

Learning Wolfram Language

Exercises for Section 1 | Starting Out: Elementary Arithmetic

1.1 Compute $1+2+3$.

```
In[13]:= 1 + 2 + 3  
Out[13]= 6
```

1.2 Add the numbers 1,2,3,4,5.

```
In[15]:= 1 + 2 + 3 + 4 + 5  
Out[15]= 15
```

1.3 Multiply the numbers 1, 2, 3, 4, 5.

```
In[16]:= 1 * 2 * 3 * 4 * 5  
Out[16]= 120
```

1.4 Compute 5 squared (i . e . 5^5 or 5 raised to the power 2)

```
In[17]:= 5 ^ 2  
Out[17]= 25
```

1.5 Compute 3 raised to the fourth power .

```
In[18]:= 3 ^ 4  
Out[18]= 81
```

1.6 Compute 10 raised to the power 12 (a trillion) .

```
In[20]:= 10 ^ 12  
Out[20]= 1 000 000 000 000
```

1.7 Compute 3 raised to the power 7×8 .

```
In[19]:= 3 ^ (7 * 8)  
Out[19]= 523 347 633 027 360 537 213 511 521
```

1.8 Add parentheses to $4 - 2 * 3 + 4$ to make 14.

```
In[21]:= (4 - 2) * (3 + 4)
```

```
Out[21]= 14
```

1.9 Compute twenty - nine thousand mutiplied by seventy - three .

```
In[22]:= 29 000 * 73
```

```
Out[22]= 2 117 000
```

+1.1 Add all integers from - 3 to + 3.

```
In[23]:= - 3 + - 2 + - 1 + 1 + 2 + 3
```

```
Out[23]= 0
```

+1.2 Compute 24 divided by 3.

```
In[24]:= 24 / 3
```

```
Out[24]= 8
```

+1.3 Compute 5 raised to the power 100.

```
In[25]:= 5 ^ 100
```

```
Out[25]= 7 888 609 052 210 118 054 117 285 652 827 862 296 732 064 351 090 230 047 702 789 306 640 625
```

+1.4 Subtract 5 squared from 100

```
In[26]:= 100 - (5 ^ 2)
```

```
Out[26]= 75
```

+1.5 Multiply 6 by 5 squared, and add 7

```
In[27]:= (6 * (5 ^ 2)) + 7
```

```
Out[27]= 157
```

+1.6 Compute 3 squared minus 2 cubed .

```
In[28]:= (3 ^ 2) - (2 ^ 3)
```

```
Out[28]= 1
```

+1.7 Compute 2 cubed times 3 squared

```
In[29]:= (2 ^ 3) * (3 ^ 2)
```

```
Out[29]= 72
```

+1.8 Compute "double the sum of eight and negative eleven"

In[30]:= `(8 - 11) * 2`

Out[30]= `- 6`

Exercises for Section 2 | Introducing Functions

2.1 Compute $7 + 6 + 5$ using the function Plus

In[31]:= `Plus[7, 6, 5]`

Out[31]= `18`

2.2 Compute $2 \times (3 + 4)$ using Times and Plus

In[32]:= `Times[2, Plus[3, 4]]`

Out[32]= `14`

2.3 Use Max to find the larger of 6×8 and 5×9

In[33]:= `Max[Times[6, 8], Times[5, 9]]`

Out[33]= `48`

2.4 Use RandomInteger to generate a random number between 0 and 1000.

In[34]:= `RandomInteger[1000]`

Out[34]= `443`

2.5 Use Plus and RandomInteger to generate a number between 10 and 20.

In[35]:= `Plus[10, RandomInteger[10]]`

Out[35]= `12`

+2.1 Compute $5 \times 4 \times 3 \times 2$ using Times .

In[36]:= `Times[5, 4, 3, 2]`

Out[36]= `120`

+2.2 Compute $2 - 3$ using Subtract

In[37]:= `Subtract[2, 3]`

Out[37]= `- 1`

+2.3 Compute $(8 + 7) + (9 + 2)$ using Times and Plus

```
In[38]:= Times[Plus[8, 7], Plus[9, 2]]
```

```
Out[38]= 165
```

+2.4 Compute $(26 - 89)/9$ using Subtract and Divide

```
In[39]:= Divide[Subtract[26, 89], 9]
```

```
Out[39]= - 7
```

+2.5 Compute $100 - 5^2$ using Subtract and Power

```
In[40]:= Subtract[100, Power[5, 2]]
```

```
Out[40]= 75
```

+2.6 Find the larger of 3^5 and 5^3

```
In[41]:= Max[Power[3, 5], Power[5, 3]]
```

```
Out[41]= 243
```

+2.7 Multiply 3 and the larger of 4^3 and 3^4

```
In[42]:= Times[3, Max[Power[4, 3], Power[3, 4]]]
```

```
Out[42]= 243
```

+2.8 Add two random numbers each between 0 and 1000.

```
In[43]:= Plus[RandomInteger[1000], RandomInteger[1000]]
```

```
Out[43]= 698
```

Exercises for Section 3 | First Look at Lists

3.1 Use Range to create the list $\{1, 2, 3, 4\}$

```
In[44]:= Range[4]
```

```
Out[44]= {1, 2, 3, 4}
```

3.2 Make a list of numbers up to 100

```
In[45]:= Range[100]
```

```
Out[45]= {1, 2, 3, 4, 5, 6, 7, 8, 9, 10, 11, 12, 13, 14, 15, 16, 17, 18, 19, 20, 21, 22, 23,
24, 25, 26, 27, 28, 29, 30, 31, 32, 33, 34, 35, 36, 37, 38, 39, 40, 41, 42, 43,
44, 45, 46, 47, 48, 49, 50, 51, 52, 53, 54, 55, 56, 57, 58, 59, 60, 61, 62,
63, 64, 65, 66, 67, 68, 69, 70, 71, 72, 73, 74, 75, 76, 77, 78, 79, 80, 81,
82, 83, 84, 85, 86, 87, 88, 89, 90, 91, 92, 93, 94, 95, 96, 97, 98, 99, 100}
```

