



UNIVERSIDAD  
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# Computers Fundamentals

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Subject 4. Sequential circuits

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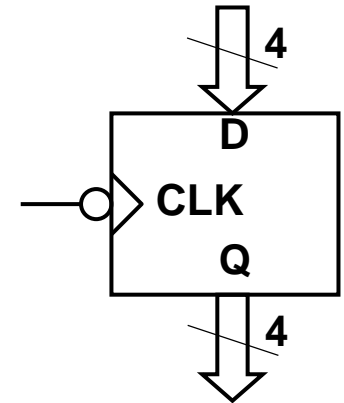
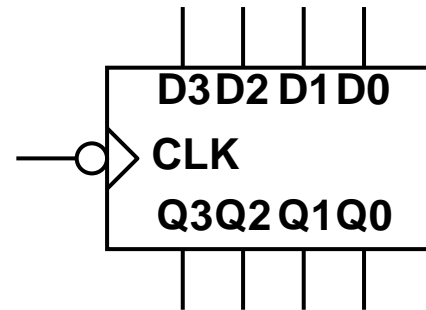
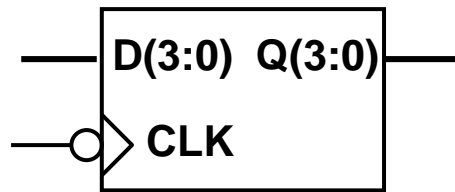
- Introduction to sequential systems (SS)
  - Classification of Sequential systems
    - **Asynchronous** sequential systems (SSA)
    - **Synchronous** sequential systems (SSS)
- Basic sequential systems
  - Storage register
  - Registers bank, Memory
  - Shift registers
  - Counters

- The most useful sequential circuits are:
  - Storage registers
    - They can store  $N$  bits of data
  - Register bank
    - Set of storage registers
  - Memory
    - Its functioning is similar to a register bank.
    - Main differences: capacity (number of storage registers, speed, design)

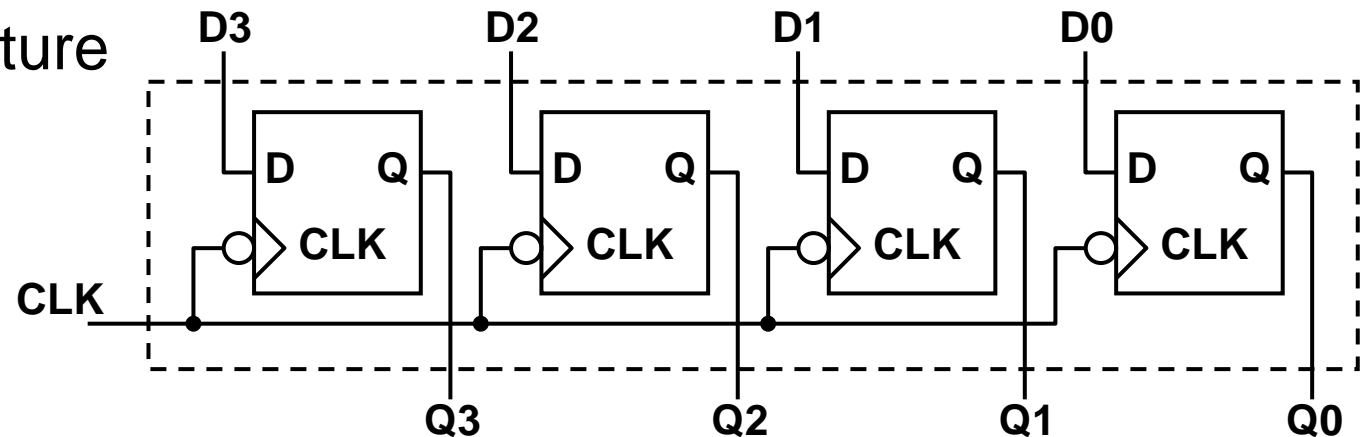
- More useful sequential circuits are:
  - Shift register
    - It stores N bits.
    - It can *shift* data to the left or to the right
  - Counter
    - The circuit changes the output value every active edge of the clock signal.
    - The output values are a sequence of predefined values
      - In general the count is binary (up-count or down-count)

- Set of D flip-flops
  - The number of D flip-flops is given by the number of bits that we want to store
    - The D flip-flop can store one bit
  - The inputs and outputs of the register are the same as the inputs and outputs of the D flip-flops
  - The input clock of all the D flip-flops is connected to the same signal. The signal is named clock
    - All the d flip-flops are identical. They are triggered by the same edge of the clock signal..

