



UNIVERSIDAD  
POLITECNICA  
DE VALENCIA



---

# Computers Fundamentals

---

Subject 1. Introduction to computers

---

---

---

At the end of the course, the student should know:

- The basic terms used in computer science
- How computer architecture has evolved
- The main functional units composing a computer
- The main data representation used in computer science

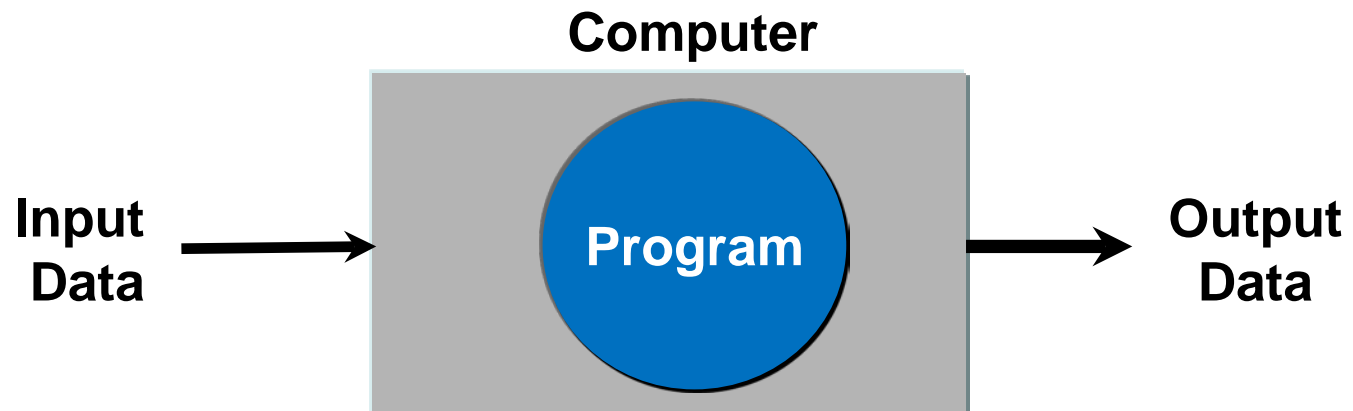
- Introducción a los Computadores.
  - J. Sahuquillo y otros. Ed. SP-UPV, 1997 (ref. 97.491).
- Fundamentos de los computadores
  - P. de Miguel Miguel Anasagasti, (Ed. Thomson-Paraninfo, 9ª edición)
- Digital design : principles and practices
  - John F. Wakerly (Ed. Upper Saddle River : Pearson Prentice Hall, 2006)

- Poliformat, sección “Recursos”
  - Ejercicios sin solución.
  - Ejercicios solucionados.
  - Página web:
    - » *conversión binario – decimal.*
  - Exámenes de años anteriores.
- Poliformat, sección “Contenidos”
  - Módulo 2: Sistemas de numeración.
    - » *Incluye teoría y ejercicios*



- Introduction
- History and evolution of computer architecture
- Von Neumann's computer architecture
- Basic computer's functional units
- Basic data representation systems

- Informática → INFORmación + autoMÁTICA
- Computer → stored program machine
- Program → A sequence of Instructions executed one by one



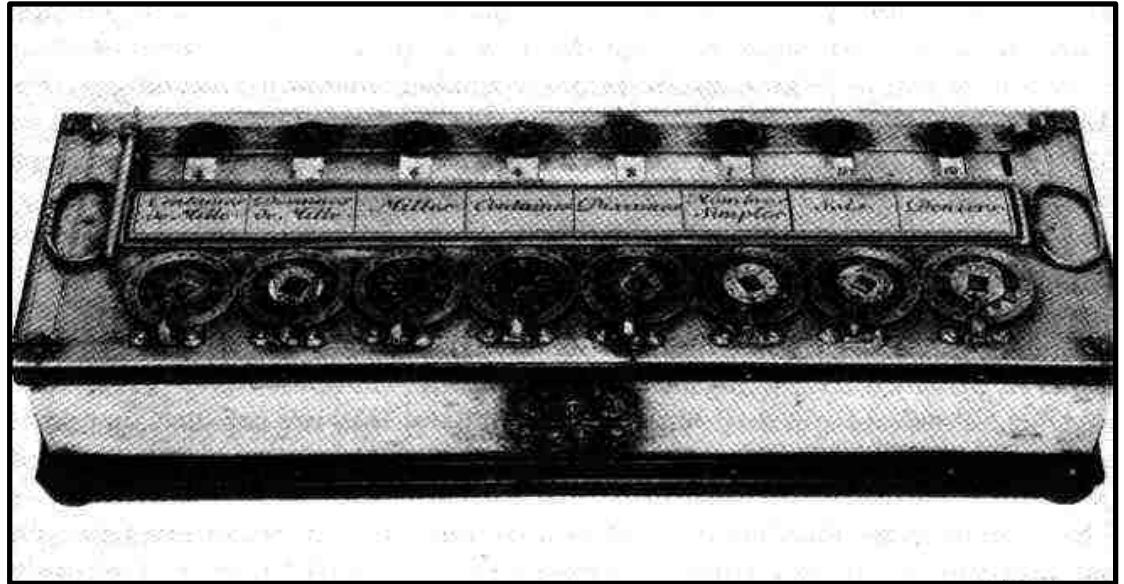
- Hardware → *the mechanical, magnetic, electronic, and electrical components making up a computer system*
- Software → *written programs (procedures or rules) and associated documentation pertaining to the operation of a computer system and that are stored in read/write memory*
- Computer functional unit → A specialized electronic device that realizes a specific task