3.3 Use Range and Reverse to create {4, 3, 2, 1}

In[46]:= **Reverse[Range[4]]**

Out[46]= {4, 3, 2, 1}

3.4 Make a list of numbers from 1 to 50 in reverse order .

In[47]:= **Reverse[Range[50]]**

Out[47]= {50, 49, 48, 47, 46, 45, 44, 43, 42, 41, 40, 39, 38, 37,
36, 35, 34, 33, 32, 31, 30, 29, 28, 27, 26, 25, 24, 23, 22, 21, 20,
19, 18, 17, 16, 15, 14, 13, 12, 11, 10, 9, 8, 7, 6, 5, 4, 3, 2, 1}

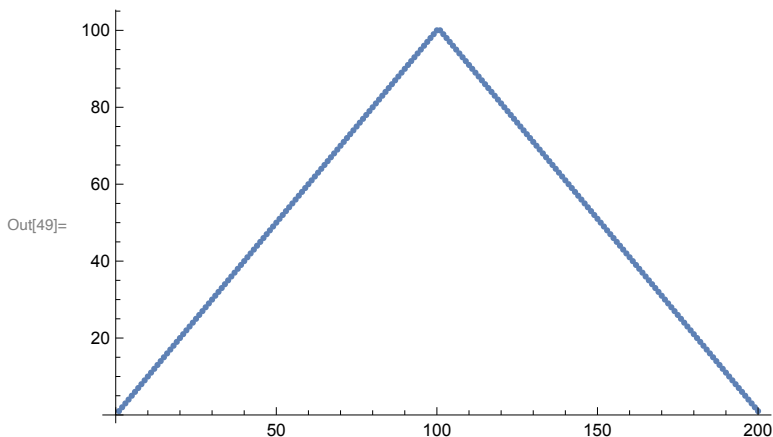
3.5 Use Range, Reverse and Join to create {1, 2, 3, 4, 4, 3, 2, 1}

In[48]:= **Join[Range[4], Reverse[Range[4]]]**

Out[48]= {1, 2, 3, 4, 4, 3, 2, 1}

3.6 Plot a list that counts up from 1 to 100, then down to 1.

In[49]:= **ListPlot[Join[Range[100], Reverse[Range[100]]]]**



3.7 Use Range and RandomInteger to make a list with a random length up to 10.

In[51]:= **Range[RandomInteger[10]]**

Out[51]= {1, 2, 3}

3.8 Find a simpler form for Reverse[Reverse[Range[10]]]

In[52]:= **Range[10]**

Out[52]= {1, 2, 3, 4, 5, 6, 7, 8, 9, 10}

3.9 Find a simpler form to `Join[{1, 2}, Join[{3, 4}, {5}]]`

In[53]:= `Range[5]`

Out[53]= `{1, 2, 3, 4, 5}`

3.10 Find a simpler form for `Join[Range[10], Join[Range[10], Range[5]]]`

In[54]:= `Join[Range[10], Range[10], Range[5]]`

Out[54]= `{1, 2, 3, 4, 5, 6, 7, 8, 9, 10, 1, 2, 3, 4, 5, 6, 7, 8, 9, 10, 1, 2, 3, 4, 5}`

3.11 Find a simpler form for `Reverse[Join[Range[20], Reverse[Range[20]]]]`

In[55]:= `Join[Range[20], Reverse[Range[20]]]`

Out[55]= `{1, 2, 3, 4, 5, 6, 7, 8, 9, 10, 11, 12, 13, 14, 15, 16, 17, 18, 19, 20, 20, 19, 18, 17, 16, 15, 14, 13, 12, 11, 10, 9, 8, 7, 6, 5, 4, 3, 2, 1}`

+3.1 Compute the reverse of the reverse of `{1, 2, 3, 4}`

In[57]:= `Reverse[Reverse[Range[4]]]`

Out[57]= `{1, 2, 3, 4}`

+3.2 Use `Range`, `Reverse` and `Join` to create the list `{1, 2, 3, 4, 5, 4, 3, 2, 1}`.

In[58]:= `Join[Range[4], Reverse[Range[4]]]`

Out[58]= `{1, 2, 3, 4, 4, 3, 2, 1}`

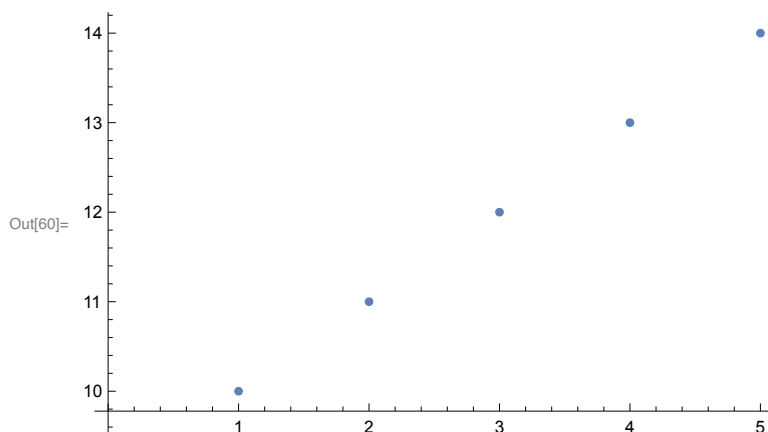
+3.3 Use `Range`, `Reverse` and `Join` to create `{3, 2, 1, 4, 3, 2, 1, 5, 4, 3, 2, 1}`

