Lectures' Topics



APROG - Algoritmia e Programação

Algorithmics

by Maria da Conceição Neves

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Contents

- 1. Software development concepts
- 2. Procedural Programming: Algorithms and Data Structures
- 3. Structured Programming Methodology
- 4. Control flow structures
- 5. Data, data types, operators and expressions
- 6. Logic basics
- 7. Analysis and description of algorithms.
- 8. ManualTracing of the algorithms.



1. Software development

- Software development is an activity very important in current society - Information and knowledge Society.
- Using computers in almost all areas of knowledge requires software solutions more and more sophisticated and complex.
- As the complexity of the problem increases is necessary to use an approach based on engineering principles.

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1. Software Crisis

- The growth of the software cost and its poor reliability become a great problem.
- In the 1970s there is the recognition of a set of problematic situations that are identified as "Software Crisis".
- It was necessary to approach the software development as an activity strictly comparable to that used in the various fields of engineering. This raises a new discipline "Software Engineering".



1. Software Engineering

- Software engineering aims producing software efficiently in terms of cost and reliability.
- Software engineering is the practical application of scientific knowledge in the stages of software development:
 - Requirements specification,
 - Analysis,
 - Design,
 - Implementation and testing
 - Maintenance.

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1 Producing software is not only Programming

- Since Requirements Specification to the creation of a software product must be done much more than programming.
- There are several paradigms to address the software development such as the procedural paradigm or object-oriented. In anyone of these paradigms the Analysis and Conception phases are very relevant.



1. APROG Purposes

- One of the APROG's goals is to introduce the students in the software development.
- Start by developing logical thinking skills through developing algorithms and data structures.
- But software developing is not only programming ...

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1 Software Process used in this course

- In simple problem solving using procedural paradigm, whose requirements are specified already, (usually in a text) we start immediately for:
 - analysis (what to do)
 - design solution (how to do) through an algorithm and data structure
 - coding them in a programming language.
 - program validation using an appropriate test plan.



2. Procedural Programming

Action oriented programming

PROGRAM =

Algorithm

+

Data Structure

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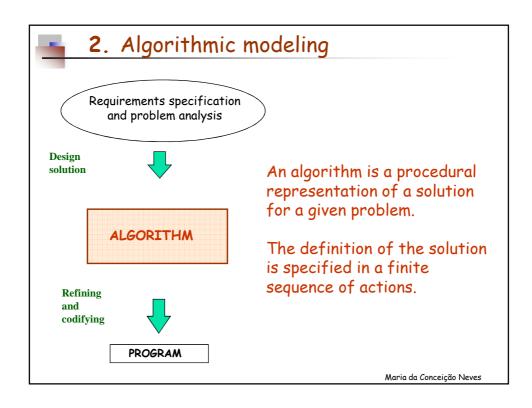
2. What is programming?

Program is

design algorithms

and

describe them in a programming language





2. Algorithm

An algorithm is a finite and well-defined (unambiguous) set of instructions describing the logical steps for performing a task.

A correct algorithm is one that face a valid input must produce a unique and correct output.

An algorithm must be effective in solving the problem and efficient in order to solve the problem with the best performance.



2. ALGORITHM

- Algorithm sequence of logical steps to perform a task
- Algorithm's Properties
 - Should allow communication with outside - Data input and results output
 - Must be finite Achieving the solution in finite time
 - Must be well defined No ambiguity

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2. Design and Description of Algorithms

- In Design phase are conceived algorithmic solutions to problems.
- The algorithms will be described in a programming language in order to be executed by a computer.
- Because programming languages are complex, at an early stage we describe algorithms using a pseudo language or flowcharts to allow the programmer to be focused on the algorithmic solution.



2. Algorithm's verification

- There are several methods to algorithm's verification.
- In this course we will use:
 - Simulate the execution step by step (manual tracing)
 - Implementation (in a programming language) and Testing

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2. Algorithms manipulate data

Data types:

integers and real numbers, characters, strings, logic values, ...

Each data type has an associated set of operations

 Data structure defines how data are organized and how they are accessed and changed.

Examples:

simple variables, arrays mono- and multi-dimensional, lists, queues, trees, graphs, ... files (data structures in secondary memory).



2. Data in main memory and secondary

- When a program is running your data is in memory. When the program ends, or you turn off the computer, the data is lost.
- To save data persistently it's necessary to save it to a file.
- Files are usually stored on disk.
- The files are usually organized into directories.
- Each file is identified by a unique name or name combined with the directory name.

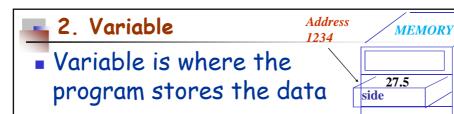
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2. Working with files

- Working with text files is like working with books, the algorithm has to describe operations
 - 1. Open the file for reading or writing
 - 2. Go to the appropriate position
 - 3. Read and write on the file
 - 4. Close the file
- When trying to read data from a file that does not exist an exception occurs this is an error in execution.