- Bit → *minimal unit of information*
- Byte → *a sequence of 8 bits (enough to represent one character of alphanumeric data) processed as a single unit of information ( $2^8 = 256$  combinations)*



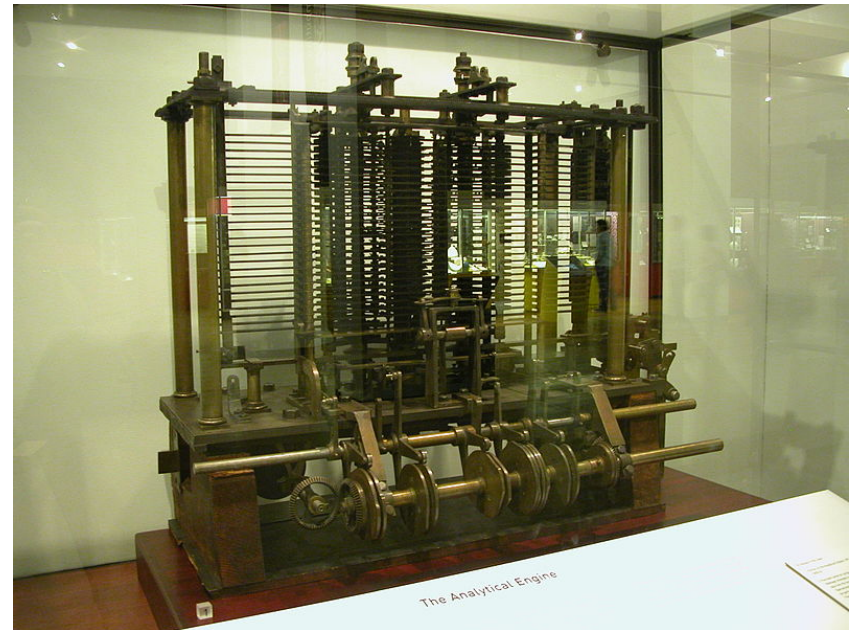
- Introduction
- History and evolution of computer architecture
- Von Neumann's computer architecture
- Basic computer's functional units
- Basic data representation systems

- The first mechanical device considered a computer was designed by Blaise Pascal (XVII century).
  - The “Pascalina” was able to add and to subtract numbers

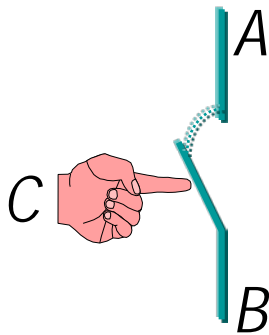


- Additional information can be found at:  
[http://en.wikipedia.org/wiki/Computer\\_history](http://en.wikipedia.org/wiki/Computer_history)

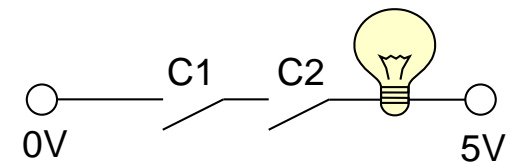
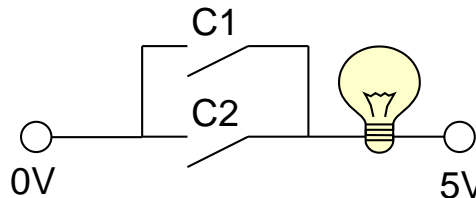
- The first device considered a programmable computer was designed by Charles Babbage en 1816
  - Its analytical machine was a mechanical device that used perforated cards for the introduction of programs and data
  - It's construction was never finished



- Modern computer's history turns around the introduction and evolution of the electronic switch
  - An electronic switch is a device that can break an electrical circuit, interrupting the current or diverting it from one conductor to another
  - An electronic switch allows the implementation of logic operations which can be combined to build a computer



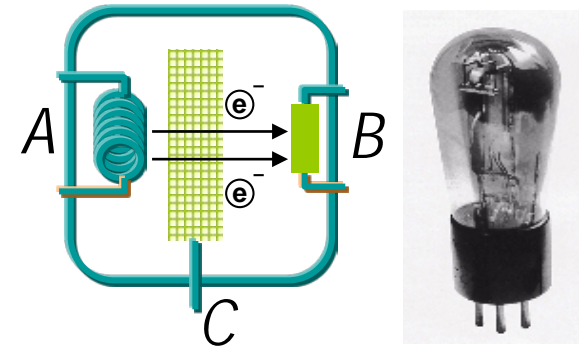
- Example: Under which circumstances the lights are on?