In[59]:= `Join[Reverse[Range[3]], Reverse[Range[4]], Reverse[Range[5]]]`

Out[59]= `{3, 2, 1, 4, 3, 2, 1, 5, 4, 3, 2, 1}`

+3.4 Plot the list numbers `{10, 11, 12, 13, 14}`

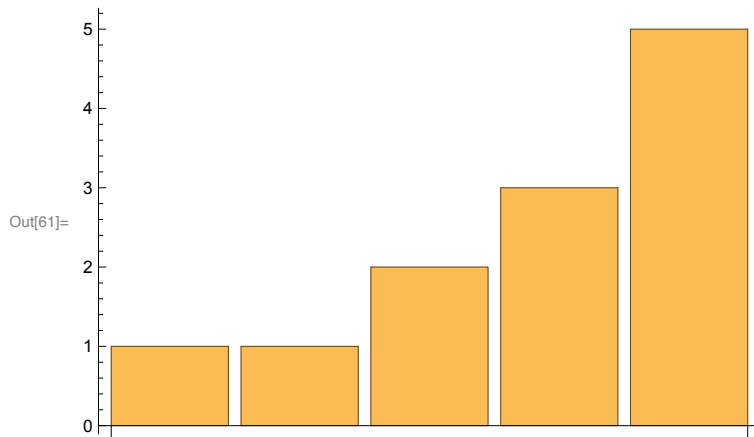
In[60]:= `ListPlot[Range[10, 14]]`



Exercises for Section 4 | Displaying Lists

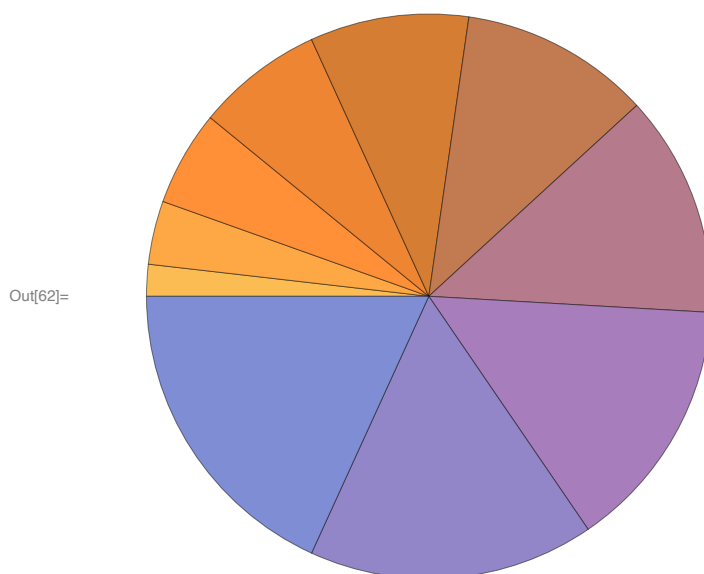
4.1 Make a bar chart of {1, 1, 2, 3, 5}

In[61]:= **BarChart**[{1, 1, 2, 3, 5}]



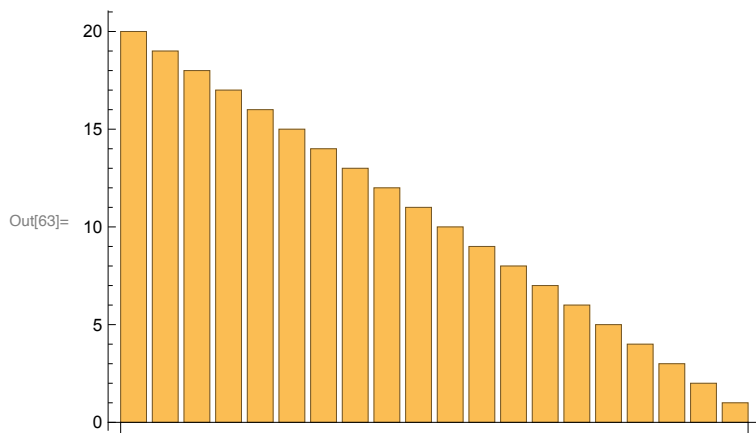
4.2 Make a pie chart of numbers from 1 to 10.

In[62]:= **PieChart**[Range[10]]



4.3 Make a bar chart of numbers counting down from 20 to 1.

In[63]:= **BarChart**[**Reverse**[**Range**[20]]]



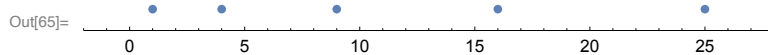
4.4 Display numbers from 1 to 5 in a column .

In[64]:= **Column**[**Range**[5]]

Out[64]=
1
2
3
4
5

4.5 Make a number line plot of the squares {1, 4, 9, 16, 25} .

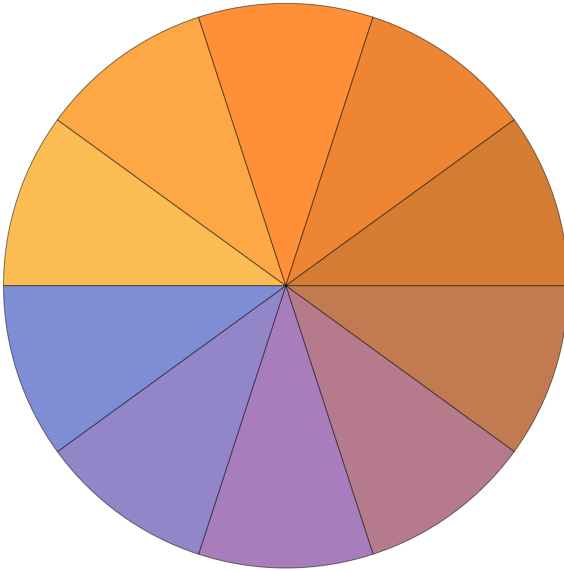
In[65]:= **NumberLinePlot**[**Range**[5]^2]



4.6 Make a pie chart with 10 identical segments, each of size 1.

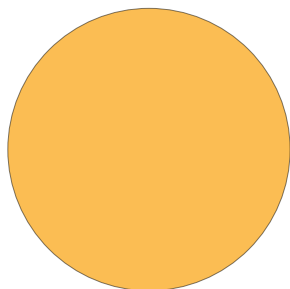
In[66]:= `PieChart[ConstantArray[1, 10]]`