OBS: This issue will be addressed in detail later in this course.



Variable is a data container

- Variable is a memory location with
 - Unique name (e.g. side) that should reflect its use
 - Address: (e.g. 1234)
 - Value or content (e.g. 27.5)

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- Variable has an associated data type that defines:
 - The set of values that the variable can store and
 - The type of operations in which the variables can occur
- The size of the memory location depends on the type of value that will store.



2. Constantes

- Constants are special variables whose value is fixed, does not change throughout the execution of a given program.
- A program in which there are fixed values they should be defined as constants
- Examples:
 - ∏ value should be defined as
 - const real pi=3.1415
 - VAT tax for luxury goods
 - const real tax=0.23
 - Majority in Portugal

const int majority=18

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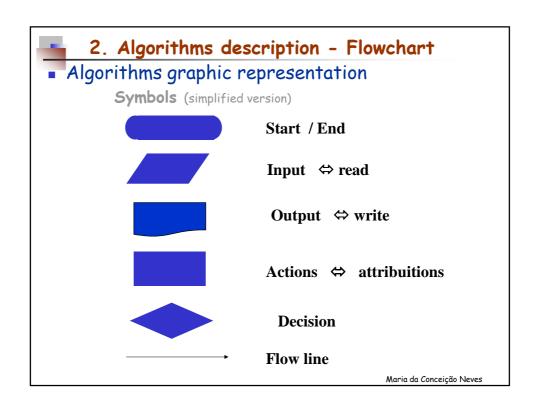