- Example: 4-bit storage register falling-edge triggered.
  - Equivalent logic symbols



- Internal structure

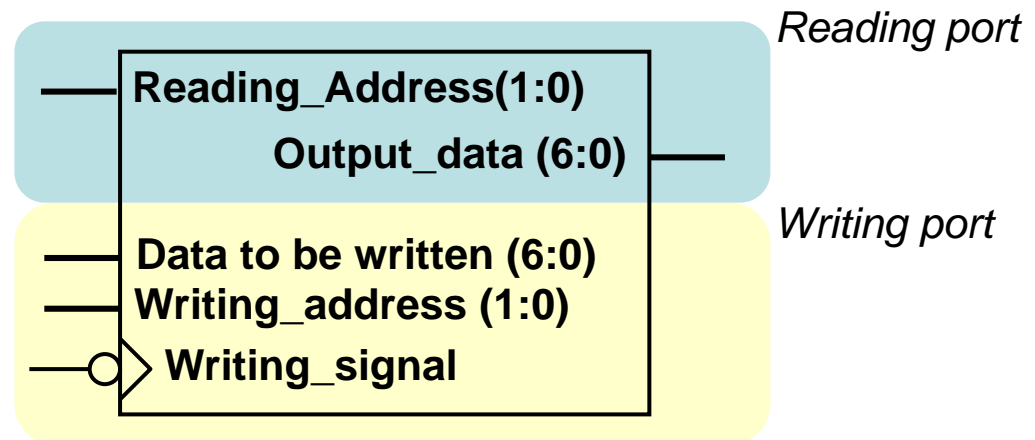


- Writing operation
  - Destructive operation
    - The data stored into the register is updated with the new data at the inputs of the register. The writing is done with the clock edge.
  - How writing operation is performed:
    - 1) Set the input-value of each D flip-flop.
    - 2) Change clock signal in order to obtain an edge
- Reading operation
  - Non destructive operation
    - The data stored into the register is not affected
  - How reading-operation is performed
    - Examining the outputs of the D Flip-flops

