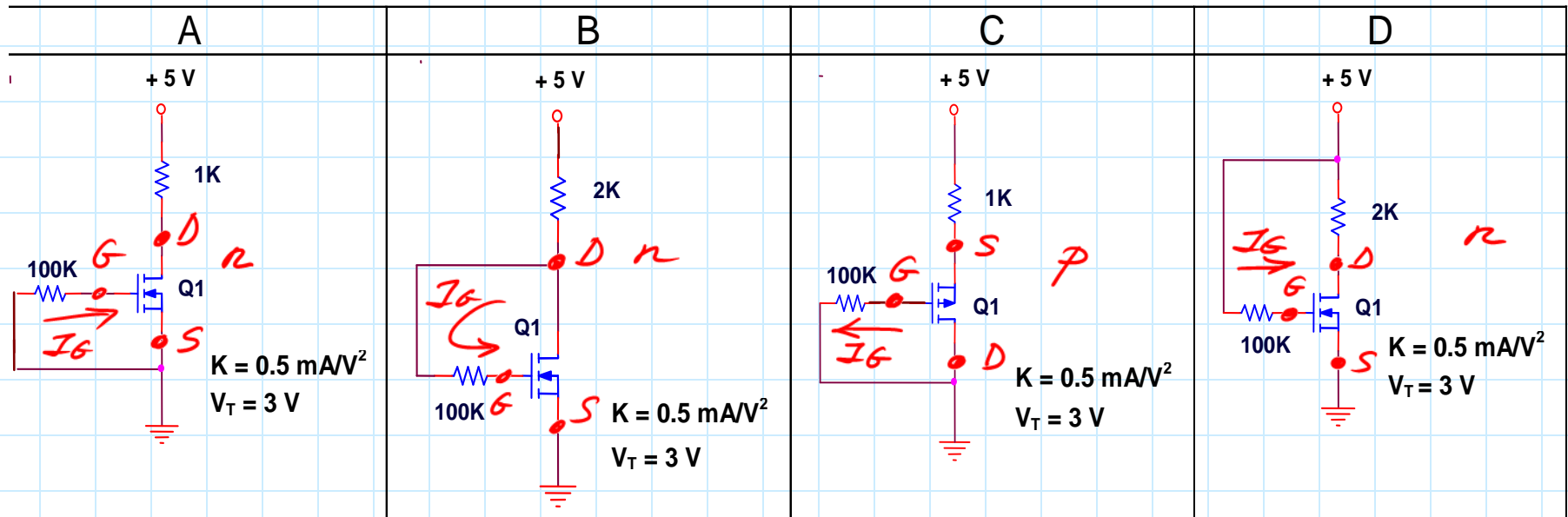


UNIT 2. MOSFETS: OPERATING REGIONS

2.1 Indicate the operating region of the MOSFET transistors of the following circuits:



$I_G = 0$ in all cases

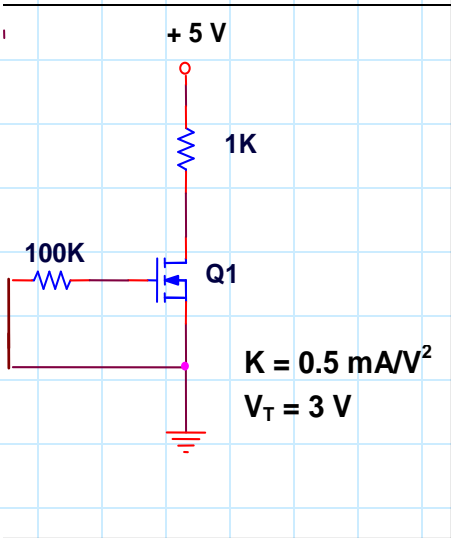
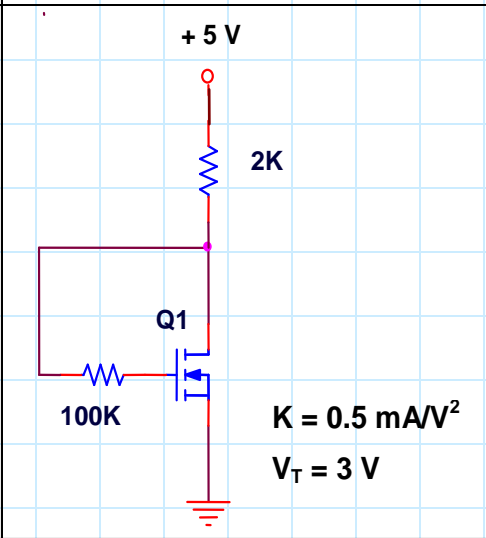
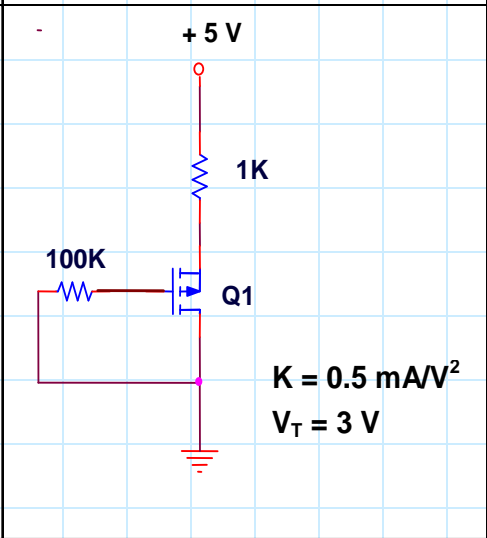
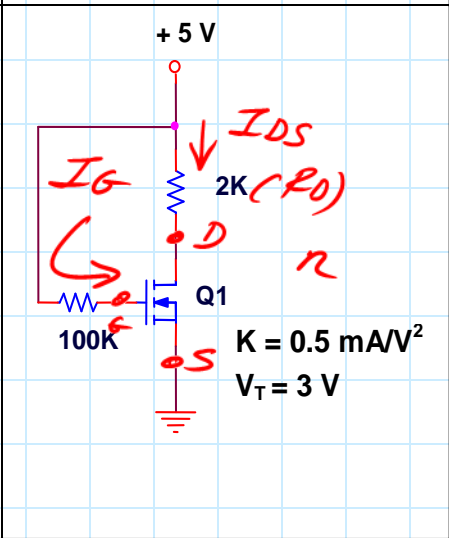
A) $V_G = 0 \text{ V}$; $V_{GS} = 0 \text{ V} < V_T \Rightarrow Q_1$ OFF (cut-off region)