2. Data Structure notion

The program's data structure refers to

- Organization of data in variables
- Assign values to variables
- Accessing the value of the variables
- and other associated operations

```
2. Algoritms description- Our Pseudo-Code
Data structure description ED
                                  // variables and data types
Process description ALG (opcional)
                      Start / Inicio
                             / Fim
                      End
Input and output instructions read() / ler()
                               write( ) / escrever( )
Attribution instruction
                          a \leftarrow b + c
Flow control instructions
          Sequence,
                      Decision
                                 and
                                        Repetition
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```





3. Structured Programming Methodology

- In the 70s, motivated by the existing software crisis, Dijkstra developed a methodology that aims to develop programs reliable and easy to maintain.
- This methodology was called structured programming and defines a set of rules for development programs.
- The Pascal language was developed to support this new methodology.



3. Fundamental Theorem of Structured Programming

Refers to the instruction execution order

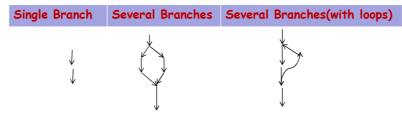
It's possible to write any program using only the three basic control flow structures:

- Sequence ordered statements executed in sequence
- Decision select alternately one or other set of statements depending on a evaluation of a condition
- Iteration a block of statements is executed in loop until the program reaches a certain state.



4. Program's flow control

- A program is a sequence of instructions.
- Programs can allow multiple branches, ie several sequences of alternative and cycles instructions.
- To direct the flow of execution among the branches there are flow control statements.



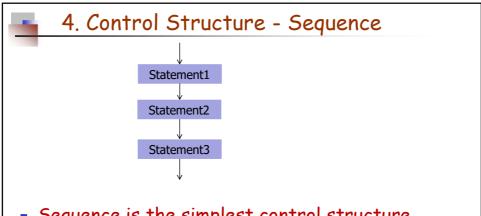
- The flow control statements are the basic units of a program.
- The flow control statements may be used in combination.
- Each flow control statement has a single entry point and a single exit Maria da Conceição Neves

Algorithm or Program Flow Control

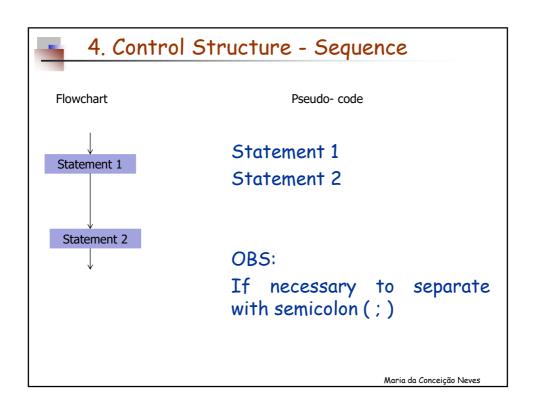
- Program flow control refers to the order in which instructions are executed.
- Basic flow control structures:
 - Sequence (Sequencial statements)
 - Decision (Conditional statement)
 - If (...) then

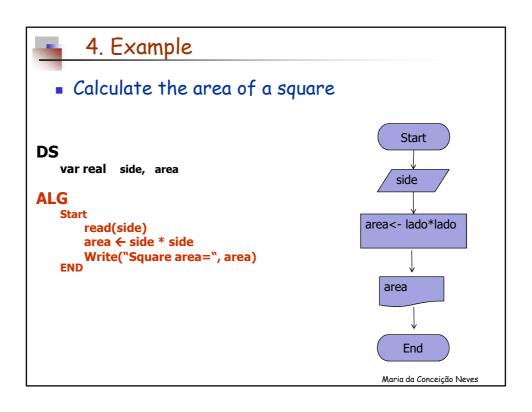
else ...

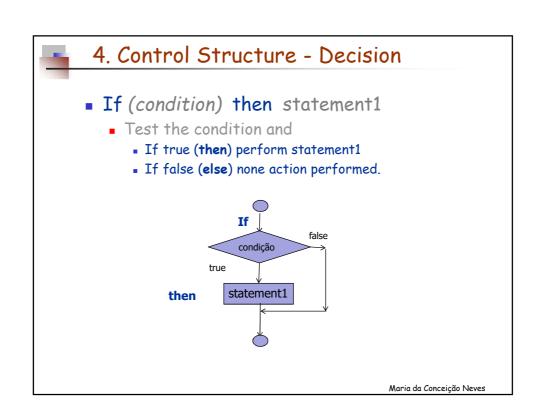
- Iteration (loops)
 - While (...) ...
 - Repeat while (...)
 - For(...) ...

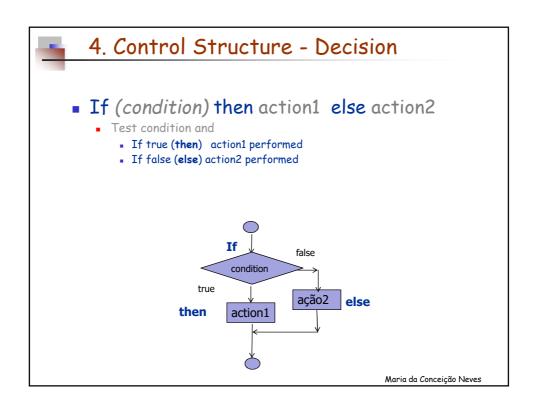


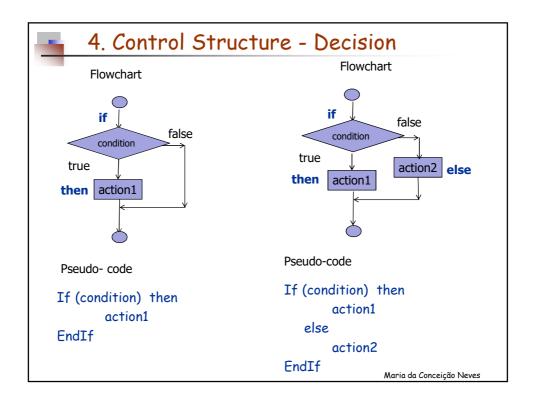
- Sequence is the simplest control structure
- Performs a statement followed by another, in the order they appear in the program
- The normal execution flow of the program is sequential unless directed otherwise by other control structure.

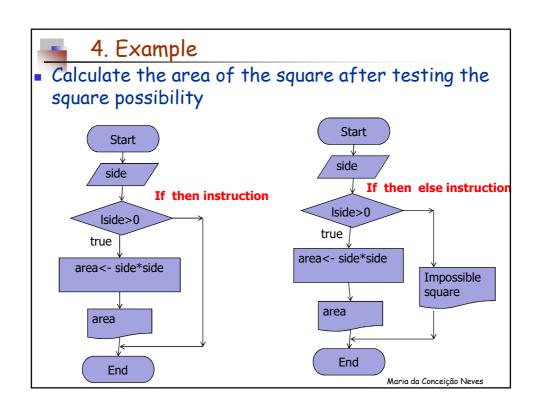


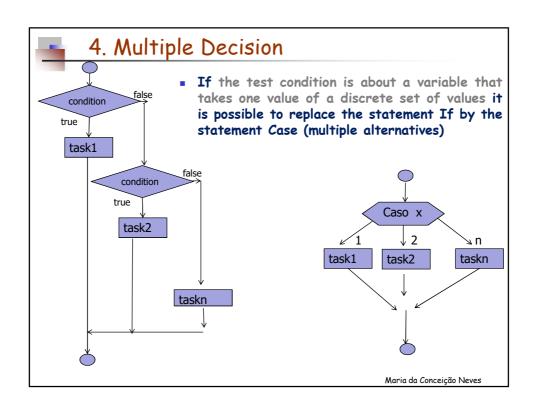