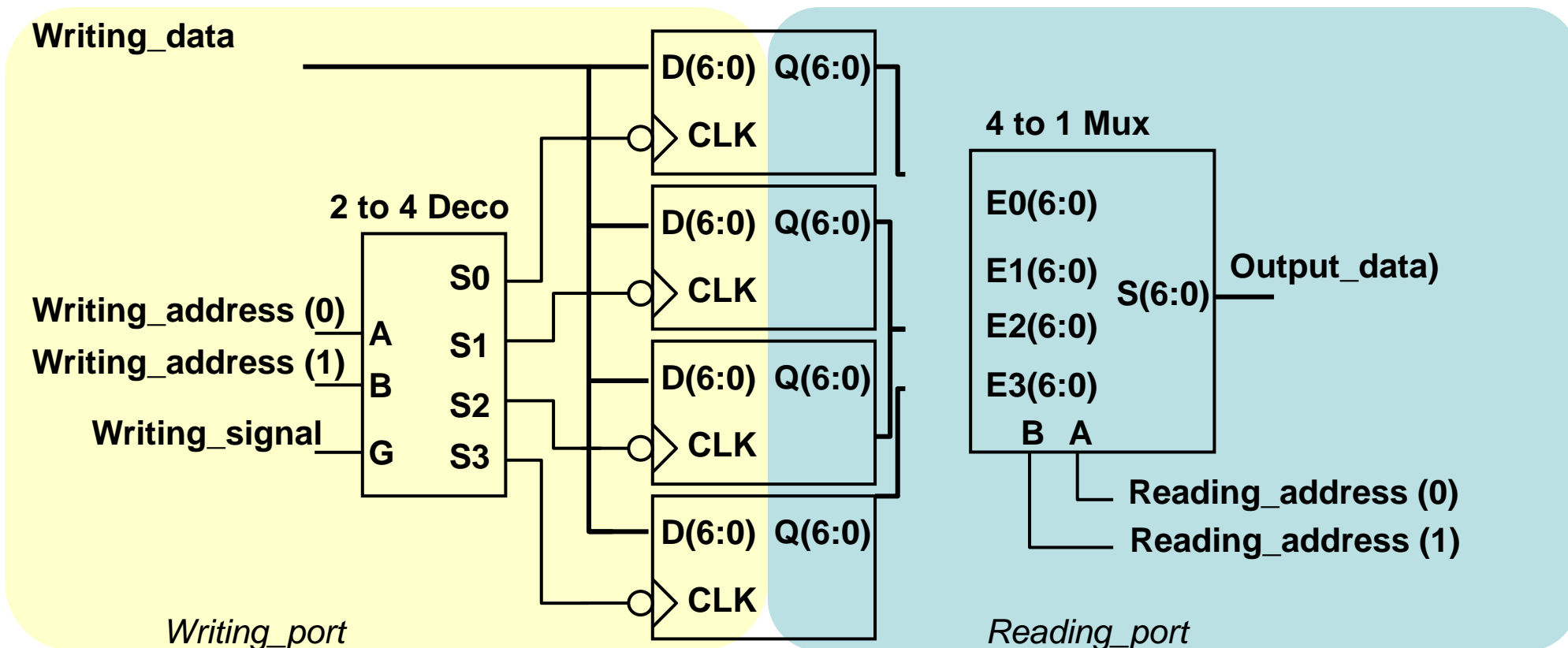
- Set of registers which allow us to:
  - Write data into one register
    - It is mandatory to select what register we want to write
      - **Writing address**
  - Read the data stored in a register
    - It is mandatory to select what register we want to read
      - **Reading address**
    - We will design a register bank which accepts ***two reading address*** in order to obtain (at the same time) the value of two registers in the data outputs



- **Example:** Register bank of 4 registers. Each register can store 7 bits. The register bank has reading address bus and one writing address bus. The reading and the writing bus are composed by 2 bits each one.
  - 4 Registers => 2 bits used to select the 4 different address
  - Input/Output data. 7 bits each signal
  - Logic symbol



- Example(cont):
  - Internal structure



- Writing operation
  - Steps
    - 1) Set the data that will be written into the register
    - 2) Set the writing address
    - 3) Modify the writing\_signal to obtain an edge
      - Enabling and disabling the decoder
- Reading operation
  - Steps
    - 1) Set the reading address
    - 2) Examining the value of the output\_value bus

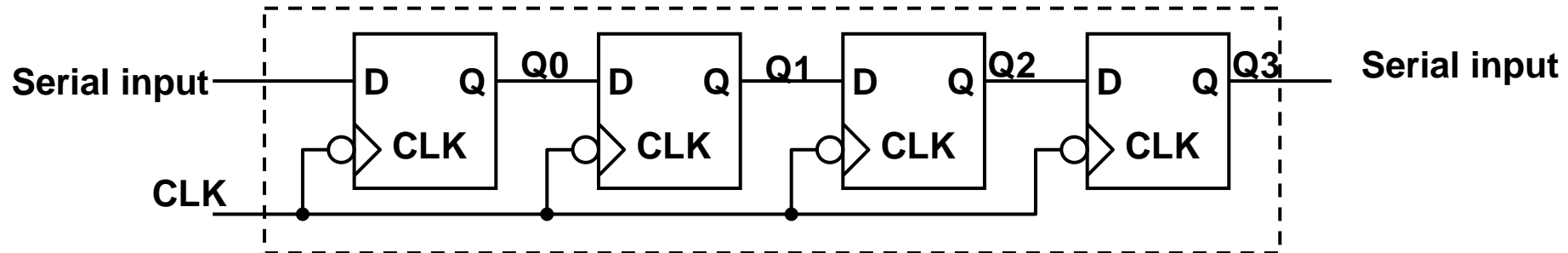
- Its functionality is like the functionality of a *register bank* with the following differences:
  - Much more capacity (Kbytes, Mbytes, Gbytes, ...)
  - Much more slower
  - The technologies used in their implementations is different
- At any time only can be performed one operation (reading or writing)
  - It has one input-address bus and one input-data bus
  - Allowed operations: reading, writing or none

