a linear track density of 30,000 tpi. The innermost diameter is 1" and the outermost diameter is 4".

1. What is the amount of useful surface in the disk? Give the result in square inches (in²).

$$\text{Innermost radius} = 1''/2 = 0.5''$$

$$\text{Outermost radius} = 4''/2 = 2''$$

$$\text{Area of circle (Innermost)} = \pi * (0.5'')^2 \approx 0.7854 \text{ in}^2$$

$$\text{Area of circle (Outermost)} = \pi * (2'')^2 \approx 12.5664 \text{ in}^2$$

$$\text{Useful surface of one disk} = 12.5664 \text{ in}^2 - 0.7854 \text{ in}^2 = 11.7810 \text{ in}^2$$

Solution:

$$\text{Useful surface} = 11.7810 \text{ in}^2 * 4 = 47.1240 \text{ in}^2$$

2. How many cylinders and tracks does it contain?

$$\text{Useful line length} = \text{outermost radius} - \text{innermost radius} = 2'' - 0.5'' = 1.5''$$

Solution:

$$\text{Cylinders} = 1.5'' * 30,000 = 45,000 \text{ cylinders}$$

$$\text{Tracks} = 45,000 * 4 = 180,000 \text{ tracks}$$

Exercise 3.- Calculate the capacity of the disk of exercise 2 assuming CAV format with 1400 sectors/track and a sector size of 512 bytes. What is the areal density of the disk? Give it in both Kbit/in² and Mbit/in² units.

Solution:

$$\begin{aligned} \text{Capacity (CAV)} &= 4 \text{ sides} * 45,000 \text{ cylinders} * 1400 \text{ sectors/track} * 512 \text{ bytes/sector} * 8 = \\ &1,032,192,000.000 \text{ bits} = 1,032,192,000 \text{ Kbits} = 1,032,192 \text{ Mbits} \end{aligned}$$

$$\begin{aligned} \text{Areal density} &= 1,032,192,000 \text{ Kbits}/47.1240 \text{ in}^2 \approx 21,903,743.3155 \text{ Kbits/in}^2 \approx \\ &21,903.7433 \text{ Mbits/in}^2 \end{aligned}$$

Exercise 4.- Calculate the capacity of the disk described in exercise 2 assuming it receives ZCAV format with the following distribution of 512 bytes.

Zone	Limits	Tpi	Sectors/track
0	3,25 "– 4,00 "	30000	3700
1	2,50 "– 3,25 "	30000	2900
2	1,75 "– 2,50 "	30000	2150
3	1,00 "– 1,75 "	30000	1400

What is the areal density of this disk? Give it in both Kbit/in² and Mbit/in² units.

Solution:

Capacity (ZCAV): 4 sides * (0.75"/2 * 30,000 tpi) * (3700 + 2900 + 2150 + 1400) * 512B * 8 = 1,870,848,000,000 bits = 1,870,848,000 Kbits = 1,870,848 Mbits

Areal density = 1,870,848,000 Kbits/47.1240 in² ≈ 39,700,534.7594 Kbits/in² ≈ 39,700.5348 Mbits/in²

Exercise 5.- Consider the disk described in exercise 4 rotates at 10,000 rpm. The average seek time is 10 ms, and the track-to-track seek time is 1 ms. Calculate:

1. The average access time for each zone.

Time of a single rotation = 60 s/min / 10,000 rpm = 0.006 s = 6 ms

Average rotational latency = 6 ms / 2 = 3 ms

Solution:

Average access time = 10 ms + 3 ms = 13 ms

2. The internal transfer speed for each zone.

Solution:

Internal transfer speed for zone 0 = (3700 sectors * 512 B/sector) / 6 ms ≈ 315.733 MB/s

Internal transfer speed for zone 1 = (2900 sectors * 512 B/sector) / 6 ms ≈ 247.467 MB/s

Internal transfer speed for zone 2 = (2150 sectors * 512 B/sector) / 6 ms ≈ 183.467 MB/s

Internal transfer speed for zone 3 = (1400 sectors * 512 B/sector) / 6 ms ≈ 119.467 MB/s

3. The average time it takes to read a 60 KB file, assuming it is stored in correlative sectors of the same track. Consider two cases: when the track is in zone 0 and when it is in zone 3.

Sector transfer time for zone 0 = 6 ms / 3700 sectors/tracks ≈ 1.6216 μs

Sector transfer time for zone 3 = 6 ms / 1400 sectors/tracks ≈ 4.2857 μs

Sectors needed = $60\text{KB} / 512 \text{ B/sector} = 117.1875 \text{ sectors} \approx 118 \text{ sectors}$

Transfer time for zone 0 (118 sectors) = $1.6216 \mu\text{s} * 118 \text{ sectors} \approx 0.1913 \text{ ms}$

Transfer time for zone 3 (118 sectors) = $4.2857 \mu\text{s} * 118 \text{ sectors} \approx 0.5057 \text{ ms}$

Solution:

Average read time for zone 0 (118 sectors) = $13 \text{ ms} + 0.1913 \text{ ms} = 13.1913 \text{ ms}$

Average read time for zone 3 (118 sectors) = $13 \text{ ms} + 0.5057 \text{ ms} = 13.5057 \text{ ms}$

- 4. The average time it takes to read a 60 KB file stored in randomly distributed sectors of cylinders located in zone 0. Assume the average seek time within the same zone is the average seek time divided by the number of zones, i.e., $10/4 = 2.5 \text{ ms}$.**

Access time for zone 0 = $2.5 + 3 = 5.5 \text{ ms}$

Solution:

Average read time for zone 0 (118 sectors) = $13 + 1.6216 \mu\text{s} + 117 * (5.5 \text{ ms} + 1.6216 \mu\text{s})$
 $\approx 656.6913 \text{ ms} \approx 0.6567 \text{ s}$

- 5. The time for reading a 100 MB file assuming it is optimally stored in zone 0 (according to the optimisations described in Section 4).**

Sectors occupied by the file = $100 \text{ MB} / 512 \text{ B/sector} = 195,312.5 \text{ sectors} \approx 195,313 \text{ sectors}$

Tracks occupied by the file = $195,313 \text{ sectors} / 3700 \text{ sectors/track} \approx 52.7873 \text{ tracks} \approx 53 \text{ tracks}$.

Cylinders occupied by the file = $53 \text{ tracks} / 4 \text{ tracks/cylinder} = 13.25 \text{ cylinders} \approx 14 \text{ cylinders}$

Track-to-track seek time = 1 ms

Transfer time for zone 0 (3700 sectors) = $1.6216 \mu\text{s} * 3700 \text{ sectors} \approx 5,99992 \text{ ms}$

Remainder sectors = $195,313 \text{ sectors} - ((53 - 1) \text{ tracks}) * 3700 \text{ sectors/track} = 2913 \text{ sectors}$

Transfer time for zone 0 (2913 sectors) = $1.6216 \mu\text{s} * 2913 \text{ sectors} \approx 4.7237 \text{ ms}$

Solution:

Average read time for zone 0 (100 MB) = $13 \text{ ms} + 5,99992 \text{ ms} * (53 - 1) \text{ tracks} + 4.7237 \text{ ms} + 1 \text{ ms} * 53 \text{ tracks} = 382.71954 \text{ ms} \approx 0.38272 \text{ s}$