B) $I_G = 0 \Rightarrow V_D = V_G \Rightarrow V_{DS} = V_{GS} \Rightarrow V_{DS} > V_{GS} - V_T = V_{DS} - V_T \Rightarrow Q_1$ saturated

C) $I_G = 0 \Rightarrow V_D = V_G \Rightarrow V_{DS} = V_{GS} \Rightarrow V_{DS} < V_{GS} + V_T = V_{DS} + V_T \Rightarrow Q_1$ saturated

UNIT 2. MOSFETS: OPERATING REGIONS

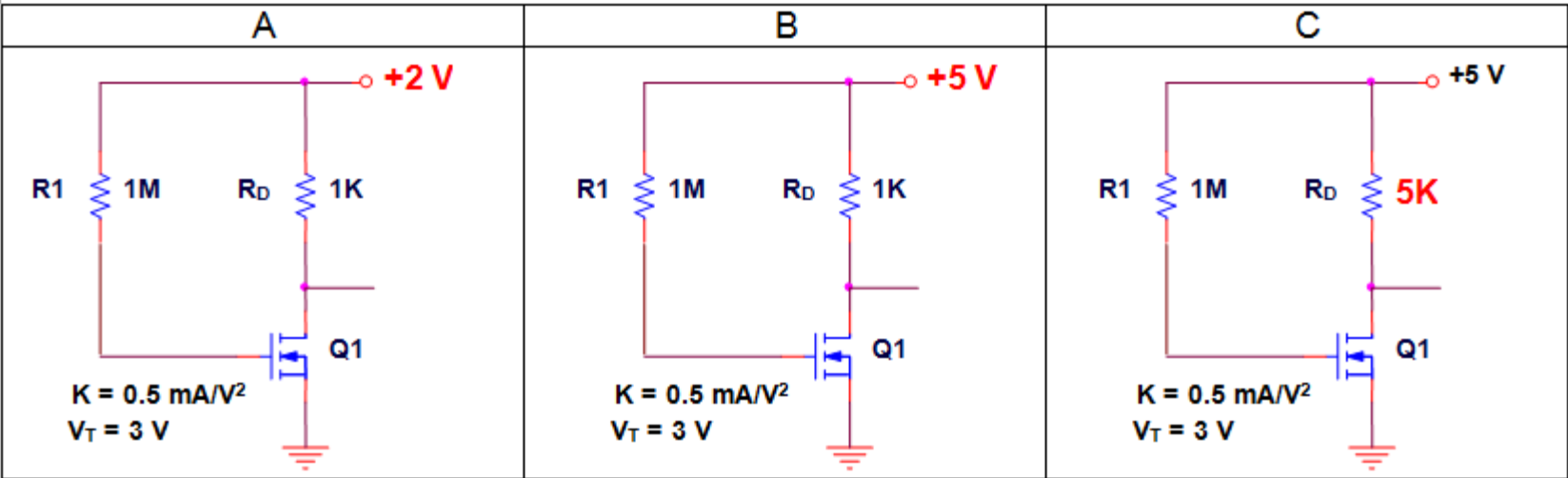
2.1 Indicate the operating region of the MOSFET transistors of the following circuits (cont.):

