

Fundamentos de los Sistemas Operativos (FSO)

Departamento de Informática de Sistemas y Computadoras (DISCA)

Universitat Politècnica de València

Part 3: Memory management

Seminar 9

Virtual memory exercises

fSO

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- Exercise 1. Paging without virtual memory
- Exercise 2. Paging with virtual memory
- Exercise 3. Replacement algorithms
- Exercise 4. Replacement scope

Exercise 1. Paging without virtual memory fSO

A processor has 16-bit logical addresses managed by paging. It is made in three versions with page sizes of 256, 1024 y 4096 bytes, respectively. A given executable file contains 2800 bytes of instructions from address 0x1000, 1198 bytes of data from address 0x3000 and reserves initially 2048 bytes for the stack from address 0x9000.

a) Compute the number of page table entries and the initial number of pages in use for every processor model

| Page size (bytes) | Number of page table entries | Initial number of pages |
|-------------------|------------------------------|-------------------------|
| 256 | | |
| 1024 | | |
| 4096 | | |

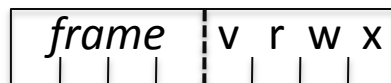
Exercise 1 (cont.)

| Region | Size (bytes) | Base (hex) |
|-----------|--------------|------------|
| Code | 2800 | 1000 |
| Variables | 1198 | 3000 |
| Stack | 2048 | 9000 |

b) Build *in binary* the initial process page table when the program is executed with 4096 bytes as page size.

Consider that physical memory size is 64 KBytes and with the process is loaded only the upper frames are allocated. The OS allocates frames in ascending order of physical addresses. It allocates first the code, then variables and finally the stack.

Page descriptors have the following content:



If a page is not in use it has to be indicated by $r=w=x=0$

| | | |
|---|--|--|
| 0 | | |
| 1 | | |
| 2 | | |
| 3 | | |
| 4 | | |
| 5 | | |
| 6 | | |
| 7 | | |
| 8 | | |
| 9 | | |
| A | | |
| B | | |
| C | | |
| D | | |
| E | | |
| F | | |

Exercise 1 (cont.)

c) Compute, if possible, the physical addresses that the MMU generates for every of the following accesses. If the translation is not possible, tell why.

| Region | Size (bytes) | Base (hex) |
|-----------|--------------|------------|
| Code | 2800 | 1000 |
| Variables | 1198 | 3000 |
| Stack | 2048 | 9000 |

| Access type | Logical address | Physical address | Legal access? (yes/no) |
|------------------|-----------------|------------------|------------------------|
| Instruction read | 1000 | | |
| Instruction read | 1004 | | |
| Instruction read | 2000 | | |
| Instruction read | 3000 | | |
| Variable read | 3010 | | |
| Variable read | 9010 | | |
| Variable write | 1000 | | |
| Variable write | 5000 | | |

Exercise 2. Paging with virtual memory

Consider the processor from exercise 1 with 4-KByte pages, and an OS with **virtual memory**. The process starts without any frame allocated and the OS allocates free frames in the following order: frame 0, frame 1, frame 2, etc.

| Region | Size (bytes) | Base (hex) |
|-----------|--------------|------------|
| Code | 2800 | 1000 |
| Variables | 1198 | 3000 |
| Stack | 2048 | 9000 |

a) Complete the next table considering that logical addresses are emitted following the “Logical address” column order.

| Access type | Logical address (hex) | Physical address (hex) | Page fault? | Legal access? |
|------------------|-----------------------|------------------------|-------------|---------------|
| Instruction read | 1000 | | | |
| Instruction read | 1004 | | | |
| Variable read | 97FC | | | |
| Instruction read | 1008 | | | |
| Variable write | 97F8 | | | |
| Instruction read | 5000 | | | |

¿How many frames has the process allocated after the fifth access?

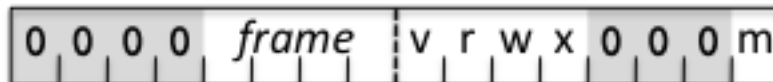
¿Can the process continue after the last access?

Exercise 2 (cont.)

b) Describe *in hexadecimal* the evolution of the process page table.

Consider that physical memory size is 64 KBytes and with the process is loaded only the upper frames are allocated. The OS allocates frames in ascending order of physical addresses.

Page descriptors are 16-bit and have the following content:



If a page is not in use it has to be indicated by $r=w=x=0$

Initial state

| | |
|---|---------|
| 0 | 0 ? 0 0 |
| 1 | 0 ? 5 0 |
| 2 | 0 ? 0 0 |
| 3 | 0 ? 6 0 |
| 4 | 0 ? 0 0 |
| 5 | 0 ? 0 0 |
| 6 | 0 ? 0 0 |
| 7 | 0 ? 0 0 |
| 8 | 0 ? 0 0 |
| 9 | 0 ? 6 0 |
| A | 0 ? 0 0 |
| B | 0 ? 0 0 |
| C | 0 ? 0 0 |
| D | 0 ? 0 0 |
| E | 0 ? 0 0 |
| F | 0 ? 0 0 |

Exercise 2 (cont.)

Read
0x1000

Read
0x1004

Read
0x97FC

Read
0x1008

Write
0x97F8

0
1
2
3
4
5
6
7
8
9
A
B
C
D
E
F

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In a computer with **32 MB of main memory**, with a memory management policy of **paging with 4KB page size**, the **OS** assigns to process A **4 main memory frames (from 0 to 3)**, that are initially empty.

Answer the following items:

- a) Describe the **physical memory address format**.
- b) If process A generates the following logical address sequence (shown in hexadecimal):

**02D4B8, 02D4B9, 02D4EB, 02D4EB, 02D86F, F0B621, F0B815,
F05963, F0B832, F0BA23, D946C3, D9B1A7, D9B1A1, F0BA25,
02D4C7, 628A31, F0B328, D9B325, D73425**

Obtain, for **FIFO and LRU algorithms**, how many page faults are generated and the final main memory state, telling the page allocated in every frame assigned to the process.

- There are two possible page replacement scopes:
 - **Local replacement:**
 - A process selects the victim between its own pages allocated into main memory frames, it can not take frames from another process.
 - The number of process allocated frames doesn't change
 - **Global replacement:**
 - A process selects the victim between whole set of main memory frames
 - The victim can belong to another process different from the one that produces the page fault

Exercise 4. Replacement scope

On a virtual memory system the OS has allocated 6 frames (from 0 to 5) to two processes A y B. At time $t = 10$, A and B page tables have the following content:

| | | Process A page table | | |
|---|---|----------------------|-----------|---------|
| | | Frame | Valid bit | Counter |
| 0 | | | i | |
| 1 | | | i | |
| 2 | 2 | | v | 10 |
| 3 | 5 | | v | 3 |
| 4 | | | i | |
| 5 | 4 | | v | 5 |
| 6 | | | i | |
| 7 | | | i | |

| | | Process B page table | | |
|---|---|----------------------|-----------|---------|
| | | Frame | Valid bit | Counter |
| 0 | | | i | |
| 1 | | | i | |
| 2 | | | i | |
| 3 | 1 | | v | 2 |
| 4 | | | i | |
| 5 | | | i | |
| 6 | | | i | |
| 7 | | | i | |

Then the processes emit the following logical address sequence. Consider that all the addresses are legal:

A,100; A,4000; B,100; A,7000; B,2100; B,1028; A,5800; A,100

Obtain what pages are allocated on every frame and the physical address translation of the first and the last access in the following situations:

- The replacement algorithm is **LRU** with **global scope**
- The replacement algorithm is **LRU** with **local scope**. Process A has 4 frames and process B has 2 frames