- Set of D flip-flops
  - It is mandatory to have as many D flip-flops as bits to store
  - Several clock-cycles are necessary to insert or **pull-out** data
    - In this case it is said that the shift register has one serial input and one serial output
    - When all the input data bits are inserted or are pulled-out using only one clock cycle, it is said that the shift-register has parallel-input and parallel-output
  - Structure with serial-input
    - The first flip-flop input is connected with the input data
    - The rest of the flip-flops connects their input with the output of the preceding flip-flop
  - Structure with serial output
    - There is only one output and is the output of the last flip-flop

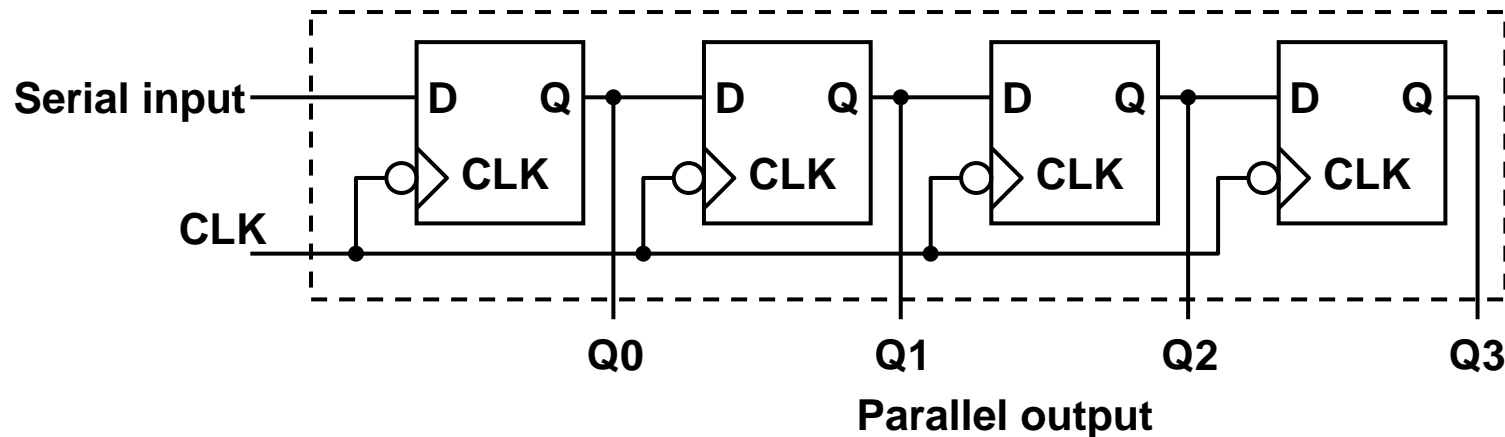
- Is a cascade of flip flops, sharing the same clock, which has the output of any one but the last flip-flop connected to the "data" input of the next one in the chain
- The shift register circuit shifts by one position the one-dimensional "bit array" stored in it, *shifting in* the data present at its input and *shifting out* the last bit in the array, when enabled to do so by a transition of the clock input.

- Shift registers can have both parallel and serial inputs and outputs.
  - These are often configured as **serial-in, parallel-out** (SIPO) or as **parallel-in, serial-out** (PISO).
- There are also types that have both serial and parallel input and types with serial and parallel output.
- There are also **bi-directional** shift registers which allow shifting in both directions:  $L \rightarrow R$  or  $R \rightarrow L$ . The serial input and last output of a shift register can also be connected together to create a **circular shift register**.