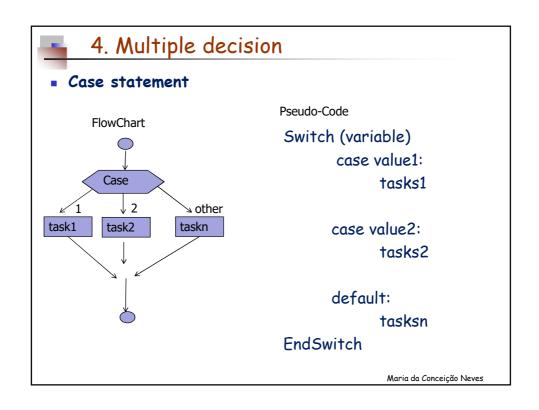


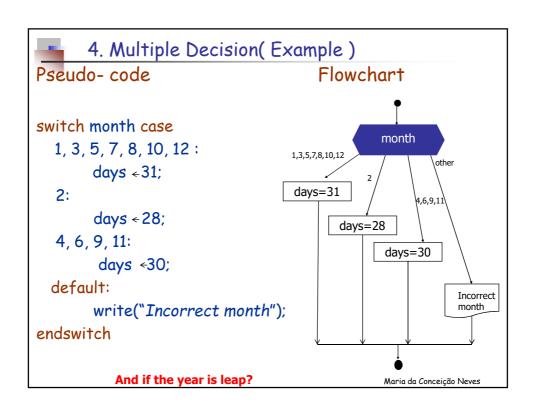












4. Control Structure - Repetition or Iteration

- This structure is also called **Loop**
- It is used when a set of instructions in a program has to be run again and again.
- Always involves the verification of a given condition to determine when to end the loop.

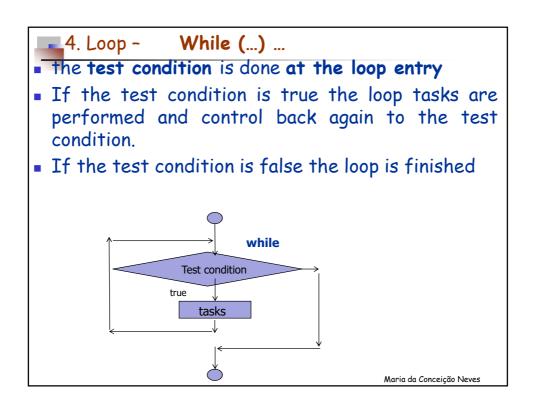
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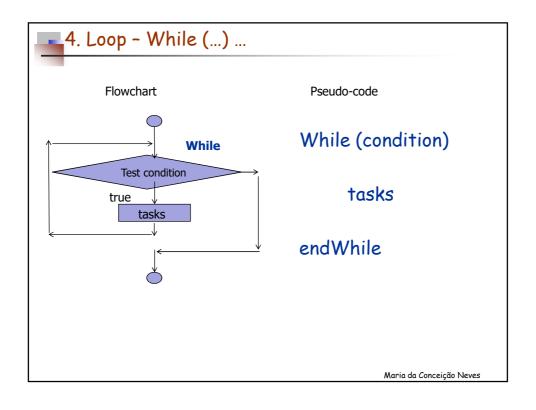
4. Several types of Loops

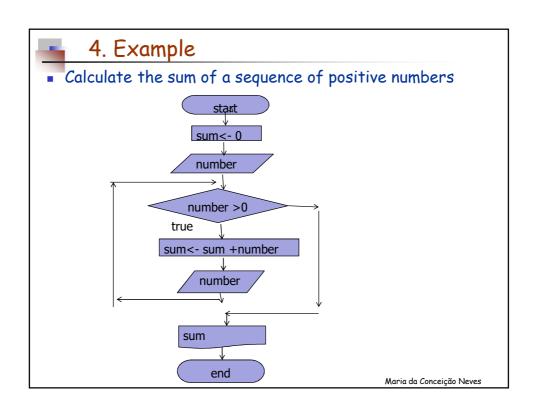
- If the test condition is done at the loop entry we will have the structure
 - While ... do ...
- If the test condition is done at the loop exit we will have the structure
 - Do ... while ...
- If known the start and end values of the loop and its progression may specify the thresholds (limits) and the step.

A counter is used to indicate the progress through the cycle. The structure will be

• For (i=...; ... ;)

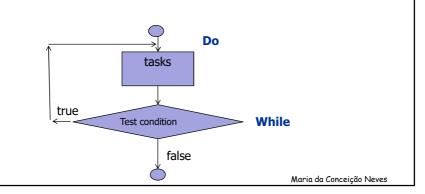


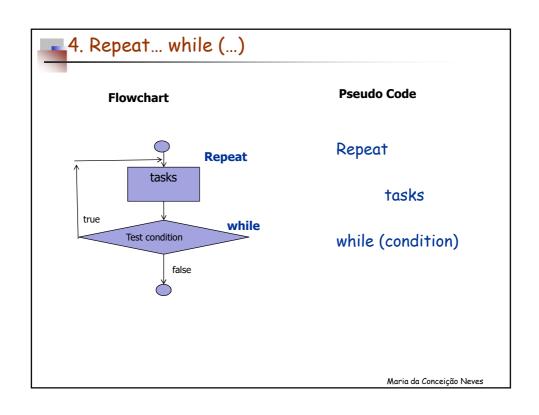


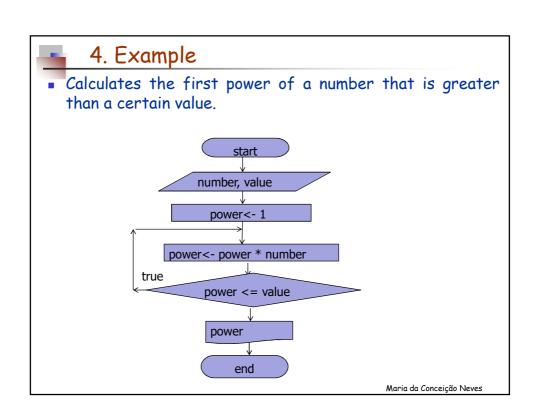


4. Loop- Repeat ... while (...)

- Start the loop performing the iteration tasks and at the end of each iteration tests the condition to verify if the loops end or not.
- If the test is true it is done a new iteration.
- If the test is false the loop ends.



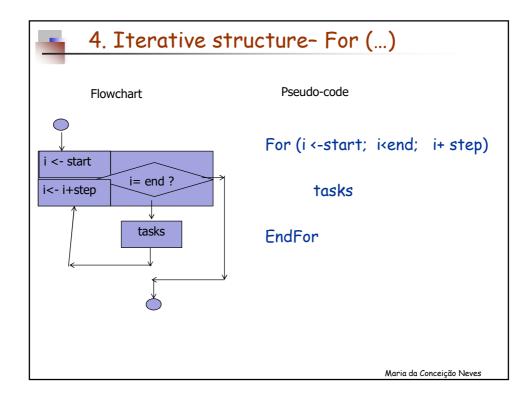






4. Loop - For(... ; ... ; ...)

- This structure is used when we knows the start and end values of the cycle and its progression.
- This structure requires that specify the limits of the cycle.
- A counter is used to indicate the progress through the cycle.
- It is necessary to indicate the step of the cycle (or as the counter is updated).



4. Iterative structures (loops)

■ What kind of loop use?

While (...)

■ This is used when the number of iterations is not known. The test of a condition to decide to enter the cycle must be made at the beginning, before performing each iteration.

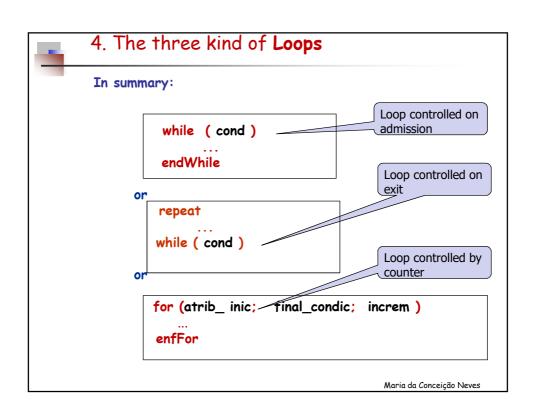
Repeat ... while (...)

■ This is used when the number of iterations is not known. The test of a condition to decide to stop the cycle must be made at the end of the cycle after performing each iteration.

• For(...;...;...)

■ This is used when we knows the number of iterations to perform

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5. Data types used in Pseudo-code

- Programming languages provide the ability to represent and manipulate various data types such as: integer, real, logical values (True or False), alphanumeric values (characters and character sequences).
- Each data type has an associated set of operations or operators to manipulate.
- For example:

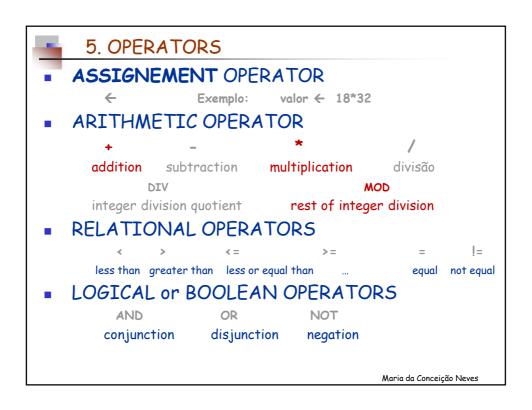
Data Type	Arithmetic operators	
INTEGER	+ addition - subtraction * multiplication DIV integer division (quotient) MOD rest of integer division	
REAL	+ addition - subtraction * multiplication / division (quotient)	

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5. EXPRESSIONS

