

Ackerman function






The Ackermann function is a classic example of a recursive function, notable especially because it is not a primitive recursive function. It grows very quickly in value, as does the size of its call tree.

The Ackermann function is usually defined as follows:

$$A(m, n) = \begin{cases} n + 1 & \text{if } m = 0 \\ A(m - 1, 1) & \text{if } m > 0 \text{ and } n = 0 \\ A(m - 1, A(m, n - 1)) & \text{if } m > 0 \text{ and } n > 0. \end{cases}$$

Its arguments are never negative and it always terminates.

Write a function which returns the value of $A(m, n)$. Arbitrary precision is preferred (since the function grows so quickly), but not required.

	<code>ack</code> should be a function.
	<code>ack(0, 0)</code> should return 1.
	<code>ack(1, 1)</code> should return 13.
	<code>ack(2, 5)</code> should return 13.
	<code>ack(3, 3)</code> should return 61.