A	B	C	D
 <p> $+5\text{ V}$ 1 K 100 K $Q1$ $K = 0.5\text{ mA/V}^2$ $V_T = 3\text{ V}$ </p>	 <p> $+5\text{ V}$ 2 K 100 K $Q1$ $K = 0.5\text{ mA/V}^2$ $V_T = 3\text{ V}$ </p>	 <p> $+5\text{ V}$ 1 K 100 K $Q1$ $K = 0.5\text{ mA/V}^2$ $V_T = 3\text{ V}$ </p>	 <p> $+5\text{ V}$ $2\text{ K (}R_D\text{)}$ 100 K $Q1$ $K = 0.5\text{ mA/V}^2$ $V_T = 3\text{ V}$ </p>

(D) $I_G = 0 \Rightarrow V_{GS} = V_G = 5\text{ V} > V_T \Rightarrow Q1 \text{ ON ; assume saturated}$
 $\Rightarrow I_{DS} = K (V_{GS} - V_T)^2 = 0.5(5-3)^2 = 2\text{ mA} \Rightarrow$
 output loop: $5 + I_{DS} R_D + V_{DS} = 0 \Rightarrow V_{DS} = 5 - R_D I_{DS} = 1\text{ V}$
 as $V_{DS} \neq V_{GS} - V_T = 5 - 3 = 2\text{ V} \Rightarrow Q1 \text{ is in } \underline{\text{OHMIC REGION}}$

