Quantum Optics, Exercise (2)

March 24, 2025

Problem 1

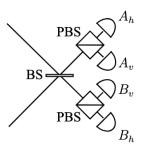
Consider two-mode states incident on a measurement setup, as shown in the figure below. The action of the 50/50 beam splitter (BS) is polarization-independent, meaning it performs the same transformation on horizontally (H) and vertically (V) polarized photons, without altering their polarization.

The two polarizing beam splitters (PBS) direct the H and V polarizations to their respective detector pairs: A_h and A_v , or B_h and B_v . Your task is to distinguish between the two Bell states in the polarization basis:

$$|\Phi_{+}\rangle = \frac{1}{\sqrt{2}} \left(|V\rangle_{1} |V\rangle_{2} + |H\rangle_{1} |H\rangle_{2} \right),$$

and

$$|\Psi_{-}\rangle = \frac{1}{\sqrt{2}} \left(|V\rangle_{1} |H\rangle_{2} - |H\rangle_{1} |V\rangle_{2} \right).$$



- (a) Express both states as the action of creation operators (which create photons of the appropriate polarizations) on the vacuum input modes.
- (b) Which detectors will click (and with what probability) if the incident state $|\Phi_{+}\rangle$?
- (c) Which detectors will click (and with what probability) if the incident state $|\Psi_{-}\rangle$?
- (d) Comment on the distinguishability of the two scenarios. Is it necessary for the detectors to distinguish between one-photon and two-photon events in order to differentiate between these two Bell states?

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