Out[66]=

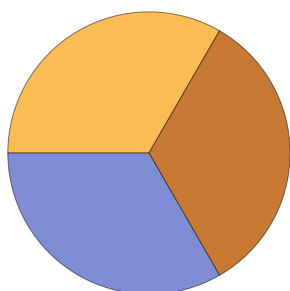
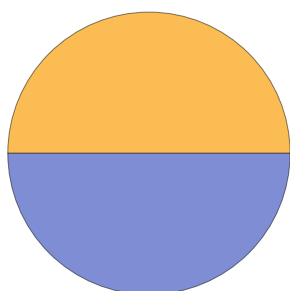


4.7 Make a column of pie charts with 1, 2 and 3 identical segments.

```
In[67]:= Column[{PieChart[{1}], PieChart[{1, 1}], PieChart[{1, 1, 1}]}, 3]
```



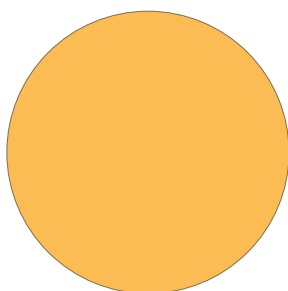
Out[67]=



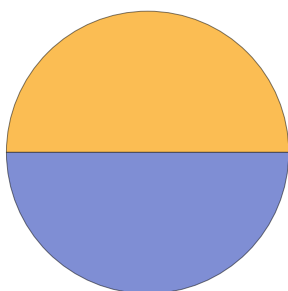
+4.1 Make a list of pie charts with 1, 2 and 3 identical segments .

```
In[68]:= {PieChart[{1}], PieChart[{1, 1}], PieChart[{1, 1, 1}]}
```

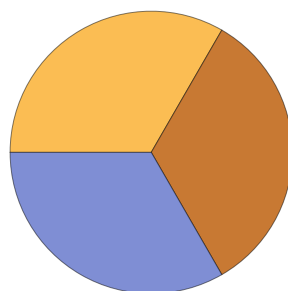
Out[68]= {



,



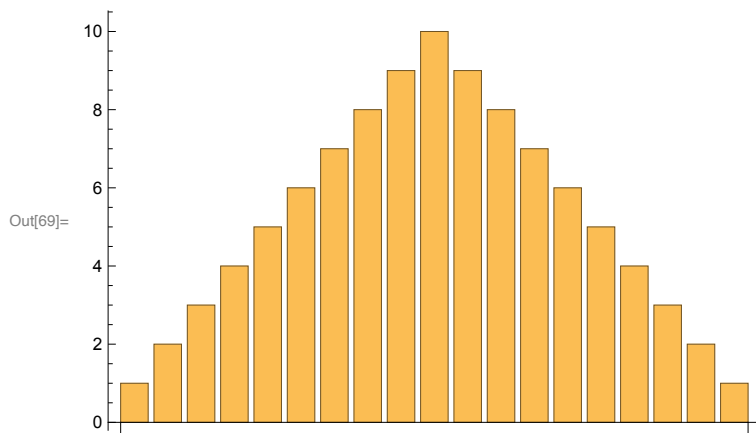
,



}

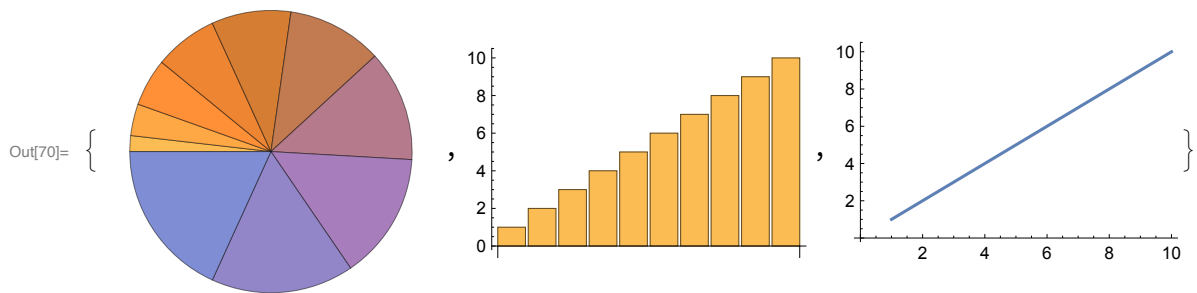
+4.2 Make a bar chart of the sequence 1, 2, 3, ..., 9, 10, 9, 8, 7, ..., 1.

In[69]:= `BarChart[Join[Range[10], Reverse[Range[9]]]]`



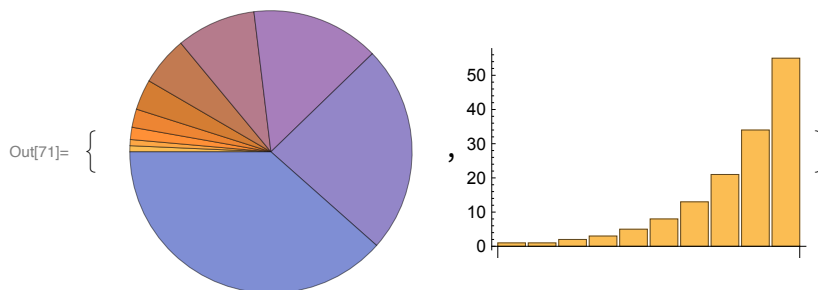
+4.3 Make a list of pie chart, bar chart and line plot of the numbers from 1 to 10.

In[70]:= `{PieChart[Range[10]], BarChart[Range[10]], ListLinePlot[Range[10]]}`



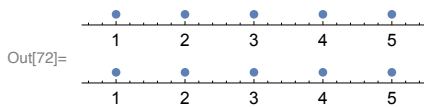
+4.4 Make a list of a pie chart and a bar chart of {1, 1, 2, 3, 5, 8, 13, 21, 34, 55}

In[71]:= `{PieChart[Fibonacci[Range[10]]], BarChart[Fibonacci[Range[10]]]}`



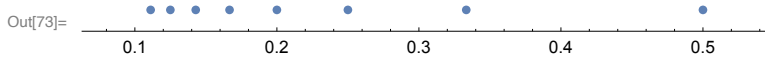
+4.5 Make a column of two number line plot of {1, 2, 3, 4, 5}

In[72]:= **Column**[{**NumberLinePlot**[**Range**[5]], **NumberLinePlot**[**Range**[5]]}]



+4.6 Make a number line of fractions 1/2, 1/3, ... through 1/9.