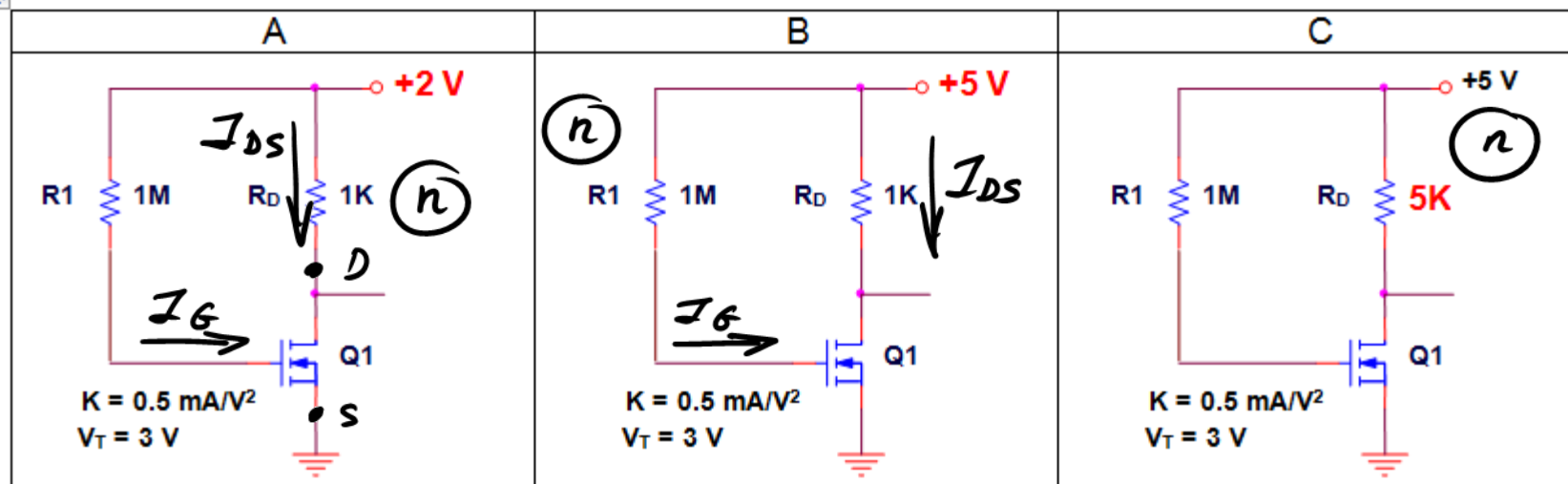
UNIT 2. MOSFETS: OPERATING REGIONS

2.2 Indicate the operating region of the MOSFET transistors of the following circuits:



UNIT 2. MOSFETS: OPERATING REGIONS

2.2 Indicate the operating region of the MOSFET transistors of the following circuits:



A) $I_G = 0 \Rightarrow V_{GS} = 2 \text{ V} < V_T \Rightarrow Q_1 \text{ OFF} \Rightarrow$

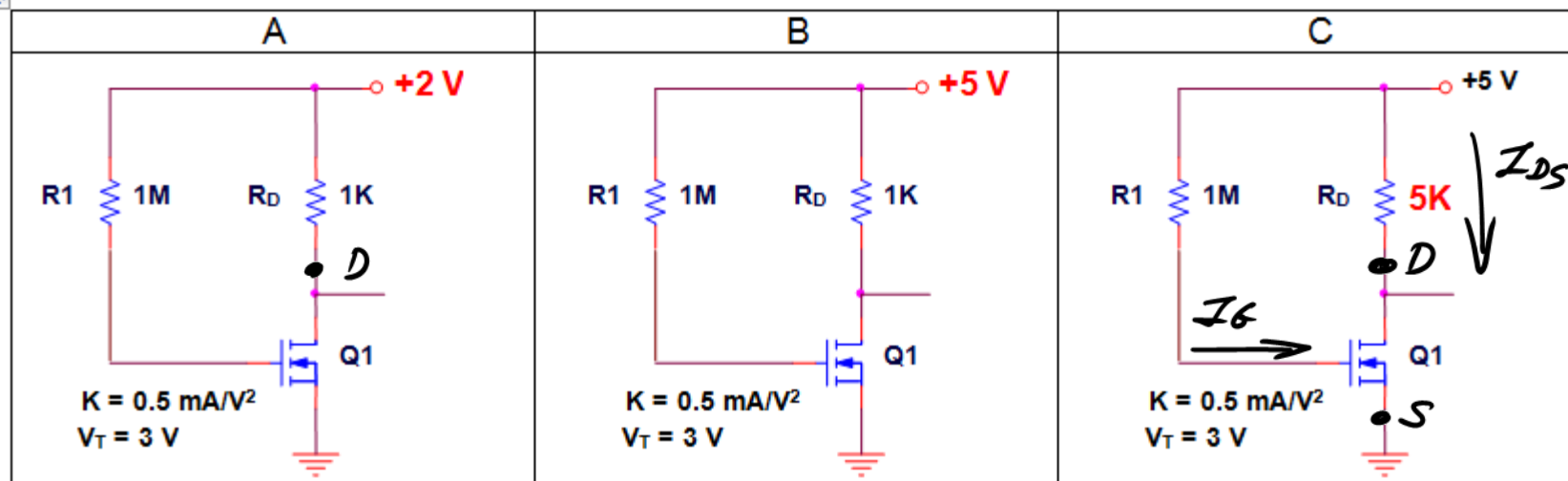
B) $I_G = 0 \Rightarrow V_{GS} = 5 \text{ V} > V_T \Rightarrow Q_1 \text{ ON}; \text{ Assume SAT} \Rightarrow$

$$I_{DS} = K(V_{GS} - V_T)^2 = 0.5(5 - 3)^2 = 2 \text{ mA}$$

$$V_{DS} = 5 - I_{DS} R_D = 5 - 2 \cdot 1 = 3 \text{ V} > V_{GS} - V_T = 2 \text{ V} \Rightarrow \text{SATURATED}$$