- Generations

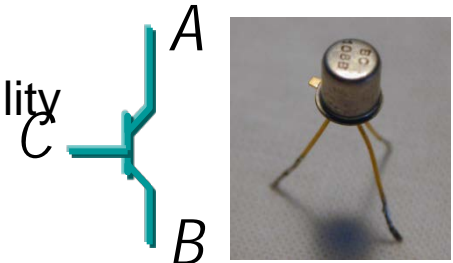
- First-generation machines (1940-1956)

- Vacuum tubes
    - High power consumption and heat dissipation
    - Low reliability



- Second generation machines (1956-1963)

- Transistors
    - Better power consumption, heat dissipation and reliability
    - Reduced costs and started the road toward miniaturization

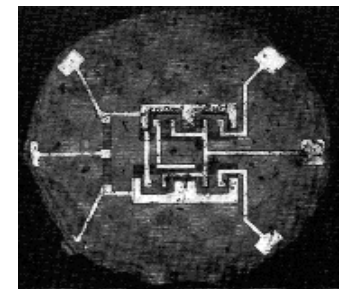


- Third-generation machines (1964-1971)

- Integrated circuits (chips)
    - Minicomputers

- Fourth-generation (1971-presente)

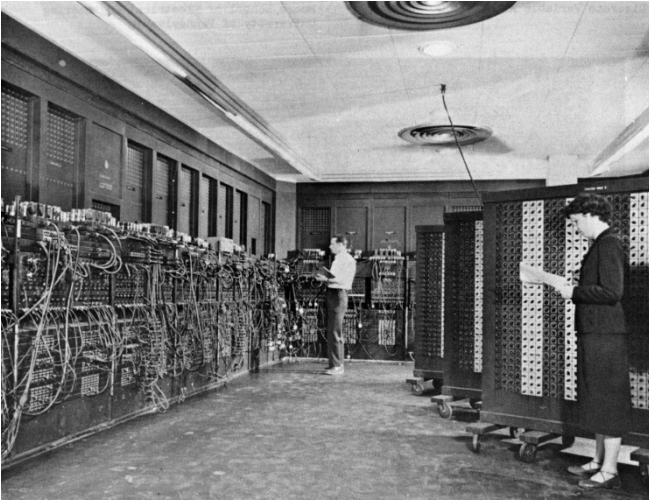
- Microprocessors
    - High integration scale
    - Personal computers





# History and evolution of computers

FCO



**ENIAC**  
**1<sup>st</sup> Gen**

**IBM 608**  
**2<sup>nd</sup> Gen.**



**PDP-11**  
**3<sup>rd</sup> Gen.**

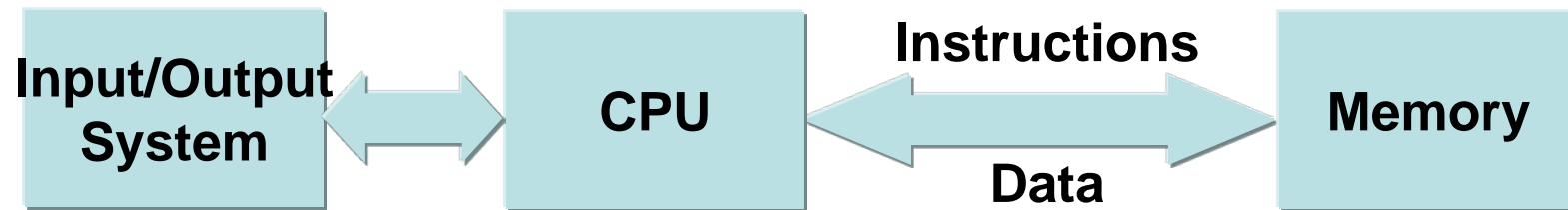


**Apple II**  
**4<sup>th</sup> gen.**

- Fifth-generation (present and future)
  - New technologies (optical, quantic, etc.)
  - Multi-core processors
  - Parallel and distributed processing
  - Ubiquitous computing and ubiquitous communications (Internet, mobile devices, social networks, etcetera)
  - Artificial intelligence applications (neuronal , expert systems, speech recognition systems, robotics, etc.)

