Practice session 3

Professor: Francisco Javier Vázquez Tavares

Name: _____

1 Exponential and logarithmic equations

For this practice session we are going to solve several logarithmic and exponential equations. Use the theory from the last two practice session and the following properties if you need help.

Algebra properties

$$a+b=b+a, (a+b)+c=a+(b+c), a(b+c)=ab+ac,$$

$$\frac{a}{b}+\frac{c}{d}=\frac{ad+bc}{bd}, \frac{a}{b}\cdot\frac{c}{d}=\frac{ac}{bd}, \frac{-a}{b}=-\frac{a}{b}=\frac{a}{-b}, \frac{\frac{a}{b}}{\frac{c}{d}}=\frac{ad}{bc}$$

$$\sqrt{ab}=\sqrt{a}\sqrt{b}, \sqrt{\frac{a}{b}}=\frac{\sqrt{a}}{\sqrt{b}}, \sqrt[n]{a}=a^{1/n}$$

$$x=\frac{-b\pm\sqrt{b^2-4ac}}{2a}, a^2-b^2=(a-b)(a+b)$$

Laws of exponents

Laws of Logarithms

$$\begin{aligned} a^r \cdot a^s &= a^{r+s}, \quad (a^r)^s = a^{rs} \\ \frac{a^r}{a^s} &= a^{r-s}, \quad (ab)^r = a^r b^r \\ \left(\frac{a}{b}\right)^r &= \frac{a^r}{b^r}, \quad b \neq 0 \end{aligned} \qquad \begin{aligned} \log_a\left(AB\right) &= \log_a\left(A\right) + \log_a\left(B\right) \\ \log_a\left(\frac{A}{B}\right) &= \log_a\left(A\right) - \log_a\left(B\right) \\ \log_a\left(A^C\right) &= C\log_a\left(A\right) \end{aligned}$$

Inverse functions property

$$(f \circ f^{-1})(x) = x = (f^{-1} \circ f)(x) \rightarrow \log_a(a^x) = x = a^{\log_a(x)}$$

2 Excersices

From the following equations, solve for x,

1.
$$e^{3x-2} = e^{x^2}$$

2.
$$3\log(x) = 6 - 2x$$

3.
$$\log_3(x-8) + \log_3(x) = 2$$

4.
$$\log_2(x+a) + \log_2(x-b) = c$$

5.
$$5^{x/10} + 1 = 7$$

6.
$$4 - x^2 = e^{-2x}$$

7.
$$ln(x-2) + ln(3) = ln(5x-7)$$

$$8. \left(1 - e^{t/\alpha}\right)^x = \frac{a}{b}$$