UNIT 2. MOSFETS: OPERATING REGIONS

2.2 Indicate the operating region of the MOSFET transistors of the following circuits:



C) $V_{GS} = 5 \text{ V} > V_T \Rightarrow Q_1 \text{ ON ; assume SAT}$

$$I_{DS} = K(V_{GS} - V_T)^2 = 0.5(5 - 3)^2 = 2 \text{ mA}$$

$$V_{DS} = 5 - I_{DS} \cdot R_D = 5 - 10 = -5 \text{ V} \Rightarrow \text{OHMIC REGION}$$

Then $I_{DS} = K[2(V_{GS} - V_T)V_{DS} - V_{DS}^2] = 0.5[4V_{DS} - V_{DS}^2]$
and from output loop:

$$I_{DS} = \frac{5 - V_{DS}}{5 \text{ K}} \text{ , Combining both equations:}$$

$$0.5(4V_{DS} - V_{DS}^2) = \frac{5 - V_{DS}}{5 \text{ K}}$$

$$0.5(4V_{DS} - V_{DS}^2) = \frac{5 - V_{DS}}{5K}; \quad 2.5(4V_{DS} - V_{DS}^2) = 5 - V_{DS}$$

$$10V_{DS} - 2.5V_{DS}^2 = 5 - V_{DS}; \quad 2.5V_{DS}^2 - 11V_{DS} + 5 = 0$$

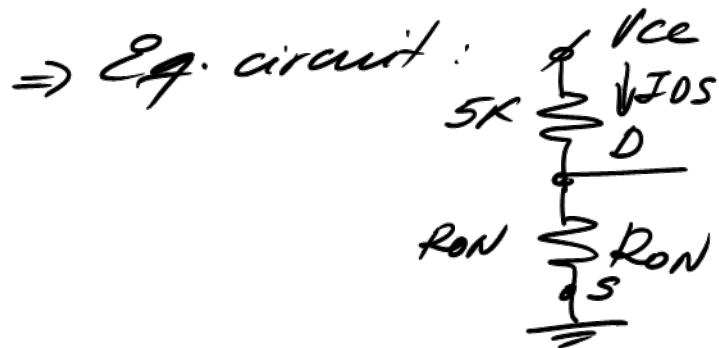
$$V_{DS} = \frac{11 \pm \sqrt{121 - 50}}{5} = \frac{11 \pm 8.426}{5} = \begin{cases} V_{DS} = 3.89 \times \\ \underline{\underline{V_{DS} = 0.51 \text{ V}}} \end{cases} \checkmark, \text{ as}$$

$$V_{DS} < V_{GS} - V_T = 2V$$

$$I_{DS} = \frac{5 - V_{DS}}{5K} = \underline{\underline{0.898 \text{ mA}}} \Rightarrow \underline{\underline{Q = (V_{GS} = 5V, V_{DS} = 0.51V, I_{DS} = 0.898 \text{ mA})}}$$

Approximate solution.