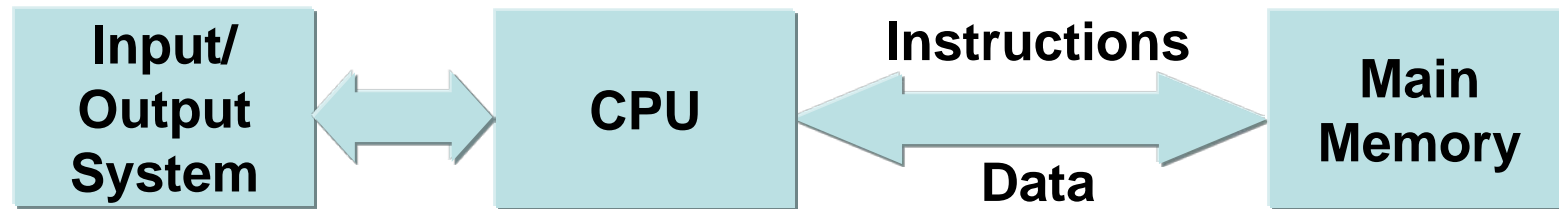
- Introduction
- History and evolution of computer architecture
- Von Neumann's computer architecture
- Basic computer's functional units
- Basic data representation systems





- Modern computers architecture are based on the Von Newmann's architecture
  - Memory stores data and instructions
  - The CPU exutes the instructions
  - The instructions can read and write data in memory
  - Instructions can access the Input/Output system

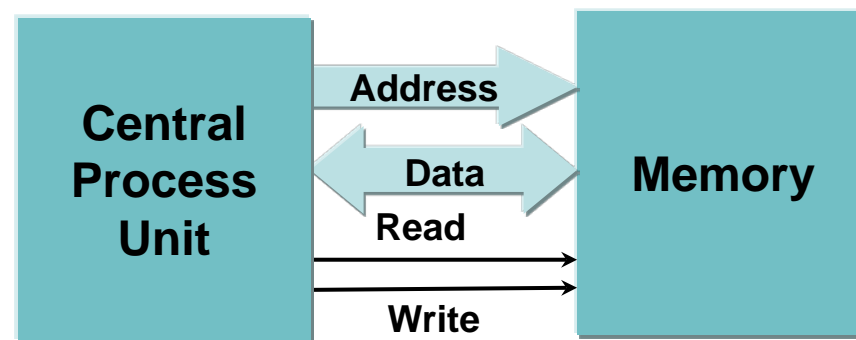
- Introduction
- History and evolution of computer architecture
- Von Neumann's computer architecture
- Basic computer's functional units
- Basic data representation systems



- It is the basis of the vast majority of current computers
  - The main memory stores instructions and data
  - The CPU executes instructions
  - The execution of an instruction can result in reading and / or write to main memory or access to the input / output system

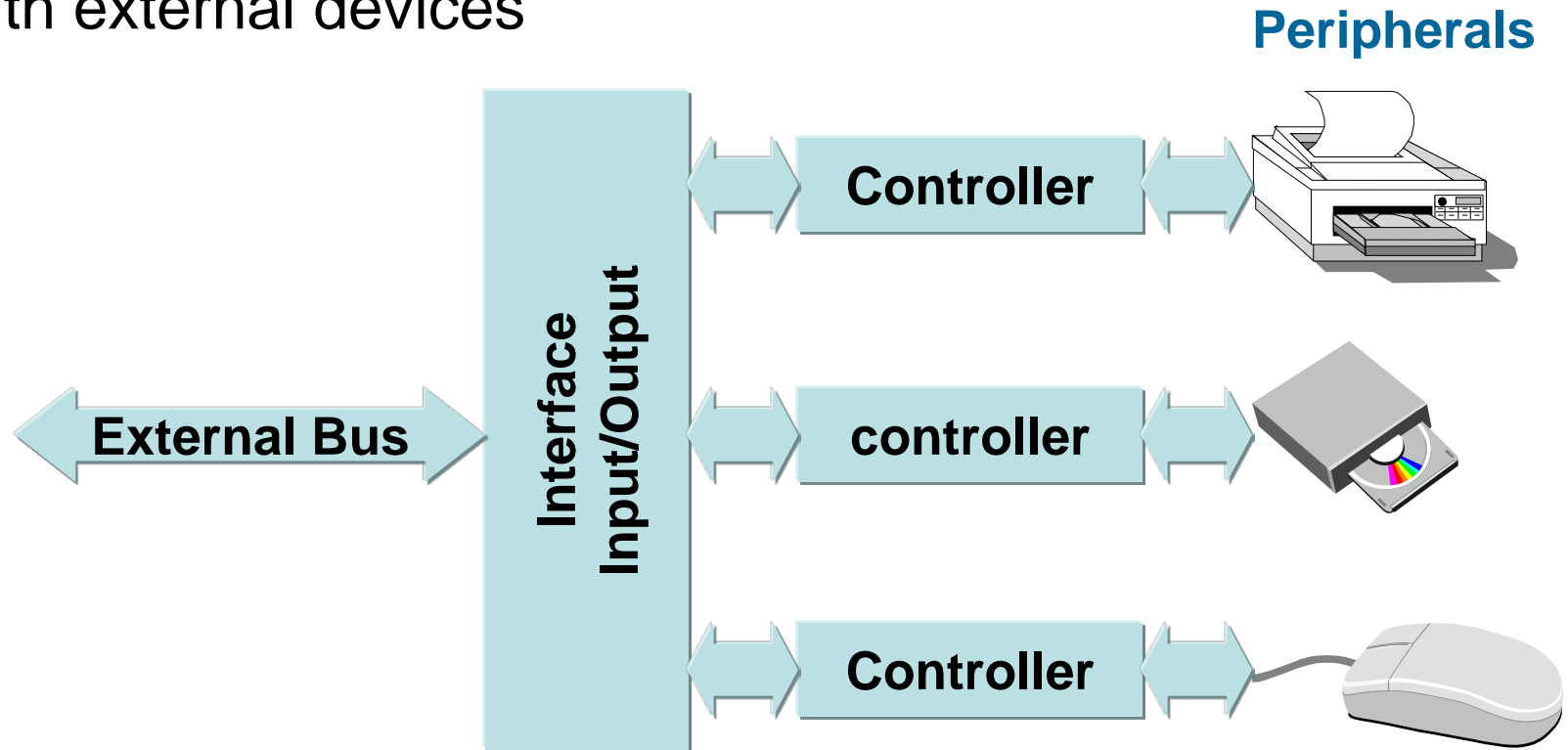
- Introduction
- History and evolution of computer architecture
- Von Neumann's computer architecture
- **Basic computer's functional units**
- Basic data representation systems