- With operands and operators are constructed expressions.
- An expression is a sequence of operands and operators.
- We will organize the operators:
 - ASSIGNMENT OPERATOR
 - ARITHMETIC OPERATORS
 - RELATIONAL OPERATORS
 - LOGICAL OPERATORS





5. Arithmetics Operators

- Operands:
 - They are numbers or numeric expressions
- Operators:
 - Adding +
 - Subtraction -
 - Multiplication *
 - Division /
 - Rest of Integer Division MOD
 - Integer quotient DIV
- Tables of operations
- Properties of operations



5. Floating point numbers

- Floating point numbers are represented in the hardware of a computer as binary fractions.
 - The decimal 0.125 is the value 1/10 + 2/100 + 5/1000
 - The binary fraction 0.001 has the value 0/0 + 2/4 + 1/8
 - They have the same value but the first is written in base 2 and the other at the base 10
- Most of the decimal fractions can not be represented exactly as binary fractions.
- Programming languages that support floating point arithmetic deal with approximate values.

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6. Fundamentals of Logic

- In a language an expression with meaning is a designation or a statement that can be affirmative, exclamative,
 - Designation refers to or denotes an object or entity
 2
 7-3
 a
 - Affirmative Statement refers to an affirmation
 2 > 7
 5+1=6
- In Logic only be considered affirmative statements that are either true or false.

These statements are called **propositions**.

 Every proposition has one and only one logic value that is True (1) or False (0).



6. Propositions

- Simple Propositions
 - 2+3 = 5 logic value True
 - 4 is an odd number logic value False
- Compound Propositions combines two or more propositions using logic operators (connectives)
 - (2+1 > 2) AND (3 < 5) logic value True
 - (7 <= 2) OR (3 >2) logic value True
 - \bullet (3+1 = 2) AND (3 > 2) logic value False
 - NOT (5>9) logic value True

logic value True is represented by 1 logic value False is represented by 0

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6. Proposicional calculus (Basics)

- Propositional calculus is the study of logical operations on propositions.
- Operands are logical values of propositions
- Logical or Boolean operations:
 - Conjunction AND
 - Disjunction OR
 - Negation
 NOT (operador unário)
 - Implicação
 - Equivalência



- Operator NOT (operator unary)
- Truth tables:

Consider **p** being a **proposition**

		NOT
	NOT	
р	0	1
	1	0

If p for falso NOT p é verdadeiro
If p for verdadeiro NOT p é falso

Properties

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6. Conjunction Operation (AND)

Consider p, q and r as propositions

Truth TableP AND q

	_	q	
p	AND	0	1
	0	0	0
	1	0	1

p AND q is true if and only if p is true and q is true.

Properties of Conjunction

Commutative

Associative

 $(p AND q) AND r \Leftrightarrow p AND (q AND r)$

Neutral Element 1 $p AND 1 \Leftrightarrow 1 AND p \Leftrightarrow p$

Absorber Element 0 p AND 0 ⇔ 0 AND p ⇔ 0



6. Disjunction operation (OR)

Consider \mathbf{p} , \mathbf{q} and \mathbf{r} as propositions

Truth Table