$$R_{ON} = \frac{1}{2K(V_{GS} - V_T)} = \frac{1}{2 \cdot 0.5(5 - 3)} = 0.5K$$



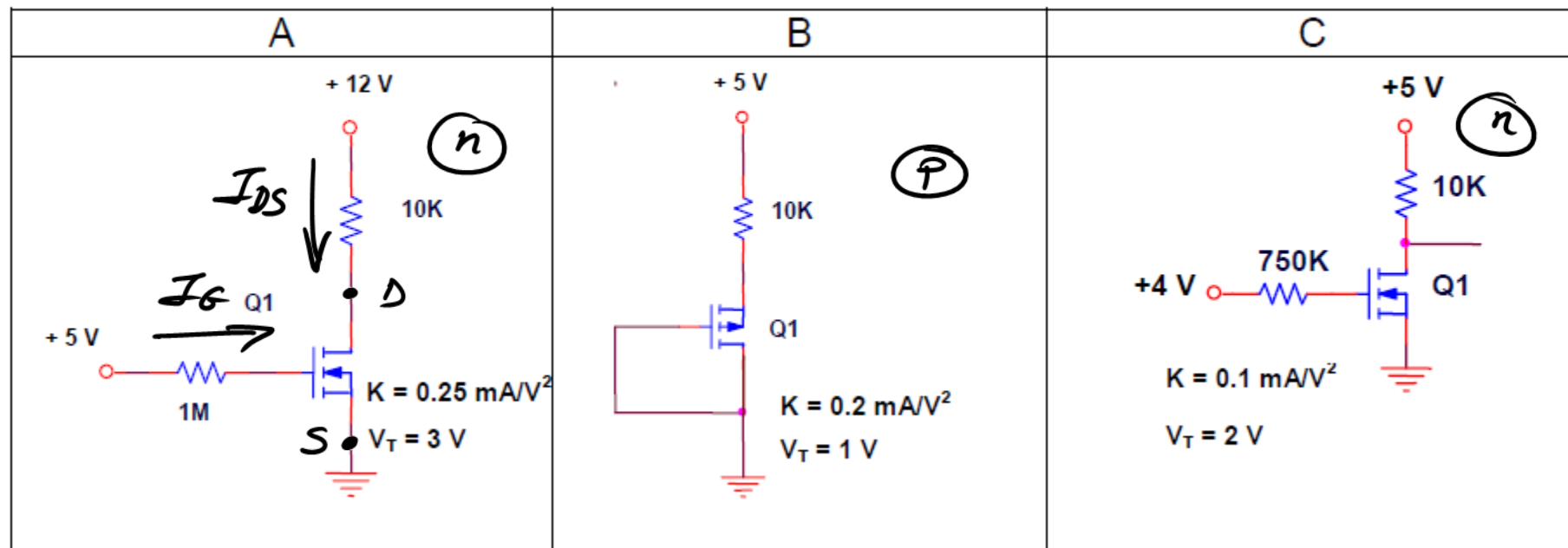
$$V_D = V_{DS} = V_{CE} \frac{R_{ON}}{5 + R_{ON}} = 5 \frac{0.5}{5.5} = \underline{\underline{0.45V}}$$

(Quite good approx)

$$I_{DS} = \frac{V_{CE}}{5 + R_{ON}} = \frac{V_{CE}}{5.5} = \underline{\underline{0.91 \text{ mA}}}$$

UNIT 2. MOSFETS: OPERATING REGIONS

(3.1) Analyze the operating point Q (V_{GS} , I_{DS} , V_{DS}) of the MOSFETs of the following circuits:



[A] $I_G = 0 \Rightarrow V_G = 5V = V_{GS} > V_T \Rightarrow T_{ON}$; assume SAT

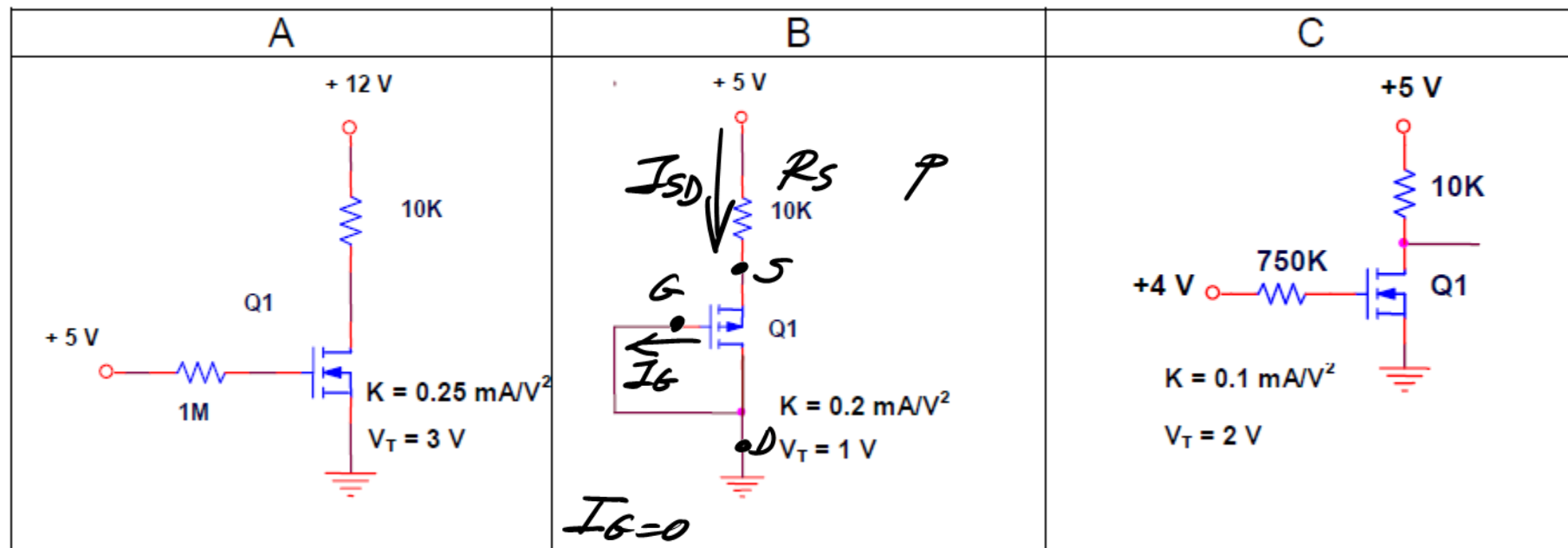
$$I_{DS} = K(V_{GS} - V_T)^2 = 0.25(5 - 3)^2 = 1 \text{ mA}$$