- Serial input, serial output (SISO) shift register:



- Serial input, parallel output (SIPO) shift Register

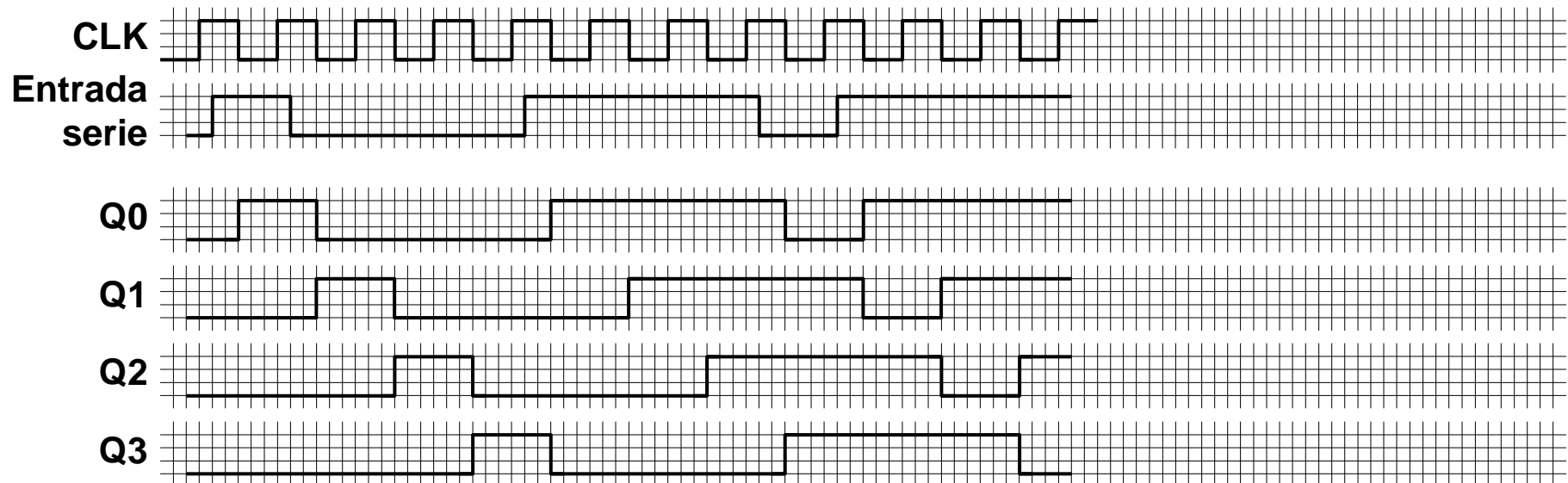




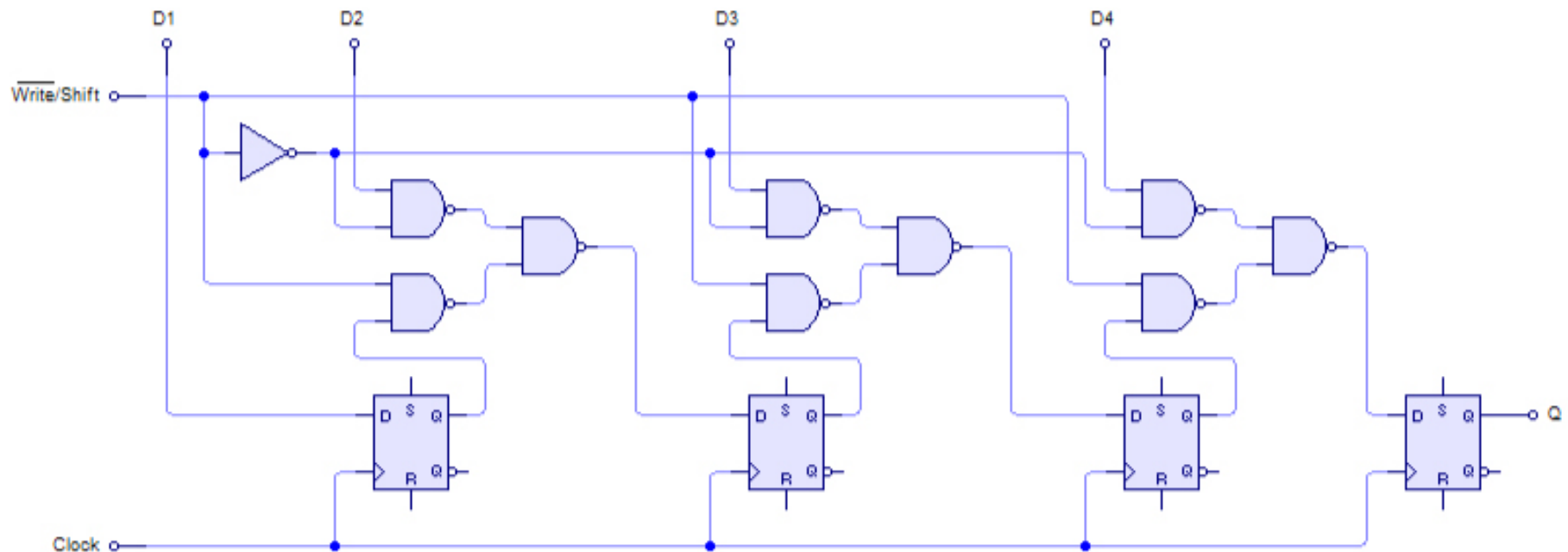
- SIPO Shift Register

- Example

- Initial state  $Q_3Q_2Q_1Q_0 = 0000$
    - The serial-input takes the values indicated in the timing diagram



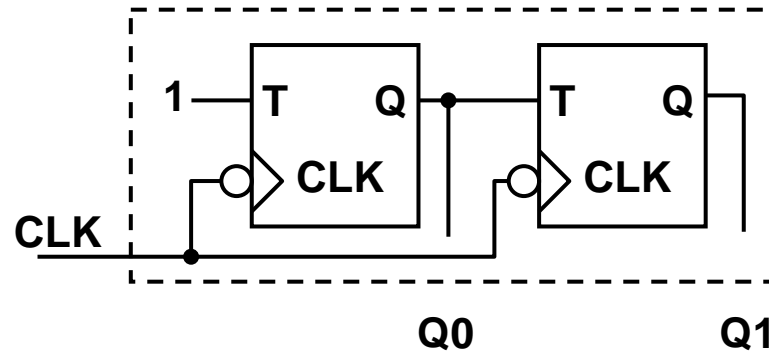
- Parallel Input/serial output



- Can shift data to the left or can shift data to the right
  - There is no unanimity in how to define what means ***shift to the left*** or ***shift to the right***. The direction must be defined explicitly
- Can shift in both directions
  - Not at the same time
  - A direction-input is added plus two serial-inputs used to put the bit that will be shifted to the left and the bit which will be shifted to the right
- Data can be inserted into the shift-register in two ways:
  - Serial (In each clock-cycle only one bit can be shifted into the register)
  - Parallel (all the data bits can be inserted in just one clock-cycle)
- The output can be pulled-out of the shift register in two ways:
  - Serial (One bit can be read from the output, each clock cycle the output changes)
  - Parallel (the whole data stored in the register can be read )

- Digital circuit whose output changes with each active edge of the clock.
- The output is a binary sequence that in decimal is a count.
- The count can be only up count or only down count
- The count can be up count or down count
  - A control-input is added to control if the count must be up count or down count
  - Never can be up count and down count at the same time!

- T flip-flops are used
  - Synchronous circuits do not generate glitches
  - Example: 2 bits synchronous up-counter
    - Output count:  $00_2, 01_2, 10_2, 11_2$



- Classification

- Binary counter

- Generates all the possible binary sequences using N bits.

- N-module counters

- Generates N different output binary sequences, where  $N < 2^{\text{number of flip-flops}-1}$

- Normally the output sequence includes the binary sequence equivalent to  $0_{10}$ . The count obtained (in decimal) is into the range  $[0, N-1]$

- Examples

- A ten-module counter outputs the binary sequence:  
 $0000_2, 0001_2, 0010_2, 0011_2, 0100_2, 0101_2, 0011_2, 0111_2, 1000_2, 1001_2, 1100, 0000$