MATHEMATICAL ANALYSIS

L3 - EXERCISES LIST 1: Riemann's integrals

1. Evaluate the following integrals:

a)
$$\int \frac{1-x}{\sqrt{1-x^2}} dx$$

b)
$$\int \frac{2+3\cos(x)}{\sin^2(x)} dx$$

c)
$$\int \frac{1 + \log(x)}{3 + x \log(x)} dx$$

a)
$$\int \frac{1-x}{\sqrt{1-x^2}} dx$$
 b) $\int \frac{2+3\cos(x)}{\sin^2(x)} dx$ c) $\int \frac{1+\log(x)}{3+x\log(x)} dx$ d) $\int \frac{\sin^3(x)}{\sqrt{\cos(x)}} dx$

2. Evaluate the following integrals using integration by parts:

a)
$$\int x \log(x) dx$$

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 b) $\int \arcsin(x) dx$ c) $\int e^x \sin(x) dx$ d) $\int \frac{x}{\cos^2(x)} dx$

c)
$$\int e^x \sin(x) dx$$

d)
$$\int \frac{x}{\cos^2(x)} dx$$

3. Evaluate the following integrals using the adequate change of variable:

a)
$$\int x\sqrt{x-5}dx$$
 b) $\int \frac{x^3}{1+x^8}dx$ c) $\int \frac{dx}{1+e^x}$

b)
$$\int \frac{x^3}{1+x^8} dx$$

c)
$$\int \frac{dx}{1+e^x}$$

4. Evaluate the following Riemmann's integrals, using Barrow's rule. Apply integration by parts, substitution, or both, if it would be necessary.

a)
$$\int_0^1 \frac{\sqrt{x}}{1+\sqrt{x}} dx$$
 b)
$$\int_0^2 \frac{dx}{2+\sqrt{x}}$$

b)
$$\int_0^2 \frac{dx}{2+\sqrt{x}}$$

c)
$$\int_{-\pi}^{\pi} x \sin(kx) dx$$
, $k \in \mathbb{Z}$

$$d) \quad \int_1^4 \frac{\sqrt{x}}{x(x+4)} dx$$

e)
$$\int_0^1 \arctan(x) dx$$
 f) $\int_0^2 x^2 e^{-x} dx$

$$f) \quad \int_0^2 x^2 e^{-x} dx$$

g)
$$\int_0^{\pi} e^x \cos(x) dx$$

g)
$$\int_0^{\pi} e^x \cos(x) dx$$
 h) $\int_0^{\log(5)} \frac{e^x \sqrt{e^x - 1}}{e^x + 3} dx$ i) $\int_0^{\pi/2} \cos^3(x) dx$

i)
$$\int_0^{\pi/2} \cos^3(x) dx$$

j)
$$\int_2^{\pi} \cos\left(\sqrt{x-2}\right) dx$$
 k) $\int_1^4 \frac{\sqrt{1+\sqrt{x}}}{\sqrt{x}} dx$ l) $\int_1^3 \frac{dx}{x\sqrt{x+1}}$

$$k) \quad \int_1^4 \frac{\sqrt{1+\sqrt{x}}}{\sqrt{x}} dx$$

$$1) \quad \int_{1}^{3} \frac{dx}{x\sqrt{x+1}}$$

- 5. Evaluate the area of the region delimited by $y = x^2 + x 2$ and the OX axis, in the interval [-3, 2]
- 6. Evaluate the area delimited by $f(x) = \frac{1}{x^2 + 3}$ and $g(x) = \frac{x 1}{8x}$ in the first quadrant