$$V_{DS} = 12 - 10 I_{DS} = 2V = V_{GS} - V_T \Rightarrow \text{limit OHMIC-SAT}$$

$$Q(V_{GS} = 5V; I_{DS} = 1 \text{ mA}; V_{DS} = 2V)$$

UNIT 2. MOSFETS: OPERATING REGIONS

(3.1) Analyze the operating point Q (V_{GS} , I_{DS} , V_{DS}) of the MOSFETs of the following circuits:



[B] $V_G = V_D \Rightarrow V_{GS} = V_{DS} \Rightarrow V_{DS} < V_{DS} + V_T = V_{GS} - V_T \Rightarrow Q1 \text{ SAT}$

a) $I_{SD} = K(V_{GS} + V_T)^2 = 0.2(V_{GS} + 1)^2 = 0.2(V_{DS} + 1)^2 \quad (1)$

b) Output loop: $5 - I_{SD}R_S - V_{SD} = 0 \Rightarrow I_{SD} = \frac{5 - V_{SD}}{R_S}$

$I_{SD} = \frac{5 + V_{DS}}{R_S} \quad (2); \text{ Combining (1) and (2)}$

$0.2(V_{DS}^2 + 2V_{DS} + 1) = \frac{5 + V_{DS}}{10}$

$\Rightarrow (V_{DS}^2 + 2V_{DS} + 1) = 5 + V_{DS}$

$$2V_{DS}^2 + 3V_{DS} - 3 = 0 \Rightarrow V_{DS} = \frac{-3 \pm \sqrt{9 + 24}}{4}$$

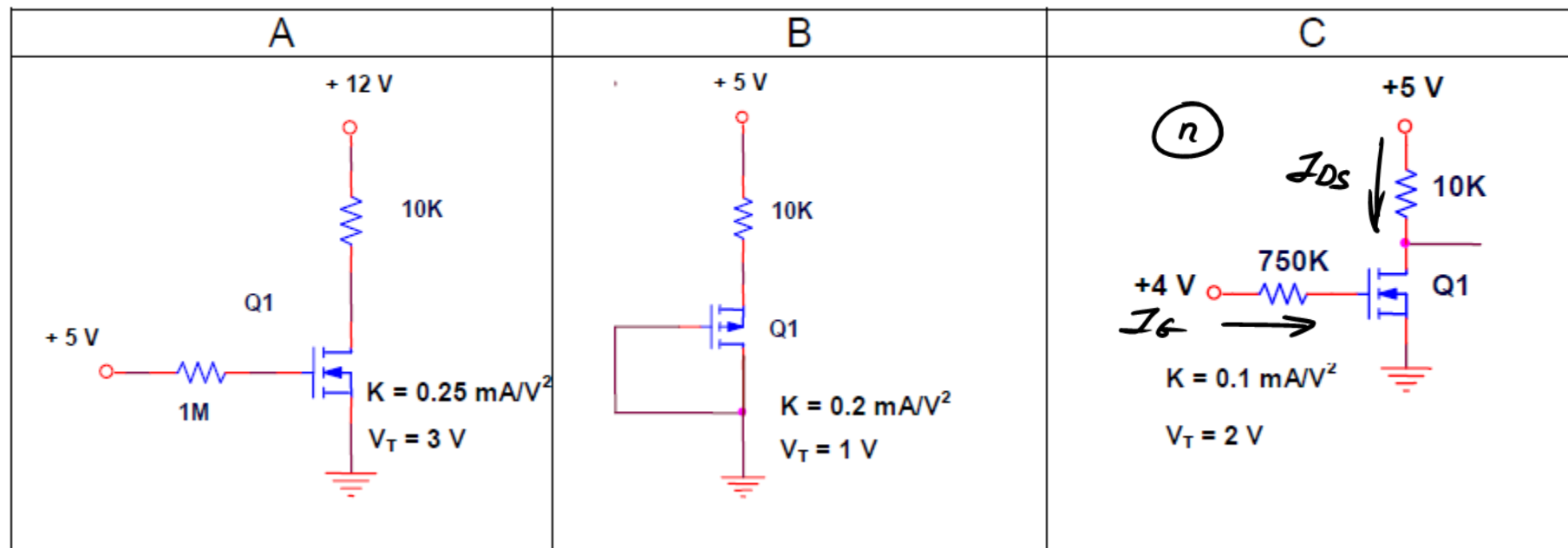
$$V_{DS} = -\frac{3 \pm}{4} \begin{cases} \nearrow 0.69 \times \\ \searrow -2.19V < -V_T \Rightarrow \text{Correct} \end{cases}$$