```
p OR q q
OR 0 1
0 0 1
1 1 1
```

 $p\ OR\ q$ is true if at least one of the propositions was true

Properties of Disjunction

Commutative

Associative

$$(p OR q) OR r \Leftrightarrow p OR (q OR r)$$

Neutal Element 0 p OR 0 \Leftrightarrow 0 OR p \Leftrightarrow p

Absorber Element 1 p OR 1 \Leftrightarrow 1OR p \Leftrightarrow 1



6. Morgan's Laws

Consider p, q and r propositions

The negation of a conjunction is the disjunction of the negations.

NOT
$$(p \ AND \ q) \Leftrightarrow (NOT \ p) \ OR \ (NOT \ q)$$

The negation of a disjunction is the conjunction of the negations.

NOT
$$(p OR q) \Leftrightarrow (NOT p) AND (NOT q)$$



6.Conditions

Condition or propositional expression - any expression with variables that turns into a proposition (true or false) whenever you assign values (belonging to the respective domains) to variables

Logics Conditions					
N>0	N<100	NOT(N>0)	(N>0) AND (N<100)	(N>0) OR (N<100)	
1	1	0	1	1	
0	1	1	0	1	
1	0	0	0	1	

If n=45 If n=-5 If n=105

Examples:

Condition	Negated condition
N>0	N<=0
(N>0) AND (N<=100)	(N<=0) OR (N>100)
(N>=0) OR (N<100)	(N<0) AND (N>=100)

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7. Algorithm to calculate the area of a triangle

ED