In[73]:= **NumberLinePlot**[{**ConstantArray**[1, 8] / **Range**[2, 9]]}



Exercises for Section 5 | Operations on Lists

5.1 Make a list of the first 10 squares, in reverse order .

In[74]:= **Reverse**[**Range**[10] ^ 2]

Out[74]= {100, 81, 64, 49, 36, 25, 16, 9, 4, 1}

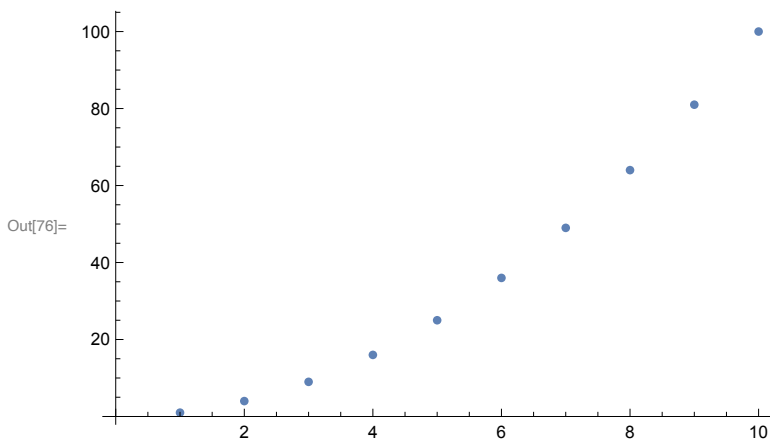
5.2 Find the total of the first 10 squares .

In[75]:= **Total**[**Reverse**[**Range**[10] ^ 2]]

Out[75]= 385

5.3 Make a plot of the first 10 squares, starting at 1.

In[76]:= **ListPlot**[**Range**[10] ^ 2]



5.4 Use Sort, Join and Range to create {1, 1, 2, 2, 3, 3, 4, 4}.

In[78]:= **Sort**[**Join**[**Range**[4], **Range**[4]]]

Out[78]= {1, 1, 2, 2, 3, 3, 4, 4}

5.5 Use Range and + to make a list of numbers from 10 to 20, inclusive .

In[79]:= **Range[0, 10] + 10**

Out[79]= {10, 11, 12, 13, 14, 15, 16, 17, 18, 19, 20}

5.6 Make a combined list of the first 5 squares and cubes (numbers raised to the power 3), sorted into order .

In[80]:= **Sort[Join[Range[5]^2, Range[5]^3]]**

Out[80]= {1, 1, 4, 8, 9, 16, 25, 27, 64, 125}

5.7 Find the number of digits in 2^{128} .

In[81]:= **Length[IntegerDigits[2^128]]**

Out[81]= 39

5.8 Find the first digit of 3^{32}

In[82]:= **First[IntegerDigits[2^32]]**

Out[82]= 4

5.9 Find the first 10 digits in 2^{100} .

In[83]:= **Take[IntegerDigits[2^100], 10]**

Out[83]= {1, 2, 6, 7, 6, 5, 0, 6, 0, 0}

5.10 Find the largest digit that appears in 2^{20} .

In[84]:= **Max[IntegerDigits[2^20]]**

Out[84]= 8

5.11 Find how many zeros appear in the digits of 2^{1000} .

In[85]:= **Count[IntegerDigits[2^1000], 0]**

Out[85]= 28

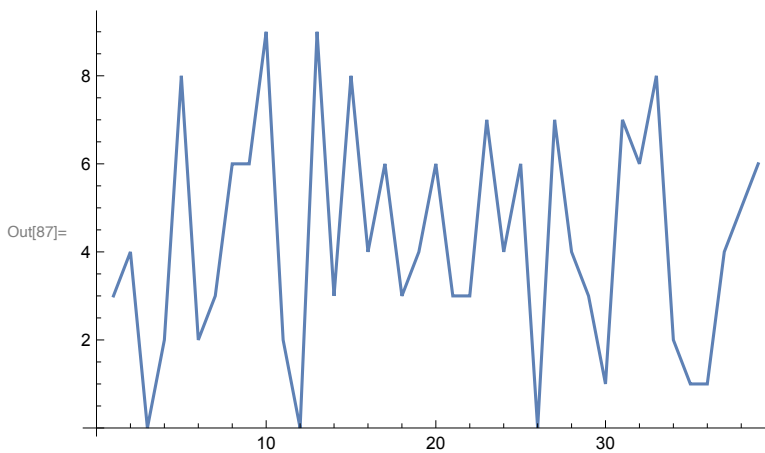
5.12 Use Part, Sort and IntegerDigit to find the second - smallest digit in 2^{20} .

In[86]:= **Part[Sort[IntegerDigits[2^20]], 2]**

Out[86]= 1

5.13 Make a line plot of the sequence of digits that appear in 2^{128} .

In[87]:= **ListLinePlot**[IntegerDigits[2^{128}]]



5.14 Use Take and Drop to get the sequence 11 through 20 from Range[100].

In[88]:= **Take**[**Drop**[Range[100], 10], 10]

Out[88]= {11, 12, 13, 14, 15, 16, 17, 18, 19, 20}

+5.1 Make a list of the first 10 multiples of 3.

In[89]:= **Range**[10] * 3

Out[89]= {3, 6, 9, 12, 15, 18, 21, 24, 27, 30}

+5.2 Make a list of the first 10 squares using only Range and Times .

In[90]:= **Times**[Range[10], Range[10]]

Out[90]= {1, 4, 9, 16, 25, 36, 49, 64, 81, 100}

+5.3 Find the last digit of 2^{37} .