- Central process unit (CPU)
  - It is the component that interprets instructions and process data stored in programs
- Memory
  - Storage device (it can be read or write)
  - Processor access memory as if it were an independent indexed vector



- Input/Output System

- Allows the communication between the CPU and the memory with external devices



- Peripherals
  - Input: mouse, keyboard, touch screen ...
  - Output: screen, loudspeaker, printer...
  - Storage: DVD, flash memory ...
  - Communication: Modem, wireless network, ethernet ...
- CPU-memory versus peripherals
  - Different technologies
  - Different data transfer rates
  - Different data representation format
- Interface or controller
  - hardware/software devices which allow the communication between CPU-memory and the peripheral
  - It is used to make independent the CPU-memory from the peripheral

- Introduction
- History and evolution of computer architecture
- Von Neumann's computer architecture
- Basic computer's functional units
- **Basic data representation systems**



- **A numeral system (or system of numeration)** is a writing system for expressing numbers
  - It is a mathematical notation for representing numbers of a given set, using graphemes or symbols in a consistent manner
  - Examples: Decimal
- **Numeral system Base**
  - The Numeral system base is the number of different symbols used by the numeral system
  - Each symbol is called digit
  - Examples: Decimal (10 digits), binario (2 digits)

- **Positional systems**

- A number is defined as a sequence of digits where each digit is multiplied by a scale factor.
- The position of digits is important
  - Example: In decimal system,  $32 \neq 23$

- In a positional **base- $b$**  numeral system (with  $b$  a positive natural number known as the **radix**),  $b$  basic symbols (or digits) corresponding to the first  $b$  natural numbers including zero are used.

- Example:
  - Decimal: 0,1,2,3,4,5,6,7,8,9
  - Octal: 0,1,2,3,4,5,6,7
  - Binary; 0,1
  - Hexadecimal: 0,1,2,3,4,5,6,7,8,9,A,B,C,D,E,F

- To generate the rest of the numerals, the position of the symbol in the figure is used
- The symbol in the last position has its own value, and as it moves to the left its value is multiplied by  $b$
- For example, in the decimal system (base 10), the numeral 4327 means  $(4 \times 10^3) + (3 \times 10^2) + (2 \times 10^1) + (7 \times 10^0)$ , noting that  $10^0 = 1$

- In general, if  $b$  is the base, we write a number in the numeral system of base  $b$  by expressing it in the form
$$a_n b^n + a_{n-1} b^{n-1} + a_{n-2} b^{n-2} + \dots + a_0 b^0$$
and writing the enumerated digits  $a_n a_{n-1} a_{n-2} \dots a_0$  in descending order.
- The digits are natural numbers between 0 and  $b - 1$ , inclusive
- By using a dot to divide the digits into two groups, one can also write fractions in the positional system. For example, the base-2 numeral 10.11 denotes  $1 \times 2^1 + 0 \times 2^0 + 1 \times 2^{-1} + 1 \times 2^{-2} = 2.75$ .
- In general, numbers in the base  $b$  system are of the form:

$$(a_n a_{n-1} \dots a_1 a_0 . c_1 c_2 c_3 \dots)_b = \sum_{k=0}^n a_k b^k + \sum_{k=1}^{\infty} c_k b^{-k}.$$

- Binary system
  - Base = 2, Radix=2, Digits = 0 y 1 (called bits)
  - A quantity N is represented by a sequence of bits
    - Example. N = 1 0 1 1

MSB  
(Most Significant Bit)

LSB  
(Least Significant Bit)
- The decimal value represented is obtained developing the power series expansion:
  - Ejemplo.  $N = 1011_2 = 1 \times 2^3 + 0 \times 2^2 + 1 \times 2^1 + 1 \times 2^0 = 8 + 0 + 2 + 1 = 11_{10}$
  - Ejemplo.  $R = 10,11_2 = 1 \times 2^1 + 1 \times 2^{-1} + 1 \times 2^{-2} = 2 + 0,5 + 0,25 = 2,75_{10}$
- Power series expansion can be used to obtain the decimal value of any quantity represented in any numeral system.