```
var real base, altura, area
```

ALG

INICIO

```
ler(base, altura)
area <- base*altura /2
escrever("Area do Triângulo=", area)
FIM
```

The input values validation is essencial.

What to do in order to ensure that the input data is valid?

ler(base, altura)

```
repetir
ler(base, altura)
enquanto (base <=0 OR altura<=0)
```

The algorithms presented in this paper, for simplicity, we assume that then the input will always be valid. However algorithms could be responsible for validating the data proceeding analogously as shown.

```
Algorithm to calculate the area of a rectangle

ED

var real lado1, lado2, area

ALG

INICIO

ler(lado1,lado2);

area ← lado1 * lado2;

se (lado1=lado2)

então escrever("Area Quadrado=", area);

senão escrever("Area Rectângulo", area);

fimse

FIM

Plano de Testes

Traçagem

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```

```
7. Loop controlled at the entrance
Determine the average of a sequence of numbers ended by "sentinel value"
E.D. real num, sum, media
                         int count
INICIO
  count ← 0
                                 start counter
  sum \leftarrow 0
                                 start sum
   read (num)
   WHILE (num <> sentinel)
      count \leftarrow count +1
                                increment the counter
      sum ← sum +num
                                 update count
      ler (nota)
   ENDWHILE
   media ← sum /count
                              ATTENTION: Divide by Zero is impossible
   write(media)
FIM
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```

7. Example Make a program that receive a set of values representing the number of km traveled by a car and the spent fuel determine the average fuel consumption by 100km. The input values end when introduced km equal (Pseudo code in portuguese) ED var real km, litros, somakm, somalitros, media ALG INICIO somakm←0; somalitros←0 ler(km); ENQUANTO (km>0) FAZER ler(litros) somakm←somakm+km somalitros←somalitros+litros ler(km) FIMENQUANTO; media← somalitros/somakm*100 escrever(media) FIM Maria da Conceição Neves



7. Loops with test condition at the end of each iteration

Elaborate an algorithm to determine the first power of a given number that is greater than another given number N

```
E.D. var int number, N, power
ALG.
START
  read(number)
  read(N);
  power \leftarrow 1
                            start variable potencia
  DO
       power ← power * number
  WHILE (potwer <= N)
  write(power)
                                          Attention
                                          You must change the algorithm
END
                                          in order to deal with exceptional cases
                                          powers of 0 and 1
```

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7. Example Loop Do ... while()

Make a program that allows writing in sequence the digit of units, tens, ... of an integer. Consider that have the div and mod operators respectively calculate the quotient and rest of the integer division

```
ED var int n,d
```

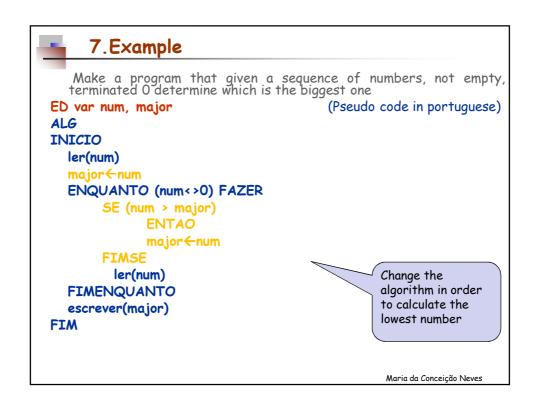
TRAÇAGEM

```
start n=453 d=453 \mod 10=3 d=45 \mod 10=5 d=4 \mod 10=4 d=4 \mod 10=4
```

```
7. Example
  Write a program that given an integer builds constituted by the same digits, but in reverse order.
                                                   builds a new integer
Example: Input: 453
                          Output: 354
                                             (Pseudo code in portuguese)
ED var int n,novo,y
                              TRAÇAGEM
ALG
                              início
INICIO
   ler(n)
                              n=453
   novo<-0
                              novo=0
   REPETIR
                              v=453 mod 10=3 | y=45 mod 10=5
      y ←n mod 10
                                                               y=4 mod 10=4
                              novo=0*10+3=3 | novo=3*10+5=35
     novo ←novo*10+y
                                                              novo=35*10+4=354
                              n=453 div 10 =45 | n=45 div 10 =4
                                                               n=4 div 10 =0
     n ← n div 10
                                             4 ≠ 0? Sim
                             45 ≠ 0? Sim
                                                              0 ≠ 0? Não
   ENQUANTO (n!=0);
   escrever("Novo=",novo)
                                                               Novo=354
FIM
                                                               fim
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```

```
7. Loop controlled by counter
Determine the average of ingress note of nalunos students in a class
E.D. var real nota, soma, media var int contador, nalunos
INICIO
                                        (Pseudo code in portuguese)
  ler(nalunos)
  contador ← 0
                               iniciar contador
  soma ← 0
                                   iniciar acumulador
  enquanto (contador < nalunos) fazer
      ler (nota)
      contador ← contador +1 incrementar contador
      soma ← soma +nota
                                  actualizar acumulador
  fimenquanto;
  media ← soma /contador
  escrever(media)
FIM
                                                  Maria da Conceição Neves
```

```
1. Loop controlled by counter
            ( number of iterations defined)
Determine the average of ingress note of nalunos
  students in a class
E.D. var real nota, soma, media var int i, nalunos
  read(nalunos)
  soma ← 0
                                     iniciar acumulador
  for (i←1 até nalunos passo 1)
     read (nota)
     soma ← soma +nota
                                    actualizar acumulador
  endFor
  media ← soma /nalunos
  write(media)
END
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```



```
7. Other examples:

1. Make a program that allows write the multiplication table of a given number

ED var int num, i

ALG

INICIO

ler(num)

PARA( i=1 ATE 10 PASSO 1)

escrever(num,"x",i,"=", num*i)