In[91]:= **Last**[IntegerDigits[2^{37}]]

Out[91]= 2

+5.4 Find the second-to-last digit of 2^{32} .

In[92]:= **Last**[**Drop**[IntegerDigits[2^{32}], -1]]

Out[92]= 9

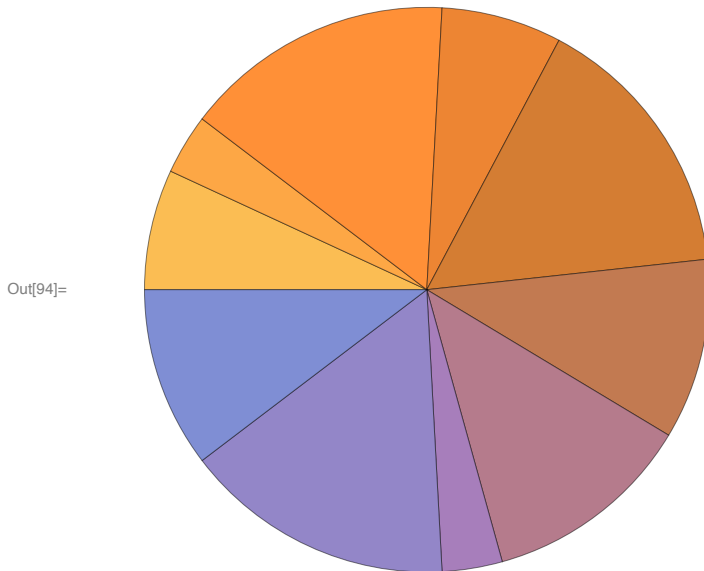
+5.5 Find the sum of all the digits of 3^{126} .

In[93]:= **Total**[IntegerDigits[3^{126}]]

Out[93]= 234

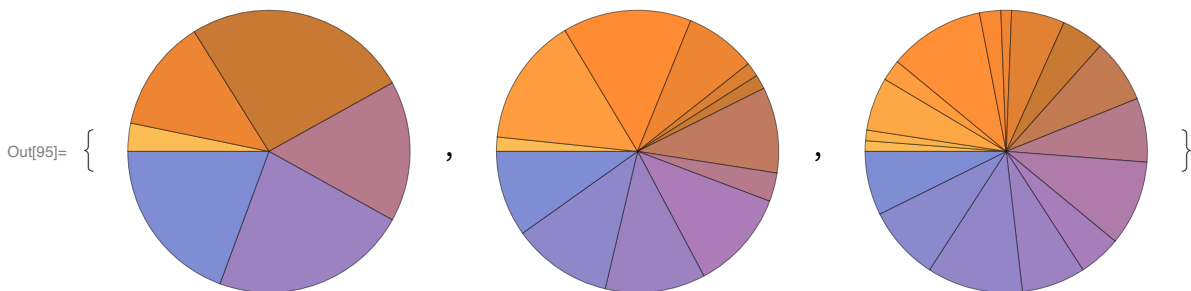
+5.6 Make a pie chart of the sequence of digits that appear in 2^{32} .

In[94]:= `PieChart[IntegerDigits[2^32]]`



+5.7 Make a list of pie charts for the sequence of digits in 2^{20} , 2^{40} , 2^{60} .

In[95]:= `{PieChart[IntegerDigits[2^20]],
PieChart[IntegerDigits[2^40]], PieChart[IntegerDigits[2^60]]}`



Exercises for Section 6 | Making Tables

6.1 Make a list in which the number 1000 is repeated 5 times .

In[96]:= `Table[1000, {5}]`

Out[96]= `{1000, 1000, 1000, 1000, 1000}`

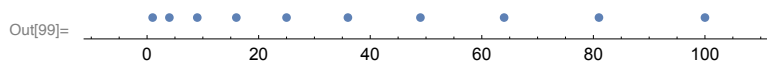
6.2 Make a table of the value of n^3 for n from 10 to 20.

In[97]:= **Table**[n^3 , { n , 10, 20}]

Out[97]= {1000, 1331, 1728, 2197, 2744, 3375, 4096, 4913, 5832, 6859, 8000}

6.3 Make a number line plot of the first 20 squares .

In[99]:= **NumberLinePlot**[**Table**[n^2 , { n , 10}]]



6.4 Make a list of the even numbers (2, 4, 6, ...) up to 20.

In[98]:= **Table**[$n * 2$, { n , 10}]

Out[98]= {2, 4, 6, 8, 10, 12, 14, 16, 18, 20}

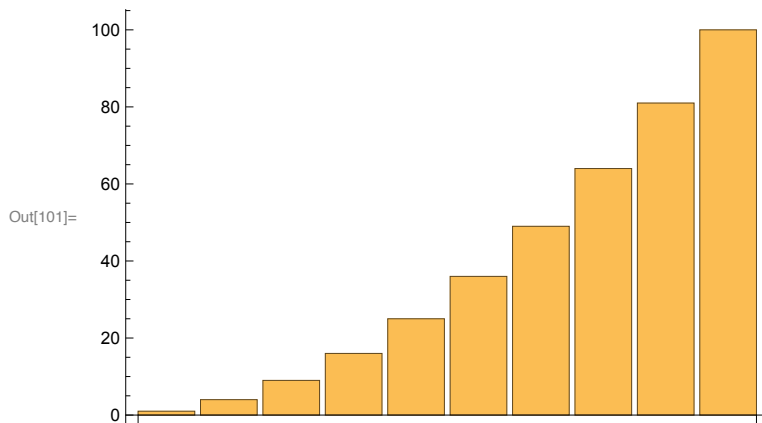
6.5 Use Table to get the same result as Range[10].