- How to change the base of a number (decimal to binary)
  - The process is known as **Successive Division Method**
  - It can be used only with integer numbers
  - The method consists in divide the decimal quantity by the new base ( $b=2$ ). If the cocient is greater or equal than the new base it must be applied another division between the cocient and the new base.
  - When the cocient is lesser than the new base, the result is the concatenation of the cocients
  - See [http://www.frontiernet.net/~prof\\_tcarr/SuccDiv/](http://www.frontiernet.net/~prof_tcarr/SuccDiv/)
- Example: The binary representation of the decimal number  $348_{10}$  is
$$348 \div 2 = 174 \div 2 = 87 \div 2 = 43 \div 2 = 21 \div 2 = 10 \div 2 = 5 \div 2 = 2 \div 2 = 1 \text{ (MSB)}$$
$$\text{(LSB)} \quad 0 \leftarrow 0 \leftarrow 1 \leftarrow 1 \leftarrow 1 \leftarrow 0 \leftarrow 1 \leftarrow 0$$

Solution:  $348_{10} = 101011100_2$
- The **Successive Division Method** can be used to obtain the representation of a decimal number in any numeral system

- How to change the base of a number (decimal to binary)
  - Successive multiplications method
    - It is applied to decimal quantities which **only** have a fractional part
    - It consists on multiply the decimal quantity by the new base ( $b=2$ ). The resulting integer part (0 ó 1) will be one of the digits of the resulting sequence
    - If the fractional part is not zero, the fractional part must be multiplied one more time
  - Example: Obtain the equivalent base 2 sequence of the decimal quantity  $0,625_{10}$ 
    - $0,625 \times 2 = \mathbf{1},250 \rightarrow 1$  (MSB)
    - $0,250 \times 2 = 0,50 \rightarrow 0$
    - $0,50 \times 2 = 1 \rightarrow 1$  (LSB)
  - The Successive multiplications Method can be used to obtain the representation of a decimal number in any numeral system
  - It is possible that a decimal quantity, which is represented by a finite number of digits, require an infinitum number of digits when it is represented in another numeral system.

- How to obtain the representation of a decimal number  $R = e, f$  to a numeral system of base  $b$ 
  - Convert the integer part ( $e$ ) obtaining the base  $b$  digit sequence  $a_n a_{n-1} \dots a_1 a_0$
  - Convert the fractional part ( $f$ ) obtaining another base  $b$  digit sequence  $a_{-1} a_{-2} \dots a_{-p}$
  - To concat the obtained sequences to obtain the resulting base  $b$  sequence corresponding to the decimal number  
 $R = a_n a_{n-1} \dots a_1 a_0 , a_{-1} a_{-2} \dots a_{-p}$
- Example: To convert  $10,625_{10}$  to binary
  - $10_{10} = 1010_2$  y  $0,625_{10} = 0,101_2 \rightarrow 10,625_{10} = 1010,101_2$
  - It is possible to verify the result evaluating the decimal value of the binary sequence obtained:  
 $1010,101_2 = 2^3 + 2^1 + 2^{-1} + 2^{-3} = 8 + 2 + 0,5 + 0,125 = 10,625_{10}$



- Other numeral systems widely used are
  - Octal (base  $8 = 2^3$ )
    - Each octal digit represents a set of 3 binary digits
    - Octal digits: 0, 1, 2, 3, 4, 5, 6, 7
  - Hexadecimal (base  $16 = 2^4$ )
    - Each hexadecimal digit represents a set of 4 binary digits
    - Hexadecimal Digits: 0, 1, 2, 3, 4, 5, 6, 7, 8, 9, A ( $=10_{10}$ ), B ( $=11_{10}$ ), C ( $=12_{10}$ ), D ( $=13_{10}$ ), E ( $=14_{10}$ ), F ( $=15_{10}$ )
- Their use is widely extended because:
  - The facility to convert to and from binary
  - They allow to represent long sequences of binary digits in a compact way

- Change of binary, octal or hexadecimal base
  - Taking into account that octal and hexadecimal bases are multiples of base 2 it can be shown that:
    - In octal (base  $2^3$ ) a digit represents a set of 3 bits
    - In hexadecimal (base  $2^4$ ) a digit represents a set of 4 bits
    - In both cases, the change from one representation to other one is made using a table, groping bits in blocs of 3 or 4 bits