FIMPARA

FIM

2. Make a program to write on A4 sheet the multiplication tables from 1 through 9.

Obs. Follow the usual format

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```

4

7. What does the following program written in pseudo-code?

```
E.D. var real Lado1, Area
```

```
ALG
Início
ler (Lado1) // Instrução de entrada de dados
Area ← Lado1* Lado1 //Instrução de atribuição
/* Instrução de saída de resultados */
escrever( "Area do quadrado =", Area);
Fim
```

- 1. What would happen if it were introduced a negative number?
- 2. What changes would make in the algorithm?

```
7. What does the following program written in pseudo-code?
         var real Lado1, Area
E.D.
ALG
Início
                     /* Instrução de entrada de dados */
  ler (Lado1)
                    /* Instrução de decisão */
 Se ( Lado1<= 0)
    Então
         escrever( "Quadrado impossível") /*Inst saída resultados */
    Senão
        Area <-- Lado1* Lado1 /* Instrução de atribuição*/
       escrever( " Area do quadrado = ", Area) /*Inst saída result */
                 /* Fim de estrutura de decisão*/
 FimSe
Fim
                                                  Maria da Conceição Neves
```

```
7. What does the following program written in pseudo-code?

E.D. var real Lado1, Area
ALG
Início
ler (Lado1)
Enquanto ( Lado1>0) /* Ciclo com teste à entrada */
Area <-- Lado1* Lado1
escrever( " Area do quadrado = ", Area)
ler (Lado1)
FimEnquanto /* Fim de ciclo*/
Fim
```

```
E.D. var int num, quad

ALG

Início

Repete /* Ciclo com teste à saída */
ler (num)
quad <-- num* num
escrever(" O quadrado de", num, "=",quad)
enquanto (quad < 1000) /*teste à saída */

Fim
```

```
7. Determining the least common multiple of two positive
integers
ED int num1, num2, i
Alg
INÍCIO
     ler(num1, num2)
     SE (num1>num2)
      ENTÃO
             x=num1; num1=num2; num2=x;
     FIMSE
     ENQUANTO (num2*i mod num1 <> 0) FAZER
                    i=i+1
     FIMENQUANTO
     escrever ("O menor múltiplo comum entre", num1, "e",
              num2 ,"é ", num2*i)
FIM
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```

```
7. Determining the greatest common divisor of two positive integers
 ED int num1, num2, x, div, enc;
 ALG
 INICIO
    ler(num1, num2)
    SE (num1=num2)
         ENTÃO
                       escrever (" O máximo divisor comum é", num1)
         SENÃO
                 SE (num1 > num2)
                      ENTÃO
                                 x=num1; num1=num2; num2=x
              FIMSE
              enc=0
              div=num1
              ENQUANTO (enc=0) FAZER
                   SE (num1 mod div =0)
                     ENTÃO
                           SE (num2 mod div =0) ENTAO enc=1
                                     SENÃO div= div-1
                           FIMSE
                     SENÃO div =div -1
                 FIMSE
               FIMENQUANTO
               escrever ("O mdc entre", num1, "e", num2, "é ", div)
    FIMSE
 FIM
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```

```
7. Determining the greatest common divisor of two positive
      integers (A more efficient algorithm)
ED int num1, num2, x, div;
ALG
INICIO
  ler(num1, num2)
  SE (num1=num2)
       ENTÃO
                 escrever (" O máximo divisor comum é",num1)
       SENÃO
               SE (num1>num2)
                      ENTÃO
                              x=num1; num1=num2; num2=x
               FIMSE
               div=num1
               ENQUANTO (num1 MOD div <> 0 OR num2 MOD div <> 0)
                      div <- div-1
               FIMENQUANTO
               escrever ("O mdc entre", num1, "e", num2, "é", div)
  FIMSE
FIM
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```



7. Problem solving

Essentially there are two kinds of problems

1. Those for which it is possible to describe a deterministic algorithm which ensures success.

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2. Those problems that are not possible to be described by an algorithm that ensures the solution, require a solution search. The resolution of such problems is widely studied in the field of Artificial Intelligence. Several solution search strategies are proposed..

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7. Concluding remarks

- The description of real problems includes a set of superfluous details. Must identify the abstract problem.
- Abstraction allows common solutions to problems that are similar.
- The specification of algorithms and data structures can be performed in any language. It must avoid ambiguity.
- We need to select and design the data structures.
- An algorithm defines a process. The process is specified in terms of simple instructions. Each process step has to be implemented via an instruction or some other algorithm.
- Correct algorithm produces correct "outputs" (final stages) in the presence of "inputs" (initial states) valid.



- Given the complexity of programming languages such as for example JAVA, we must begin by describing the algorithms in pseudo code or flowchart focusing us well in the design of the algorithm.
- Code or program is implemented in a programming language the data structures and algorithms.
- A program is not only to run is also to be read. Proper indentation of the code is very important as it helps to display the program structure and better understand the associated semantics.