In[100]:= **Table**[n , { n , 10}]

Out[100]= {1, 2, 3, 4, 5, 6, 7, 8, 9, 10}

6.6 Make a bar chart of the first 10 squares .

In[101]:= **BarChart**[**Table**[n^2 , { n , 10}]]



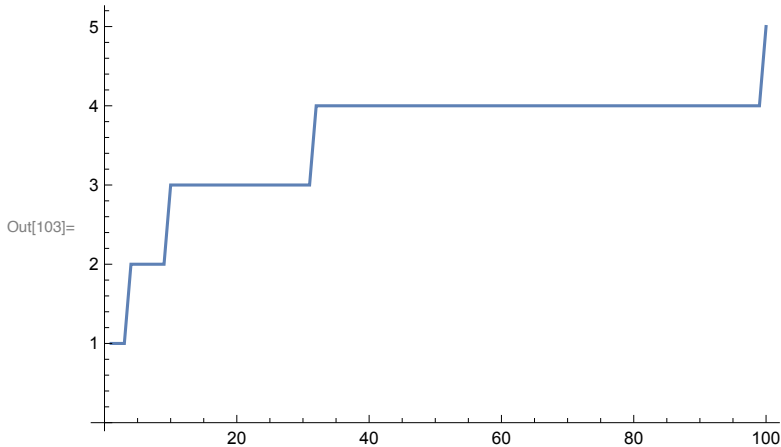
6.7 Make a table of lists of digits for the first 10 squares.

In[102]:= **Table**[**IntegerDigits**[n^2], { n , 10}]

Out[102]= {{1}, {4}, {9}, {1, 6}, {2, 5}, {3, 6}, {4, 9}, {6, 4}, {8, 1}, {1, 0, 0}}

6.8 Make a list line plot of the length of the sequence of digits for each of the first 100 squares.

```
In[103]:= ListLinePlot[Table[Length[IntegerDigits[n^2]], {n, 100}]]
```



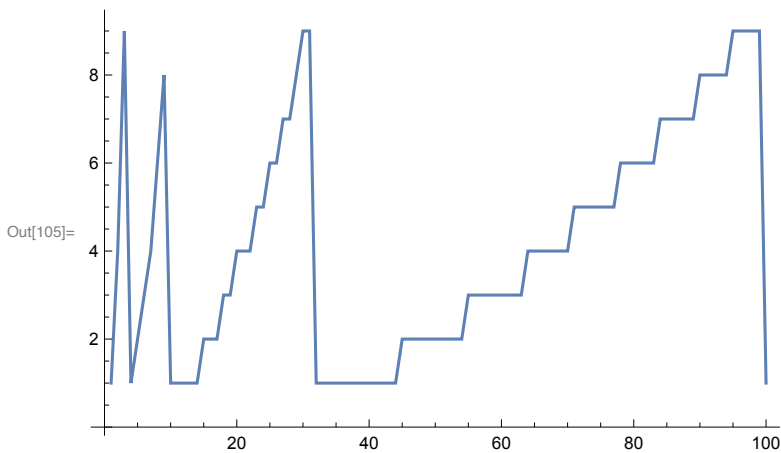
6.9 Make a table of the first digit of the first 20 squares.

```
In[104]:= Table[First[IntegerDigits[n^2]], {n, 20}]
```

```
Out[104]= {1, 4, 9, 1, 2, 3, 4, 6, 8, 1, 1, 1, 1, 1, 2, 2, 2, 3, 3, 4}
```

6.10 Make a list line plot of the first digits of the first 100 squares.

```
In[105]:= ListLinePlot[Table[First[IntegerDigits[n^2]], {n, 100}]]
```



+6.1 Make a list of the differences between n^3 and n^2 with n up to 10.

```
In[106]:= Table[(n^3) - (n^2), {n, 10}]
```

```
Out[106]= {0, 4, 18, 48, 100, 180, 294, 448, 648, 900}
```

+6.2 Make a list of the odd numbers (1, 3, 5, ...) up to 100.

```
In[107]:= Table[(n * 2) - 1, {n, 50}]
```

$$\text{Out}[107]= \{1, 3, 5, 7, 9, 11, 13, 15, 17, 19, 21, 23, 25, 27, 29, 31, \\ 33, 35, 37, 39, 41, 43, 45, 47, 49, 51, 53, 55, 57, 59, 61, 63, 65, \\ 67, 69, 71, 73, 75, 77, 79, 81, 83, 85, 87, 89, 91, 93, 95, 97, 99\}$$

+6.3 Make a list of the squares of even numbers up to 100.

```
In[108]:= Table[(n * 2) ^ 2, {n, 50}]
```

```
Out[108]= {4, 16, 36, 64, 100, 144, 196, 256, 324, 400, 484, 576, 676, 784, 900,
           1024, 1156, 1296, 1444, 1600, 1764, 1936, 2116, 2304, 2500, 2704, 2916,
           3136, 3364, 3600, 3844, 4096, 4356, 4624, 4900, 5184, 5476, 5776, 6084,
           6400, 6724, 7056, 7396, 7744, 8100, 8464, 8836, 9216, 9604, 10000}
```

+6.4 Create the list $\{-3, -2, -1, 0, 1, 2\}$ using Range .

```
In[109]:= Range[-3, 2]
```

```
Out[109]= {-3, -2, -1, 0, 1, 2}
```

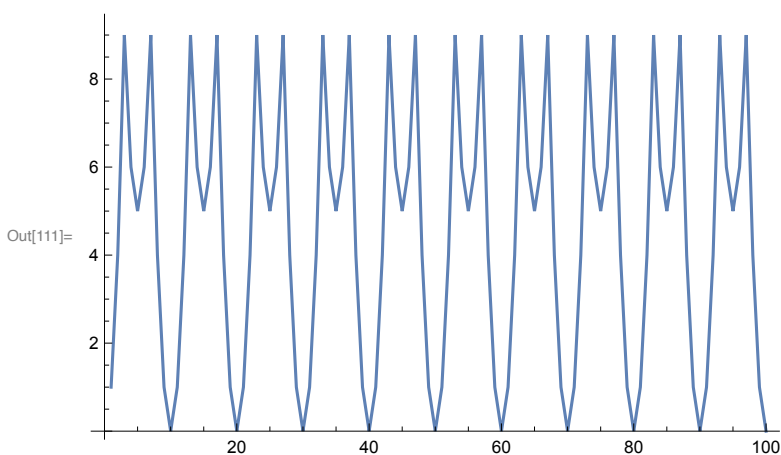
+6.5 Make a list for the numbers n up to 20 in which each element is a column of the value of n, n^2 and n^3 .

```
In[110]:= Table[Column[{n, n^2, n^3}], {n, 20}]
```