Octal	Binario
0	000
1	001
2	010
3	011
4	100
5	101
6	110
7	111

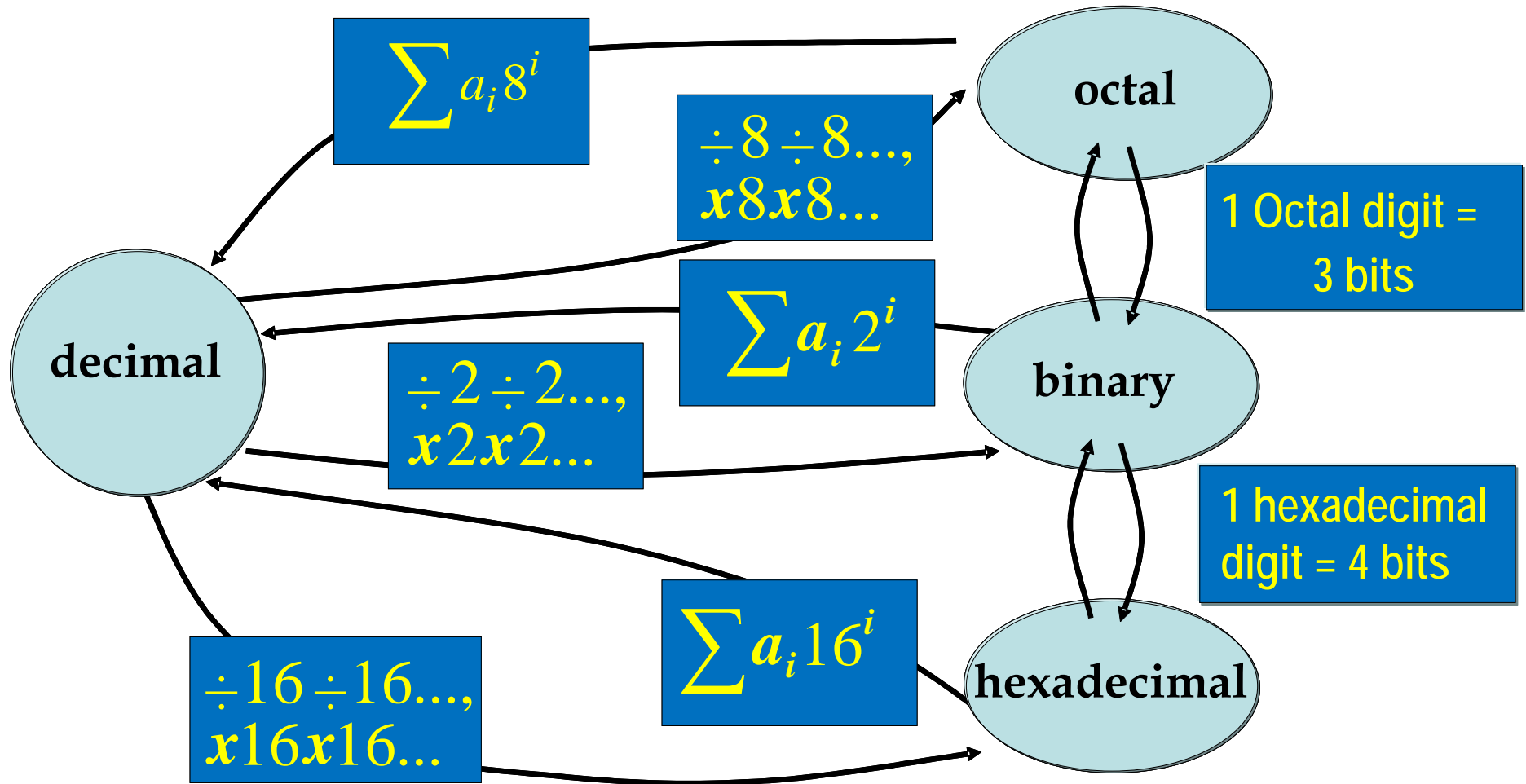
Hexadecimal	Binario
0	0000
1	0001
2	0010
3	0011
4	0100
5	0101
6	0110
7	0111

Hex.	Binario
8	1000
9	1001
A	1010
B	1011
C	1100
D	1101
E	1110
F	1111

- Change to/from binary from/to octal and hexadecimal
  - When the group of 3/4 bits it is not full it is fulfilled with zeros
    - Zeros to the left if the bits belong to the integer part
    - Zeros to the right if the bits belongs to the fractional part
  - A bit group never must contain the decimal point
    - The bits belonging to the integer part never must be combined with bits belonging to the fractional part
    - The bit grouping must be started from the decimal point

*Stuffing bit*

$$111000011011,10000001_2 = 111\ 000\ 011\ 011\ ,\ 100\ 000\ 010_2 = 7033,402_8$$
$$111000011011,10000001_2 = 1110\ 0001\ 1011\ ,\ 1000\ 0001_2 = E1B,81_{16}$$



- BCD (Binary Coded Decimal)
  - Simple Method to code decimal values using binary digits
  - There are used 4 bits (called D, C, B y A) to code a decimal digit
  - Each decimal digit is coded separately using a table