$$I_{SD} = \frac{5 + V_{DS}}{10} = 0.281 \text{ mA}$$

$$Q(V_{GS} = -2.19V, I_{SD} = 0.281 \text{ mA}, V_{DS} = -2.19V)$$

UNIT 2. MOSFETS: OPERATING REGIONS

(3.1) Analyze the operating point Q (V_{GS} , I_{DS} , V_{DS}) of the MOSFETs of the following circuits:



CC) $V_{GS} = 4V > V_T \Rightarrow Q1 \text{ ON. ASSUME SAT.}$

$$I_{DS} = K (V_{GS} - V_T)^2 = 0.1 (4 - 2)^2 = 0.4 \text{ mA}$$

$V_{DS} = 5 - 10 I_{DS} = 1V \neq V_{GS} - V_T \Rightarrow \text{OHMIC REGION}$

$$I_{DS} = K [2(V_{GS} - V_T)V_{DS} - V_{DS}^2] = 0.1 [2(4 - 2)V_{DS} - V_{DS}^2]$$

$$I_{DS} = 0.4V_{DS} - 0.1V_{DS}^2 \quad (1)$$

From output loop:

$$I_{DS} = \frac{5 - V_{DS}}{10} \quad (2)$$

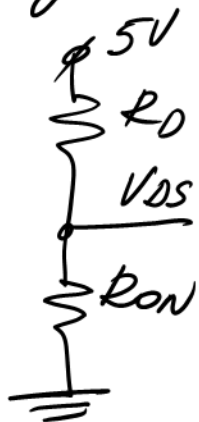
$$\left. \begin{array}{l} (1) \\ (2) \end{array} \right\} 0.4V_{DS} - 0.1V_{DS}^2 = \frac{5 - V_{DS}}{10}$$

$$4V_{DS} - V_{DS}^2 = 5 - V_{DS}; \quad V_{DS}^2 - 5V_{DS} + 5 = 0$$

$$V_{DS} = \frac{5 \pm \sqrt{25 - 20}}{2} = \frac{5 \pm 2.24}{2} = \begin{cases} 3.62 \text{ V} \times \\ 1.38 \text{ V} (V_{DS} < V_{GS} - V_T) \end{cases}$$

$$\text{Then } V_{DS} = 1.38 \text{ V} \Rightarrow \left. \begin{aligned} I_{DS} &= \frac{5 - 1.38}{10} = 0.362 \text{ mA} \end{aligned} \right\} Q(V_{GS} = 4 \text{ V}, I_{DS} = 0.362 \text{ mA}, V_{DS} = 1.38 \text{ V})$$

Assuming linear region: $R_{ON} = \frac{1}{2K(V_{GS} - V_T)} = \frac{1}{2 \cdot 0.1(4 - 2)} = 2.5 \text{ k}\Omega$



$$V_{DS} = 5 \frac{R_{ON}}{R_D + R_{ON}} = 5 \frac{2.5}{10 + 2.5} = 1 \text{ V}$$

$$I_{DS} = \frac{5}{R_D + R_{ON}} = 0.4 \text{ mA}$$

(Note the error in approximation, because $V_{DS} \uparrow$ and we can't neglect V_{DS}^2).