$$\text{Out}[110]= \left\{ \begin{array}{cccccccccccc} 1 & 2 & 3 & 4 & 5 & 6 & 7 & 8 & 9 & 10 & 11 \\ 1, & 4, & 9, & 16, & 25, & 36, & 49, & 64, & 81, & 100, & 121, \\ 1 & 8 & 27 & 64 & 125 & 216 & 343 & 512 & 729 & 1000 & 1331 \\ \\ 12 & & 13 & & 14 & & 15 & & 16 & & 17 & & 18 & & 19 & & 20 \\ 144, & 169, & 196, & 225, & 256, & 289, & 324, & 361, & 400 & & & & & & & & \\ 1728 & 2197 & 2744 & 3375 & 4096 & 4913 & 5832 & 6859 & 8000 \end{array} \right\}$$

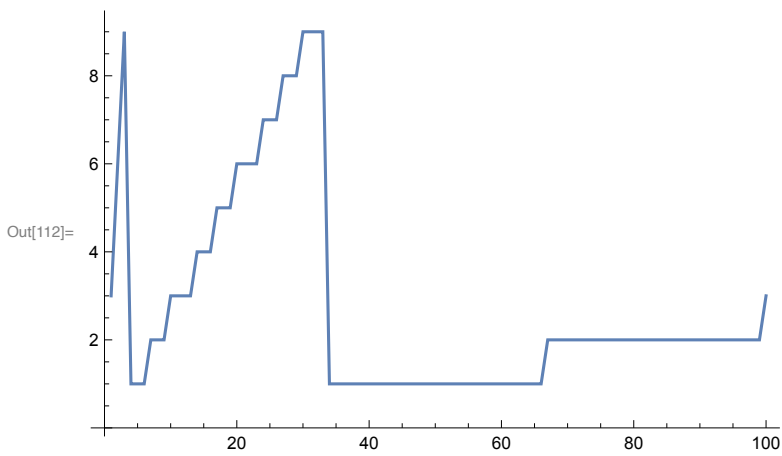
+6.6 Make a list line plot of the last digit of the first 100 squares.

```
In[111]:= ListLinePlot[Table[Last[IntegerDigits[n^2]], {n, 100}]]
```



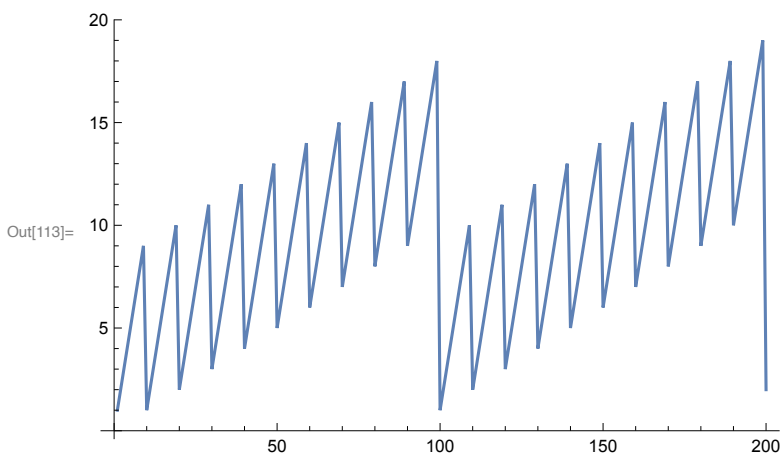
+6.7 Make a list line plot of the first digit of the first 100 multiplies of 3.

```
In[112]:= ListLinePlot[Table[First[IntegerDigits[n * 3]], {n, 100}]]
```



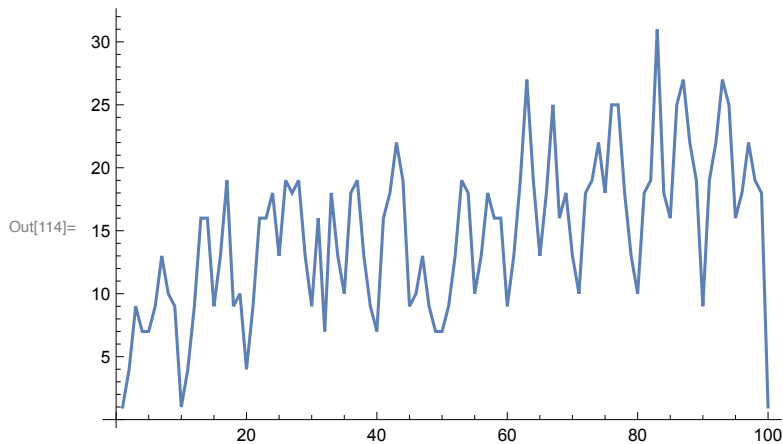
+6.8 Make a list line plot of the total of the digits for each number up to 200.

```
In[113]:= ListLinePlot[Table[Total[IntegerDigits[n]], {n, 200}]]
```



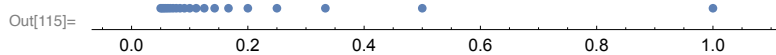
+6.9 Make a list line plot of the total of the digits for each of the first 100 squares.

```
In[114]:= ListLinePlot[Table[Total[IntegerDigits[n^2]], {n, 100}]]
```



+6.10 Make a number line plot of the numbers $1/n$ with n from 1 to 20.

```
In[115]:= NumberLinePlot[Table[1 / n, {n, 1, 20}]]
```



+6.11 Make a line plot of a list of 100 random integers where the n th integer is between 0 and n .

```
In[116]:= ListLinePlot[Table[RandomInteger[n], {n, 100}]]
```