Decimal Digit	BCD digit			
	D	C	B	A
0	0	0	0	0
1	0	0	0	1
2	0	0	1	0
3	0	0	1	1
4	0	1	0	0
5	0	1	0	1
6	0	1	1	0
7	0	1	1	1
8	1	0	0	0
9	1	0	0	1

- Example: Code  $348_{10}$  en BCD  
 $3_{10} = 0011_{\text{BCD}}$ ,  $4_{10} = 0100_{\text{BCD}}$ ,  $8_{10} = 1000_{\text{BCD}}$   
 $348_{10} = 001101001000_{\text{BCD}}$
- Example: What decimal value represents  $00101001_{\text{BCD}}$ ?  
 $0010_{\text{BCD}} = 2_{10}$ ,  $1001_{\text{BCD}} = 9_{10}$   
 $00101001_{\text{BCD}} = 29_{10}$

- Character representation
  - Characters are:
    - Letters (“a”, ..., “z”, “A”, ..., “Z”)
    - Digits (“0”, ..., “9”)
    - Punctuation symbols (“.”, “,”, “;”, ...)
    - Special symbols (“\*”, “&”, “\$”, ...)
- To represent characters it is used a code for each character. A table is used to relate codes and characters
- The computer always works with the codes, never with the symbols
- The characteristics of a representation are:
  - Length of the codes in bits
  - Number of different characters that can be represented
  - The relationship between a code and a character is made by means of a table

- E.B.C.D.I.C. (Extended Binary Coded Decimal Interchange Code)
  - Created in 1964 to be used by the system IBM S360
  - Fixed length of 8 bits
  - *A few mainframe systems use that code*
- A.S.C.I.I. (American Standard Code for Information Interchange)
  - Fixed length for every one of the codes
  - ASCII. Code length of 7 bits
  - Extended ASCII. International characters implementation. Fixed length of 8 bits. Different implementations: ISO-8859-15, CP850 ...
- U.T.F. (Unicode Transformation Format)
  - Implementations: UTF-8, UTF-16, UTF-32, UTF-8 is the most used
  - In UTF-8 the number of bytes needed to represent a character that is variable. However, to represent any ascii character it is needed only one byte

- ASCII Table (7 bits)

	0	16	32	48	64	80	96	112
+0	<i>NUL</i>	<i>DLE</i>	<i>SP</i>	0	@	P	`	p
+1	<i>SOH</i>	<i>DC1</i>	!	1	A	Q	a	q
+2	<i>STX</i>	<i>DC2</i>	"	2	B	R	b	r
+3	<i>ETX</i>	<i>DC3</i>	#	3	C	S	c	s
+4	<i>EOT</i>	<i>DC4</i>	\$	4	D	T	d	t
+5	<i>ENQ</i>	<i>NAK</i>	%	5	E	U	e	u
+6	<i>ACK</i>	<i>SYN</i>	&	6	F	V	f	v
+7	<i>BEL</i>	<i>ETB</i>	'	7	G	W	g	w
+8	<i>BS</i>	<i>CAN</i>	(	8	H	X	h	x
+9	<i>HT</i>	<i>EM</i>	)	9	I	Y	i	y
+10	<i>LF</i>	<i>SUB</i>	*	:	J	Z	j	z
+11	<i>VT</i>	<i>ESC</i>	+	;	K	[	k	{
+12	<i>FF</i>	<i>FS</i>	,	<	L	\	l	
+13	<i>CR</i>	<i>GS</i>	-	=	M	]	m	}
+14	<i>S0</i>	<i>RS</i>	.	>	N	^	n	~
+15	<i>S1</i>	<i>US</i>	/	?	O	_	o	<i>DEL</i>

The ASCII code  
of "z" is  
 $112 + 10 = 122$



- Word length

- The word length is the number of bits used by the basic data unit of the computer. There are computers of 8, 16, 32, 64 bits, etc.
- Computers support other word lengths.
  - Example: The MIPS R2000 can work with bytes (8 bits) or with real numbers coded with 64 bits

- Memory capacity

- Normally the memory capacity is expressed in bytes. Sometimes, there are used bits
- Prefixes
  - Depending on the context it can be used binary ( $2^n$ ) or metric ( $10^n$ ).  
For instance, the main memory capacity always is expressed using binary prefixes.
  - On the other hand, Peripherals capacity (as hard drives) uses metric prefixes

Prefijo	$2^n$	$10^n$
Kilo (K)	$2^{10}$	$10^3$
Mega (M)	$2^{20}$	$10^6$
Giga (G)	$2^{30}$	$10^9$
Tera (T)	$2^{40}$	$10^{12}$
Peta (P)	$2^{50}$	$10^{15}$



UNIVERSIDAD  
POLITECNICA  
DE VALENCIA



---

# Computers Fundamentals

---

Subject 1. Introduction to computers

---

---